

## Gradient descent

Optimization algorithm to minimize a cost function  
Goal is to find the optimal set of parameters that minimizes cost function  
Primary idea is the to move in the direction of steepest descent of a function to reach local minimum

Learning rate:- It is a hyperparameter that determines the size of the steps taken

$$x_{\text{new}} = x_{\text{old}} + \alpha * f'(x)$$

$$f(x) = x^2 - 2x + 2$$

$$f'(x) = 2x - 2$$

for suppose  $x = 3$  &  $\alpha = 0.2$

$$\therefore x_{\text{new}} = x_{\text{old}} + 0.2 * f'(3)$$

$$= 3 + 0.2 * (6 - 2)$$

$$= 3 + 0.2 * 4$$

$$x_{\text{new}} = 3 - 0.8 = 2.2$$



$$\text{Now } X_{\text{old}} = 2.2$$

$$\begin{aligned} \therefore X_{\text{new}} &= 2.2 - 0.2 \times 4'(2.2) \\ &= 2.2 - 0.2 \times (2 \times 2.2 - 2) \\ &= 2.2 - 0.2 \times 2.4 \\ &= 2.2 - 0.48 \\ &= 1.72 \end{aligned}$$

Repeat the steps until you reach the minimum

Batch vs Mini batch

Batch gradient descent

Mini-batch gradient descent

The entire training dataset is used in each iteration to compute the gradient

It divides the dataset into smaller batches & compute the gradient for each batch.

Accurate gradient

Computationally intensive

Stable updates parameters are more stable

can be parallelized

faster convergence

slow convergence

Noisy updates.

## Stochastic gradient Descent

Variant of gradient descent which processes a single randomly selected training example instead of processing the entire dataset in each iteration