

# Linear Regression with One Variable

TOTAL POINTS 5

1. Consider the problem of predicting how well a student does in her second year of college/university, given how well she did in her first year.

1 point

Specifically, let  $x$  be equal to the number of "A" grades (including A-, A and A+ grades) that a student receives in their first year of college (freshmen year). We would like to predict the value of  $y$ , which we define as the number of "A" grades they get in their second year (sophomore year).

Refer to the following training set of a small sample of different students' performances (note that this training set may also be referenced in other questions in this quiz). Here each row is one training example. Recall that in linear regression, our hypothesis is  $h_{\theta}(x) = \theta_0 + \theta_1 x$ , and we use  $m$  to denote the number of training examples.

$x$	$y$
3	4
2	1
4	3
0	1

For the training set given above, what is the value of  $m$ ? In the box below, please enter your answer (which should be a number between 0 and 10).

4

2. For this question, assume that we are

1 point

using the training set from Q1. Recall our definition of the

cost function was  $J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$ .

What is  $J(0, 1)$ ? In the box below,

please enter your answer (Simplify fractions to decimals when entering answer, and '.' as the decimal delimiter e.g., 1.5).

0.5

3. Suppose we set  $\theta_0 = -2, \theta_1 = 0.5$  in the linear regression hypothesis from Q1. What is  $h_{\theta}(6)$ ?

1 point

1

4. Let  $f$  be some function so that

1 point

$f(\theta_0, \theta_1)$  outputs a number. For this problem,

$f$  is some arbitrary/unknown smooth function (not necessarily the cost function of linear regression, so  $f$  may have local optima).

Suppose we use gradient descent to try to minimize  $f(\theta_0, \theta_1)$

as a function of  $\theta_0$  and  $\theta_1$ . Which of the

following statements are true? (Check all that apply.)

- ☐ Setting the learning rate  $\alpha$  to be very small is not harmful, and can only speed up the convergence of gradient descent.
- ☐ No matter how  $\theta_0$  and  $\theta_1$  are initialized, so long as  $\alpha$  is sufficiently small, we can safely expect gradient descent to converge to the same solution.
- ☒ If  $\theta_0$  and  $\theta_1$  are initialized at the global minimum, then one iteration will not change their values.
- ☒ If the first few iterations of gradient descent cause  $f(\theta_0, \theta_1)$  to **increase** rather than decrease, then the most likely cause is that we have set the learning rate  $\alpha$  to too large a value.

5. Suppose that for some linear regression problem (say, predicting housing prices as in the lecture), we have some training set, and for our training set we managed to find some  $\theta_0, \theta_1$  such that  $J(\theta_0, \theta_1) = 0$ .

1 point

Which of the statements below must then be true? (Check all that apply.)

☐ This is not possible: By the definition of  $J(\theta_0, \theta_1)$ , it is not possible for there to exist

$\theta_0$  and  $\theta_1$  so that  $J(\theta_0, \theta_1) = 0$

☒ For these values of  $\theta_0$  and  $\theta_1$  that satisfy  $J(\theta_0, \theta_1) = 0$ ,

we have that  $h_{\theta}(x^{(i)}) = y^{(i)}$  for every training example  $(x^{(i)}, y^{(i)})$

☐ For this to be true, we must have  $\theta_0 = 0$  and  $\theta_1 = 0$

so that  $h_{\theta}(x) = 0$

☐ We can perfectly predict the value of  $y$  even for new examples that we have not yet seen.

(e.g., we can perfectly predict prices of even new houses that we have not yet seen.)