

Assignment 11 - Main Program

```
1 import assign_11_mod as ruth #import the content from the other file, '
   wk11_mod.py', use the name 'ruth' (as in 'Rutherford') to refer to it
   instead
2
3 iteration_counter = 0 #initialise a counter for the total number of
   iterations
4
5 c = 137.035999 #speed of light in a.u.
6 q_au = 79.0 #charge on gold nucleus
7 q_alpha = 2.0 #charge on alpha particle
8 k = 1.0 #coulomb constant
9 m_alpha = 7294.3 #mass of alpha particle
10 dt = 1E-5 #timestep size, also a.u.
11
12 r = ruth.Vector(0.0,-0.005) #initialise the position vector
13 v = ruth.Vector(0.0,0.0) #initialise the velocity vector
14
15 #read in the x-offset for the position
16 r.x = float(raw_input('Please specify the x-offset of the incident Alpha
   particle in Bohr Radii: '))
17
18 #read in the y-velocity and scale by speed of light
19 v.y = float(raw_input('Please specify the y-velocity of the incident Alpha
   particle as a fraction of c: '))
20 v.y *= c
21
22 #initialise the current distance minimum
23 min_distance = r.mag()
24
25 #set the radial boundary
26 r_limit = 1.1 * r.mag()
27
28 #open and write initial condition to output file
29 fout = open('assign_11.out','w')
30 fout.write('%e %e\n'%(r.x,r.y))
31
32 #keep looping while the position is within the radial boundary
33 while (r.mag() < r_limit):
34     a = ((k*q_au*q_alpha)/(m_alpha * r.mag()**2)) * r.unit() #acceleration
        vector calculation
35     v += a*dt #change velocity by dv (=a*dt)
36     r += v*dt #change position by dr (=v*dt)
37     fout.write('%e %e\n'%(r.x,r.y)) #output new coordinate
38     min_distance = min(r.mag(),min_distance) #update if new minimum distance is
        found
39     iteration_counter += 1 #increment counter of steps by 1
40
41 #output the number of iterations, simulated time, and distance of closest
   approach
42 print 'Calculation took %d iterations; simulated time %e t_A'%(
   iteration_counter,float(iteration_counter)*dt)
43 print 'Distance of closest approach = %e a_0'%(min_distance)
44
45 #close output file
46 fout.close()
```

Assignment 11 - Module

```

1 import numpy
2
3 #Vector object and methods, all vector forms and operations
4 #class Vector:
5 class Vector(object):
6     #initialisation
7     __slots__ = ('x','y') #limit properties to include only x and y components
8                             #otherwise random additional unrelated to vectors can be added
8                             #dynamically, which could break other parts of the vector operations)
9
10    def __init__(self, x, y):
11        self.x = x
12        self.y = y
13
14    #method to display contents of vector object (default separated by commas)
15    def show(self, mode='comma'):
16        if (mode == 'comma'):
17            a = ','
18        elif (mode == 'space'):
19            a = ' '
20        elif (mode == 'tab'):
21            a = '\t'
22        else:
23            a = str(mode)
24        return '[' + str(self.x) + a + str(self.y) + ']'
25
26    def __repr__(self):
27        return self.show()
28
29    def __str__(self):
30        return self.show()
31
32    #method which returns the magnitude of a vector object
33    def mag(self):
34        a = numpy.sqrt(self.x*self.x + self.y*self.y)
35        return a
36
37    ###Unique methods within vector type
38    #method which adds two vector objects together
39    def add(a,b):
40        x = a.x + b.x
41        y = a.y + b.y
42        return Vector(x, y)
43
44    #method which subtracts two vector objects
45    def sub(a,b):
46        x = a.x - b.x
47        y = a.y - b.y
48        return Vector(x, y)
49
50    #scale a vector by a scalar
51    def scale(a,b):
52        x = a.x * b
53        y = a.y * b
54        return Vector(x, y)
55
56    ###Replacement to default operations when using vectors
57    def __add__(self,other):
58        return self.add(other)
59
60    def __sub__(self,other):
61        return self.sub(other)
62
63    def __mul__(self,other):
64        return self.scale(other)
65
66    def __rmul__(self,other):
67        return self.scale(other)
68
69    #perform dot product between two vectors
70    def dot(a,b):
71        x = a.x * b.x
72        y = a.y * b.y

```

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59     return x + y
60 #perform cross product between two vectors
61 #def cross(a,b):
62 # x = (a.y * b.z) - (a.z * b.y)
63 # y = (a.z * b.x) - (a.x * b.z)
64 # z = (a.x * b.y) - (a.y * b.x)
65 # return Vector(x, y, z)
66 #return unit vector for one vector
67 def unit(a):
68     b = a.scale(1.0 / a.mag())
69     return b
70
71 Null = Vector(0.0,0.0)
```