16. Understanding Shapes-II Quadrilaterals

16. understanding Shapes - 2 (Quadrilaterals).

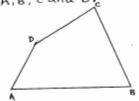
solution - 01:-

(i) Quadrilateral:-

Let A, B, c and D be four points in a plane such that:

- (i) no three of them are collinear, and,
- intersect except at their and points.

then, the figure formed by made up of the four line segments is called the quadrilateral with vertices A,B, c and D;



convex Quadrilateral:

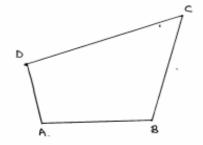
A quadrilateral is called convex quadrilateral, if the Line containing any side of the quadrilateral has the remaining vertices on the same side of it. In fig below quadrilateral ABCD is a convex quadrilateral, because.

Vertices A,B Lie on the same side of Line CD,

Vertices B,c Lie on the same side of Line DA,

Vertices C,D Lie on the same side of Line AB,

and Vertices D,A Lie on the same side of Line BC



50lution-02:-

(i) sides :-

In a quadrilateral ABCD, the four Line segments AB, BC, CD and DA are called its sides.

(ii) vertices:

In a quadrilaterals ABCP The Points A,B,C and D are called as Vertices.

(111) Angles:-

In the quadrilateral ABCD, the angles, LDAB, LABC, LBCD and LD (07) LCDA are called its angles. These angles tan be denoted LA, LB, LC and LD respectively.

(iv) Adjacent angles:-

and LE, LD are rathed Adjacent angles.

(common side)

(V) piagonals:-

In the quadrilaterals ABCD, the line segments Ac and BD are called. its diagonals.

(vi) Adjacent sides :-

Two sides or a quadrilateral are called its adjacent sides, if they have a common end-point.

(VII) opposite sides:

Two sides of a quadrilateral are called its opposite sides, if they do not have a common end-point.

Will) opposite Angles:-

Two angles of a quadrilateral are called its opposite angles, if they donot have a common end-point. side (or) Arm.

(ix) Interior :-

The part of the plane made up by all such points as are enclosed by anadrilateral ABCD. This part os the plane is called the interior of the anadrilateral ABCD and any point of part is called an interior point of the quadrilateral.

Exterior:-

The part of the plane made up by all points as are not enclosed by the quadrilateral ABCD. This part of the plane is called the exterior of the quadrilateral ABCD and any point of this part is called an exterior point of the quadrilateral.

solution - 3 %-

(i) 4

(ii) 4

(iii) 4, collinear.

(v) 2.

(v) q

(vi) 2

(VII) 366

(VIII) opposite

(1x) four

(x) less than

(XI) the interior

(XII) interiors

(XIII) Nestices.

Solution-4%

- (i) AB. BC OF BC, CD OF CD, DA OF AD, AB.
- (ii) AB, CD OT BC, DA.
- (III) FOUT
- (iv) Two.
- (V) له، لق ۲۵ لق، لا ۲۵ لو، له ۲۵ مر لو، له.
- (VI) LA, LE ON B, LD
- (VII) 4.
- (VIII) 2.

solution -os :-

The angles of a quadritaterals are 110,72°,55° and 2°.

we know that,

sum of angles of a quadrilaterals

⇒110+72+55+x=366

The opposite analess of a anabrilateral = 123°.

required angle is 123°.

6. The given three Angles of a Quadrilaterals

are respectively equal to 110, 50 and 40.

Sum of the angles in a Quadrilateral = 360

Let the fourth angle be'x1

7. Given that.

Three acute ansles each measures 88.

Let the fourth angle bex.

Three angles of Quadrilateral are 80,80 and 80.

we know that,

sum of the angles on a quadrilateral = 360.

: The fourth angle be x = 128.

8. Given that.

A quadrilateral has all its four angles of the same measure:

Let it be'x'

we know that,

sum of the angles of a Quadrilakral=368.

10, Given that.

Three ansles of a quadrilateral are equal.

Fourth angle is of measure 150.

war, sum of the angles of a quadrilateral =

q. Two angles of a quadrilateral are of measure 65° and the other two angles are acqual.

Let it be 'x'

Then WKT,

sum of the ansles of a quadrilateral = 360.

11. The four ansles of a quadrilaterals are

we have , LA: 18:10: 10 = 3:5:7:9.

So, Let LA=3x, LB=5x, LS=7x, LD=9x

.. LA + LB + LC + LD = 36 %

⇒ 3×+5×+¬×+9× =36°

: LA = 3(15) =45° B = 76; B=105°, LP = 135°.

solution-12:-

Given that,

sum of the two angles of a Quadrilateral = 1800 wkT.

sum of the gangles in a quadrilateral = 36%

- => Sum of 2 angles + remaining 2 angles = 368
 - ⇒ 180+ Remaîning 2 angles = 36:
 - ⇒ sum of Remaining 2 ansles = 360°-180° = 180°.

solution-13:-

Given that,

LNOM = 45, LOMP = 90, LONP = 90 and LMPN = 9. we know that,

LNOM + LOMP + LONP+ LMPN = 360

⇒ 45+90+90+ LMPN =360

→ LMPN=360-225°

=> LMPN = 135°.

Required anole is 136.

14. The sides of a quadrilateral are produced in order.

sum of the four exterior angles = 368

[: Let 0,,02,03,04 be the angles of a quadrilateral Then 180-0,,180-01, 180-03 and 180-04 respectively.

$$\begin{array}{ll} .. & 180 - \theta_1 + 180 - \theta_2 + 180 - \theta_3 + 180 - \theta_4 = 360 \\ \\ \Rightarrow & 720 - (\theta_1 + \theta_2 + \theta_3 + \theta_4) = 360 \\ \\ \Rightarrow & \theta_1 + \theta_2 + \theta_3 + \theta_4 = 360 \end{array}$$

15:- Given that,

Le = 100 and P=50 and LA and LB meet at a point P.

sum of the 4 ansles in a quadrilateral = 36%.

$$LA + LB + LC + LP = 36^{\circ}$$

$$LA + LB = 36^{\circ} - 50^{\circ} - 100^{\circ}$$

$$LA + LB = 210^{\circ}$$

$$LA + LB = 210^{\circ}$$

$$LB = 210^{\circ} - 8^{\circ}$$

We know that,

Sum of the angles in a anadoilateral

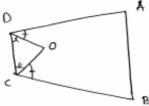
:. The required angle is 75°.

16. The angles in a quadrilateral ABCD are LA,B, LE, LD age in the ratio 1:2:4:5.

プナシハナ 42+52 = 366

Consider a quadrilateral ABCD.

let OD & OC be the angular bisectors of D and C respectively



Let the angle LD be θ^* .

We know that sum of all angles in

ZA4 LB4 LC 4 LD= 360

Here LODC = 12

(because they are

7000 = 1 CC

bisectors.

angular

In Ale ODC,

Sun of all angles = 180'

$$\frac{\theta}{f}$$
 + $2 \cos + \frac{18}{18} - \frac{1}{2} (2A1 + 2B) - \frac{\theta}{f} = \frac{186}{2}$

-> Hence proved.

(8)

(1) Given Exterior angle = 180 - Given interior angle

Given that, interior angle = 160°

=> Exterior angle = 180°-160°

No. of sides = 360 Exterior angle

n = . 18

(ii) Given,

interior anole = 136

Exterior angle = 180 - Given interior angle = 180-135 = 45.

: No of sides = 8.

. (11) Given

(iv) Given,

Interior angle = 162°.

Exterior anole = 18: - Interior angle

Interior angle = 150.

Exterior angle = 180-150

: No . 05 sides = 12,

19. Exterior angle of a regular Pentagon = 360

=7.2°.

. required no of degrees = 72°.

20. Sum of the exterior angles in a hexagon = 36° Given interior angles are 2, 2-5,2-5,22-5, and (22420)°

Then Exterior angles are

180(5) - 2-2+5-2+5-2+5-2+-20-36

=> 97 =1080°-360°

=> x=720/8 => 2=80

Solution -21:-

Hence proved

Solution - 22:-

Let the given Polygon ontain in sides

let the vertices be 1,2,3 ---- n

Sun of exterior angles = 360.

Sum of interior angles

1344 given that

sum of interior angles = 9x sum of interior

$$\Rightarrow$$
 $u = (3x360 + 360)$

=> polygon is edugon.

But given

$$\Rightarrow \frac{360}{500} = \frac{1}{5}$$

$$=> \frac{2}{N-2} = \frac{1}{5}$$

No of side in polygon = 12



Let. Parstu is regular Henagon

Me know

we know,