

A research project on simulating the properties of three-dimensional  $z_2$  lattice gauge model

1) The equilibrium properties of 3D Lattice Gauge Model (also called Classic Toric Code model)

Here we apply Metropolis algorithm to simulate the equilibrium properties of the 3D Lattice Gauge Model at different temperature.

The process for simulation is:

- a) Build the lattice for the 3D Lattice Gauge Model
- b) Initialize the system with random spins
- c) Performing Monte Carlo steps to equilibrium the system at the initial temperature  $T_i$  ( $T_i$  comes from input)
- d) Take measurements: energy, magnetization etc.
- e) Decrease the temperature by  $dT$
- f) Repeat c)-e) till the final temperature  $T_f$  is reached
- g) Write results to files

The folder contains the following code:

to.h: header file with declarations of arrays, functions etc.

to\_equ.cxx : functions are defined within this file, such as initialization, Monte Carlo update, taking measurement etc.

to.cxx: main program, calculating the order parameter, energy for different temperatures with Monte Carlo.

to\_binaverage.cxx : calculating the averages and error bars of the original measurements after running to.cxx.

To compile:

`g++ to_equ.cxx to.cxx`

To Run:

`./a.out`

The input file "input.txt" has the following format:

```
ll dd
init istp mstp nbin
filename confname
ti tf
```

ll: system size

dd: system dimension, here  $dd=3$

init: an indicator about whether or not to initialize the system (0 yes, otherwise no)

istp: number of Monte Carlo steps to equilibrium the system

mstp: number of repetitions of taking measurement within one bin  
nbin: number of bins  
filename: the output filename  
confname: file name for storing the configuration  
ti: initial temperature  
tf: final temperature

## 2) The dynamical properties of 3D Lattice Gauge Model (also called Classic Toric Code model)

In this part, we employed Simulated Annealing to calculate the dynamical properties of the correlations within the 3D Lattice Gauge Model.

The process for simulation is:

- a) Build the lattice for the 3D Lattice Gauge Model
- b) Initialize the system with random spins
- c) Performing Monte Carlo steps to equilibrium the system at the initial temperature  $T_i$  ( $T_i$  comes from input)
- d) Take measurements: energy, magnetization etc.
- e) Decrease the temperature by  $dT$
- f) Perform one Monte Carlo Step
- e) Repeat d) to f) till final temperature  $T_f$  is reached
- f) Write results to files

The folder contains the following code:

corr.h: header file with declarations of arrays, functions etc.

corr\_quench.cxx: functions are defined within this file, such as Monte Carlo update, decreasing temperature, taking measurements etc.

corr.cxx: main program, taking measurement at each step with simulated annealing.

corr\_binaverage.cxx: calculating the averages and error bars of the original measurements after running corr\_quench.cxx.

To compile:

g++ to\_equ.cxx to.cxx

To Run:

./a.out

The input file "input.txt" has the following format:

ll dd  
init istp mstp nbin  
qtime qpnt  
filename confname  
ti tf

ll: system size  
dd: system dimension, here dd=3  
init: an indicator about whether of not to initialize the system (0 yes, otherwise no)  
istp: number of Monte Carlo steps to equilibrium the system at  $T_i$   
mstp: number of repetitions of taking measurement within one bin  
nbin: number of bins  
qtime: total annealing time  
qpnt: number of data points to save and write  
filename: the output filename  
confname: file name for storing the configuration  
ti: initial temperature  
tf: final temperature