

Identitas Trigonometri

$$\begin{array}{lll}
 \sin^2 x + \cos^2 x = 1 & \sin(x \pm y) = \sin x \cos y \pm \cos x \sin y & \sin x + \sin y = 2 \sin\left(\frac{x+y}{2}\right) \cos\left(\frac{x-y}{2}\right) \\
 \sin(-x) = -\sin x & \cos(x \pm y) = \cos x \cos y \mp \sin x \sin y & \sin x - \sin y = 2 \cos\left(\frac{x+y}{2}\right) \sin\left(\frac{x-y}{2}\right) \\
 \cos(-x) = \cos x & \sin(2x) = 2 \sin x \cos x & \cos x + \cos y = 2 \cos\left(\frac{x+y}{2}\right) \cos\left(\frac{x-y}{2}\right) \\
 \tan(-x) = -\tan x & \cos(2x) = \cos^2 x - \sin^2 x & \cos x - \cos y = -2 \sin\left(\frac{x+y}{2}\right) \sin\left(\frac{x-y}{2}\right) \\
 \sin(90^\circ - x) = \cos x & = 2 \cos^2 x - 1 & \\
 & = 1 - 2 \sin^2 x & \\
 \cos(90^\circ - x) = \sin x & &
 \end{array}$$

Rumus Euler : $e^{ix} = \cos x + i \sin x$

Teorema De Moivre : $(\cos x + i \sin x)^n = \cos nx + i \sin nx$, $n \in \mathbb{Z}$

Eksansi deret Taylor untuk $\sin x$: $\sin x = x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!} + \dots$

$$= \sum_{n=0}^{\infty} \frac{(-1)^n}{(2n+1)!} \cdot x^{2n+1}$$

Eksansi deret Taylor untuk $\cos x$: $\cos x = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \frac{x^6}{6!} + \dots$

$$= \sum_{n=0}^{\infty} \frac{(-1)^n}{(2n)!} \cdot x^{2n}$$

Limit Fungsi Trigonometri

$$\lim_{x \rightarrow 0} \frac{\sin ax}{bx} = \frac{ax}{\sin bx} = \frac{\sin ax}{\sin bx} = \frac{a}{b}$$

$$\lim_{x \rightarrow 0} \frac{1 - \cos x}{x} = 0$$

$$\lim_{x \rightarrow 0} \frac{\tan ax}{bx} = \frac{ax}{\tan bx} = \frac{\tan ax}{\tan bx} = \frac{a}{b}$$

$$\lim_{x \rightarrow 0} \frac{1 - \cos x}{x^2} = \frac{1}{2}$$

$$\lim_{x \rightarrow 0} \frac{\tan ax}{\sin bx} = \frac{\sin ax}{\tan bx} = \frac{a}{b}$$

Aturan L'Hôpital (L'H) :

Jika $\lim_{x \rightarrow a} f(x) = \lim_{x \rightarrow a} g(x) = 0$ atau $\pm \infty$ maka

$$\lim_{x \rightarrow a} \frac{f(x)}{g(x)} = \lim_{x \rightarrow a} \frac{f'(x)}{g'(x)} = \lim_{x \rightarrow a} \frac{f''(x)}{g''(x)} = \dots$$

Turunan Fungsi Trigonometri

$$\frac{d}{dx}(\sin x) = \cos x$$

Aturan – Aturan Turunan

$$\frac{d}{dx}(\cos x) = -\sin x$$

$$\text{Aturan pangkat : } \frac{d}{dx}(ax^n) = nax^{n-1}$$

$$\frac{d}{dx}(\tan x) = \sec^2 x$$

Aturan kelipatan konstanta : $(c \cdot f)' = cf'$, dengan c adalah konstanta

$$\frac{d}{dx}(\cot x) = -\csc^2 x$$

$$\text{Aturan fungsi konstan : } \frac{d}{dx}(c) = 0$$

$$\frac{d}{dx}(\sec x) = \tan x \sec x$$

Aturan – aturan turunan Fungsi Komposisi

Untuk sembarang fungsi f , g , dan h , aturan – aturan berikut berlaku.

$$\frac{d}{dx}(\csc x) = -\csc x \cot x$$

Aturan penjumlahan & pengurangan :

$$(f \pm g)' = f' \pm g'$$

Aturan perkalian :

$$(f \cdot g)' = fg' + f'g \quad (\text{kiri kanan aksien} + \text{kanan kiri aksien})$$

Aturan pembagian :

$$\left(\frac{f}{g}\right)' = \frac{gf' - fg'}{g^2} \quad (\text{bawah atas aksien} - \text{atas bawah aksien, semuanya per bawah}^2)$$

Aturan rantai :

$$\text{Jika } h = (f \circ g) \text{ maka } h' = (f' \circ g) \cdot g'$$

