## Part V

# 11 Construction of scoring matrix

## 11.1 Scoring schemes for protein sequence alignment

Applying an appropriate scoring scheme is critical to create biologically accurate alignments and phylogenetic trees.

### Different types of scoring schemes for proteins

- Use of identity
- Use of the genetic code
- Use of a classification of amino acids
- Scoring matrix

#### Use of identity

The score is calculated by counting identical amino acids. It is equivalent with a simple scoring scheme with match: 1, mismatch: 0, and gap penalty: 0.

## Example of "use of identity"

Calculate the SP score by counting identical amino acids.

```
Seq1 F-NV  \begin{array}{l} {\rm Seq2\ FPN-} \\ {\rm Seq3\ FC-V} \\ \\ S(\bar{s}^1,\bar{s}^2)=2 \\ S(\bar{s}^1,\bar{s}^3)=2 \\ S(\bar{s}^2,\bar{s}^3)=1 \\ \\ S(\mathcal{A})=S(\bar{s}^1,\bar{s}^2)+S(\bar{s}^1,\bar{s}^3)+S(\bar{s}^2,\bar{s}^3)=2+2+1=5 \\ \\ {\rm Score:}\ 5 \\ \end{array}
```

#### Use of the genetic code

The score is based on the distance between two amino acids at the codon level.

#### Example of "use of the genetic code"

Seq1 FFFF Seq2 FCNG

```
Phe (UUU, UUC) & Phe (UUU, UUC): 3
Phe (UUU, UUC) & Cys (UGU, UGC): 2
Phe (UUU, UUC) & Asn (AAU, AAC): 1
Phe (UUU, UUC) & Glu (GAA, GAG): 0
```

Score: 6

#### Use of a classification of amino acids

The score is based on the physio-chemical properties. For example, AACH (amino acid class hierarchy) can be used as a scoring scheme.

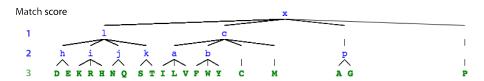


Figure 11.1: Example of amino acid class hierarchy (AACH)

#### Example of "Use of a classification of amino acids"

Calculate the score by using AACH.

```
Seq1 DDDP
Seq2 DEKD

D & D: 3, D & E: 2, D & K: 1, P & D: 0
Score: 6
```

#### Scoring matrix

• DNA/RNA:  $4 \times 4$ 

• Protein:  $20 \times 20$ 

#### PAM and BLOSUM

BLAST parameters

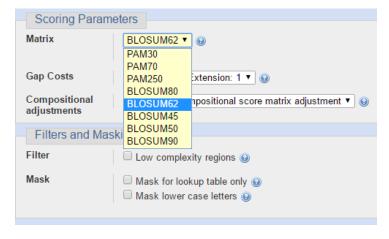


Figure 11.2: BLAST score parameters (source: )

Correspondence between PAM and BLOSUM

PAM 120 PAM 160 PAM 250 BLOSUM 80 BLOSUM 62 BLOSUM 45

## Types of substitutions

There are several types of substitutions between two sequences from the common ancestor.

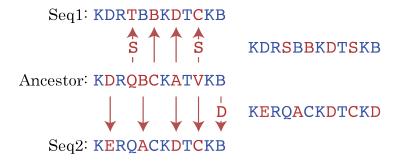


Figure 11.3: Different types of substitutions

#### Exercise 11.1

Calculate the score of the alignment by using different scoring schemes.

Seq1 K-RI Seq2 KDCC

- Use the identity.
- Use the genetic code.

K	Lys	AAA, AAG
D	Asp	GAU, GAC
R	Arg	CGU, CGC, CGA
I	Ile	AUU, AUC AUA
С	Cys	UGU, UGC

• Use AACH.

# 11.2 PAM accepted mutations

PAM is a popular scoring scheme for protein sequence alignments. It is based on substitution matrices created from experiment data.

#### Accepted point mutations

- Independent of positions and neighbor residues
- Independent from previous mutations at the same position
- Biological clock is assumed (the rate of mutations is constant)

#### PAM (point accepted mutation)

One PAM means one accepted point mutation per 100 residues. Resources of constructing a PAM score

- 34 super-families
- 71 groups of homologous sequences (85% identity)

#### Preparations for constructing a PAM score

Counting the number of mutations is the fist step to make a PAM score. Several sub-steps are involved.

- Create a phylogenetic tree
- Estimate ancestor sequences
- Count all occurrences of mutations

### Frequencies of estimated mutations

Frequencies of estimated mutations are counted in internal nodes of the reconstructed tree.

 $f_{ab}$ : The number of mutations from a to b or from b to a

 $f_a$ : The total number of mutations in which a takes part

f: Twice the total number of mutations

#### Example of frequency calculation

Calculate  $f_{CA}$ ,  $f_C$ , and f from the phylogenetic tree and the table below.

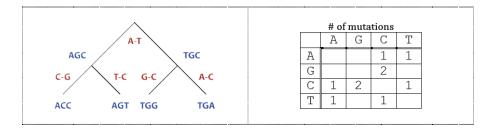


Figure 11.4: Phylogenetic tree and a table of the number of mutations

$$f_{CA} = 1$$
  
 $f_C = 1 + 2 + 1 = 4$   
 $f = 10$ 

## Background frequencies

The background probabilities are calculated from the data source.

 $p_a$ : The relative occurrence of a in the observed sequences

### Example of background frequencies

Calculate  $p_G$  from the sequences below.

Seq1 ACC

Seq2 AGT

Seq3 TGG

Seq4 TGA

$$p_G = \frac{4}{12} \approx 0.333$$

#### 11.3 PAM substitution matrix

PAM is based on a substitution matrix created from experimental data.

## Relative mutability

The probabilities of amino acid mutations are calculated based on relative mutability.

$$m_a: \frac{1}{100p_a} \times \frac{f_a}{f}$$

#### Example of relative mutability calculation

• Frequencies of estimated mutations

$f_A$ :	2	$f_G$ :	2	$f_C$ :	4	$f_T$ :	2
f:	10						

• Background frequencies

$p_A$ :	3/12	$p_G$ :	4/12	$p_C$ :	2/12	$p_T$ :	3/12
$100p_{A}$ :	23	$100p_G$ :	33.33	$100p_C$ :	16.67	$100p_T$ :	25

• Relative mutability (1 PAM)

$$m_A$$
: 0.008  $m_G$ : 0.006  $m_C$ : 0.024  $m_T$ : 0.008

#### Mutation probability

Mutation probabilities are summarized in a matrix format called substitution matrix.

$$M_{ab}: m_a \times \frac{f_{ab}}{f_a} \quad M_{aa}: 1 - m_a$$

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#### Example of substitution matrix

• Frequencies of estimated mutations

$f_A$	AC:	1	$f_{AT}$ :	1	$f_{GC}$ :	2	$f_{CT}$ :	1
$f_{\epsilon}$	$c_A$ :	1	$f_{TA}$ :	1	$f_{CG}$ :	2	$f_{TC}$ :	1
j	$f_A$ :	2	$f_G$ :	2	$f_C$ :	4	$f_T$ :	2

• Relative mutability (1 PAM)

• Mutation probabilities

$m_{AC}$ :	0.004	$m_{AT}$ :	0.004				
$m_{GC}$ :	0.006						
$m_{CA}$ :	0.006	$m_{GC}$ :	0.012	$m_{CT}$ :	0.006		
$m_{TA}$ :	0.004	$m_{TC}$ :	0.004				
$m_{AA}$ :	0.992	$m_{GC}$ :	0.994	$m_{CC}$ :	0.976	$m_{TT}$ :	0.992

• Substitution matrix

#### Matrices for general evolutionary time

Markov chains can be used to generalize PAM with arbitrary values. For instance, the substitution value for 2 PAM (=2) for amino acids a to b can be calculated as:

$$M_{ab}^2 = M_{ab}M_{bb} + M_{aa}M_{ab} + \sum_{c \notin \{a,b\}} M_{ac}M_{cb} = \sum_{c \in M} M_{ac}M_{cb}$$

#### Odds matrix

Substitution scores can be transformed to odds values. Odds values  $O_{ab}$  are equal to  $O_{ba}$ , and therefore an odds matrix is symmetrical.

$$O_{ab} = \frac{M_{ab}}{p_b}$$

when  $a \neq b$ :

$$O_{ab} = \frac{M_{ab}}{p_b} = m_a \times \frac{f_{ab}}{f_a} \times \frac{1}{p_b} = \frac{1}{100p_a} \times \frac{f_a}{f} \times \frac{f_{ab}}{f_a} \times \frac{1}{p_b} = \frac{f_{ab}}{100fp_ap_b}$$

# Transformation of an odds matrix to a score matrix

Odds values can be further transformed to log-odds values.

$$R_{ab} = \log O_{ab} = \log \frac{M_{ab}}{p_b}$$