Awkward State Machines

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1 Introduction

Imagine you had a ball of yarn of infinite length and a pair of scizzors. Now choose some arbitrary length of yarn and cut it - we'll refer to this length as 1. Next, cut a second strand of yarn that has length 2 relative to your original piece of yarn and set it aside. Now, extend the yarn to length 3 and repeat the following instructions:

- 1. For every strand of yarn you have cut so far (other than the strand of length 1), check if the current extension of yarn can be split into even segments of the same length as the current strand by 'walking' the shorter strand up the longer one until you reach the end of or pass the end of the extended piece of yarn; if you reach the end of the extended piece exactly, then the extension can be divided into even segments. If none of the previous strands can be used to divide the current extension evenly, then double the length of the extended peice of yarn, then cut it in half, finally, set the cut strand aside with the others. Do not cut the extension if one of the previous strands does divide the extension evenly.
- 2. Using your strand of length 1, increase the length of the extension by 1.
- 3. Repeat the above two steps.

If you follow the above instructions, then order the strands of yarn you cut by their length, and finally wrote out their lengths relative to the strand of length 1, then you will find yourself writing down the prime numbers in consequetive order. The fact that this simple experiment derives the prime numbers using relative distance has always fascinated me. I've always had an itching notion that an algorithm based solely on relative distance, rather

than integer arithmetic, would outperform the standard methods for discovering the primes in consequetive order. However, the problem of how to encode distance and divisibility without actually using numbers seemed to be impossible; after all, how do you tell a computer to use a ball of yarn and scizzors? And even if we could, the act of walking the strands up the extension is going to be pretty slow.

Let's modify our experiment slightly to include tacks and a corkboard. Start again by cutting some length of yarn for defining length 1. Now, using your piece of yarn, seperate two tacks on your board 1 unit away from one another. You can now determine the strand of length two by wrapping your ball of yarn around the tacks such that you start at one tack, wrap around the second, and then return to the first tack, then cut the yarn to produce the strand of length two. Now use the strand of length two to place two more tacks in your board at 2 units apart. Now using the tacks for length 1, create a strand of length 3 and repeat the following instructions:

- 1. For every pair of tacks on the board (other than the unit tacks), wrap the current extension of yarn around the tacks to check for divisibility. The extension is divisible if the yarn perfectly touches one of the tacks when it runs out of length. If none of the current pairs of tacks divide the extension evenly, then double the extension, cut it in half, and use the new strand to set apart a new pair of tacks on your board.
- 2. Use the unit pair of tacks to increase the length of the extension by 1.
- 3. Repeat the above two steps.

The above experiment is very simliar to the first. The pairs of tacks you've placed will wind up enumerating the primes once again. We are also still stuck with the problem of how could we encode this algorithm without integers, and the algorithm still isn't performing very quickly. However, the algorithm does highlight an important concept, our tacks use circles (technically ovals) in order to check the length of the extended piece of yarn. This is amazing because it allows us to check for divisiblity without counting anything out, instead, we just keep wrapping the yarn around until we get to the end; thus we don't need to know how many times we've wrapped the yarn around, we just have to look where it winds up at the end.

Let's modify our experiment once again. This time, you need tacks, a corkboard, and little flags that you can stick into the board (a needle with red tape for example). Start by placing two tacks down on the leftmost side of the board in a vertical line, and place a flag next to the bottom tack. Next, place three tacks in a vertical line to the right of those (imagine you

are creating a bar graph with the tacks) and place a flag next to the highest tack. This expirement will require you to keep the vertical lines you create with the tacks distinct from one another, we shall refer to each line as a bar. Each bar in your board will always have a flag next to one of it's tacks. Repeat the following to run the experiment:

- 1. For every bar except the rightmost, move the flag to the tack above the one it is currently at; unless the flag is currently at the topmost tack in the bar, then move the flag to the bottom tack in the bar.
- 2. If there are no flags on any of the bottom tacks after you've moved every bar (other than the rightmost), then move the flag of the rightmost bar to its bottom tack and then create a new bar to the right of it that has one more tack than it, and place the new bar's flag at it's top tack.
- 3. If there was a flag on one of the bottom tacks, then add a new tack to the top of the rightmost bar, and place it's flag next to the new tack.
- 4. Repeat the above three steps.

If you run the above experiment and then count the number of tacks in each bar, you will find that the number of tacks in the bars enumerate the prime numbers in consequetive order. How did this happen? Well, this experiment is much more similar to the last two than it first appears. In this case, the way we move the flags on each bar is the same as wrapping the extended piece of yarn around the tacks in experiment two, or 'walking' the yarn up the extended piece of yarn from experiment one. However, this time our flags our able to preserve the state from the last iteration since you just have to move the flags one tack forward. The moving of each tack can be done in constant time for each bar, and is incredibly fast relative to the time it takes to re-wrap the extended strand of yarn around the tacks, or perform the 'walks'. Furthermore, this expirement doesn't need distance; rather, it only needs relative position (bottom tack, tack above that, ..., tack below top tack, top tack). By replacing distance with relative position, we can easily encode our experiment without the use of numbers using cycle graphs implemented via linked lists.

2 Cycle Graphs

Definition

A cycle graph is a directed, connected graph whose points form a circle. More explicity, for any n > 1, the cycle graph CG_n has points $\{p_0, p_1, ..., p_{n-1}\}$

such that for any i < n - 1, p_i has only one edge which goes to p_{i+1} , and p_{n-1} has only one edge going to p_0 .

Lemma

For any cycle graph CG_n , for any $p_i \in CG_n$, a walk of length k = n - i will end at point p_0 .

Proof

For any point $p_j \in CG_n$, there is only one edge that can be traversed, thus there is only one walk that can be made.

Furthermore, point p_j is h = n - j - 1 steps from point p_{n-1} .

Thus, moving k = h + 1 = n - j - 1 steps from p_j will land you on the point p_{n-1} has an edge to, which is p_0 by defining of the cycle graph. Q.E.D

Lemma

For any cycle graph CG_n , a walk of length n from p_i will end at point p_i .

Proof

For any $p_i \in CG_n$, a walk of length n-i will end at point p_0 .

Thus, moving the final j = n - (n - i) = i steps from point p_0 will land you on point p_i .

Q.E.D

Corollary

For any cycle graph CG_n , a walk of length kn, k > 0, from p_0 will end at point p_0 .

Proof

If we move n steps from p_i we will return to p_i by the above.

Assume after moving in, $i \ge 1$ steps from p_i , you have returned to point p_i .

Then, moving n more steps from there will again return to point p_i .

Thus moving in + n = (i + 1)n steps from p_i returns you to p_i . Q.E.D

Lemma

For any cycle graph C_n , for any k>0, for any $p_i\in C_n$, a walk of length k

starting at p_i will end at point p_j where $j = i + k \mod n$.

Proof

Let CG_n be at point p_i .

Let 0 > k.

If k > n, then there exists $q \ge 0$ such that qn + r = k with $0 \le r < n$.

Furthermore, moving qn positions from p_i will return the cycle to p_i , leaving r moves left.

Let e = i + r.

Assume e < n, then moving r positions from p_i will land on p_{i+r} .

Thus, if e < n, moving k = qn + r positions resulted in position $i + r = i + (qn + r) \mod n = i + k \mod n$.

Assume $e \geq n$.

Then e = n + a = i + r for $0 \le a < n$.

Thus, a = (i + r) - n = e - n

We can move n-i positions from p_i to return to point p_0 .

Leaving r - (n - i) = r - n + i = (r + i) - n = e - n = a < n moves remaing. Therefore, the cycle will land on point p_a .

We need to show that $a = i + k \mod n$. Substituting give us:

 $i + k \mod n = i + (qn + r) \mod n = i + r \mod n$ = $e \mod n = (n + a) \mod m = a \mod m$.

Thus we have shown that moving k steps from p_i will result in point p_j where $j = k + i \mod n$.

Q.E.D

3 Activation Cycle Machines

Definition

An activation cycle machine (ACM) is state machine that runs on top of a cycle graph CG_n , that has been equipped with a subset of 0 < a < n activator points $A = \{ p_i \mid 0 \le i < a < n \}$.

Each state of an ACM is associated with a position $p \in CG_n$. The initial state (state 0) of any ASM has position $p_0 \in CG_n$. If the position of an ACM is p_j on state i-1, then the position at state i will be the point connected to by p_j . Thus, if j < n-1, then the next state's position will be p_{j+1} ; otherwise, if j = n-1, then the next state's position will be p_0 .

We denote the ACM containing cycle graph CG_n and a activator nodes as $C_{n,a}$.

For simplicity, if the current position of $C_{n,a}$ is p_i on state j, we write $\overline{C}_{n,a}^j = i$.

If the current position of an ACM, $C_{n,a}$ is within the set of activotors ($\overline{C}_{n,a} < a$), then we say the ACM is *active*; otherwise, we say the ACM is *inactive*.

Theorem

For any ACM, $C_{n,a}$, for any state, k, the position of state (k+i) is given by taking a walk of length i starting at position $\overline{C^k}$ around CG_n , thus the position of state k+i is: $\overline{C^k}+i \mod n$.

Proof

By defininiton of an ACM, if the position of an ACM is p_j on state i-1, then the position at state i will be the point connected to by p_j , which is equivalent to taking a walk of length 1 on CG_n starting on point p_j .

Assume for some j, $1 \leq j \leq i$, that the position of state k + j is given by taking a walk of length j starting at position $\overline{C^k}$ around $CG_{n,a}$.

Then the position on state k+j is given by $\overline{C^k}+j \mod n$. Thus, the the next state's position will be given by $\overline{C}^{k+j+1}=\overline{C^k}+j+1 \mod n$, which is the end position of a walk of length j+1 when starting at point $\overline{C^k}$ on $CG_{n,a}$. Q.E.D

Corollary

The position of $C_{n,a}$ on state k is given by $k \mod n$.

Proof

The initial state, 0, starts at position $0 = 0 \mod n$.

Thus the position of state k = k + 0 is given by: $|C^0| + k \mod n = 0 + k \mod n = k \mod n$. Q.E.D

Corollary

 $C_{n,a}$ is active on state k if and only if $k \mod n < a$.

Proof

An ACM, $C_{n,a}$ is active if and only if it's position is on one of it's activators. The activators of $C_{n,a}$ are defined to be $p_{0 \le i < a}$, or equivalenty positions $0 \le i < a$.

Thus, an $C_{n,a}$ is only active if it's position is less than a. Thus, C is active if and only if $a > \overline{C^k} = k \mod n$. Q.E.D

4 Awkward State Machines

Definition

An activation branch is directed graph that forms a line. Explicity, the activation branch of length n has points $\{p_0, p_1..., p_{n-1}\}$ such that for every point $p_{i< n-1}$ has a single edge connecting it to p_{i+1} , and p_{n-1} does not have any edges extending from it.

Furthermore, an activation branch is equipped with a > 0 activator points: $A = \{ p_i \mid 0 \le i < a < n \}.$

We denote the activation branch with length n and a activator nodes $B_{n,a}$.

Lemma

For any $B_{n,a}$, adding an edge extending from p_{n-1} to p_0 produces the cycle graph CG_n for ACM $C_{n,a}$.

Proof

By definition of $B_{n,a}$, all points $p_{i< n-1}$ have the same edges as the first n-1 points in CG_n for ACM $C_{n,a}$.

Furthermore, the first a points of $B_{n,a}$ are it's activator points, which are the activators of $C_{n,a}$.

Thus, the only edge missing from $B_{n,a}$ that is contained within CG_n is from p_{n-1} to p_0 .

Therefore, adding the edge will convert $B_{n,a}$ into CG_n for $C_{n,a}$. Q.E.D

Definition

An awkward state machine (ASM) is state machine running on top of a directed graph composed of a set of ACMs and a single activation branch.

Every ASMs initial state contains a single ACM, $C_{m,a} = C_0$, and the activation branch, $B_{m+1,a}$.

Furthermore, the position of C_0 on the initial state is 0.

We denote the ASM with an initial state containing $C_{m,a}$ as $S_{a,n=m-a}$.

To progress from state i-1 to state i for ASM, S, first move every ACM in S to it's next state.

If none of the ACMs in S are active after moving to their next state, then:

- 1. Create a copy of the activation branch, giving you branches B and B'.
- 2. Convert B into an ACM, C, by adding an edge to it's last point, thus leaving a single activation branch B. Set the position of C to 0. Now C is contained within the set of ACMs for S.

Regardless of whether one of the ACMs were active, add a new point to the end of the activation branch. Explicitly, if the activation branch had length n, then add an edge extending from p_{n-1} to the new point p_n , thus creating an activation branch of length n+1.

If none of the ACMs were active after moving them to their next state, we say that S is *inactive* after moving; otherwise we say S is *active* after moving. Therefore, we only add a new ACM to S when S is inactive after moving.

We denote the inition cycle of an ASM C_0 , the first discovered cycle C_1 , and the *n*th discovered cycle C_n .

We denote the graph of ASM $S_{a,n}$ on state k as S^k .

If $C_{p,a}$ is discovered by ASM $S_{a,n}$ on some step k, then we say that $C_{p,a}$ is discoverable by S.

Definition

We'll define $[S^a] = \{ C_i \text{ within the graph of } S \text{ on step } a \}$, and $[S] = \{ C_0 \text{ and all } C_i \text{ disoverable by } S \}$.

Lemma

For $S_{a,n}$, the length of the branch, B, on step k is given by $|B^k| = k+a+n+1$.

Proof

One step 0, the length of branch B is given by $|B^0| = 0 + a + n + 1$. With each step, a single node is added to the branch B. Thus, $|B^{i+1}| = |B^i| + 1$.

Assume
$$|B^i| = i + a + n + 1$$
.
Then $|B^{i+1}| = |B^i| + 1 = (i + a + n + 1) + 1 = (i + 1) + a + n + 1$.

Thus we have shown that $|B^k| = k + a + n + 1$ by induction. Q.E.D

Lemma

For $S_{a,n}$, if C_i is discovered on step k, then the length of $|C_i| = |B^{k-1}| = k + a + n$.

Assume for $S_{a,n}$, that C_i is discovered on step k.

To produce state k, the ASM algorithm first moved all C_j for j < i from state C^{k-1} to state C^k . After doing so, there did not exist a j < i such that C_j was active. Therefor, the algorithm copied the branch B^{k-1} and closed one of the two branches to create C_i .

Thus, the length of C_i is equal to the length of the branch B^{k-1} : $|C_i| = |B^{k-1}| = (k-1) + a + n + 1 = k + a + n$. Q.E.D

Lemma

For
$$S_{a,n}$$
, $|C_i| \ge |C_{i-1}| + a$.

Proof

Assume cycle C_i is discovered by $S_{a,n}$ on step k.

Then
$$\overline{C_i^k} = 0$$
.

Furthermore, the new branch, B, will have $|C_i| + 1$ nodes at step k.

For next, $1 \leq j < a$ steps, the cycle C_i^{k+j} will be active since there are a activation nodes.

Furthermore, the length of the branch B at each step will be given by $|B| = |C_i| + j + 1$.

The ath step after discovering C_i will be the first time that C_i will be inactive. The branch length of the (a-1)th step is given by $|B^{j+a-1}| = |C_i| + a$. Thus, if C_p for $0 \le p < i$ are also inactive on step ath step after discovering C_i , then we will have to close B on the ath step, thus creating cycle C_{i+1} with length $|C_{i+1}| = |B^{j+a-1}| = |C_i| + a$. Furthermore, if any of the cycles C_p were active on the ath step after discovering C_i , then the branch would not close, thus the next cycle's length is at least as long as the branch on the (j+a)th step: $|C_{i+1}| >= |B^{j+a}| = |C_i| + a + 1$.

Thus, we have shown that $|C_i| \ge |C_{i-1}| + a$. Q.E.D

Lemma

For any $C_i, C_j \in [S_{a,n}]$ with j < i, it holds that $|C_i| \ge |C_j| + (i-j)a$.

Proof

If
$$i = j + 1$$
, then $j - i = 1$.
Thus, $|C_i| \ge |C_j| + a = |C_j| + (j - i)a$.

Assume for $k, i < k \le j$, that $|C_k| \ge |C_i| + (k-i)a$.

Then
$$|C_{k+1}| \ge |C_k| + a \ge (|C_i| + (k-i)a) + a = |C_i| + (k+1-i)a$$
.

Thus we have shown that $|C_i| \ge |C_j| + (i-j)a$ by induction. Q.E.D

Corollary

For any cycle C_j of an ASM, $S_{a,n}$, C_j has at least n+ja non-activator nodes.

Proof

 C_0 is defined to have n activator nodes.

Let
$$C_{j>0} \in [S_{a,n}]$$
.

Then
$$|C_j| \ge |C_1| + (j-1)a \ge (|C_0| + a) + (j-1)a$$

= $(2a+n) + (j-1)a = n + (j+1)a$.

Thus, after removing the a activator nodes from C_j , there are at least n+ja non-activator nodes left.

Q.E.D

Lemma

Every ASM discovers at least one cycle.

Proof

Let C_0 by the initial cycle for ASM, $S_{a,n}$.

After taking a steps from the initial state of the S, the ASM will be on it's first non-activator node.

Since C_0 is the only cycle, the ASM would be inactive, thus a new cycle would be created.

Q.E.D

Lemma

For any step, k, for any $C_i \in [S_{a,n}^k]$, it holds that $\overline{C_i^k} = (k+a+n) \mod |C_i|$.

Proof

The initial cycle C_0 starts at position 0 on step 0. By properties of ACM's, we know that the position of C_0 is given by:

$$\overline{C_0^k} = k \mod |C_0| = [k + (a+n)] \mod (a+n) = (k+a+n) \mod |C_0|.$$

If a cycle, C_i , is discovered on step k, then we know it's length is given by $|C_i| = k + a + n$. Furthermore, when it's discovered, it's position is set to 0.

Thus, the position of C_i^k is given by:

$$\overline{C_i^k} = 0 = (k + a + n) \mod (k + a + n) = (k + a + n) \mod |C_i|.$$

By properties of ACM's, the position for all steps j > k will be given by:

$$\overline{C^j} = (\overline{C^k} + (j - k)) \mod |C^i| = (0 + (j - k)) \mod (k + a + n)$$
$$= (k + a + n) + (j - k) \mod |C_i| = (j + a + n) \mod |C_i|.$$

Therefor we have shown that the position of C_i on step k for any $C_i \in [S_{a,n}^k]$ is given by $\overline{C_i^k} = (k+a+n) \mod |C_i|$ for any C_i in $[S^k]$. Q.E.D

Corollary

For any cycle $C_j \in [S_{a,n}]$, moving $k|C_j|$ steps will maintain C_j 's position.

Proof

Let $C_i \in [S]$.

Assume S is on step p.

Then $\overline{C_j} = p + a + n \mod |C_j|$.

Thus, if we move $k|C_j|$ steps from p, the position of C_j will be given by:

$$p + a + n + k|C_j| \mod |C_j| = p + a + n \mod |C_j|.$$

Therefor C_j 's position was maintained. Q.E.D

Lemma

For any cycle $C \in [S]$, if $k \ge |C|$, then the position of C after moving k steps from C's discovery is the same as moving $k \mod |C|$ steps.

Proof

Assume $C \in [S]$, and S is on step p.

Then the position of C is given by $p + a + n \mod |C|$.

Let k > |C|, $b = k \mod |C|$.

The position of C on step p + k is given by:

 $p+k+a+n \mod C=p+b+a+n \mod C$ which is the position after moving b steps from p. Q.E.D

Lemma

For any $C_i, C_j \in [S_{a,n}]$ with j < i, it holds that $|C_i| \mod |C_j| \ge a$.

Proof

Assume for ASM, $S_{a,n}$, that ACM, C_i , is discovered on step k.

Then
$$|C_i| = k + a + n$$
.

We know also know that the position of C_j^k must be greater than or equal to a; otherwise, C_j would be active on step k and we would not have discovered C_j .

Furthermore, we know the position of C_j^k is given by:

$$\overline{C_j^k} = (k + a + n) \bmod |C_j|.$$

Finally, substituting gives us: $\overline{C_j^k} = |C_i| \mod |C_j| \ge a$.

Thus we have shown that, $|C_i| \mod |C_j| \ge a$. Q.E.D

Lemma

For any $C_i \in [S_{a,n}]$, $|C_i|$ is the least positive integer greater than $|C_{i-1}|$ such that $|C_i| \mod |C_j| \ge a$ for all j < i.

Proof

Assume you discovered C_{i-1} on step p.

Assume k is the first step after discovering C_{i-1} such that all cycles are inactive (if we can show that cycle C_i is discovered on step k, then our proof will be complete).

Then, on all steps, $q, p \leq q < k$, there must exist at least one cycle C_j that is active (implying $q + a + n \mod |C_j| < a$). Therefore, the ASM algorithm cannot create cycle C_i on any step $p \leq q < k$.

Furthermore, on step k, the algorithm must create C_i , giving us $\overline{C_i^k} = 0 = k + a + n \mod |C_i|$.

Thus, since $k + a + n = |C_i|$ is the least positive integer such that $|C_i|$ $mod |C_j| \ge a$ for all j < i, and have proved our lemma. Q.E.D

Definition

A positive integer is prime if it's only factors are 1 and itself.

Axiom

The *i*th prime number, p_i , is the least integer that is greater than the (i-1)th prime number and is not divisible by p_j for all j < i (with the first prime number $p_0 = 2$).

Note: This is only an axiom because proving the statement is distracting to ASMs.

Lemma

 $|S_{1,1}| = P = \{ \text{ the set of prime numbers } \}$

Proof

 $S_{1,1}$ starts with an initial cycle of length 1+1=2, thus giving us the first prime number.

For all i, j such that $i > j \ge 0$, C_i will have the property that $|C_i| \mod |C_j| \ge 1$, equivalenty, $|C_i|$ is not divisible by any of the previous lengths $|C_j|$. Furthermore, $|C_i|$ is the smallest such integer greater than $|C_{i-1}|$ with the property of not being divisible by the previous cycle lengths.

Thus, by our axiom, $S_{1,1}$ produces the prime numbers. Q.E.D

Theorem

For every ASM, S, the set [S] is non-finite.

Proof

Assume there exists an ASM, $S_{a,n}$ such that $[S_{a,n}]$ is finite. Let s be the number of cycles in $[S_{a,n}]$.

Then there exists some step p on which the last cycle, $C_{max} = C_{s-1}$ of

the ASM is discovered.

We know C_{max} must have at least n+(s-1)a>(s-1)a non-activator nodes.

We also know that on step p, all cycles $C_{i < s}$ must have been inactive to have discovered C_{max} .

Furthermore, on step j, C_{max} 's position is at 0.

Let
$$z = \prod_{i < s} |C_i|$$
.

If we move the $ASM\ z$ steps, then the position of every $C_{i < z}$ will be maintained since z is a multiple of the length of every $C_{i < z}$.

Thus, if after moving z steps from p, C_{max} is inactive, then we would need to create a new cycle, and we'd be finished with our proof.

Assume C_{max} was active after moving the z steps.

Let
$$n = \overline{C_{max}}$$

We know n < a since C_{max} is inactive.

Note: the position of C_{max} after moving zt steps is the same as after moving nt steps since $z > |C_{max}|$ (if z were less than $|C_{max}|$, then moving z steps would have inactivated C_{max} since z > a).

Let j be the greatest integer such that jn < a.

Then your position after moving jz steps will be a - jn.

Thus, the (j+1)zth step will put C_{max} at position $(a-jn)+n \geq a$.

If the ASM is to remain active, then (a-jn)+n must go beyond all (s-1)a non-activator nodes in C_{max} .

Thus,
$$(a - jn) + n > a + (s - 1)a \ge sa \ge 2a$$
.

But both n and (a - jn) are less then a.

But that means: $a + a = 2a > (a - jn) + n \ge 2a$, which is a contradiction!

Therefore, moving (j+1)z steps from the discovery of C_{max} will maintain the (inactive) positions of all $C_{i < z}$ and also move C_{max} into one of it's inactive

nodes, requiring a new cycle to be made, and completing our proof. Q.E.D

Corollary

There are an infinite number of prime numbers.

Proof

 $S_{1,1}$ produces the prime numbers, and $[S_{1,1}]$ is non-finite by the above theorem.

Q.E.D

5 Needy Cycle Machines

Definition

A Needy Cycle Machine (NSM) is state machine running on top of a directed graph composed of a set of ACMs and a single activation branch.

A NSM starts with k > 0 initial cycles, $\{C_0, ..., C_{k-1}\}$. Each of the k initial cycles must have a unique length and contain the same number of activator nodes. Futhermore, the initial position of every initial cycle is 0. The initial branch length is a single node longer than the longest initial cycle.

Like an ASM, every cycle in an NSM is moved one state with each iteration. However, an NSM is *active* only if at least k cycles are active; otherwise, the NSM is *inactive*.

If an NSM is inactive after moving all of it's cycles, then it behaves exactly as an ASM by copying its activation branch and creating a new cycle with one of the two branches.

Regardless of whether an NSM is active after moving all of it's cycles, a new node is added to the end of the activation branch.

6 Complicated Cycle Machines

Definition

A Complicated Cycle Machine (CCM) is basically the same as an ASM; however, the activators nodes of an CCM can be any of the nodes within the

initial cycle, with the condition that position 0 is always one of the activator nodes.