C++ for Scientific Computation

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Contents

1	Day	1: Basic input/output												
	1.1	aa_hello_world.c												
	1.2	ab_hello_world.cpp												
	1.3	ac_hello_world.cpp												
	1.4	ad_powers_of_integer.cpp												
	1.5	ae_powers_of_real.cpp												
2	Day 2: Pointers/References, Arithmetic/Logical													
	2.1	af_pointer.cpp												
	2.2	ag_reference.cpp												
	2.3	ah_arithmetic_operators.cpp												
	2.4	ai_relational_logical.cpp												
3	Day	3: Scope, Conditional, Loops												
	3.1	aj_blocks_scope.cpp												
	3.2	ak_scope.cpp												
	3.3	al_if_else.cpp												
	3.4	am_for_loop.cpp												
	3.5	an_while_loop.cpp												
	3.6	ao_do_while_loop.cpp												
	3.7	ap_break.cpp												
	3.8	aq_break_nested_loop.cpp												
	3.9	ar_break_all_loops.cpp												
4	Day 4: Functions, Call by value/reference 2													
	4.1	as_function_square.cpp												
	4.2	at_function_factorial.cpp												
	4.3	au_function_call_by_value.cpp												
	4.4	av_function_call_by_reference.cpp												
	4.5	aw_function_call_by_reference_using_pointers.cpp												
	4.6	ax_function_multiple_return_values.cpp												

5	Day	5: Functions- default args, function pointers; Arrays 30													
	5.1	ay_function_default_arguments.cpp													
	5.2	az_function_inline.cpp													
	5.3	ba_function_pointers.cpp													
	5.4	bb_function_pointers_as_arguments.cpp													
	5.5	bc_static_variables.cpp													
	5.6	bd_array.cpp													
	5.7	be_function_with_array_argument.cpp													
	5.8	bf_multidimensional_arrays.cpp													
	5.9	bg_array_and_pointer.cpp													
6	Day 6: Dynamic memory, Multidimensional Array, BLAS 39														
	6.1	bh_dynamic_memory.cpp													
	6.2	bi_dynamic_array_size_input.cpp													
	6.3	bj_multidimensional_array_with_pointer.cpp													
	6.4	$bk_multidimensional_dynamic_array.cpp \ . \ . \ . \ . \ . \ . \ . \ . \ . \$													
	6.5	bl_multidimensional_dynamic_array_size_input.cpp													
	6.6	$bm_multidimensional_array_with_mapping.cpp \ . \ . \ . \ . \ . \ . \ . \ . \ . \$													
7	Day	7: String, Advanced Datatypes, BLAS, Sparse Matrices 48													
	7.1	bn_strings.cpp													
	7.2	bo_typedef.cpp													
	7.3	bp_struct.cpp													
	7.4	bq_struct_pointer.cpp													
	7.5	br_struct_array.cpp													
8	Day 9: Modules and Namespaces, Classes 53														
	8.1	bs_struct_with_functions.cpp													
	8.2	bt_struct_constructor_destructor.cpp													
9	Day	10: Classes Continued 58													
		bu_struct_this_pointer.cpp													
	9.2	bv_copy_constructor.cpp													
	9.3	bw_default_copy_constructor.cpp													
	9.4	bx_struct_with_const_functions.cpp													
	9.5	by_struct_visibility.cpp													
	9.6	bz_safely_changing_size_of_array.cpp													
10	Day	11: Classes Continued, Templates 70													
		ca_operator_overloading.cpp													
		cb_templates.cpp													
11	Dav	14: STL 73													
-		cc_list.cpp													
		cd_vector.cpp													
		ce_valarray.cpp													
		cf_complex_numbers.cpp 70													

	11.5 cg_auto_pointer.cpp	77
12	Day 15: Boost	78
	12.1 ch_boost_array.cpp	78
	12.2 ci_boost_multi_array.cpp	79
	12.3 cj_boost_mulitprecision_cpp_int.cpp	80
	12.4 ck_boost_mulitprecision_gmp.cpp	81
	12.5 cl_boost_mulitprecision_cpp_int_2.cpp	82
	12.6 cm_boost_random_uniform.cpp	84
	12.7 cn_boost_ublas_vector.cpp	85
	12.8 co_boost_ublas_unit_vector.cpp	86
	12.9 cp_boost_ublas_zero_vector.cpp	87
	12.10cq_boost_ublas_scalar_vector.cpp	88
		89
	12.11cr_boost_ublas_sparse_vector_mapped.cpp	
	12.12cs_boost_ublas_sparse_vector_compressed.cpp	90
	12.13ct_boost_ublas_sparse_vector_coordinate.cpp	91
13	Day 16: Boost Continued	92
	13.1 cu_boost_ublas_vector_expressions_conj_etc.cpp	92
	13.2 cv_boost_ublas_vector_expressions_binary.cpp	93
	13.3 cw_boost_ublas_vector_expressions_outer_prod.cpp	94
	13.4 cx_boost_ublas_vector_expressions_scalar_multi.cpp	95
	13.5 cy_boost_ublas_vector_expressions_reductions.cpp	96
	13.6 cz_boost_ublas_vector_expressions_inner_prod.cpp	97
	13.7 da_boost_ublas_matrix_basic.cpp	98
	13.8 db_boost_ublas_matrix_special.cpp	99
		100
		101
		102
		103
		104
		10^{5}
		106
	1 0 11	100
	v · · · · · · · · · · · · · · · · · · ·	
	1	108
		109
	1	110
	$13.20 \\ dn_boost_ublas_matrix_expressions_matrix_matrix_triangular_solver.cpp .$	111
14	Day 17: Boost Continued	112
	14.1 do_mpi.cpp	112
		113
		114
		115
		116
	1 11	117

	14.7 du_boost_mpi_reduce.cpp	118
	14.8 dv_boost_mpi_reduce_2.cpp	119
	14.9 dw_boost_python_hello_world.cpp	120
	14.10dx_boost_python_exposing_classes.cpp	121
15	Day 18: MTL	122
	15.1 dy_mtl_vector1.cpp	122
	15.2 dz_mtl_vector2.cpp	123
	15.3 ea_mtl_dense2D.cpp	124
	15.4 eb_mtl_morton_dense.cpp	125
	15.5 ec_mtl_compressed2D.cpp	126
	15.6 ed_mtl_element_structure.cpp	127
	15.7 ee_mtl_multi_vector.cpp	129
	15.8 ef_mtl_insert.cpp	130
	15.9 eg_mtl_insert_scope.cpp	132
	15.10eh_mtl_element_matrix.cpp	133
	15.11ei_mtl_insert_class_expensive.cpp	135
16	Day 19: MTL Continued	136
10	16.1 ej_mtl_insert_scope.cpp	136
	16.2 ek_mtl_array_initialization.cpp	138
	16.3 el_mtl_vector_expr.cpp	139
	16.4 em_mtl_rich_vector_expr.cpp	140
	16.5 en_mtl_matrix_expressions1.cpp	141
	16.6 eo_mtl_matrix_expressions2.cpp	$141 \\ 142$
	16.7 ep_mtl_matrix_expressions3.cpp	143
	16.8 eq_mtl_matrix_vector1.cpp	143
	16.9 er_mtl_matrix_vector2.cpp	145
	16.10es_mtl_vector_norm.cpp	146
	16.11et_mtl_matrix_norm.cpp	140 147
		148
	16.12eu_mtl_vector_reduction.cpp	149
	16.13ev_mtl_vector_min_max.cpp	$149 \\ 150$
	16.14ew_mtl_dot_example.cpp	150 151
	16.15ex_mtl_conj_trans_hermitian.cpp	
	16.16ey_mtl_sub_matrices.cpp	152
	16.17ez_mtl_permutation.cpp	154
	16.18fa_mtl_reordering.cpp	155
	16.19fb_mtl_reordering2.cpp	156
	16.20fc_mtl_reordering3.cpp	157
	16.21fd_mtl_indirection.cpp	158
	16.22fe_mtl_upper.cpp	159
	16.23ff_mtl_lower.cpp	160
	16.24fg_mtl_bands.cpp	161
	16.25fh_mtl_rank_one_and_two_update.cpp	162
	16.26fi_mtl_other.cpp	163
	16.27fj_mtl_eigenvalue_example.cpp	164

16.28fk_mtl_eigenvalue_example2.cpp				 							165
$16.29 fl_mtl_qr_givens_example.cpp$				 							167

1 Day 1: Basic input/output

1.1 aa_hello_world.c

```
// C program to print "Hello World".
// Rajeev Singh
// 2013-03-27

#include <stdio.h>
int main() {
    printf("Hello World from C\n");
    return 0;
}
```

${\bf 1.2}\quad ab_hello_world.cpp$

```
// C++ program to print "Hello World".
//
// Rajeev Singh
// 2013-03-27

#include <iostream>
int main() {
    std::cout << "Hello World from C++";// << std::endl;
    return 0;
}</pre>
```

${\bf 1.3 \quad ac_hello_world.cpp}$

```
// C++ program to print "Hello World".
//
// Rajeev Singh
// 2013-03-27

#include <iostream>
using namespace std;
int main() {
    cout << "Hello World from C++" << endl;
    return 0;
}</pre>
```

1.4 ad_powers_of_integer.cpp

```
// Program to calculate powers of given integer.
// Rajeev Singh
// 2013-03-27
#include <iostream>
#include <cmath>
using namespace std;
int main() {
    //int given_number;
    long int given_number;
    cout << "Enter an integer: ";</pre>
    cin >> given_number;
    cout << "Given number = " << given_number << endl</pre>
          << "Square = " << pow(given_number,2) << endl
<< "Cube = " << pow(given_number,3) << endl</pre>
          << "Forth power = " << pow(given_number,4) << endl;
    return 0;
}
```

1.5 ae_powers_of_real.cpp

```
// Program to calculate powers of given integer.
// Rajeev Singh
// 2013-03-27
#include <iostream>
#include <cmath>
using namespace std;
int main() {
    double given_number;
    //long double given_number;
    cout << "Enter a real number : ";</pre>
    cin >> given_number;
    cout << "Given number = " << given_number << endl</pre>
          << "Square = " << pow(given_number,2) << endl
<< "Square root = " << pow(given_number,1./2) << endl</pre>
          << "Cube = " << pow(given_number,3) << endl</pre>
          << "Forth power = " << pow(given_number,4) << endl;
    return 0;
}
```

2 Day 2: Pointers/References, Arithmetic/Logical

2.1 af_pointer.cpp

```
// Program to illustrate pointers.
//
// Rajeev Singh
// 2013-03-28
#include <iostream>
using namespace std;
int main() {
   int *np = NULL;
    int n = 10;
    cout << "Initial" << endl</pre>
         << "n = " << n << endl
         << "np = " << np << endl
         << "*np = " << "since np is NULL, printing *np gives segmentation fault"
<< endl << endl;
    np = &n;
    cout << "After: np = &n" << endl</pre>
         << "n = " << n << end1
         << "np = " << np << endl
         << "*np = " << *np << endl << endl;
    *np = 22;
    cout << "After: *np = 22" << end1</pre>
         << "n = " << n << endl
         << "np = " << np << end1
         << "*np = " << *np << endl << endl;
   return 0;
}
```

2.2 ag_reference.cpp

```
// Program to illustrate the use of references (special pointers).
// Rajeev Singh
// 2013-03-28
#include <iostream>
using namespace std;
int main() {
    int n = 5;
    int & r = n;
    int m;
    cout << "Initial" << endl</pre>
         << "n = " << n << end1
         << "r = " << r << end1
         << "m = " << m << endl << endl;
    m = r + 3; // m == n + 3
    cout << "After: m = r + 3" << endl
         << "n = " << n << endl
         << "r = " << r << end1
         << "m = " << m << endl << endl;
    r = m;
                 // r still points to n and n == m
    cout << "After: r = m" << endl</pre>
         << "n = " << n << endl
         << "r = " << r << endl
         << "m = " << m << endl << endl;
              // r and n are unchanged
    cout << "After: m = 0" << end1</pre>
         << "n = " << n << endl
         << "r = " << r << endl
         << "m = " << m << endl << endl;
    int & s = m;
                // r still points to n and n == m (== 0)
    r = s;
    cout << "After: r = s where s is new reference to m" << end1</pre>
         << "n = " << n << endl
         << "r = " << r << end1
         << "m = " << m << endl << endl;
   return 0;
}
```

2.3 ah_arithmetic_operators.cpp

```
// Program to illustrate basic arithmetic operators.
// Rajeev Singh
// 2013-03-28
#include <iostream>
using namespace std;
int main() {
   int m = 100,
        n = 200;
    cout << "Initial" << endl</pre>
         << "m = " << m << end1
         << "n = " << n << end1
         << "m + n = " << m + n << end1
         << "m - n = " << m - n << end1
         << "m * n = " << m * n << endl
         << "m / n = " << m / n << endl
         << "m \% n = " << m \% n << endl << endl;
    //m = m + 200;
    m += 200;
                    // both this commands are same
    cout << "After: m += 200" << end1</pre>
         << "m = " << m << end1
         << "n = " << n << end1
         << "m + n = " << m + n << endl
         << "m - n = " << m - n << endl
         << "m * n = " << m * n << endl
         << "m / n = " << m / n << endl
         << "m \% n = " << m \% n << endl << endl;
    m++;
    cout << "After: m++" << endl</pre>
         << "m = " << m << end1
         << "n = " << n << end1
         << "m + n = " << m + n << end1
         << "m - n = " << m - n << end1
         << "m * n = " << m * n << endl
         << "m / n = " << m / n << endl
         << "m \% n = " << m \% n << endl << endl;
   return 0;
```

2.4 ai_relational_logical.cpp

```
// program to illustrate logical and relational operators.
// Rajeev Singh
// 2013-03-28
#include <iostream>
using namespace std;
int main() {
   int x = 2;
   int y = 4;
   int z = 4;
   bool b;
   cout << "x = " << x << end1
        << "y = " << y << endl
        << "z = " << z << endl << endl;
   // z == 4 is not tested
   b = (x == 2 \&\& y == 3 \&\& z == 4);
   << "b = " << b << endl << endl;
   // only x == 2 is tested
   b = (x == 2 | | y == 3 | | z == 4);
   cout << "b = ( x == 2 \mid | y == 3 \mid | z == 4 )" << endl
        << "b = " << b << endl << endl;
   // correct, since x \neq 0 in "y/x"
   b = (x != 0 \&\& y/x > 1);
   cout << "b = (x != 0 \&\& y/x > 1)" << endl
        << "b = " << b << endl << endl;
   return 0;
}
```

3 Day 3: Scope, Conditional, Loops

3.1 aj_blocks_scope.cpp

```
// program to illustrate blocks.
// Rajeev Singh
// 2013-03-29
#include <iostream>
using namespace std;
int main() {
   { // block 1
      int n1 = 1;
       double f1 = 0.0;
       cout << "n1 = " << n1 << endl;
       cout << "f1 = " << f1 << endl;</pre>
   }
   { // block 2
       int n1 = 2;
       // n1 has value 2 in this block
       //int n1 = 5; // ERROR
   }
   return 0;
}
```

3.2 ak_scope.cpp

```
// program to illustrate scope of variables
// Rajeev Singh
// 2013-03-29
#include <iostream>
using namespace std;
int main() {
    { // block 1
        int m, n1 = 1;
        { // block 1.1
            int n2 = 2;
            { // block 1.1.1
                m = n1 + n2; // evaluates to m = 3
                cout << "Block 1.1.1: m = " << m << endl;</pre>
            }
        }
        { // block 1.2
            int n2 = 3;
            m = n1 + n2;
                            // evaluates to m = 4
            cout << "Block 1.2 : m = " << m << endl;</pre>
        }
    }
    return 0;
}
```

3.3 al_if_else.cpp

```
\begin{tabular}{ll} // program & to & illustrate & conditional & structure \\ \end{tabular}
// Rajeev Singh
// 2013-03-29
#include <iostream>
using namespace std;
int main() {
    int n = 1;
    if (n > 0)
        n = n / n;
    if (n < 0)
        n += 5; // NOTE: trivial block!
         cout << "hello " << n << endl;</pre>
    else if ( n \%2 == 0 ) {
        n += 1;
         cout << "hello " << n << endl;</pre>
    else {
        n -= 6;
        cout << "hello " << n << endl;</pre>
    cout << "n = " << n << endl;</pre>
    return 0;
}
```

3.4 am_for_loop.cpp

```
// program to illustrate for loop
//
// Rajeev Singh
// 2013-03-29

#include <iostream>
using namespace std;

int main() {
   int n = 1;

   for (int i=1; i<10; i++) {
      if (i>5) {
            n *= i;
            cout << "n = " << n << endl;
      }
   }

   return 0;
}</pre>
```

3.5 an_while_loop.cpp

```
// program to illustrate while loop
//
// Rajeev Singh
// 2013-03-29

#include <iostream>
using namespace std;

int main() {
    int n = 1;
    int i = 1;

    while (i < 10) {
        n *= i;
        i++;
        cout << "n = " << n << endl;
    }

    return 0;
}</pre>
```

3.6 ao_do_while_loop.cpp

```
// program to illustrate do-while loop
//
// Rajeev Singh
// 2013-03-29

#include <iostream>
using namespace std;

int main() {
    int n = 1;
    int i = 100;

    do {
        n *= i;
        i++;
        cout << "n = " << n << endl;
    } while (i < 10);

    return 0;
}</pre>
```

3.7 ap_break.cpp

```
// program to illustrate use of break
//
// Rajeev Singh
// 2013-03-29
#include <iostream>
using namespace std;
int main() {
    int n = 1;
    for ( int i = 1; i < 20; i++ ) {
        // avoid overflow
        if ( n > 21474836 )
            break;
        n *= i;
        cout << "n = " << n << endl;</pre>
    }
   return 0;
}
```

${\bf 3.8}\quad aq_break_nested_loop.cpp$

```
// program to illustrate behavior of break in nested loops
// Rajeev Singh
// 2013-03-29
#include <iostream>
using namespace std;
int main() {
   for ( int i = 1; i < 20; i++ ) {
       int n = 1;
        for ( int j = 1; j < i; j++ ) {
           if (n > 21474836)
               break;
           n *= j;
        }
       cout << "n = " << n << endl;
    }
   return 0;
}
```

$3.9 \quad ar_break_all_loops.cpp$

```
// program to illustrate breaking all nested loops
// Rajeev Singh
// 2013-03-29
#include <iostream>
using namespace std;
int main() {
    int flag = 0;
    for ( int i = 1; i < 20; i++ ) {
        int n = 1;
        for ( int j = 1; j < i; j++ ) {
            if (n > 21474836) {
                flag = 1;
                break;
            }
            n *= j;
        }
        if (flag == 1)
           break;
        cout << "n = " << n << endl;</pre>
    }
   return 0;
}
```

4 Day 4: Functions, Call by value/reference

4.1 as_function_square.cpp

4.2 at_function_factorial.cpp

```
// program to illustrate defining the factorial function
// Rajeev Singh
// 2013-03-31
#include <iostream>
using namespace std;
factorial (const int n) {
   int f = 1;
    for (int i = 1; i \le n; i++)
       f *= i;
   return f;
}
int main() {
   int m = 10;
    cout << "m = " << m << endl
         << "m! = " << factorial(m) << endl;
   return 0;
```

4.3 au_function_call_by_value.cpp

```
// program to illustrate call by value feature
// Rajeev Singh
// 2013-03-31
#include <iostream>
using namespace std;
int
f (int n) {
  n = 10;
  return n;
int main() {
   int m = 5;
  cout << "funtion output = " << f(m) << endl;</pre>
   return 0;
}
```

4.4 av_function_call_by_reference.cpp

```
// program to illustrate call by reference feature
// Rajeev Singh
// 2013-03-31
#include <iostream>
using namespace std;
int
f (int & n) {
  n = 10;
  return n;
int main() {
   int m = 5;
   cout << "funtion output = " << f(m) << endl;</pre>
   return 0;
}
```

${\bf 4.5 \quad aw_function_call_by_reference_using_pointers.cpp}$

```
// program to illustrate call by reference feature using general
// pointers
// Rajeev Singh
// 2013-03-31
#include <iostream>
using namespace std;
int
f (int * n) {
  *\mathbf{n} = 10;
   return *n;
}
int main() {
   int m = 5;
   cout << "funtion output = " << f(&m) << endl;</pre>
   return 0;
}
```

4.6 ax_function_multiple_return_values.cpp

```
// program to illustrate funtions with multiple return values using
// call by reference
// Rajeev Singh
// 2013-03-31
#include <iostream>
using namespace std;
void
min_max ( const int n1, const int n2,
 int & min, int & max );
int main() {
   int m1, m2, min, max;
    cout << "Enter two integers :";</pre>
   cin >> m1 >> m2;
   min_max(m1, m2, min, max);
   << "min(m1,m2) = " << min << endl
        << "max(m1,m2) = " << max << endl;
   return 0;
}
void
min_max ( const int n1, const int n2,
  int & min, int & max ) {
   if (n1 < n2) {
       min = n1;
       max = n2;
   }
    else {
       min = n2;
       max = n1;
   }
}
```

5 Day 5: Functions- default args, function pointers; Arrays

5.1 ay_function_default_arguments.cpp

```
// program to illustrate function with default arguments
//
// Rajeev Singh
// 2013-04-01

#include <iostream>
using namespace std;

double
square (const double x = 10.0) {
    return x*x;
}

int main() {
    double a = 2.5;

    cout << "a = " << a << endl;
    cout << "a^2 = " << square(a) << endl;
    cout << "square() = " << square() << endl;
    return 0;
}</pre>
```

5.2 az_function_inline.cpp

```
/* program to illustrate inline functions
 st WARNING: do not inline functions with large bodies. it can cause
          the final executable to be very large in size and decrease
           performance.
 * Rajeev Singh
 * 2013-04-01
*/
#include <iostream>
using namespace std;
inline double
square (const double x = 10.0) {
   return x*x;
int main() {
   double a = 2.5;
   cout << "square() = " << square() << endl;</pre>
  return 0;
}
```

5.3 ba_function_pointers.cpp

```
/* program to illustrate function pointers
* Rajeev Singh
* 2013-04-01
 */
#include <iostream>
using namespace std;
double
square (const double x) {
   return x*x;
int main() {
    double a = 2.5;
    double (* pf) (const double x);
    pf = square;
   cout << "a
                     = " << a << endl;
    cout << "square(a) = " << square(a) << endl;</pre>
    cout << "pf(a) = " << pf(a) << endl;
   return 0;
}
```

5.4 bb_function_pointers_as_arguments.cpp

```
/* program to illustrate funtion pointers as arguments
 * Rajeev Singh
 * 2013-04-01
 */
#include <iostream>
using namespace std;
double
square (const double x) {
   return x*x;
double
cube (const double x) {
   return x*x*x;
double
f ( double ( * func ) ( const double x ),
 const double x ) {
   return func( x );
int main() {
    double a = 2.5;
    cout << "a = " << a << endl;
cout << "f(square, a) = " << f(square, a) << endl;</pre>
    cout << "a
    cout << "f(cube, a) = " << f(cube, a) << endl;</pre>
   return 0;
}
```

5.5 bc_static_variables.cpp

```
/* program to illustrate static variables
 * Rajeev Singh
* 2013-04-01
 */
#include <iostream>
using namespace std;
double
f ( const double x, long & cnt ) {
    static long counter = 0; // allocated and initialised
                            // once per program
   cnt = ++counter;
    return 2.0*x*x - x;
}
int main() {
   long cnt = 0;
    for ( double x = -10; x \le 10.0; x += 0.1 )
        f(x, cnt);
    cout << "num times f called = " << cnt << endl;</pre>
   return 0;
}
```

5.6 bd_array.cpp

```
/* program to illustrate array
 * Rajeev Singh
 * 2013-04-01
 */
#include <iostream>
using namespace std;
int main() {
    double f[5];
    for ( int i = 0; i < 5; i++ )
        f[i] = 2*i;
    cout << "f = " << f << endl;</pre>
    for ( int i = 0; i < 5; i++ )
        cout << "f[" << i << "] = " << f[i] << endl;
    cout << "f[5] = " << f[5] << endl; // bug but program still compiles</pre>
    // if you lucky such bugs will be detected by segmentation fault
   return 0;
```

${\bf 5.7} \quad be_function_with_array_argument.cpp$

```
/* program to illustrate arrays as function arguments
 * Rajeev Singh
 * 2013-04-01
 */
#include <iostream>
using namespace std;
void
copy (const double x[3], double y[3]) {
    for ( int i = 0; i < 3; i++ )
        y[i] = x[i];
}
void
add ( const double x[3], double y[3] ) {
    for ( int i = 0; i < 3; i++ )
        y[i] += x[i];
}
int main() {
    double a[3],
           b[] = \{0, 0, 0\}; // b \text{ is automaticall of size } 3
    for ( int i = 0; i < 3; i++ )
        a[i] = 2*i;
    cout << "Intial a and b:" << endl;</pre>
    for ( int i = 0; i < 3; i++ )
        cout << "a[" << i << "] = " << a[i]
             << " b[" << i << "] = " << b[i] << endl;
    copy( a, b );
    cout << endl << "After calling copy funtion:" << endl;</pre>
    for ( int i = 0; i < 3; i++ )
        cout << "a[" << i << "] = " << a[i]
             << " b[" << i << "] = " << b[i] << endl;
    add( a, b );
    cout << endl << "After calling sum funtion:" << endl;</pre>
    for ( int i = 0; i < 3; i++ )
        cout << "a[" << i << "] = " << a[i]
             << " b[" << i << "] = " << b[i] << endl;
    return 0;
}
```

5.8 bf_multidimensional_arrays.cpp

```
/* program to illustrate multidimensional arrays
 * Rajeev Singh
 * 2013-04-01
 */
#include <iostream>
using namespace std;
void
mulvec ( const double M[3][3],
          const double x[3],
               double y[3] ) {
    for ( int i = 0; i < 3; i++ ) {
        y[i] = 0.0;
        for ( int j = 0; j < 3; j++ )
             y[i] += M[i][j] * x[j];
    }
}
int main() {
    double M[3][3],
            x[3], y[3];
    for ( int i = 0; i < 3; i++ ) {
        x[i] = 2*i;
         for ( int j = 0; j < 3; j++ )
             M[i][j] = 3*i+j;
    }
    mulvec(M, x, y);
    cout << "M:" << endl;</pre>
    for ( int i = 0; i < 3; i++ ) {
        for ( int j = 0; j < 3; j++ )
             cout << " " << M[i][j];</pre>
    cout << endl;</pre>
    cout << "x:" << endl;</pre>
    for ( int j = 0; j < 3; j++ )
         cout << " " << x[j] << endl;</pre>
    cout << "y = M*x:" << endl;</pre>
    for ( int j = 0; j < 3; j++ )
         cout << " " << y[j] << endl;</pre>
    return 0;
}
```

5.9 bg_array_and_pointer.cpp

```
/* program to illustrate pointers as arrays
 * in {\it C/C++} there is NO distinction between a pointer and an array.
 * Rajeev Singh
 * 2013-04-01
 */
#include <iostream>
using namespace std;
int main() {
    int n[5] = \{ 2, 3, 5, 7, 11 \};
    int * p = n;
int * q = &n[1];
    cout << "n:" << endl;</pre>
    for ( int j = 0; j < 5; j++ )
         cout << " " << n[j] << endl;</pre>
    cout << "p:" << endl;</pre>
    for ( int j = 0; j < 5; j++ )
         cout << " " << p[j] << endl;</pre>
    cout << "q:" << endl;</pre>
    for ( int j = 0; j < 5; j++ )
         cout << " " << q[j] << endl;</pre>
    return 0;
}
```

6 Day 6: Dynamic memory, Multidimensional Array, BLAS

6.1 bh_dynamic_memory.cpp

```
/* program to illustrate dynamic memory
 * this example shows the C++ way of doing the job. this will not work
 * for C.
 * Rajeev Singh
 * 2013-04-02
 */
#include <iostream>
using namespace std;
int main() {
   int n = 10;
    double * v = new double[n];
    for ( int i = 0; i < n; i++ )
        v[i] = double(i*i);
    cout << "n = " << n << endl;
    cout << "v:" << endl;</pre>
    for ( int j = 0; j < n; j++ )
        cout << " " << v[j] << endl;</pre>
    delete[] v;
    return 0;
}
```

6.2 bi_dynamic_array_size_input.cpp

```
/* program to illustrate dynamic memory
 * Rajeev Singh
 * 2013-04-02
 */
#include <iostream>
using namespace std;
int main() {
    int n;
    cout << "Enter the size of the array: ";</pre>
    cin >> n;
    double * v = new double[n];
    for ( int i = 0; i < n; i++ )
         v[i] = double( i*i );
    cout << "n = " << n << endl;</pre>
    cout << "v:" << endl;</pre>
    for ( int j = 0; j < n; j++ )
        cout << " " << v[j] << endl;
    delete[] v;
    return 0;
```

6.3 bj_multidimensional_array_with_pointer.cpp

```
/* program to illustrate dynamic memory
 * Rajeev Singh
 * 2013-04-02
 */
#include <iostream>
using namespace std;
int main() {
    int n1[4], n2[4], n3[4], n4[4];
                                    // p1 -> pointer
    int * p1 = n1;
    int * p2 = n2;
    int * p3 = n3;
    int * p4 = n4;
    int *p[4] = \{p1, p2, p3, p4\}; // p \rightarrow pointer of pointers
    for (int i = 0; i < 4; i++)
        for (int j = 0; j < 4; j++)
            p[i][j] = 4*i+j;
    cout << "p:" << endl;</pre>
    for (int i = 0; i < 4; i++) {
        for (int j = 0; j < 4; j++)
           cout << " " << p[i][j];
        cout << endl;</pre>
    return 0;
}
```

6.4 bk_multidimensional_dynamic_array.cpp

```
/* program to illustrate dynamic memory
 * Rajeev Singh
 * 2013-04-02
 */
#include <iostream>
using namespace std;
int main() {
    int * p1 = new int[4];
    int * p2 = new int[4];
    int * p3 = new int[4];
    int * p4 = new int[4];
    int **p = new int*[4];
    p[0] = p1;
    p[1] = p2;
    p[2] = p3;
    p[3] = p4;
    for (int i = 0; i < 4; i++)
        for (int j = 0; j < 4; j++)
             p[i][j] = 4*i+j;
    cout << "p:" << endl;</pre>
    for (int i = 0; i < 4; i++) {
        for (int j = 0; j < 4; j++ )
    cout << " " << p[i][j];</pre>
        cout << endl;</pre>
    }
    return 0;
}
```

6.5 bl_multidimensional_dynamic_array_size_input.cpp

```
/* program to illustrate dynamic memory
 * Rajeev Singh
 * 2013-04-02
 */
#include <iostream>
using namespace std;
int main() {
   int m, n;
    cout << "Enter the size of the matrix: ";</pre>
    cin >> m >> n;
    int **p = new int*[m];
    for (int i = 0; i < m; i++)
        p[i] = new int[n];
    for (int i = 0; i < m; i++)
        for (int j = 0; j < n; j++)
            p[i][j] = n*i+j;
    cout << "p:" << endl;</pre>
    for (int i = 0; i < m; i++) {
        for (int j = 0; j < n; j++)
           cout << " " << p[i][j];
        cout << endl;</pre>
    }
   return 0;
}
```

6.6 bm_multidimensional_array_with_mapping.cpp

```
/* program to illustrate dynamic memory
 * NOTE: using pointer of pointers can be slower than using mappings
 * for big arrays for the following reason:
 * pointer of pointers -> two access to RAM to get an element
 * mapping
                        -> single access to RAM for the same
 st accessing RAM is much more expensive than simple integer
 * multiplication and addition
 * Rajeev Singh
 * 2013-04-02
 */
#include <iostream>
using namespace std;
int main() {
   int m, n;
    cout << "Enter the size of the matrix: ";</pre>
    cin >> m >> n;
    int *p = new int[m*n];
    for (int i = 0; i < m; i++)
        for (int j = 0; j < n; j++)
            p[n*i+j] = n*i+j;
    cout << "p:" << endl;</pre>
    for (int i = 0; i < m; i++) {
        for (int j = 0; j < n; j++)
cout << " " << p[n*i+j];
        cout << endl;</pre>
    }
    return 0;
}
```

GO TO THE TALK TO DISCUSS BLAS

7 Day 7: String, Advanced Datatypes, BLAS, Sparse Matrices

7.1 bn_strings.cpp

```
/* program to illustrate strings as array of characters
 * Rajeev Singh
 * 2013-04-03
 */
#include <iostream>
using namespace std;
int main() {
    char str1[] = { 'S', 't', 'r', 'i', 'n', 'g', '\0' };
    char str2[] = "String"; // '\0' is appended automatically
    char str3[] = "This is a very long \
string";
    cout << str1 << endl;</pre>
    cout << str2 << endl;</pre>
    cout << str3 << endl;</pre>
    return 0;
}
```

7.2 bo_typedef.cpp

```
/* program to illustrate renaming datatypes using typedef

*
    *Rajeev Singh
    * 2013-04-03
    *
    */

#include <iostream>
using namespace std;

int main() {
    typedef char * string_t;
    string_t str2 = "String"; // '\0' is appended automatically string_t str3 = "This is a very long \
string";

    cout << str2 << endl;
    cout << str3 << endl;
    return 0;
}</pre>
```

7.3 bp_struct.cpp

```
/* program to illustrate defining new datatypes using struct
 * Rajeev Singh
 * 2013-04-03
 */
#include <iostream>
using namespace std;
typedef double real_t;
struct vector_t {
   size_t size;
    real_t * coeffs;
};
void
add_vec ( const vector_t & x,
          const vector_t & y,
          vector_t & z ) {
    for ( int i = 0; i < x.size; i++ )
        z.coeffs[i] = x.coeffs[i] + y.coeffs[i];
}
int main() {
   int n = 10;
    vector_t a, b, c;
    a.size = n;
    b.size = n;
    c.size = n;
    a.coeffs = new real_t[n];
    b.coeffs = new real_t[n];
    c.coeffs = new real_t[n];
    for ( int i = 0; i < n; i++ ) {
        a.coeffs[i] = i;
        b.coeffs[i] = 2*i;
    add_vec( a, b, c );
    cout << "a:" << endl;</pre>
    cout << "a.size = " << a.size << endl;</pre>
    cout << "a.coeffs:" << endl;</pre>
    for ( int i = 0; i < n; i++ )
                         " << a.coeffs[i] << endl;
        cout << "
    cout << "b:" << endl;</pre>
    cout << "b.size = " << b.size << endl;</pre>
    cout << "b.coeffs:" << endl;</pre>
```

7.4 bq_struct_pointer.cpp

```
/* program to illustrate using pointers to struct
 * Rajeev Singh
 * 2013-04-03
 */
#include <iostream>
using namespace std;
typedef double real_t;
struct vector_t {
   size_t size;
    real_t * coeffs;
};
void
add_vec ( const vector_t * x,
          const vector_t * y,
          vector_t * z ) {
    for ( int i = 0; i < x->size; i++ )
        z->coeffs[i] = x->coeffs[i] + y->coeffs[i];
}
int main() {
    int n = 10;
    vector_t * a = new vector_t,
             * b = new vector_t,
             * c = new vector_t;
    a \rightarrow size = n;
    b \rightarrow size = n;
    c \rightarrow size = n;
    a->coeffs = new real_t[n];
    b->coeffs = new real_t[n];
    c->coeffs = new real_t[n];
    for ( int i = 0; i < n; i++ ) {
       a->coeffs[i] = i;
        b \rightarrow coeffs[i] = 2*i;
    add_vec( a, b, c );
    cout << "a:" << endl;</pre>
    cout << "a->size = " << a->size << endl;</pre>
    cout << "a->coeffs:" << endl;</pre>
    for ( int i = 0; i < n; i++ )
        cout << "
                       " << a->coeffs[i] << endl;
```

```
cout << "b:" << endl;</pre>
    cout << "b->size = " << b->size << endl;</pre>
    cout << "b->coeffs:" << endl;</pre>
    for ( int i = 0; i < n; i++ )
                          " << b->coeffs[i] << endl;
        cout << "
    cout << "c:" << endl;</pre>
    cout << "c->size = " << c->size << endl;</pre>
    cout << "c->coeffs:" << endl;</pre>
    for ( int i = 0; i < n; i++ )
                          " << c->coeffs[i] << endl;
        cout << "
    delete[] a->coeffs;
    delete[] b->coeffs;
    delete[] c->coeffs;
    delete a;
    delete b;
    delete c;
   return 0;
}
```

7.5 br_struct_array.cpp

```
/* program to illustrate using struct array
 * Rajeev Singh
 * 2013-04-03
 */
#include <iostream>
using namespace std;
typedef double real_t;
struct vector_t {
   size_t size;
    real_t * coeffs;
};
void
add_vec ( const vector_t * x,
          const vector_t * y,
          vector_t * z ) {
    for ( int i = 0; i < x->size; i++ )
        z->coeffs[i] = x->coeffs[i] + y->coeffs[i];
}
int main() {
    int n = 10;
    vector_t * a = new vector_t[3];
    for ( int i = 0; i < 3; i++ ) {
        a[i].size = n;
        a[i].coeffs = new real_t[n];
    for ( int i = 0; i < n; i++ ) {
        a[0].coeffs[i] = i;
        a[1].coeffs[i] = 2*i;
    add_vec( &a[0], &a[1], &a[2] );
    cout << "a[0]:" << endl;</pre>
    cout << "a[0].size = " << a[0].size << endl;</pre>
    cout << "a[0].coeffs:" << endl;</pre>
    for ( int i = 0; i < n; i++ )
                         " << a[0].coeffs[i] << endl;
        cout << "
    cout << "a[1]:" << endl;</pre>
    cout << "a[1].size = " << a[1].size << endl;</pre>
    cout << "a[1].coeffs:" << endl;</pre>
    for ( int i = 0; i < n; i++ )
        cout << "
                        " << a[1].coeffs[i] << endl;
```

GO TO THE TALK TO DISCUSS BLAS AND SPARSE MATRICES

8 Day 9: Modules and Namespaces, Classes GO TO THE TALK TO DISCUSS MODULES AND NAMESPACES

8.1 bs_struct_with_functions.cpp

```
/* program to illustrate using struct with functions as members
 * Rajeev Singh
 * 2013-04-05
 */
#include <iostream>
using namespace std;
typedef double real_t;
struct vector_t {
   size_t size;
    real_t * coeffs;
    void init ( const unsigned n );
    void del ();
    void fill ( const real_t f );
    void scale ( const real_t f );
    void print ();
};
int main() {
   vector_t x;
   x.init(10);
    x.print();
    x.fill(1.0);
    x.print();
   x.scale(5.0);
   x.print();
   x.del();
    return 0;
}
void vector_t::init (const unsigned n ) {
   size = n;
    coeffs = new real_t[n];
}
void vector_t::del () {
   delete[] coeffs;
}
void vector_t::fill ( const real_t f ) {
    for (int i = 0; i < size; i++)
        coeffs[i] = f;
}
void vector_t::scale ( const real_t f ) {
   for (int i = 0; i < size; i++ )
```

8.2 bt_struct_constructor_destructor.cpp

```
/* program to illustrate using struct with special functions for
 * construction and destruction of objects
 * Rajeev Singh
 * 2013-04-05
 */
#include <iostream>
using namespace std;
typedef double real_t;
struct vector_t {
    size_t size;
    real_t * coeffs;
    vector_t ( const unsigned n );
    ~vector_t ();
    void fill ( const real_t f );
    void scale ( const real_t f );
    void print ();
};
int main() {
   vector_t x(10);
    x.print();
    x.fill(1.0);
    x.print();
    x.scale(5.0);
    x.print();
    return 0;
}
vector_t::vector_t (const unsigned n ) {
    size = n;
    coeffs = new real_t[n];
vector_t::~vector_t () {
    delete[] coeffs;
void vector_t::fill ( const real_t f ) {
    for (int i = 0; i < size; i++)
        coeffs[i] = f;
}
void vector_t::scale ( const real_t f ) {
    for (int i = 0; i < size; i++ )</pre>
        coeffs[i] *= f;
```

9 Day 10: Classes Continued

9.1 bu_struct_this_pointer.cpp

```
/* program to illustrate the use of this pointer
 * members
 * Rajeev Singh
 * 2013-04-07
 */
#include <iostream>
using namespace std;
typedef double real_t;
struct vector_t {
private:
   size_t size;
    real_t * coeffs;
public:
    vector_t ( const unsigned n );
    ~vector_t ();
    void fill ( const real_t
                                f );
    void scale ( const real_t
    void add ( const real_t alpha, const vector_t & a );
    void print () const;
};
int main() {
    vector_t x(10), y(10);
    x.fill( 1.0 );
    y.fill( 2.0 );
    cout << "x:" << endl;</pre>
    x.print();
    cout << "y:" << endl;</pre>
    y.print();
    x.add( 10.0, y );
    cout << "x:" << endl;</pre>
    x.print();
    cout << "y:" << endl;</pre>
    y.print();
    return 0;
}
vector_t::vector_t (const unsigned n ) {
    size = n;
    coeffs = new real_t[n];
vector_t::~vector_t () {
```

```
delete[] coeffs;
void vector_t::fill ( const real_t f ) {
   for (int i = 0; i < size; i++ )
       coeffs[i] = f;
}
void vector_t::scale ( const real_t f ) {
   for (int i = 0; i < size; i++ )
       coeffs[i] *= f;
}
void vector_t::add ( const real_t alpha, const vector_t & a ) {
   for (int i = 0; i < this -> size; i++)
      this->coeffs[i] += alpha * a.coeffs[i];
}
void vector_t::print () const {
   cout << "size = " << size << endl;</pre>
    cout << "coeffs:" << endl;</pre>
   for (int i = 0; i < size; i++)
       }
```

9.2 bv_copy_constructor.cpp

```
/* program to illustrate the use of copy constructor
 * members
 * Rajeev Singh
 * 2013-04-07
 */
#include <iostream>
using namespace std;
typedef double real_t;
struct vector_t {
private:
    size_t size;
    real_t * coeffs;
public:
    vector_t ( const unsigned n );
    vector_t ( const vector_t & a );
    ~vector_t ();
   void fill ( const real_t f );
    void add ( const real_t alpha, const vector_t & a );
    void print () const;
};
int main() {
    vector_t x(10);
    x.fill( 1.0 );
    cout << "x:" << endl;</pre>
    x.print();
    vector_t y(x);
    cout << "y:" << endl;</pre>
    y.print();
   x.scale(5.0);
    cout << "x:" << endl;</pre>
    x.print();
    cout << "y:" << endl;</pre>
    y.print();
    return 0;
}
vector_t::vector_t (const unsigned n ) {
    size = n;
    coeffs = new real_t[n];
}
```

```
vector_t::vector_t (const vector_t & a ) {
    this->size = a.size;
    this->coeffs = new real_t[a.size];
    for (int i = 0; i < a.size; i++ )</pre>
        this->coeffs[i] = a.coeffs[i];
}
vector_t::~vector_t () {
    delete[] coeffs;
void vector_t::fill ( const real_t f ) {
   for (int i = 0; i < size; i++ )
        coeffs[i] = f;
}
void vector_t::scale ( const real_t f ) {
    for (int i = 0; i < size; i++)
        coeffs[i] *= f;
}
void vector_t::add ( const real_t alpha, const vector_t & a ) {
    for (int i = 0; i < this->size; i++)
        this->coeffs[i] += alpha * a.coeffs[i];
}
void vector_t::print () const {
    cout << "size = " << size << endl;</pre>
    cout << "coeffs:" << endl;</pre>
    for (int i = 0; i < size; i++)
        cout << "
                    " << coeffs[i] << endl;
}
```

9.3 bw_default_copy_constructor.cpp

```
/* program to illustrate the problem with the default copy constructor
 * members
 * Rajeev Singh
 * 2013-04-07
 */
#include <iostream>
using namespace std;
typedef double real_t;
struct vector_t {
private:
    size_t size;
    real_t * coeffs;
public:
    vector_t ( const unsigned n );
    //~vector_t ();
    void fill ( const real_t f );
    void scale ( const real_t f );
void add ( const real_t alpha, const vector_t & a );
    void print () const;
};
int main() {
    vector_t x(10);
    x.fill( 1.0 );
    cout << "x:" << endl;</pre>
    x.print();
    vector_t y(x);
    cout << "y:" << endl;</pre>
    y.print();
    x.scale(5.0);
    cout << "x:" << endl;</pre>
    x.print();
    cout << "y:" << endl;</pre>
    y.print();
    return 0;
vector_t::vector_t (const unsigned n ) {
    size = n;
    coeffs = new real_t[n];
}
/*
```

```
vector_t::~vector_t () {
   delete[] coeffs;
*/
void vector_t::fill ( const real_t f ) {
   for (int i = 0; i < size; i++ )
       coeffs[i] = f;
}
void vector_t::scale ( const real_t f ) {
   for (int i = 0; i < size; i++ )
       coeffs[i] *= f;
}
void vector_t::add ( const real_t alpha, const vector_t & a ) {
   for (int i = 0; i < this->size; i++)
       this->coeffs[i] += alpha * a.coeffs[i];
}
void vector_t::print () const {
   cout << "size = " << size << endl;</pre>
    cout << "coeffs:" << endl;</pre>
   for (int i = 0; i < size; i++ )
       }
```

9.4 bx_struct_with_const_functions.cpp

```
/* program to illustrate using struct with const functions
 * Rajeev Singh
 * 2013-04-05
 */
#include <iostream>
using namespace std;
typedef double real_t;
struct vector_t {
   size_t size;
   real_t * coeffs;
    vector_t ( const unsigned n );
    ~vector_t ();
   void fill ( const real_t f );
    void scale ( const real_t f );
   void print () const;
};
int main() {
   const vector_t x(10);
   x.print();
   //x.fill(1.0); // error
   //x.print();
   //x.scale(5.0); // error
   //x.print();
   return 0;
}
vector_t::vector_t (const unsigned n ) {
   size = n;
    coeffs = new real_t[n];
}
vector_t::~vector_t () {
   delete[] coeffs;
}
void vector_t::fill ( const real_t f ) {
   for (int i = 0; i < size; i++ )
       coeffs[i] = f;
void vector_t::scale ( const real_t f ) {
   for (int i = 0; i < size; i++)
       coeffs[i] *= f;
}
```

```
void vector_t::print () const {
    cout << "size = " << size << endl;
    cout << "coeffs:" << endl;
    for (int i = 0; i < size; i++ )
        cout << " " << coeffs[i] << endl;
}</pre>
```

9.5 by_struct_visibility.cpp

```
/* program to illustrate using struct with different visibility for
* members
 * Rajeev Singh
 * 2013-04-05
 */
#include <iostream>
using namespace std;
typedef double real_t;
struct vector_t {
private:
    size_t size;
    real_t * coeffs;
public:
    vector_t ( const unsigned n );
    ~vector_t ();
   void fill ( const real_t f );
    void scale ( const real_t f );
    void print () const;
};
int main() {
   vector_t x(10);
    x.print();
    x.fill( 1.0 );
   x.print();
   x.scale(5.0);
    x.print();
    //cout << x.size << endl; // error
   return 0;
}
vector_t::vector_t (const unsigned n ) {
    size = n;
    coeffs = new real_t[n];
vector_t::~vector_t () {
    delete[] coeffs;
void vector_t::fill ( const real_t f ) {
    for (int i = 0; i < size; i++ )
        coeffs[i] = f;
}
```

9.6 bz_safely_changing_size_of_array.cpp

```
/* program to illustrate using visibility to change the size of array
 * safely
 * Rajeev Singh
 * 2013-04-07
 */
#include <iostream>
using namespace std;
typedef double real_t;
struct vector_t {
private:
    size_t size;
   real_t * coeffs;
public:
    vector_t ( const unsigned n );
    ~vector_t ();
   int get_size ();
    void set_size ( const unsigned n );
    void fill ( const real_t f );
    void scale ( const real_t     f );
    void print () const;
};
int main() {
    vector_t x(10);
   x.print();
   x.fill(1.0);
    x.print();
   x.scale(5.0);
   x.print();
    cout << "Size of x = " << x.get_size() << endl;</pre>
    x.set_size( 4 );
   x.print();
    return 0;
}
vector_t::vector_t (const unsigned n ) {
    size = n;
    coeffs = new real_t[n];
vector_t::~vector_t () {
    delete[] coeffs;
int vector_t::get_size () {
```

```
return size;
void vector_t::set_size ( const unsigned n ) {
    if (size != n) {
        size = n;
        delete coeffs; // delete the old data
        coeffs = new real_t[n];
    }
}
void vector_t::fill ( const real_t f ) {
   for (int i = 0; i < size; i++)
        coeffs[i] = f;
}
void vector_t::scale ( const real_t f ) {
    for (int i = 0; i < size; i++)
        coeffs[i] *= f;
}
void vector_t::print () const {
    cout << "size = " << size << endl;</pre>
    cout << "coeffs:" << endl;</pre>
    for (int i = 0; i < size; i++ )</pre>
        cout << "
                       " << coeffs[i] << endl;
}
```

10 Day 11: Classes Continued, Templates

10.1 ca_operator_overloading.cpp

```
/* program to illustrate operator overloading
 * safely
 * Rajeev Singh
 * 2013-04-08
 */
#include <iostream>
using namespace std;
typedef double real_t;
struct vector_t {
private:
   size_t size;
   real_t * coeffs;
public:
    vector_t ( const unsigned n );
    ~vector_t ();
    int get_size ();
    void set_size ( const unsigned n );
    void fill ( const real_t f );
    void scale ( const real_t f );
    void print () const;
    vector_t & operator += (const vector_t & a) {
        for (size_t i = 0; i < size; i++ )
            coeffs[i] += a.coeffs[i];
        return *this;
    }
    vector_t & operator -= (const vector_t & a) {
        for (size_t i = 0; i < size; i++ )
            coeffs[i] -= a.coeffs[i];
        return *this;
};
int main() {
    vector_t x(4), y(4);
    x.fill(3.0);
    y.fill( 1.0 );
    x.print();
    y.print();
    x += y;
    x.print();
    y.print();
```

```
return 0;
}
vector_t::vector_t (const unsigned n ) {
    size = n;
    coeffs = new real_t[n];
}
vector_t::~vector_t () {
    delete[] coeffs;
}
int vector_t::get_size () {
   return size;
}
void vector_t::set_size ( const unsigned n ) {
    if (size != n) {
        size = n;
        delete coeffs; // delete the old data
        coeffs = new real_t[n];
    }
}
void vector_t::fill ( const real_t f ) {
   for (int i = 0; i < size; i++ )
        coeffs[i] = f;
void vector_t::scale ( const real_t f ) {
    for (int i = 0; i < size; i++)
        coeffs[i] *= f;
}
void vector_t::print () const {
    cout << "size = " << size << endl;</pre>
    cout << "coeffs:" << endl;</pre>
    for (int i = 0; i < size; i++ )
        cout << "
                    " << coeffs[i] << endl;
}
```

$10.2 \quad cb_templates.cpp$

```
/* program to illustrate generic programming using templates
* safely
 * Rajeev Singh
 * 2013-04-08
 */
#include <iostream>
using namespace std;
template <typename T>
T square(const T f) {
   return f*f;
}
int main() {
    double x = square( 2.1 );
   int m = square(2);
   cout << "x = : " << x << endl;
    cout << "m = : " << m << endl;</pre>
   return 0;
```

GO TO THE TALK TO DISCUSS BLAS AND TEMPLATES

11 Day 14: STL

OPEN http://www.cplusplus.com/reference/

11.1 cc_list.cpp

```
/* program to illustrate lists from STL
 * Rajeev Singh
 * 2013-04-11
 */
#include <iostream>
#include <list>
using namespace std;
int main() {
    list < int > ilist;
    ilist.push_front( 1 );
    ilist.push_front( 2 );
    ilist.push_back( 3 );
    ilist.push_back( 4 );
    for ( list<int>::iterator it = ilist.begin(); it != ilist.end(); it++)
        cout << *it << endl;</pre>
    int sum = 0;
    while ( ! ilist.empty() ) {
        sum += ilist.front();
        ilist.pop_front();
    cout << "Sum of the list = " << sum << endl;</pre>
    return 0;
}
```

11.2 cd_vector.cpp

```
/* program to illustrate vector from STL
 * Rajeev Singh
 * 2013-04-11
 */
#include <iostream>
#include <vector>
using namespace std;
int main() {
    vector< int > ivector;
    ivector.push_back( 1 );
    ivector.push_back( 2 );
    ivector.push_back( 3 );
    ivector.push_back( 4 );
    for ( vector<int>::iterator it = ivector.begin(); it != ivector.end(); it++)
        cout << *it << endl;</pre>
    cout << endl;</pre>
    for ( int i = 0; i < ivector.size(); i++ )</pre>
        cout << ivector[i] << endl;</pre>
    int sum = 0;
    while ( ! ivector.empty() ) {
        sum += ivector.back();
        ivector.pop_back();
    cout << "Sum of the vector = " << sum << endl;</pre>
    return 0;
}
```

11.3 ce_valarray.cpp

```
/* program to illustrate valarray from STL
 * Example taken from:
 * http://www.cplusplus.com/reference/valarray/valarray/operators/
 * Rajeev Singh
 * 2013-04-11
 */
// valarray operators example
#include <iostream>
#include <valarray>
using namespace std;
void print_all( valarray<int> & foo, valarray<int> & bar ) {
 cout << endl << "foo: " << "bar:" << endl;</pre>
 for (int i = 0; i < foo.size(); i++ )
     }
int main () {
 int init[] = {10,20,30,40};
                               // foo:
                                                   bar:
 valarray<int> foo (init, 4); // 10 20 30 40
                              // 10 20 30 40 25 25 25 25
 valarray<int> bar (25,4);
 print_all(foo, bar);
                              // 10 20 30 40 35 45 55 65
 bar += foo;
 print_all(foo, bar);
                               // 45 55 65 75 35 45 55 65
 foo = bar + 10;
 print_all(foo, bar);
 foo -= 10;
                               // 35 45 55 65 35 45 55 65
 print_all(foo, bar);
 valarray < bool > comp = (foo == bar);
 if ( comp.min() == true )
         cout << "They are equal.\n";</pre>
  else
         cout << "They are not equal.\n";</pre>
 return 0;
}
```

11.4 cf_complex_numbers.cpp

```
/* program to illustrate complex numbers from STL
 * Rajeev Singh
 * 2013-04-11
 */
#include <iostream>
#include <complex>
using namespace std;
int main () {
    complex < float > c1;
    c1.real() = 1.0;
    c1.imag() = -2.0;
    cout << "c1 = " << c1 << endl << endl;</pre>
    complex < double > I ( 0.0, 1.0 );
    complex < double > r ( 5.0 );
    complex < double > z;
    complex < double > i = I;
    cout << "I = " << I << endl;
    cout << "r = " << r << endl;
    cout << "z = " << z << endl;
    cout << "i = " << i << endl;
    cout << endl;</pre>
    cout << " sqrt( r + i ) = " << sqrt( r + i ) << endl;</pre>
    cout << " sin(r + i) = " << sin(r + i) << endl;
  return 0;
}
```

11.5 cg_auto_pointer.cpp

GO TO THE TALK TO DISCUSS THE NEED FOR AUTO POINTER

```
/* program to illustrate the use of auto-pointers from STL
* Rajeev Singh
 * 2013-04-11
 */
#include <iostream>
#include <memory>
using namespace std;
int main () {
    {
        double x[100];
        double * y = new double[100];
    } // "x" is deallocated, but not "y"
        double x[100];
        auto_ptr < double > y( new double[100] );
    } // both "x" and "y" are deallocated
    cout << "done" << endl;</pre>
 return 0;
}
```

12 Day 15: Boost

OPEN Boost Document

12.1 ch_boost_array.cpp

```
/* program to illustrate the use of boost::array
 * Rajeev Singh
 * 2013-04-12
 */
#include <iostream>
#include <boost/array.hpp>
using namespace std;
using namespace boost;
void print_all( array<int,4> & foo, array<int,4> & bar ) {
 cout << endl << "foo: " << "bar:" << endl;</pre>
 for (int i = 0; i < foo.size(); i++ )</pre>
     int main () {
                             // foo:
 array<int,4> foo = {10,20,30,40}; // 10 20 30 40
 array<int,4> bar = {25}; // 10 20 30 40 25 25 25 25
 print_all(foo, bar);
 //foo += bar; // doesn't work as '+' is not overloaded
              // not really sure what is the use of it
 return 0;
```

12.2 ci_boost_multi_array.cpp

```
/* program to illustrate the use of boost::multi_array
 * example taken from the documentation of Boost.MultiArray
 * Rajeev Singh
 * 2013-04-12
 */
#include <iostream>
#include "boost/multi_array.hpp"
#include <cassert>
using namespace std;
int
main () {
  // Create a 3D array that is 3 x 4 x 2
  typedef boost::multi_array<double, 3> array_type;
  typedef array_type::index index;
  array_type A(boost::extents[3][4][2]);
  // Assign values to the elements
  int values = 0;
  for(index i = 0; i != 3; ++i)
    for(index j = 0; j != 4; ++ j)
      for(index k = 0; k != 2; ++k)
        A[i][j][k] = values++;
  // Verify values
  int verify = 0;
  for(index i = 0; i != 3; ++i) {
    for(index j = 0; j != 4; ++j) {
      for(index k = 0; k != 2; ++k) {
        assert(A[i][j][k] == verify++);
        cout << A[i][j][k] << " ";</pre>
      } // k
      cout << endl;</pre>
    } // j
    cout << endl;</pre>
  } // i
  return 0;
```

12.3 cj_boost_mulitprecision_cpp_int.cpp

```
/* program to illustrate the use of boost::multiprecision
 * example taken from boost document
 * Rajeev Singh
 * 2013-04-12
 */
#include <boost/multiprecision/cpp_int.hpp>
using namespace boost::multiprecision;
int main () {
    int128_t v = 1;
    // Do some fixed precision arithmetic:
    for(unsigned i = 1; i \le 20; ++i)
       v *= i;
    std::cout << v << std::endl; // prints 20!
    // Repeat at arbitrary precision:
    cpp_int u = 1;
    for(unsigned i = 1; i \le 100; ++i)
       u *= i;
    std::cout << u << std::endl; // prints 100!
    return 0;
}
```

12.4 ck_boost_mulitprecision_gmp.cpp

```
/* program to illustrate the use of boost::multiprecision
 * example taken from boost document
 * compile command:
   g++ -I /home/rajeev/software/general/boost_1_53_0/
    ck\_boost\_mulitprecision\_gmp.cpp -lgmp
 * Rajeev Singh
 * 2013-04-12
 */
#include <boost/multiprecision/gmp.hpp>
using namespace boost::multiprecision;
int main () {
   mpz_int v = 1;
    // Do some arithmetic:
    for(unsigned i = 1; i \le 1000; ++i)
       v *= i;
    std::cout << v << std::endl; // prints 1000!
    // Access the underlying representation:
    mpz_t z;
    mpz_init(z);
    mpz_set(z, v.backend().data());
   return 0;
}
```

12.5 cl_boost_mulitprecision_cpp_int_2.cpp

```
/* program to illustrate the use of boost::multiprecision
 * example taken from boost document
 * Rajeev Singh
 * 2013-04-12
 */
#include <boost/multiprecision/cpp_int.hpp>
#include <iostream>
#include <iomanip>
#include <vector>
void print_factorials()
{
   using boost::multiprecision::cpp_int;
   // Print all the factorials that will fit inside a 128-bit integer.
   //
   // Begin by building a big table of factorials, once we know just how
   // large the largest is, we'll be able to "pretty format" the results.
   // Calculate the largest number that will fit inside 128 bits, we could
   // also have used numeric_limits<int128_t>::max() for this value:
   cpp_int limit = (cpp_int(1) << 128) - 1;</pre>
   //
   // Our table of values:
   std::vector<cpp_int> results;
   // Initial values:
   unsigned i = 1;
   cpp_int factorial = 1;
   // Cycle through the factorials till we reach the limit:
   while(factorial < limit)</pre>
      results.push_back(factorial);
      factorial *= i;
   }
   //
   // Lets see how many digits the largest factorial was:
   unsigned digits = results.back().str().size();
   /\!/\!\!\!\!/ \  \, \text{Now print them out, using right justification, while we're at it}
   // we'll indicate the limit of each integer type, so begin by defining
   // the limits for 16, 32, 64 etc bit integers:
   cpp_int limits[] = {
      (cpp_int(1) << 16) - 1,
      (cpp_int(1) << 32) - 1,
      (cpp_int(1) << 64) - 1,
```

```
(cpp_int(1) << 128) - 1,
   };
   std::string bit_counts[] = { "16", "32", "64", "128" };
   unsigned current_limit = 0;
   for(unsigned j = 0; j < results.size(); ++j)</pre>
      if(limits[current_limit] < results[j])</pre>
      {
         std::string message = "Limit of " + bit_counts[current_limit] + " bit integ
         std::cout << std::setfill('.') << std::setw(digits+1) << std::right << mes</pre>
         ++current_limit;
      }
      std::cout << std::setw(digits + 1) << std::right << results[j] << std::endl;</pre>
   }
}
int main() {
    print_factorials();
    return 0;
}
```

$12.6 \quad cm_boost_random_uniform.cpp$

```
/* program to illustrate the use of boost::random
 * Rajeev Singh
* 2013-04-12
 */
#include <iostream>
#include <boost/random/mersenne_twister.hpp>
#include <boost/random/uniform_real.hpp>
using namespace std;
int main (void) {
    boost::random::mt19937 generator;
    boost::uniform_real<> uni_dist(0,1);
    int i, j;
    for (i = 0; i < 100; i++)
        cout << uni_dist(generator) << endl;</pre>
   return 0;
}
```

12.7 cn_boost_ublas_vector.cpp

$12.8 \quad co_boost_ublas_unit_vector.cpp$

```
/* program to illustrate the use of boost::numeric::ublas

* example taken from boost document

*
    Rajeev Singh
    * 2013-04-12

*
    *
    */

#include <boost/numeric/ublas/vector.hpp>
#include <boost/numeric/ublas/io.hpp>

int main () {
    using namespace boost::numeric::ublas;
    for (int i = 0; i < 3; ++ i) {
        unit_vector<double> v (3, i);
        std::cout << v << std::endl;
    }
}</pre>
```

$12.9 \quad cp_boost_ublas_zero_vector.cpp$

$12.10 \quad cq_boost_ublas_scalar_vector.cpp$

$12.11 \quad cr_boost_ublas_sparse_vector_mapped.cpp$

12.12 cs_boost_ublas_sparse_vector_compressed.cpp

12.13 ct_boost_ublas_sparse_vector_coordinate.cpp

```
/* program to illustrate the use of boost::numeric::ublas

* example taken from boost document

* Rajeev Singh

* 2013-04-12

*

*include <boost/numeric/ublas/vector_sparse.hpp>
#include <boost/numeric/ublas/io.hpp>

int main () {
    using namespace boost::numeric::ublas;
    coordinate_vector<double> v (6, 3);
    for (unsigned i = 0; i < v.size ()/2; ++ i)
        v (2*i) = i+10;
    std::cout << v << std::endl;
}</pre>
```

13 Day 16: Boost Continued

OPEN Boost Document

13.1 cu_boost_ublas_vector_expressions_conj_etc.cpp

```
/* program to illustrate the use of boost::numeric::ublas
 * example taken from boost document
 * Rajeev Singh
 * 2013-04-14
#include <boost/numeric/ublas/vector.hpp>
#include <boost/numeric/ublas/io.hpp>
int main () {
    using namespace boost::numeric::ublas;
    vector<std::complex<double> > v (3);
    for (unsigned i = 0; i < v.size (); ++ i)
        v (i) = std::complex < double > (i, i);
    std::cout << - v << std::endl;
    std::cout << conj (v) << std::endl;</pre>
    std::cout << real (v) << std::endl;</pre>
    std::cout << imag (v) << std::endl;</pre>
    std::cout << trans (v) << std::endl;</pre>
    std::cout << herm (v) << std::endl;</pre>
}
```

13.2 cv_boost_ublas_vector_expressions_binary.cpp

```
/* program to illustrate the use of boost::numeric::ublas

* example taken from boost document

* Rajeev Singh

* 2013-04-14

*

*/

#include <boost/numeric/ublas/vector.hpp>
#include <boost/numeric/ublas/io.hpp>

int main () {
    using namespace boost::numeric::ublas;
    vector<double> v1 (3), v2 (3);
    for (unsigned i = 0; i < std::min (v1.size (), v2.size ()); ++ i)
        v1 (i) = v2 (i) = i;

    std::cout << v1 + v2 << std::endl;
    std::cout << v1 - v2 << std::endl;
}</pre>
```

13.3 cw_boost_ublas_vector_expressions_outer_prod.cpp

13.4 cx_boost_ublas_vector_expressions_scalar_multi.cpp

13.5 cy_boost_ublas_vector_expressions_reductions.cpp

```
/* program to illustrate the use of boost::numeric::ublas
 * example taken from boost document
 * Rajeev Singh
 * 2013-04-14
 */
#include <boost/numeric/ublas/vector.hpp>
int main () {
    using namespace boost::numeric::ublas;
    vector < double > v (3);
    for (unsigned i = 0; i < v.size (); ++ i)
        v(i) = i;
    std::cout << sum (v) << std::endl;</pre>
    std::cout << norm_1 (v) << std::endl;
    std::cout << norm_2 (v) << std::endl;</pre>
    std::cout << norm_inf (v) << std::endl;</pre>
    std::cout << index_norm_inf (v) << std::endl;</pre>
}
```

13.6 cz_boost_ublas_vector_expressions_inner_prod.cpp

$13.7 \quad da_boost_ublas_matrix_basic.cpp$

13.8 db_boost_ublas_matrix_special.cpp

```
/* program to illustrate the use of boost::numeric::ublas
 * example taken from boost document
 * Rajeev Singh
 * 2013-04-14
 */
#include <boost/numeric/ublas/matrix.hpp>
#include <boost/numeric/ublas/io.hpp>
int main () {
    using namespace boost::numeric::ublas;
    identity_matrix < double > m (3);
    std::cout << "Identity:" << std::endl;</pre>
    std::cout << m << std::endl;</pre>
    }
    {
    zero_matrix < double > m (3, 3);
    std::cout << "Zero:" << std::endl;</pre>
    std::cout << m << std::endl;</pre>
    scalar_matrix < double > m (3, 3);
    std::cout << "Scalar:" << std::endl;</pre>
    std::cout << m << std::endl;</pre>
}
```

13.9 dc_boost_ublas_triangular_matrix.cpp

```
/* program to illustrate the use of boost::numeric::ublas
 * example taken from boost document
 * Rajeev Singh
 * 2013-04-14
 */
#include <boost/numeric/ublas/triangular.hpp>
#include <boost/numeric/ublas/io.hpp>
int main () {
    using namespace boost::numeric::ublas;
    triangular_matrix < double, lower > ml (3, 3);
    for (unsigned i = 0; i < ml.size1 (); ++ i)
        for (unsigned j = 0; j \le i; ++ j)
            ml(i, j) = 3 * i + j;
    std::cout << ml << std::endl;</pre>
    triangular_matrix < double, upper > mu (3, 3);
    for (unsigned i = 0; i < mu.size1 (); ++ i)
        for (unsigned j = i; j < mu.size2 (); ++ j)
            mu(i, j) = 3 * i + j;
    std::cout << mu << std::endl;</pre>
```

13.10 dd_boost_ublas_symmetric_matrix.cpp

```
/* program to illustrate the use of boost::numeric::ublas
 * example taken from boost document
 * Rajeev Singh
 * 2013-04-14
 */
#include <boost/numeric/ublas/symmetric.hpp>
#include <boost/numeric/ublas/io.hpp>
int main () {
    using namespace boost::numeric::ublas;
    symmetric_matrix < double, lower > ml (3, 3);
    for (unsigned i = 0; i < ml.size1 (); ++ i)
        for (unsigned j = 0; j \le i; ++ j)
            ml(i, j) = 3 * i + j;
    std::cout << ml << std::endl;</pre>
    symmetric_matrix < double, upper > mu (3, 3);
    for (unsigned i = 0; i < mu.size1 (); ++ i)
        for (unsigned j = i; j < mu.size2 (); ++ j)
            mu(i, j) = 3 * i + j;
    std::cout << mu << std::endl;</pre>
```

13.11 de_boost_ublas_hermitian_matrix.cpp

```
/* program to illustrate the use of boost::numeric::ublas
 * example taken from boost document
 * Rajeev Singh
 * 2013-04-14
 */
#include <boost/numeric/ublas/hermitian.hpp>
#include <boost/numeric/ublas/io.hpp>
int main () {
    using namespace boost::numeric::ublas;
    hermitian_matrix<std::complex<double>, lower> ml (3, 3);
    for (unsigned i = 0; i < ml.size1 (); ++ i) {
        for (unsigned j = 0; j < i; ++ j)
            ml(i, j) = std::complex < double > (3 * i + j, 3 * i + j);
        ml (i, i) = std::complex < double > (4 * i, 0);
    std::cout << ml << std::endl;</pre>
    hermitian_matrix<std::complex<double>, upper> mu (3, 3);
    for (unsigned i = 0; i < mu.size1 (); ++ i) {</pre>
        mu (i, i) = std::complex < double > (4 * i, 0);
        for (unsigned j = i + 1; j < mu.size2 (); ++ j)
            mu (i, j) = std::complex < double > (3 * i + j, 3 * i + j);
    std::cout << mu << std::endl;</pre>
```

13.12 df_boost_ublas_banded_matrix.cpp

13.13 dg_boost_ublas_sparse_matrix.cpp

```
/* program to illustrate the use of boost::numeric::ublas
 * example taken from boost document
 * Rajeev Singh
 * 2013-04-14
 */
#include <boost/numeric/ublas/matrix_sparse.hpp>
#include <boost/numeric/ublas/io.hpp>
int main () {
    using namespace boost::numeric::ublas;
        mapped_matrix < double > m (3, 3, 3 * 3);
        for (unsigned i = 0; i < m.size1 (); ++ i)</pre>
            for (unsigned j = 0; j < m.size2 (); ++ j)
                m(i, j) = 3 * i + j;
        std::cout << m << std::endl;</pre>
    }
    {
        compressed_matrix < double > m (3, 3, 3 * 3);
        for (unsigned i = 0; i < m.size1 (); ++ i)
            for (unsigned j = 0; j < m.size2 (); ++ j)
                 m(i, j) = 3 * i + j;
        std::cout << m << std::endl;</pre>
    }
        coordinate_matrix < double > m (3, 3, 3 * 3);
        for (unsigned i = 0; i < m.size1 (); ++ i)
            for (unsigned j = 0; j < m.size2 (); ++ j)
                 m(i, j) = 3 * i + j;
        std::cout << m << std::endl;</pre>
    }
}
```

13.14 dh_boost_ublas_matrix_expressions_conj_etc.cpp

```
/* program to illustrate the use of boost::numeric::ublas
 * example taken from boost document
 * Rajeev Singh
 * 2013-04-14
 */
#include <boost/numeric/ublas/matrix.hpp>
#include <boost/numeric/ublas/io.hpp>
int main () {
    using namespace boost::numeric::ublas;
    matrix < std::complex < double > > m (3, 3);
    for (unsigned i = 0; i < m.size1 (); ++ i)
        for (unsigned j = 0; j < m.size2 (); ++ j)
             m (i, j) = std::complex < double > (3 * i + j, 3 * i + j);
    std::cout << - m << std::endl;</pre>
    std::cout << conj (m) << std::endl;</pre>
    std::cout << real (m) << std::endl;</pre>
    std::cout << imag (m) << std::endl;</pre>
    std::cout << trans (m) << std::endl;</pre>
    std::cout << herm (m) << std::endl;</pre>
}
```

13.15 di_boost_ublas_matrix_expressions_binary.cpp

13.16 dj_boost_ublas_matrix_expressions_scalar_multi.cpp

```
/* program to illustrate the use of boost::numeric::ublas
 * example taken from boost document
 * Rajeev Singh
 * 2013-04-14
 */
#include <boost/numeric/ublas/matrix.hpp>
#include <boost/numeric/ublas/io.hpp>
int main () {
    using namespace boost::numeric::ublas;
    matrix < double > m (3, 3);
    for (unsigned i = 0; i < m.size1 (); ++ i)
        for (unsigned j = 0; j < m.size2 (); ++ j)
            m(i, j) = 3 * i + j;
    std::cout << 2.0 * m << std::endl;
    std::cout << m * 2.0 << std::endl;
}
```

13.17 dk_boost_ublas_matrix_expressions_matrix_vector_multi.cpp

```
/* program to illustrate the use of boost::numeric::ublas
 * example taken from boost document
 * Rajeev Singh
 * 2013-04-14
 */
#include <boost/numeric/ublas/matrix.hpp>
#include <boost/numeric/ublas/io.hpp>
int main () {
    using namespace boost::numeric::ublas;
    matrix < double > m (3, 3);
    vector < double > v (3);
    for (unsigned i = 0; i < std::min (m.size1 (), v.size ()); ++ i) {
        for (unsigned j = 0; j < m.size2 (); ++ j)
            m(i, j) = 3 * i + j;
        v(i) = i;
    }
    std::cout << prod (m, v) << std::endl;</pre>
    std::cout << prod (v, m) << std::endl;</pre>
}
```

13.18 dl_boost_ublas_matrix_expressions_matrix_vector_triangular_solver.

```
/* program to illustrate the use of boost::numeric::ublas
 * example taken from boost document
 * Rajeev Singh
 * 2013-04-14
 */
#include <boost/numeric/ublas/triangular.hpp>
#include <boost/numeric/ublas/io.hpp>
int main () {
    using namespace boost::numeric::ublas;
    matrix < double > m (3, 3);
    vector < double > v (3);
    for (unsigned i = 0; i < std::min (m.size1 (), v.size ()); ++ i) {
        for (unsigned j = 0; j \le i; ++ j)
            m(i, j) = 3 * i + j + 1;
        v (i) = i;
    }
    std::cout << solve (m, v, lower_tag ()) << std::endl;</pre>
    std::cout << solve (v, m, lower_tag ()) << std::endl;</pre>
}
```

13.19 dm_boost_ublas_matrix_expressions_matrix_matrix_multi.cpp

13.20 dn_boost_ublas_matrix_expressions_matrix_matrix_triangular_solver

14 Day 17: Boost Continued

OPEN Boost Document

14.1 do_mpi.cpp

```
/* program to illustrate the use of boost::mpi
 * example taken from boost document
 * Rajeev Singh
 * 2013-04-15
 */
#include <mpi.h>
#include <iostream>
int main(int argc, char* argv[])
  MPI_Init(&argc, &argv);
  int rank;
  MPI_Comm_rank(MPI_COMM_WORLD, &rank);
  if (rank == 0) {
   int value = 17;
   int result = MPI_Send(&value, 1, MPI_INT, 1, 0, MPI_COMM_WORLD);
    if (result == MPI_SUCCESS)
      std::cout << "Rank 0 OK!" << std::endl;</pre>
  } else if (rank == 1) {
    int value;
    int result = MPI_Recv(&value, 1, MPI_INT, 0, 0, MPI_COMM_WORLD,
                           MPI_STATUS_IGNORE);
    if (result == MPI_SUCCESS && value == 17)
      std::cout << "Rank 1 OK!" << std::endl;</pre>
  }
 MPI_Finalize();
  return 0;
```

14.2 dp_boost_mpi_1.cpp

```
/* program to illustrate the use of boost::mpi
 * example taken from boost document
 * compile command:
 * mpic++-I /home/rajeev/software/general/boost_1_53_0
 * dp\_boost\_mpi\_1.cpp -lboost\_mpi
 * Rajeev Singh
 * 2013-04-15
 */
#include <boost/mpi/environment.hpp>
#include <boost/mpi/communicator.hpp>
#include <iostream>
namespace mpi = boost::mpi;
int main(int argc, char* argv[])
 mpi::environment env(argc, argv);
 mpi::communicator world;
  std::cout << "I am process " << world.rank() << " of " << world.size()</pre>
            << "." << std::endl;
 return 0;
}
```

14.3 dq_boost_mpi_point_to_point.cpp

```
/* program to illustrate the use of boost::mpi
 * example taken from boost document
 * compile command:
 * \quad \textit{mpic++} \quad \textit{dq\_boost\_mpi\_point\_to\_point.cpp} \quad \textit{-lboost\_mpi}
   -lboost\_serialization
 * Rajeev Singh
 * 2013-04-15
 */
#include <boost/mpi.hpp>
#include <iostream>
#include <string>
#include <boost/serialization/string.hpp>
namespace mpi = boost::mpi;
int main(int argc, char* argv[])
  mpi::environment env(argc, argv);
  mpi::communicator world;
  if (world.rank() == 0) {
    world.send(1, 0, std::string("Hello"));
    std::string msg;
    world.recv(1, 1, msg);
    std::cout << msg << "!" << std::endl;
  } else {
    std::string msg;
    world.recv(0, 0, msg);
    std::cout << msg << ", ";
   std::cout.flush();
    world.send(0, 1, std::string("world"));
  return 0;
}
```

14.4 dr_boost_mpi_non_blocking.cpp

```
/* program to illustrate the use of boost::mpi
 * example taken from boost document
 * Rajeev Singh
 * 2013-04-15
 */
#include <boost/mpi.hpp>
#include <iostream>
#include <string>
#include <boost/serialization/string.hpp>
namespace mpi = boost::mpi;
int main(int argc, char* argv[])
 mpi::environment env(argc, argv);
 mpi::communicator world;
  if (world.rank() == 0) {
   mpi::request reqs[2];
    std::string msg, out_msg = "Hello";
    reqs[0] = world.isend(1, 0, out_msg);
    reqs[1] = world.irecv(1, 1, msg);
    mpi::wait_all(reqs, reqs + 2);
   std::cout << msg << "!" << std::endl;
  } else {
    mpi::request reqs[2];
    std::string msg, out_msg = "world";
    reqs[0] = world.isend(0, 1, out_msg);
    reqs[1] = world.irecv(0, 0, msg);
    mpi::wait_all(reqs, reqs + 2);
   std::cout << msg << ", ";
 return 0;
```

14.5 ds_boost_mpi_broadcast.cpp

```
/* program to illustrate the use of boost::mpi
 * example taken from boost document
 * Rajeev Singh
 * 2013-04-15
 */
#include <boost/mpi.hpp>
#include <iostream>
#include <string>
#include <boost/serialization/string.hpp>
namespace mpi = boost::mpi;
int main(int argc, char* argv[])
 mpi::environment env(argc, argv);
 mpi::communicator world;
  std::string value;
  if (world.rank() == 0) {
   value = "Hello, World!";
  broadcast(world, value, 0);
  std::cout << "Process #" << world.rank() << " says " << value
            << std::endl;
 return 0;
}
```

14.6 dt_boost_mpi_gather.cpp

```
/* program to illustrate the use of boost::mpi
 * example taken from boost document
 * Rajeev Singh
 * 2013-04-15
 */
#include <boost/mpi.hpp>
#include <iostream>
#include <vector>
#include <cstdlib>
namespace mpi = boost::mpi;
int main(int argc, char* argv[])
 mpi::environment env(argc, argv);
 mpi::communicator world;
  std::srand(time(0) + world.rank());
  int my_number = std::rand();
  if (world.rank() == 0) {
   std::vector<int> all_numbers;
    gather(world, my_number, all_numbers, 0);
    for (int proc = 0; proc < world.size(); ++proc)</pre>
      std::cout << "Process #" << proc << " thought of "</pre>
                << all_numbers[proc] << std::endl;
  } else {
    gather(world, my_number, 0);
 return 0;
```

14.7 du_boost_mpi_reduce.cpp

```
/* program to illustrate the use of boost::mpi
 * example taken from boost document
 * Rajeev Singh
 * 2013-04-15
 */
#include <boost/mpi.hpp>
#include <iostream>
#include <cstdlib>
namespace mpi = boost::mpi;
int main(int argc, char* argv[])
 mpi::environment env(argc, argv);
 mpi::communicator world;
  std::srand(time(0) + world.rank());
  int my_number = std::rand();
  if (world.rank() == 0) {
   int minimum;
   reduce(world, my_number, minimum, mpi::minimum <int >(), 0);
   std::cout << "The minimum value is " << minimum << std::endl;</pre>
    reduce(world, my_number, mpi::minimum <int >(), 0);
 return 0;
```

14.8 dv_boost_mpi_reduce_2.cpp

```
/* program to illustrate the use of boost::mpi
 * example taken from boost document
 * Rajeev Singh
 * 2013-04-15
 */
#include <boost/mpi.hpp>
#include <iostream>
#include <string>
#include <functional>
#include <boost/serialization/string.hpp>
namespace mpi = boost::mpi;
int main(int argc, char* argv[])
 mpi::environment env(argc, argv);
 mpi::communicator world;
 std::string result;
  reduce(world,
        world.rank() < 10? names[world.rank()]</pre>
                        : std::string("many "),
        result, std::plus<std::string>(), 0);
  if (world.rank() == 0)
   std::cout << "The result is " << result << std::endl;</pre>
 return 0;
```

$14.9 \quad dw_boost_python_hello_world.cpp$

```
/* program to illustrate the use of boost::python
 * example taken from boost document
 * compile command:
 * \quad \textit{g++-shared-fPIC-o-a.so-dw\_boost\_python\_hello\_world.cpp-I}
 * \quad /usr/include/python2.7 \ -lpython2.7 \ -lboost\_python
 * Rajeev Singh
 * 2013-04-15
 */
#include <Python.h>
#include <boost/python.hpp>
char const* greet()
   return "hello, world";
}
BOOST_PYTHON_MODULE(a)
    using namespace boost::python;
    def("greet", greet);
}
```

14.10 dx_boost_python_exposing_classes.cpp

```
/* program to illustrate the use of boost::python
 * example taken from boost document
 * compile command:
 * \quad \textit{g++-shared -fPIC -o a.so } dx\_boost\_python\_exposing\_classes.cpp \quad \textit{-I}
   /usr/include/python2.7 -lpython2.7 -lboost_python
 * Rajeev Singh
 * 2013-04-15
 */
#include <boost/python.hpp>
using namespace boost::python;
struct World
{
    void set(std::string msg) { this->msg = msg; }
    std::string greet() { return msg; }
    std::string msg;
};
BOOST_PYTHON_MODULE(a)
    class_<World>("World")
        .def("greet", &World::greet)
        .def("set", &World::set)
}
```

15 Day 18: MTL

Open MTL Document

15.1 dy_mtl_vector1.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-16
 */
// File: vector1.cpp
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
int main(int, char**)
    using namespace mtl;
    // Define dense vector of doubles with 10 elements all set to 0.0.
    dense_vector < double > v(20, 0.0);
    // Set element 7 to 3.0.
    v[7] = 3.0;
    std::cout << "v is " << v << "\n";
   return 0;
}
```

15.2 dz_mtl_vector2.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-16
 */
// File: vector2.cpp
#include <complex>
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
int main(int, char**)
{
    using namespace mtl;
    // Define dense vector of complex with 7 elements.
    dense_vector < std::complex <float >, mtl::vector::parameters < tag::row_major > >
v(7);
    // Set all elements to 3+2i
    v= std::complex <float > (3.0, 2.0);
    std::cout << "v is " << v << "\n";
    // Set all elements to 5+0i
    v = 5.0;
    std::cout << "v is " << v << "\n";</pre>
    std::cout << "v is " << v << "\n";
    return 0;
}
```

15.3 ea_mtl_dense2D.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-16
 */
// File: dense2D.cpp
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
int main(int, char**)
   using namespace mtl;
    // A is a row-major matrix
                                A(10, 10);
    dense2D < double >
   A = -5.0;
   // Assign a value to a matrix element
   A(2, 3) = 7.0;
   // You can also use a more C-like notation
    A[2][4] = 3.0;
    std::cout << "A is \n" << A << "\n";
    // B is a column-major matrix
    dense2D < float, matrix::parameters < tag::col_major > B(10, 10);
    // Assign the identity matrix times 3 to B
   std::cout << "B is \n" << B << "\n";
   return 0;
}
```

15.4 eb_mtl_morton_dense.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-16
 */
// File: morton_dense.cpp
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
int main(int, char**)
    using namespace mtl;
    // Z-order matrix
    morton_dense < double , recursion::morton_z_mask > A(10, 10);
    A = 0;
    A(2, 3) = 7.0;
    A[2][4] = 3.0;
    std::cout << "A is \n" << A << "\n";
    // B is an N-order matrix with column-major 4x4 blocks, see paper
    morton_dense <float, recursion::doppled_4_col_mask > B(10, 10);
    // Assign the identity matrix times 3 to {\it B}
    std::cout << "B is \n" << B << "\n";
    return 0;
}
```

15.5 ec_mtl_compressed2D.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-16
 */
// File: compressed2D.cpp
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
int main(int, char**)
    using namespace mtl;
    // CRS matrix
    compressed2D < double > A(12, 12);
    // Laplace operator discretized on a 3x4 grid
    matrix::laplacian_setup(A, 3, 4);
    std::cout << "A is \n" << A;
    // Element access is allowed for reading
    std::cout << "A[3][2] is " << A[3][2] << "\n\n";
    std::cout << "A[3][1] is " << A[3][1] << "\n\n";
    // CCS matrix
    compressed2D <float, matrix::parameters <tag::col_major> > B(10, 10);
    // Assign the identity matrix times 3 to B
    B = 3;
    std::cout << "B is \n" << B << "\n";</pre>
   return 0;
}
```

15.6 ed_mtl_element_structure.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-16
 */
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
using namespace std;
int main(int, char**)
{
    typedef double value_type;
    typedef int
                 size_type;
    const int nb_elements= 6, nb_nodes= 12;
    value_type array[][4]= {{2, 3, 4,
                            {4, 10, 13, 16},
                             {6, 25, 38, 46},
                            {8, 32, 77, 100}};
    mtl::dense2D < value_type > E_mat(array);
    std::cout << "E_mat = \n" << E_mat << "\n";
    mtl::matrix::element_structure < value_type > A;
    typedef mtl::matrix::element<value_type> element_type;
    element_type* elements = new element_type[nb_elements];
    mtl::dense_vector < size_type > index_a(4, 0),
                                    index_b(4, 0),
                                    index_c(4, 0),
                                    index_d(4, 0),
                                    index_e(4, 0),
                                    index_f(4, 0);
    // construct nodes for every element
    index_a[0] = 0; index_a[1] = 1; index_a[2] = 4; index_a[3] = 5;
    index_b= index_a + 1;
    index_c= index_a + 2;
    index_d= index_a + 4;
    index_e= index_a + 5;
    index_f = index_a + 6;
    //construct the 6 elements from the example grid
    element_type a(0, index_a, E_mat);
    element_type b(1, index_b, E_mat);
    element_type c(2, index_c, E_mat);
    element_type d(3, index_d, E_mat);
    element_type e(4, index_e, E_mat);
```

```
element_type f(5, index_f, E_mat);
    //construct neighborhood information for each element
    a.add_neighbors(&b, &d, &e);
    b.add_neighbors(&a, &c, &d, &e, &f);
    c.add_neighbors(&a, &b, &e);
    d.add_neighbors(&a, &b, &e);
    e.add_neighbors(&a, &b, &c, &d, &f);
    f.add_neighbors(&b, &c, &e);
    std::cout << "a=" << a << "\n";
    //construct array of elements
    elements[0] = a;
    elements[1]=b;
    elements[2]=c;
    elements[3]=d;
    elements[4] = e;
    elements[5] = f;
    //construct element_structure from the 6 single elements
    A.consume(nb_elements, nb_nodes, elements);
    mtl::dense_vector < value_type > x(nb_nodes, 1.0), test(A * x);
    std::cout << "test="<< test << "\n";
    return 0;
}
```

15.7 ee_mtl_multi_vector.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-16
 */
// File: multi_vector.cpp
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
int main(int, char**)
    using namespace mtl;
    typedef dense_vector < double > Vector;
                                v(2, 3.4), w(3, 2.5);
    Vector
    mtl::multi_vector < Vector >
                                A(2, 3);
    dense2D < double >
                                 B(2,2), C(3,2), D(3,3);
    // Initialize matrices
    A = 3.0; B = 4.0; C = 5.0; D = 6.0;
    std::cout << "A = " << A << std::endl;
    // vector= multi_vector * vector
    v = A * w;
    std::cout << "v = " << v << std::endl;
    // vector= transposed multi_vector * vector
    w = trans(A) * v;
    std::cout << "w = " << w << std::endl;
    // vector= matrix * vector
    v = B * A.vector(1);
    std::cout << "v = " << v << std::endl;
    // vector= matrix * vector
    A.vector(0) = B * A.vector(1);
    std::cout << "A.vector(0) = " << A.vector(0) << std::endl;
    // Orthogonalize multi_vectorq
    A(0,0) = 1;
    orth(A);
    std::cout << "A = " << A << std::endl;
   return 0;
}
```

15.8 ef_mtl_insert.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-16
 */
// File: insert.cpp
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
using namespace mtl;
template <typename Matrix>
void fill(Matrix& m)
{
    // Matrices are not initialized by default
    m = 0.0;
    // Create inserter for matrix m
    matrix::inserter < Matrix > ins(m);
    // Insert value in m[0][0]
    ins[0][0] << 2.0;</pre>
    ins[1][2] << 0.5;</pre>
    ins[2][1] << 3.0;</pre>
    // Destructor of ins sets final state of m
}
template <typename Matrix>
void modify(Matrix& m)
{
    // Type of m's elements
    typedef typename Collection < Matrix >:: value_type value_type;
    // Create inserter for matrix m
    // Existing values are not overwritten but inserted
    matrix::inserter<Matrix, update_plus<value_type> > ins(m, 3);
    // Increment value in m[0][0]
    ins[0][0] << 1.0;</pre>
    // Elements that doesn't exist (in sparse matrices) are inserted
    ins[1][1] << 2.5;</pre>
    ins[2][1] << 1.0;</pre>
    ins[2][2] << 4.0;</pre>
    // Destructor of ins sets final state of m
}
```

```
int main(int, char**)
    // Matrices of different types
    compressed2D < double >
                                       A(3, 3);
                                       B(3, 3);
    dense2D < double >
    morton_dense < float, morton_mask > C(3, 3);
    // Fill the matrices generically
    fill(A); fill(B); fill(C);
    std::cout << "A is \n" << A << "\nB is \n" << B << "\nC is \n" << C;
    // Modify the matrices generically
    modify(A); modify(B); modify(C);
    std::cout << "\n\nAfter modification:\nA is \n" << A</pre>
              << "\nB is \n" << B << "\nC is \n" << C;
    return 0;
}
```

15.9 eg_mtl_insert_scope.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-16
 */
// Filename: insert_scope.cpp
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
using namespace mtl;
int main(int, char**)
    compressed2D < double >
                                      A(3, 3);
        matrix::inserter<compressed2D<double> > ins(A);
        ins[0][0] << 2.0;</pre>
        ins[1][2] << 0.5;</pre>
        ins[2][1] << 3.0;</pre>
    //} // ins is destroyed here
    std::cout << "A is \n" << A; // we can access A now
   return 0;
}
```

15.10 eh_mtl_element_matrix.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-16
 */
// File: element_matrix.cpp
#include <iostream>
#include <vector>
#include <boost/numeric/mtl/mtl.hpp>
using namespace mtl;
template <typename Matrix>
void fill(Matrix& m)
    // Matrices are not initialized by default
    m = 0.0;
    // Type of m's elements
    typedef typename Collection < Matrix >:: value_type value_type;
    // Create inserter for matrix m
    // Existing values are not overwritten but inserted
    matrix::inserter<Matrix, update_plus<value_type> > ins(m, 3);
    // Define element matrix (array)
    double m1[2][2] = \{\{1.0, -.4\}, \{-0.5, 2.0\}\};
    // Corresponding indices of the elements
    std::vector<int> v1(2);
    v1[0] = 1; v1[1] = 3;
    // Insert element matrix
    ins << element_array(m1, v1);</pre>
    // Insert same array with different indices
    v1[0]= 0; v1[1]= 2;
    ins << element_array(m1, v1);</pre>
    // Use element matrix type with dynamic size
    dense2D < double > m2(2, 3);
    m2[0][0] = 1; m2[0][1] = 0.2; m2[0][2] = 0.1;
    m2[1][0] = 2; m2[1][1] = 1.2; m2[1][2] = 1.1;
    // Vector for column indices
    dense_vector <int > v2(3);
    // Indices can be out of order
    v2[0] = 4; v2[1] = 1; v2[2] = 3;
```

```
// Use element_matrix and separate vectors for row and column indices
    ins << element_matrix(m2, v1, v2);</pre>
}
int main(int, char**)
    // Matrices of different types
                                         A(5, 5);
    compressed2D < double >
    dense2D < double >
                                         B(5, 5);
    morton_dense <float, morton_mask > C(5, 5);
    // \ \textit{Fill the matrices generically} \\
    fill(A); fill(B); fill(C);
    std::cout << "A is \n" << with_format(A, 4, 3)</pre>
               << "\nB is \n" << with_format(B, 4, 3)
               << "\nC is \n" << with_format(C, 4, 3);
    return 0;
}
```

15.11 ei_mtl_insert_class_expensive.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-16
 */
// Filename: insert_class_expensive.cpp
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
using namespace mtl;
class world_matrix
 public:
    world_matrix(unsigned nrows, unsigned ncols) : A(nrows, ncols) {}
    void add_entry(unsigned row, unsigned col, double value)
        // Extremely expensive -> must not be done
        matrix::inserter<compressed2D<double>, update_plus<double> > ins(A);
        ins[row][col] << value;</pre>
    friend inline std::ostream& operator<<(std::ostream& os, const world_matrix& w)</pre>
    { return os << w.A; }
 private:
    compressed2D < double >
                                      A;
};
int main(int, char**)
                              A(3, 3);
    world_matrix
    A.add_entry(0, 0, 2.0);
    A.add_entry(1, 2, 0.5);
    A.add_entry(2, 1, 3.0);
    std::cout << "A is \n" << A; // we can access A now
    return 0;
}
```

16 Day 19: MTL Continued

Open MTL Document

16.1 ej_mtl_insert_scope.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-16
 */
// Filename: insert_scope.cpp
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
using namespace mtl;
class world_matrix
    typedef matrix::inserter<compressed2D<double>, update_plus<double> > inserter_ty
  public:
    world_matrix(unsigned nrows, unsigned ncols) : A(nrows, ncols), ins(0) {}
    void add_entry(unsigned row, unsigned col, double value)
    { (*ins)[row][col] << value;
    void start_insertion() // must be called before first insertion
    { if (!ins) ins= new inserter_type(A); }
    void finish_insertion() // must be called before first usage
        if (ins) {
            delete ins;
            ins = 0;
        }
    }
    friend inline std::ostream& operator << (std::ostream& os, const world_matrix& w)
    { return os << w.A; }
  private:
    compressed2D <double >
                               A;
    inserter_type*
                               ins;
};
```

16.2 ek_mtl_array_initialization.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-16
 */
// File: array_initialization.cpp
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
int main(int, char**)
    using namespace mtl;
    double array[][4] = \{\{3, 7.2, 0, 6\},\
                        {2, 4.444, 5, 3},
                        {1, 7, 9, 2}};
    dense2D < double > A(array);
    std::cout << "A = \n" << A << "\n";
   return 0;
}
```

16.3 el_mtl_vector_expr.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-16
 */
// File: vector_expr.cpp
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
int main(int, char**)
    using namespace mtl;
    typedef std::complex <double > cdouble;
    dense_vector < cdouble >
                                  u(10), v(10);
    dense_vector < double >
                                  w(10), x(10, 4.0);
    for (unsigned i= 0; i < size(v); i++)</pre>
        v[i] = cdouble(i+1, 10-i), w[i] = 2 * i + 2;
    u = v + w + x;
    std::cout << "u is " << u << "\n";
    u = 3 * w;
    std::cout << "u is " << u << "\n";
    u*=6;
    std::cout << "u is " << u << "\n";
    u/= 2;
    std::cout << "u is " << u << "\n";
    u += dot(v, w) * w + 4.0 * v + 2 * w;
    std::cout << "u is " << u << "\n";</pre>
    std::cout << "i * w is " << cdouble(0,1) * w << "\n";
   return 0;
}
```

16.4 em_mtl_rich_vector_expr.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-16
 */
// File: rich_vector_expr.cpp
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
int main(int, char**)
    using namespace mtl;
    typedef std::complex <double > cdouble;
    dense_vector < cdouble >
                                  u(10), v(10);
    dense_vector < double >
                                  w(10), x(10, 4.0);
    for (unsigned i= 0; i < size(v); i++)</pre>
        v[i] = cdouble(i+1, 10-i), w[i] = 2 * i + 2;
    // Increment w by x
    // and assign the sum of--the incremented--w and v to u
    u = v + (w + = x);
    std::cout << "u is " << u << "\n";</pre>
    // w = w * 3; x = 2; v = v + w + x; u = u + v;
    u+=v+=(w*=3)+(x=2);
    std::cout << "u is " << u << "w is " << w << "\n";
   return 0;
}
```

16.5 en_mtl_matrix_expressions1.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-16
 */
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
int main(int, char**)
    using namespace mtl;
    const unsigned n= 10;
    compressed2D < double >
                                                   A(n, n);
    dense2D<int, matrix::parameters<col_major> > B(n, n);
    morton_dense < double , 0x555555f0 >
                                                   C(n, n), D(n, n);
    matrix::laplacian_setup(A, 2, 5);
    matrix::hessian_setup(B, 1);
    matrix::hessian_setup(C, 2.0);
    matrix::hessian_setup(D, 3.0);
    D += A - 2 * B + C;
    std::cout << "The matrices are: A=\n" << A << "B=\n" << B << "C=\n" << C << "D=" ^{\circ}
    return 0;
}
```

16.6 eo_mtl_matrix_expressions2.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-16
 */
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
int main(int, char**)
{
    using namespace mtl; using namespace mtl::matrix;
    const unsigned n=20;
                                               A(n, n), B(n, n);
    dense2D < double >
    morton_dense < double , doppled_64_row_mask > C(n, n);
    hessian_setup(A, 3.0); hessian_setup(B, 1.0);
   hessian_setup(C, 2.0);
    // Corresponds to A = B * B;
    mult(B, B, A);
    A = B * B; // use BLAS
    A= B * C; // use recursion + tiling from MTL4
    A+= B * C; // Increment A by the product of B and C
    A-= B * C; // Likewise with decrement
    std::cout << "The matrices are: A=\n" << A << "B=\n" << B << "C=\n" << C;
   return 0;
}
```

16.7 ep_mtl_matrix_expressions3.cpp

```
/* program to illustrate the use of mtl
* example taken from mtl document
* Rajeev Singh
* 2013-04-16
 */
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
int main(int, char**)
   using namespace mtl; using namespace mtl::matrix;
   const unsigned n=40;
                                         A(n, n), B(n, n);
   dense2D < double >
   morton_dense < double , doppled_64_row_mask > C(n, n), D(n, n);
   hessian_setup(A, 3.0); hessian_setup(B, 1.0);
   hessian_setup(C, 2.0); hessian_setup(D, 11.0);
   A += B * B + C * B - B * B * C * D;
   return 0;
}
```

16.8 eq_mtl_matrix_vector1.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-16
 */
#include <boost/numeric/mtl/mtl.hpp>
int main(int, char**)
{
    using namespace mtl; using namespace mtl::matrix;
                                    xd= 2, yd= 5, n= xd * yd;
    const unsigned
    dense2D < double >
                                    A(n, n);
    compressed2D < double >
                                    B(n, n);
    hessian_setup(A, 3.0); laplacian_setup(B, xd, yd);
    typedef std::complex <double > cdouble;
    dense_vector < cdouble >
                                  v(n), w(n);
    for (unsigned i= 0; i < size(v); i++)</pre>
        v[i] = cdouble(i+1, n-i), w[i] = cdouble(i+n);
    v += A * w;
    w = B * v;
    std::cout << "v is " << v << "\n";</pre>
    std::cout << "w is " << w << "\n";
   return 0;
}
```

16.9 er_mtl_matrix_vector2.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-16
 */
#include <boost/numeric/mtl/mtl.hpp>
int main(int, char**)
{
    using namespace mtl; using namespace mtl::matrix;
                                   xd= 2, yd= 5, n= xd * yd;
    const unsigned
                                   A(n, n);
    dense2D < double >
    laplacian_setup(A, xd, yd);
                                  v(n), w(n, 7.0);
    dense_vector < double >
    // Scale A with 4 and multiply the scaled view with w
    v = 4 * A * w;
    std::cout << "v is " << v << "\n";
    // Scale w with 4 and multiply the scaled view with A
    v = A * (4 * w);
    std::cout << "v is " << v << "\n";</pre>
    // \ \textit{Scale both with 2 before multiplying}
    v = 2 * A * (2 * w);
    std::cout << "v is " << v << "\n";
    // Scale v after the MVP
    v = A * w;
    std::cout << "v is " << v << "\n";
   return 0;
}
```

16.10 es_mtl_vector_norm.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-17
 */
// File: vector_norm.cpp
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
int main(int, char**)
    using namespace mtl;
    typedef std::complex <double > cdouble;
    dense_vector < cdouble >
                                  v(10000);
    // Initialize vector
    for (unsigned i= 0; i < size(v); i++)</pre>
        v[i] = cdouble(i+1, 10000-i);
    std::cout << "one_norm(v) is " << one_norm(v) << "\n";
    std::cout << "two_norm(v) is " << two_norm(v) << "\n";
    std::cout << "infinity_norm(v) is " << infinity_norm(v)<< "\n";</pre>
    // Unroll computation of two-norm to 6 independent statements
    std::cout << "two_norm <6>(v) is " << two_norm <6>(v) << "\n";
    return 0;
}
```

16.11 et_mtl_matrix_norm.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-17
 */
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
int main(int, char**)
    using namespace mtl;
    const unsigned n=10;
    dense2D<float, matrix::parameters<col_major> > B(n, n);
    matrix::hessian_setup(B, 1.0);
    std::cout << "one_norm(B) is " << one_norm(B) << "\n";</pre>
    std::cout << "infinity_norm(B) is " << infinity_norm(B) << "\n";</pre>
    std::cout << "frobenius_norm(B) is " << frobenius_norm(B) << "\n";</pre>
   return 0;
}
```

16.12 eu_mtl_vector_reduction.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-17
 */
// File: vector_reduction.cpp
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
int main(int, char**)
    using namespace mtl;
    typedef std::complex <double > cdouble;
    dense_vector < cdouble >
    for (unsigned i= 0; i < size(v); i++)</pre>
        v[i] = cdouble(i+1, 100-i);
    std::cout << "sum(v) is " << sum(v) << "\n";</pre>
    std::cout << "product(v) is " << product(v)<< "\n";</pre>
    std::cout << "sum <6>(v) is " << sum <6>(v) << "\n";
    return 0;
}
```

16.13 ev_mtl_vector_min_max.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-17
 */
// File: vector_min_max.cpp
#include <iostream>
#include <cmath>
#include <boost/numeric/mtl/mtl.hpp>
int main(int, char**)
{
    using mtl::max; using std::pow; // to avoid possible ambiguity with ARPREC
    mtl::dense_vector < double >
                                  v(100);
    for (unsigned i= 0; i < size(v); i++)</pre>
        v[i] = double(i+1) * pow(-1.0, int(i)); // Amb. in MSVC
    std::cout << "max(v) is " << max(v) << "\n";</pre>
    std::cout << "min(v) is " << min(v) << "\n";</pre>
    std::cout << "max<6>(v) is " << max<6>(v)<< "\n";</pre>
    return 0;
}
```

16.14 ew_mtl_dot_example.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-17
 */
// Filename: dot_example.cpp (part of MTL4)
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
int main(int, char**)
    using namespace mtl;
    typedef std::complex <double > cdouble;
    dense_vector < cdouble >
                                  v(10000), x(10, cdouble(3, 2));
    dense_vector < double >
                                  w(10000);
    for (unsigned i= 0; i < size(v); i++)</pre>
        v[i] = cdouble(i+1, 10000-i), w[i] = 2 * i + 2;
    std::cout << "dot(v, w) is " << dot(v, w) << "\n";
    std::cout << "dot<6>(v, w) is " << dot<6>(v, w) << "\n";
    std::cout << "dot_real <6>(v, w) is " << dot_real <6>(v, w) << "\n";
    std::cout << "conj(x) is " << conj(x)<< "\n";</pre>
    return 0;
}
```

16.15 ex_mtl_conj_trans_hermitian.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-17
 */
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
int main(int, char**)
    using namespace mtl;
    typedef std::complex <double> cdouble;
                                     xd= 2, yd= 5, n= xd * yd;
    const unsigned
    compressed2D < cdouble >
                                     A(n, n);
    matrix::laplacian_setup(A, xd, yd);
    // Fill imaginary part of the matrix
    A *= cdouble(1, -1);
    std::cout << "A is\n" << with_format(A, 7, 1) << "\n";
    std::cout << "trace(A) is " << trace(A) << "\n\n";</pre>
    std::cout << "conj(A) is\n" << with_format(conj(A), 7, 1) << "\n";
    std::cout << "trans(A) is\n" << with_format(trans(A), 7, 1) << "\n";
    std::cout << "hermitian(A) is\n" << with_format(hermitian(A), 7, 1) << "\n";
   return 0;
}
```

16.16 ey_mtl_sub_matrices.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-17
 */
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
int main(int, char**)
    using namespace mtl; using mtl::iall;
    typedef std::complex <double >
                                      cdouble;
    const unsigned
                                        xd = 2, yd = 5, n = xd * yd;
    dense2D < cdouble >
                                        A(n, n);
    matrix::laplacian_setup(A, xd, yd);
    // Fill imaginary part of the matrix
    A *= cdouble(1, -1);
    std::cout << "A is\n" << with_format(A, 7, 1) << "\n";
    std::cout << "sub_matrix(A, 2, 4, 1, 7) is\n"</pre>
               << with_format(sub_matrix(A, 2, 4, 1, 7), 7, 1) << "\n";
    //col-vector from matrix
    dense_vector < cdouble > v_c(A[iall][0]);
    std::cout << "col-vector v_c is\n" << v_c << "\n";</pre>
    //row-vector from matrix
    dense_vector < cdouble, mtl::vector::parameters < tag::row_major > v_r(A[0][iall])
    std::cout << "row-vector v_r is\n" << v_r << "\n";</pre>
    //row-vector in matrix
    RowInMatrix < dense 2D < cdouble > >::type v_r2(A[0][iall]);
    std::cout << "row-vector v_r2 is\n" << v_r2 << "\n";</pre>
    //submatrix from matrix per begin and end of row and column
    dense2D < cdouble > B = sub_matrix(A, 2, 4, 1, 7);
    std::cout << "B is\n" << B << "\n";</pre>
    B[1][2] = 88;
    std::cout << "B is\n" << B << "\n";</pre>
    //submatrix from matrix per irange
    using mtl::irange;
    irange row(2, 4), col(1, 7);
```

```
dense2D < cdouble > B1 = A[row][col];

std::cout << "B1 is\n" << B1 << "\n";

//scalar from matrix
cdouble C = A[1][1];

std::cout << "C is\n" << C << "\n";

return 0;
}</pre>
```

16.17 ez_mtl_permutation.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-17
 */
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
int main(int, char**)
    using namespace mtl;
                      array[][3]= {{1., 2., 3.}, {4., 5., 6.}, {7., 8., 9.}};
    double
    dense2D < double > A(array), A2, A3;
    // Creating a permutation matrix from a vector (or an array respectively)
    int indices[] = {1, 2, 0};
    matrix::traits::permutation<>::type P= matrix::permutation(indices);
    std::cout << "\nP =\n" << P;
    // Permutating rows
    A2 = P * A;
    std::cout << "\nP * A =\n" << A2;
    // Permutating columns
    A3 = A2 * trans(P);
    std::cout << "\nA2 * trans(P) =\n" << A3;</pre>
    dense_vector < double > v(array[2]), w(P * v);
    std::cout << "\nP * v =\n" << w << "\n";
   return 0;
}
```

16.18 fa_mtl_reordering.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-17
 */
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
int main(int, char**)
    using namespace mtl;
                      array[][3]= {{1., 2., 3.}, {4., 5., 6.}, {7., 8., 9.}};
    double
    dense2D < double > A(array), B2, B3;
    // Creating a reordering matrix from a vector (or an array respectively)
    int indices[] = {2, 1};
    matrix::traits::reorder<>::type R= matrix::reorder(indices);
    std::cout << "\nR =\n" << R;
    // Reorder rows
    B2 = R * A;
    std::cout << "\nR * A =\n" << B2;
    // Reorder columns
    B3 = B2 * trans(R);
    std::cout << "\nB2 * trans(R) =\n" << B3;</pre>
    dense_vector < double > v(array[2]), w(R * v);
    std::cout << "\nR * v =\n" << w << "\n";
   return 0;
}
```

16.19 fb_mtl_reordering2.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-17
 */
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
int main(int, char**)
    using namespace mtl;
                      array[][3]= {{1., 2., 3.}, {4., 5., 6.}, {7., 8., 9.}};
    double
    dense2D < double > A(array), B2, B3;
    // Creating a reordering matrix from a vector (or an array respectively)
    int indices[]= {2, 1, 1, 2};
    matrix::traits::reorder<>::type R= matrix::reorder(indices);
    std::cout << "\nR =\n" << R;
    // Reorder rows
    B2 = R * A;
    std::cout << "\nR * A =\n" << B2;
    // Reorder columns
    B3 = B2 * trans(R);
    std::cout << "\nB2 * trans(R) =\n" << B3;</pre>
    dense_vector < double > v(array[2]), w(R * v);
    std::cout << "\nR * v =\n" << w << "\n";
   return 0;
}
```

16.20 fc_mtl_reordering3.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-17
 */
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
int main(int, char**)
    using namespace mtl;
    double
                      array[][3] = {{1., 0., 3.},
                                   {4., 0., 6.},
                                   {7., 0., 9.},
                                   {0., 0., 0.}};
    dense2D < double > A(array), B2, B3;
    // Creating a compression (reordering) matrix from a vector
    // (or an array respectively)
    int non_zero_rows[] = {0, 1, 2}, non_zero_columns[] = {0, 2};
    // To be sure, we give the number of columns for a consistent size!
    matrix::traits::reorder <>::type RR= matrix::reorder(non_zero_rows, 4),
                                     RC= matrix::reorder(non_zero_columns);
    std::cout << "A =\n" << A << "\nRR =\n" << RR << "\nRC =\n" << RC;
    // Compress rows
    B2 = RR * A;
    std::cout << "\nRR * A, i.e. compress row of A =\n" << B2;
    // Compress columns
    B3 = B2 * trans(RC);
    std::cout << "\nB2 * trans(RC), i.e. compress columns of B2 =\n" << B3;
    // Decompress rows
    dense2D < double > C1(trans(RR) * B3);
    std::cout << "\ntrans(RR) * B3, i.e. row decompression of B3 =\n" << C1;</pre>
    // Decompress columns
    dense2D < double > C2(C1 * RC);
    std::cout << "\nC1 * RC, i.e. column decompression of C1 (should be A) =\n"</pre>
              << C2;
    return 0;
}
```

16.21 fd_mtl_indirection.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-17
 */
// Filename: matrix_indirect.cpp (part of MTL4)
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
using namespace std;
int main(int, char**)
{
    typedef mtl::dense2D < double > matrix;
    matrix A(5, 3);
    hessian_setup(A, 1.0);
    mtl::iset rows, cols;
    rows= 2, 0, 3; cols= 2, 1;
    cout << "rows = " << rows << ", cols = " << cols << "\n"
         << "The sub-matrix A[{2, 0, 3}][{2, 1}] is n << A[rows][cols];
    mtl::matrix::indirect < matrix > B(A[rows][cols]);
    cout << "B is\n" << B;</pre>
    return 0;
}
```

$16.22 \quad fe_mtl_upper.cpp$

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-17
 */
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
int main(int, char**)
    using namespace mtl;
    double
                      array[][3] = {{1., 2., 3.}, {4., 5., 6.}, {7., 8., 9.}};
    dense2D < double > A(array);
    std::cout << "\nupper(A) = \n" << upper(A);</pre>
    std::cout << "\nstrict_upper(A) = \n" << strict_upper(A);</pre>
    return 0;
}
```

16.23 ff_mtl_lower.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-17
 */
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
int main(int, char**)
    using namespace mtl;
    double
                      array[][3]= {{1., 2., 3.}, {4., 5., 6.}, {7., 8., 9.}};
    dense2D < double > A(array), L, SL;
    L= lower(A);
    std::cout << "\nlower(A) = \n" << L;</pre>
    SL= strict_lower(A);
    std::cout << "\nstrict_lower(A) = \n" << SL;</pre>
   return 0;
}
```

16.24 fg_mtl_bands.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-17
 */
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
int main(int, char**)
    using namespace mtl;
    double
                            array[][5] = {{1., 2., 3., 4., 5.}, {4., 5., 6., 7., 8.},
                                         \{7., 8., 9., 8., 7.\}, \{6., 5., 4., 3., 2.\}\};
                           A(array), B;
    dense2D < double >
    compressed2D < double >
    B= bands(A, 1, 3);
    std::cout << "\nbands(A, 1, 3) = \n" << B;</pre>
    T = bands(A, -1, 2);
    std::cout << "\ntri_diagonal(A):= bands(A, -1, 2) = \n" << T;</pre>
    return 0;
}
```

16.25 fh_mtl_rank_one_and_two_update.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-17
 */
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
int main(int, char**)
    using namespace mtl;
    typedef std::complex <double > cdouble;
    const unsigned n= 8;
    dense2D < cdouble >
                                  A(n, n);
    A = 3.0;
    dense_vector < cdouble >
                                  v(n), w(n);
    for (unsigned i= 0; i < size(v); i++)</pre>
        v[i]= cdouble(i+1, n-i), w[i]= cdouble(i+n);
    rank_one_update(A, v, w);
    std::cout << "A after rank-one update is \n"</pre>
              << with_format(A, 9, 3) << "\n";
    A = 3.0;
    rank_two_update(A, v, w);
    std::cout << "A after rank-two update is \n"</pre>
              << with_format(A, 9, 3) << "\n";
   return 0;
}
```

16.26 fi_mtl_other.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-17
 */
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
int main(int, char**)
{
    using namespace mtl;
    const unsigned n= 10;
    compressed2D < double >
                                                      A(n, n);
    dense2D<float, matrix::parameters<col_major> > B(n, n);
    morton_dense < double , 0x55555555>
                                                     C(n, n);
    morton_dense <double, 0x555555f0>
                                                      D(n, n);
    matrix::hessian_setup(B, 1.0);
    matrix::hessian_setup(C, 2.0);
    matrix::hessian_setup(D, 3.0);
    std::cout << "one_norm(B) is " << one_norm(B) << "\n";</pre>
    std::cout << "infinity_norm(B) is " << infinity_norm(B) << "\n";</pre>
    std::cout << "frobenius_norm(B) is " << frobenius_norm(B) << "\n";</pre>
    return 0;
}
```

16.27 fj_mtl_eigenvalue_example.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-17
 */
// Filename: eigenvalue_example.cpp (part of MTL4)
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
int main(int, char**)
    using namespace mtl;
    dense_vector < double >
                                                eig;
    double array[][4]= {{1, 1, 0},
                          {1, -1, -2, 0},
{1, -2, 1, 0},
{0, 0, 0, 10}};
    dense2D < double > A(array);
    std::cout << "A=\n" << A << "\n";
    eig= eigenvalue_symmetric(A,22);
    std::cout<<"eigenvalues ="<< eig <<"\n";</pre>
    eig=0;
    eig= qr_sym_imp(A);
    std::cout << "eigenvalues = " << eig << " \n";</pre>
    eig= qr_algo(A, 5); // only 5 qr iterations (Q-R-changes)
    std::cout << "eigenvalues = " << eig << " \n ";</pre>
    return 0;
}
```

16.28 fk_mtl_eigenvalue_example2.cpp

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-17
 */
// Filename: eigenvalue_example.cpp (part of MTL4)
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
using namespace std;
typedef mtl::matrix::dense2D < double > dMatrix;
int main() {
    dMatrix M1(3,3), M2(3,3), M3(3,3), M4(3,3);
    M1 = 2,0,0,
        1,1,0,
        0,1,3; //EWs: 1,2,3
    mtl::matrix::eigenvalue_solver <dMatrix > E1(M1);
    E1.setMaxIteration(10);
    E1.calc();
    cout << "M1(setting the number of iteraions): "</pre>
         << E1.get_eigenvalues() << "\n";
    M2 = 1,0,0,
        0,1,5,
        0,-2,3; //EWs: 1,2+3i,2-3i
    mtl::matrix::eigenvalue_solver<dMatrix> E2(M2);
    E2.setTolerance(1.0e-10);
    E2.calc();
    cout << "M2(providing tolerance): "</pre>
         << E2.get_eigenvalues() << "\n";
    M3 = -261, 209, -49,
        -530, 422, -98,
        -800, 631, -144; //EWs: 3,4,10
    mtl::matrix::eigenvalue_solver <dMatrix > E3(M3);
    E3.setMaxIteration(10);
    E3.setTolerance(1.0e-10);
    E3.calc();
    cout << "M3(providing both): "</pre>
         << E3.get_eigenvalues() << "\n";
    M4 = 1, -3, 3,
        3,-5,3,
```

$16.29 \quad fl_mtl_qr_givens_example.cpp$

```
/* program to illustrate the use of mtl
 * example taken from mtl document
 * Rajeev Singh
 * 2013-04-17
 */
// Filename: qr_givens_example.cpp (part of MTL4)
#include <boost/tuple/tuple.hpp>
#include <iostream>
#include <boost/numeric/mtl/mtl.hpp>
using namespace std;
typedef mtl::matrix::dense2D < double > dMatrix;
int main() {
    dMatrix M1(3,3), M2(3,3);
    M1 = 2,0,0,
        1,1,0,
        0,1,3; //EWs: 1,2,3
    mtl::matrix::qr_givens_solver<dMatrix> QR1(M1);
    QR1.setTolerance(1.0e-5);
    QR1.calc();
    cout << "M1(providing tolerance):\n Q: \n" << QR1.getQ()</pre>
         << "\n R: \n" << QR1.getR() << "\n";
    M2 = -261, 209, -49,
        -530, 422, -98,
        -800, 631, -144; //EWs: 3,4,10
    mtl::matrix::qr_givens_solver<dMatrix> QR2(M2);
    QR2.calc();
    cout << "M2(with defaults):\n Q: \n" << QR2.getQ()</pre>
         << "\n R: \n" << QR2.getR() << "\n";
    dMatrix Q2, R2;
    boost::tie(Q2, R2) = qr_givens(M2);
    cout << "M2(with defaults):\n Q: \n" << Q2</pre>
         << "\n R: \n" << R2 << "\n";
    return 0;
}
```