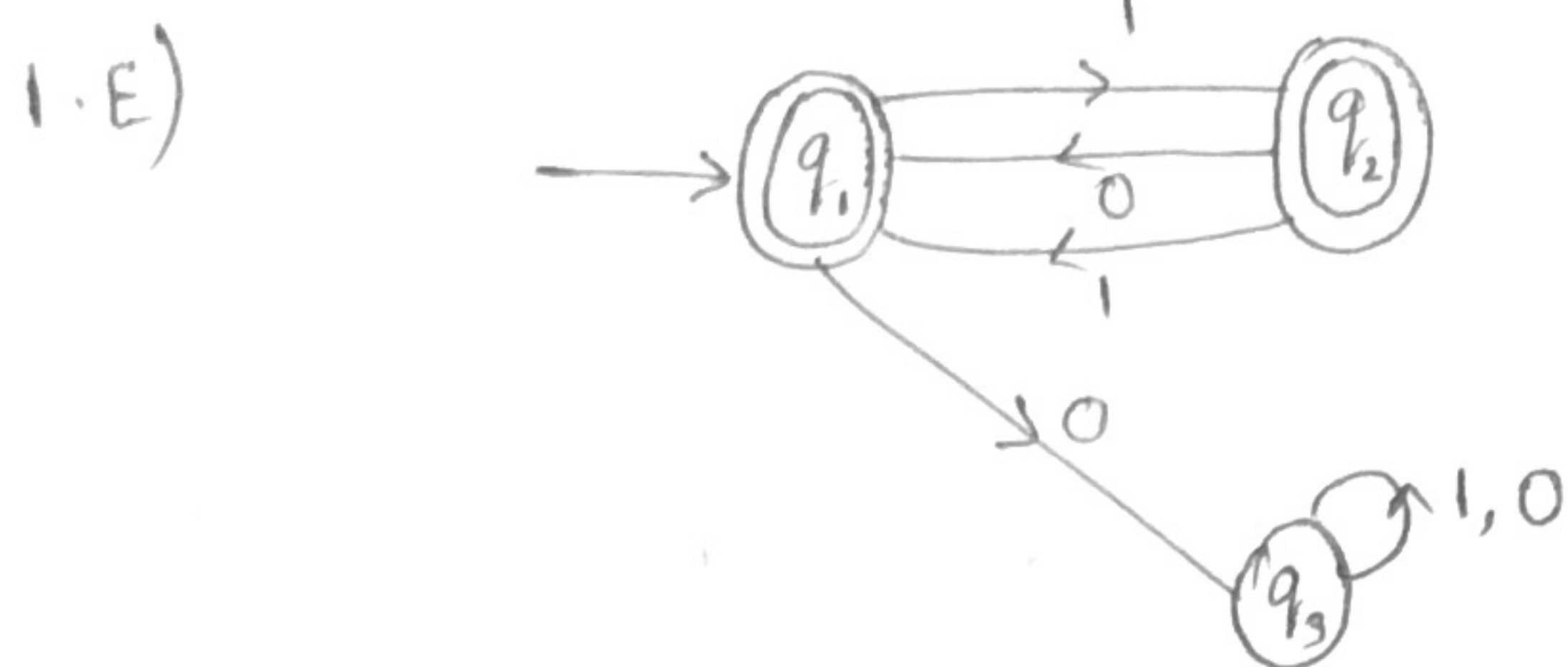


1. Draw a State diagram for DFA's that realize the following languages.
Assume $\Sigma = \{0, 1\}$.

$E = \{x \mid \text{every odd position of } x \text{ is } 1\}$.

$F = \{x \mid x \text{ contains even number of } 0\text{'s}\}$.



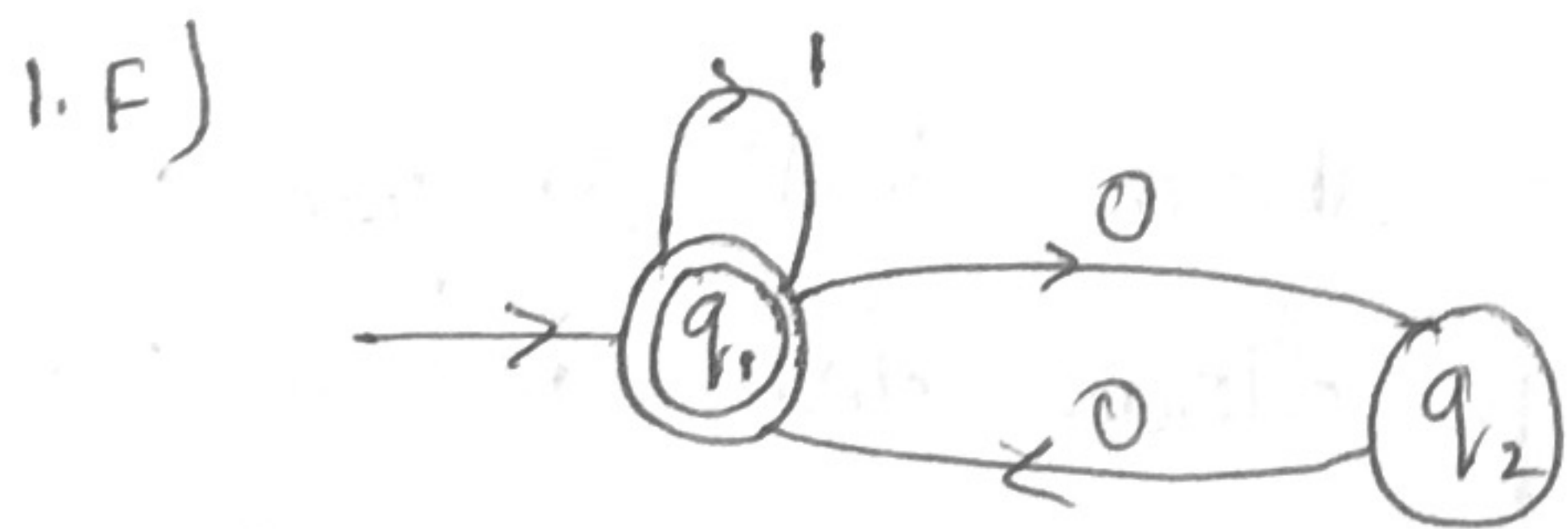
This is the state diagram for DFA for $x \mid \text{every odd position of } x \text{ is } 1$. Assume $\Sigma = \{0, 1\}$. Let's consider few example strings to see the above languages satisfies the following strings or not. The string flows from initial state q_1 and should end at final state q_2 .

q_1, q_2 . Strings are : 101010110 - rejected.

111010111 - accepted

100110101 - rejected

10101110 - accepted.



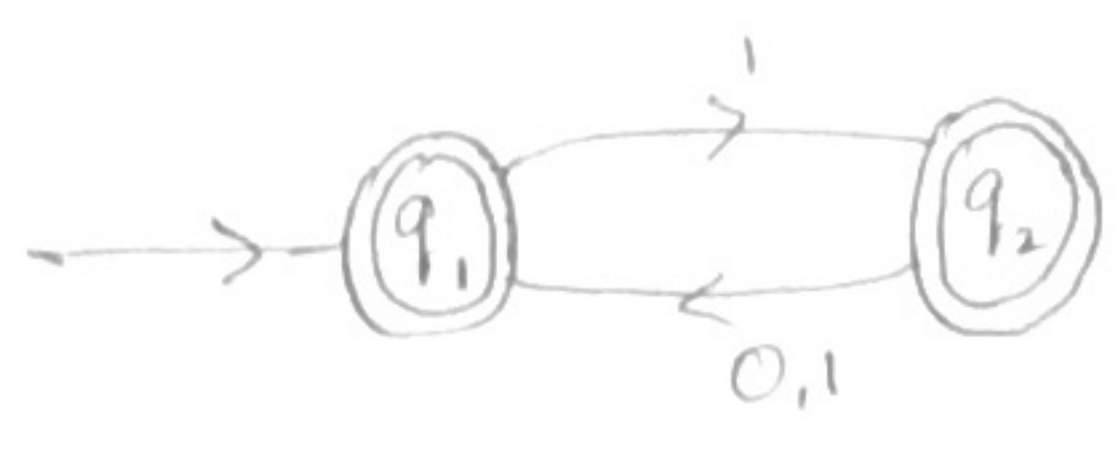
The above is the state diagram for DFA for $x \mid x \text{ contains even number of } 0\text{'s}$. Assume $\Sigma = \{0, 1\}$. By considering few strings to check the above state diagram is valid for the language we considered. Here the string flows from initial state q_1 and should end at final state q_1 . Strings are : 01010100 - rejected, 001001100 - accepted, 110101010 - accepted, 1010101000 - accepted.

2. For each of the languages, draw the simplest state diagram of an NFA that realizes it.

$E = \{x \mid \text{every odd position of } x \text{ is } 1\}$

$F = \{x \mid x \text{ contains even number of 0's}\}$

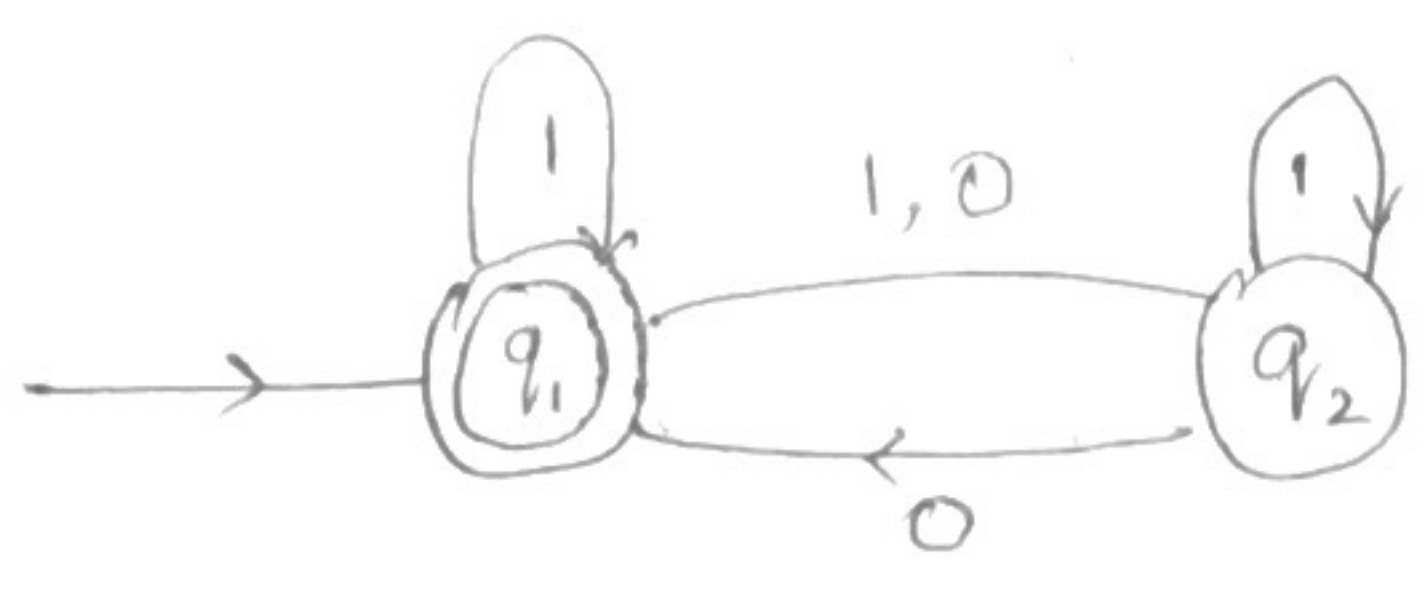
2.E)



This state diagram represents NFA for $x \mid$ every odd position of x is 1. By considering some strings to show the above state diagram is valid for language we considered. The string flows from initial state q_1 and should end at final state q_1, q_2 .

String's taken are : 11111111 - accepted, 01010101 - rejected, 101010101 - accepted, 101011101 - accepted.

2.F)



This state diagram indicates NFA for $x \mid x$ contains even number of 0's. By taking few strings to show the above state diagram is valid for language we considered. The strings flows from initial state q_1 and should end at final state q_1 . Strings considered are:

11010100 - accepted.
 111110 - rejected.
 00101001 - rejected.
 01010101 - accepted.