### hw1

#### October 9, 2020

- 1 Computer Vision
- 2 Jacobs University Bremen
- 3 Fall 2020
- 4 Homework 1

In this homework, we will go through basic linear algebra and image manipulation.

One of the aims of this homework assignment is to get you to start getting comfortable searching for useful library functions online. So in many of the functions you will implement, you will have to look up helper functions.

```
[1]: # Submitted By: Nayan Man Singh Pradhan
     #Imports the print function from newer versions of python
     from __future__ import print_function
     #Setup
     # The Random module for implements pseudo-random number generators
     import random
     # Numpy is the main package for scientific computing with Python.
     # This will be one of our most used libraries in this class
     import numpy as np
     #Imports all the methods in each of the files: linalq.py and imageManip.py
     from linalg import *
     from imageManip import *
     #Matplotlib is a useful plotting library for python
     import matplotlib.pyplot as plt
     # This code is to make matplotlib figures appear inline in the
     # notebook rather than in a new window.
```

## 5 Part 1: Linear Algebra Review

In this section, we will review linear algebra and learn how to use vectors and matrices in python using numpy. By the end of this section, you will have implemented all the required methods in linalg.py.

### 5.1 Question 1.1 (5 points)

First, let's test whether you can define the following matrices and vectors using numpy. Look up np.array() for help. In the next code block, define M as a (4,3) matrix, a as a (1,3) row vector and b as a (3,1) column vector:

$$M = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \\ 10 & 11 & 12 \end{bmatrix}$$

$$a = \begin{bmatrix} 1 & 1 & 0 \end{bmatrix}$$

$$b = \begin{bmatrix} -1\\2\\5 \end{bmatrix}$$

```
[2]: M = np.array([[1,2,3],[4,5,6],[7,8,9],[10,11,12]])
    a = np.array([[1],[1],[0]])
    a = a.transpose()
    b = np.array([[-1],[2],[5]])
    pass
    ### END CODE HERE
    print("M = \n", M)
    print("The size of M is: ", M.shape)
    print()
```

```
print("a = \n", a)
print("The size of a is: ", a.shape)

print()
print("b = \n", b)
print("The size of b is: ", b.shape)
```

```
M =
  [[ 1  2  3]
  [ 4  5  6]
  [ 7  8  9]
  [10  11  12]]
The size of M is: (4, 3)

a =
  [[1  1  0]]
The size of a is: (1, 3)

b =
  [[-1]
  [ 2]
  [ 5]]
The size of b is: (3, 1)
```

#### 5.2 Question 1.2 (5 points)

Implement the dot\_product() method in linalg.py and check that it returns the correct answer for  $a^Tb$ .

```
[3]: # Now, let's test out this dot product. Your answer should be [[1]].

aDotB = dot_product(a, b)

print(aDotB)

print("The size is: ", aDotB.shape)
```

```
[[1]]
The size is: (1, 1)
```

### 5.3 Question 1.3 (5 points)

Implement the complicated\_matrix\_function() method in linalg.py and use it to compute  $(a^Tb)Ma^T$ 

IMPORTANT NOTE: The complicated\_matrix\_function() method expects all inputs to be two dimensional numpy arrays, as opposed to 1-D arrays. This is an important distinction, because 2-D arrays can be transposed, while 1-D arrays cannot.

To transpose a 2-D array, you can use the syntax array.T

```
[4]: # Your answer should be $[[3], [9], [15], [21]]$ of shape(4, 1).
     ans = complicated_matrix_function(M, a, b)
     print(ans)
     print()
     print("The size is: ", ans.shape)
    [[ 3]
     [ 9]
     [15]
     [21]]
    The size is: (4, 1)
[5]: M = np.array(range(4)).reshape((2,2))
     a = np.array([[1,1]])
     b = np.array([[10, 10]]).T
     print(M.shape)
     print(a.shape)
     print(b.shape)
     print()
     # Your answer should be $[[ 20], [100]]$ of shape(2, 1).
     ans = complicated_matrix_function(M, a, b)
     print(ans)
     print()
     print("The size is: ", ans.shape)
    (2, 2)
    (1, 2)
    (2, 1)
    [[ 20]
     [100]]
    The size is: (2, 1)
```

### 5.4 Question 1.4 (10 points)

Implement svd() and get\_singular\_values() methods. In this method, perform singular value decomposition on the input matrix and return the largest k singular values (k is specified in the method calls below).

```
[6]: # We have changed the value for M in question 1.3_b,
# In order to get desired svd(line 6), we need to change it back to the
□ → original value

M = np.array([[1,2,3],[4,5,6],[7,8,9],[10,11,12]])
print("M =")
```

```
M =
[[ 1 2 3]
  [ 4 5 6]
  [ 7 8 9]
  [10 11 12]]
[25.46240744]
[25.46240744 1.29066168]
```

### 5.5 Question 1.5 (10 points)

Implement eigen\_decomp() and get\_eigen\_values\_and\_vectors() methods. In this method, perform eigenvalue decomposition on the following matrix and return the largest k eigen values and corresponding eigen vectors (k is specified in the method calls below).

$$M = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}$$

```
[7]: # Let's define M.
    M = np.array([[1,2,3],[4,5,6],[7,8,9]])

# Now let's grab the first eigenvalue and first eigenvector.
# You should get back a single eigenvalue and a single eigenvector.
val, vec = get_eigen_values_and_vectors(M[:,:3], 1)
print("First eigenvalue =", val[0])
print()
print("First eigenvector =", vec[0])
print()
assert len(vec) == 1

# Now, let's get the first two eigenvalues and eigenvectors.
```

```
# You should get back a list of two eigenvalues and a list of two eigenvector
 \hookrightarrow arrays.
val, vec = get_eigen_values_and_vectors(M[:,:3], 2)
print("Eigenvalues =", val)
print()
print("Eigenvectors =", vec)
assert len(vec) == 2
First eigenvalue = 16.116843969807043
First eigenvector = [[-0.23197069 -0.78583024 0.40824829]
 [-0.8186735
               0.61232756 0.40824829]
 [-0.52532209 -0.08675134 -0.81649658]]
Eigenvalues = [1.61168440e+01 -9.75918483e-16]
Eigenvectors = [[-0.23197069 -0.78583024 0.40824829]]
  [-0.8186735
               0.61232756 0.40824829]
  [-0.52532209 -0.08675134 -0.81649658]]
```

## 6 Part 2: Image Manipulation

[-0.23197069 -0.78583024 0.40824829] [-0.52532209 -0.08675134 -0.81649658]]]

0.61232756 0.40824829]

Γ[-0.8186735

Now that you are familiar with using matrices and vectors. Let's load some images and treat them as matrices and do some operations on them. By the end of this section, you will have implemented all the methods in imageManip.py

```
[8]: # Run this code to set the locations of the images we will be using.

# You can change these paths to point to your own images if you want to try

them out for fun.

#image1_path = 'Documents/fall2020/ComputerVision/ComputerVision/assignment1/

code/image1.jpg'

image1_path = './image1.jpg'

image2_path = './image2.jpg'

def display(img):

# Show image

plt.figure(figsize = (5,5))

plt.imshow(img)

plt.axis('off')

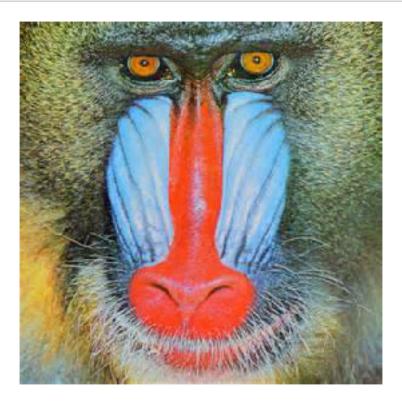
plt.show()
```

# 6.1 Question 2.1 (5 points)

Implement the load method in imageManip.py and read the display method below. We will use these two methods through the rest of the notebook to visualize our work.

```
[9]: image1 = load(image1_path)
image2 = load(image2_path)

display(image1)
display(image2)
```





## 6.2 Question 2.2 (10 points)

Implement the dim\_image() method by converting images according to  $x_n = 0.5 * x_p^2$  for every pixel, where  $x_n$  is the new value and  $x_p$  is the original value.

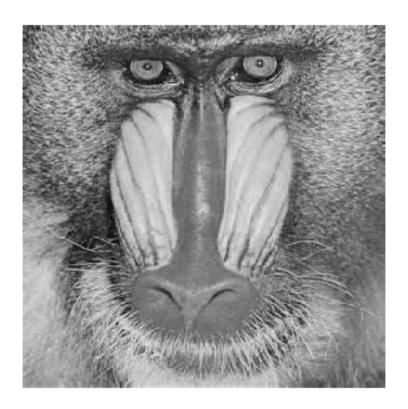
Note: Since all the pixel values of the image are in the range [0, 1], the above formula will result in reducing these pixels values and therefore make the image dimmer.



# 6.3 Question 2.3 (10 points)

 $Implement\ the\ convert\_to\_grey\_scale\ method\ and\ convert\ the\ image\ into\ grey\ scale.$ 

```
[11]: grey_image = convert_to_grey_scale(image1)
display(grey_image)
```



## 6.4 Question 2.4 (10 points)

Implement the rgb\_exclusion(), in which the input image is decomposed into the three channels: R, G and B and return the image excluding the specified channel.

```
[12]: without_red = rgb_exclusion(image1, 'R')
   without_blue = rgb_exclusion(image1, 'B')
   without_green = rgb_exclusion(image1, 'G')

   print("Below is the image without the red channel.")
   display(without_red)

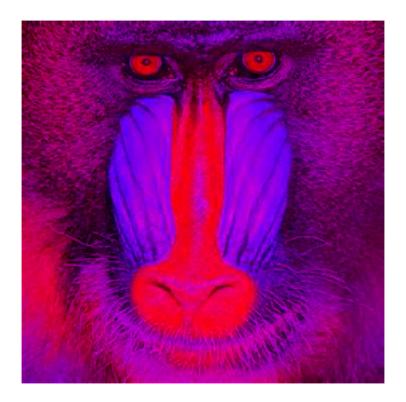
   print("Below is the image without the green channel.")
   display(without_green)

   print("Below is the image without the blue channel.")
   display(without_blue)
```

Below is the image without the red channel.



Below is the image without the green channel.



Below is the image without the blue channel.



### 6.5 Question 2.5 (10 points)

Implement the hsv\_decomposition(), in which the input image is decomposed into the three channels: H, S and V and return the values for the specified channel.

```
[13]: image_h = hsv_decomposition(image1, 'H')
    image_s = hsv_decomposition(image1, 'S')
    image_v = hsv_decomposition(image1, 'V')

print("Below is the image with only the H channel.")
    display(image_h)

print("Below is the image with only the S channel.")
    display(image_s)

print("Below is the image with only the V channel.")
    display(image_v)

# print('For LAB')
```

```
# image_l = lab_decomposition(image1, 'L')
# image_a = lab_decomposition(image1, 'A')
# image_b = lab_decomposition(image1, 'B')

# print("Below is the image with only the L channel.")
# display(image_l)
# print("Below is the image with only the A channel.")
# display(image_a)
# print("Below is the image with only the B channel.")
# display(image_b)
```

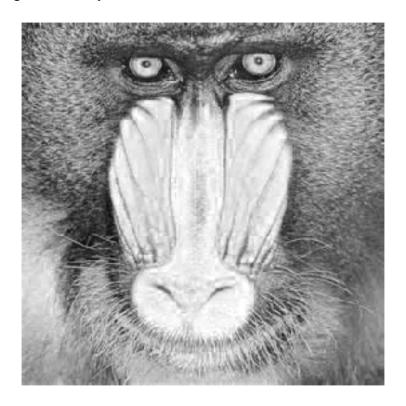
Below is the image with only the H channel.



Below is the image with only the S channel.



Below is the image with only the  $\ensuremath{\text{V}}$  channel.



#### 6.5.1 Question:

Explain in 2-3 sentences what the H, S and V channels are and what happens when you take away the both the H and S channels. ### Answer: The H, S, and V channels represents Hue, Saturation, and Value respectively. The Hue (H) is the color of the image, the Saturation (S) is the pureness of the hue color, and the Value (V) is the strength/intensity of the hue. If you take away both the H and S channels, only the Value (V) channel remains. This means only the strength/intensity of the hue color is shown (without the hue and saturation).

### 6.6 Question 2.6 (10 points)

In mix\_images method, create a new image such that the left half of the image is the left half of image1 and the right half of the image is the right half of image2. Exclude the specified channel for the given image.

You should see the left half of the monkey without the red channel and the right half of the house image with no green channel.

```
[14]: image_mixed = mix_images(image1, image2, channel1='R', channel2='G')
display(image_mixed)

#Sanity Check: the sum of the image matrix should be 76421.98
np.sum(image_mixed)
```



### [14]: 76421.98431372548

```
[15]: # Extra Credit Function

quadrants_image_mix_1 = mix_quadrants(image1)
print("For image1:")
display(quadrants_image_mix_1)

quadrants_image_mix_2 = mix_quadrants(image2)
print("For image2:")
display(quadrants_image_mix_2)
```

For image1:



For image2:

