

$P = A + \lambda \vec{v}$ vetor diretor $\neq \vec{0}$
parâmetros

Eq. Vetorial reta no espaço
 $(x, y, z) = (x_0, y_0, z_0) + \lambda(a, b, c)$

Eq. paramétricas

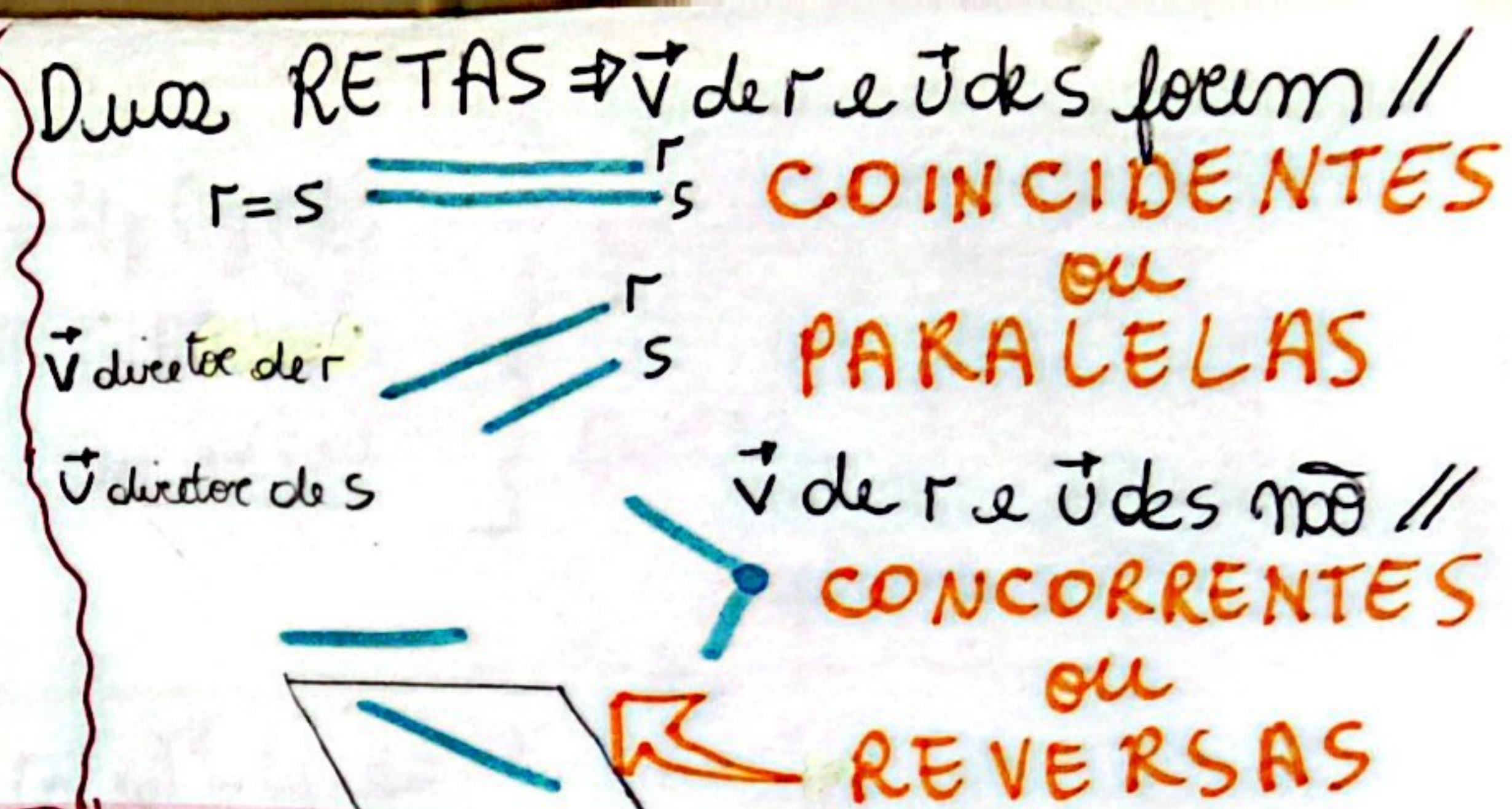
$$\begin{cases} x = x_0 + \lambda a \\ y = y_0 + \lambda b \\ z = z_0 + \lambda c \end{cases}$$
ponto A qualquer

Eq. simétricas **RETA**

$$\lambda = \frac{x-x_0}{a} = \frac{y-y_0}{b} = \frac{z-z_0}{c}$$

Eq. reduzidos

$$\begin{cases} y = mx + n \\ z = px + q \end{cases}$$



Ângulo entre duas retas

$$\cos \theta = \frac{|\vec{v}_1 \cdot \vec{v}_2|}{\|\vec{v}_1\| \cdot \|\vec{v}_2\|}$$
 $\theta \geq 0$ e $\theta \leq \frac{\pi}{2}$
 90°

PLANOS

Eq. vetorial
 $(x, y, z) = (x_0, y_0, z_0) + \lambda(a, b, c) + \mu(a_1, b_1, c_1)$

parâmetros parâmetros

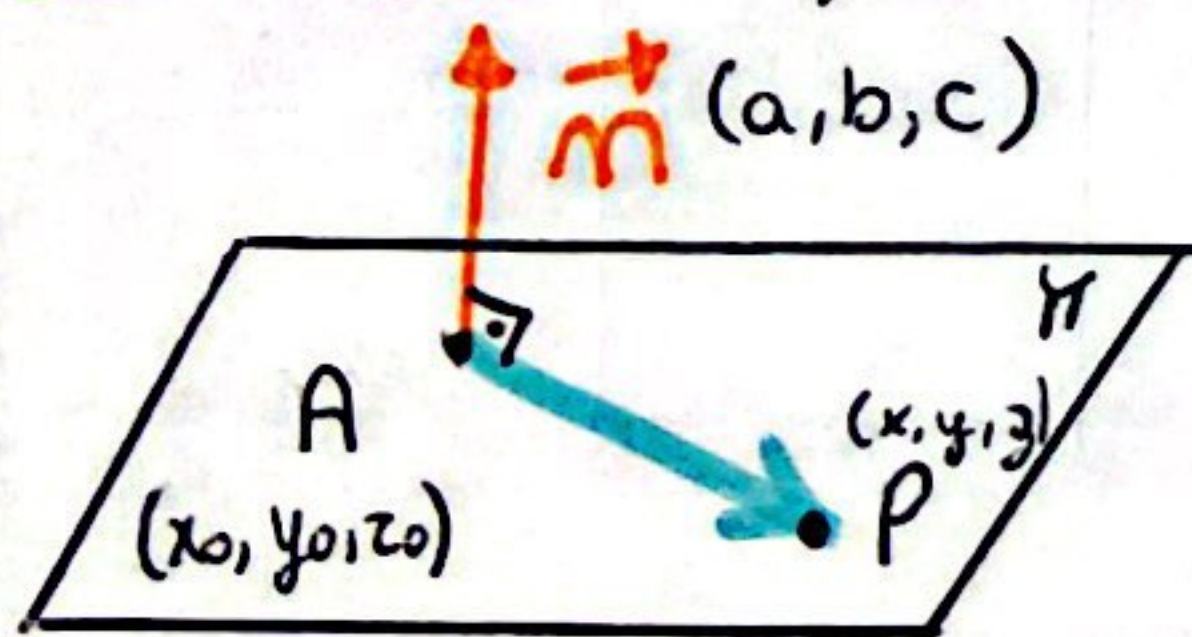
$P = A + \lambda \vec{u} + \mu \vec{v}$

Eq. paramétricas

$$\begin{cases} x = x_0 + \lambda a + \mu a_1 \\ y = y_0 + \lambda b + \mu b_1 \\ z = z_0 + \lambda c + \mu c_1 \end{cases}$$

$A(x_0, y_0, z_0)$
 PONTO
 QUALQUER

EQUAÇÃO GERAL de um plano



$\vec{AP} \cdot \vec{n} = 0$

$$ax + by + cz + d = 0$$

Ângulo entre reta e plano no espaço

$$\sin(\theta) = \frac{|\vec{v} \cdot \vec{n}|}{\|\vec{v}\| \cdot \|\vec{n}\|}$$

$\theta \geq 0$
 $\theta \leq 90^\circ = \frac{\pi}{2}$

A, B, C
 não
 colineares
 formam



Ângulo entre dois planos no espaço

$$\cos(\theta) = \frac{|\vec{n}_1 \cdot \vec{n}_2|}{\|\vec{n}_1\| \cdot \|\vec{n}_2\|}$$

$\theta \geq 0$
 e
 $\theta \leq \frac{\pi}{2} = 90^\circ$

PARÁBOLA

$$f(x) = y = ax^2 + bx + c$$

FOCO $(x_0, y_0 + p)$

$$f(y) = x = ay^2 + by + c$$

$$V(-\frac{b}{2a}, -\frac{\Delta}{4a})$$

$$V(x_0, y_0)$$

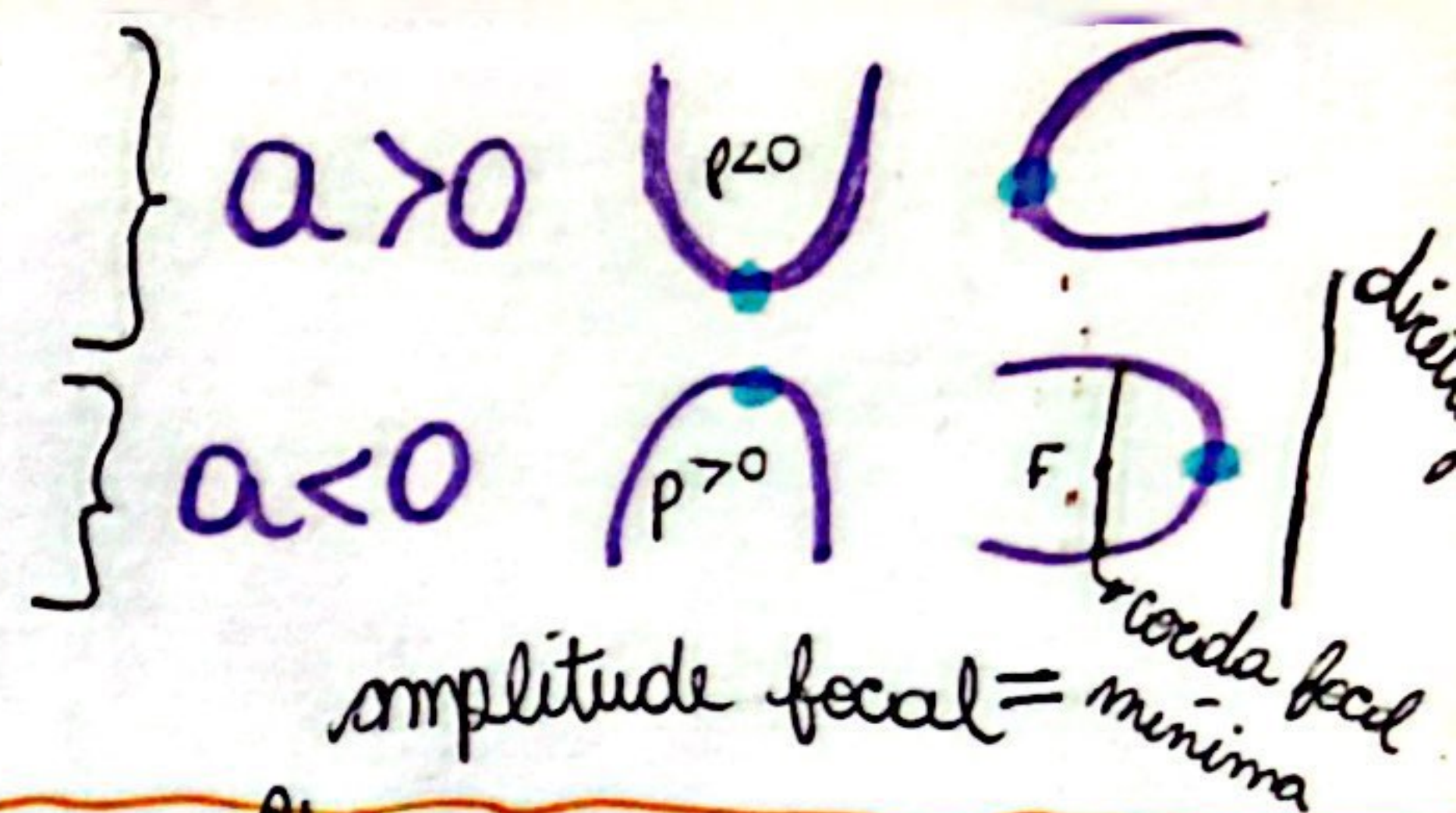
$$V(-\frac{\Delta}{4a}, -\frac{b}{2a})$$

$$(x - x_0)^2 = 4p(y - y_0)$$

EQ. REDUZIDA

$$(y - y_0)^2 = 4p(x - x_0)$$

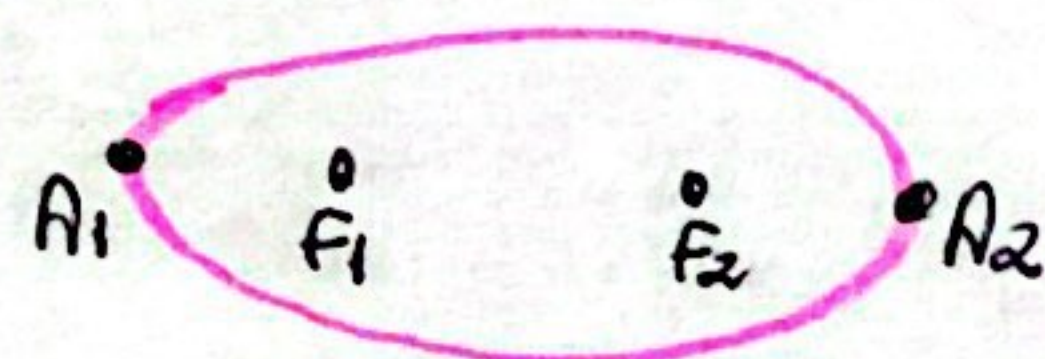
$$e = 1$$



amplitude focal = mínima

ELIPSE

$$\frac{(x - x_0)^2}{a^2} + \frac{(y - y_0)^2}{b^2} = 1$$



$$\frac{(x - x_0)^2}{b^2} + \frac{(y - y_0)^2}{a^2} = 1$$



$$e = \frac{c}{a}$$

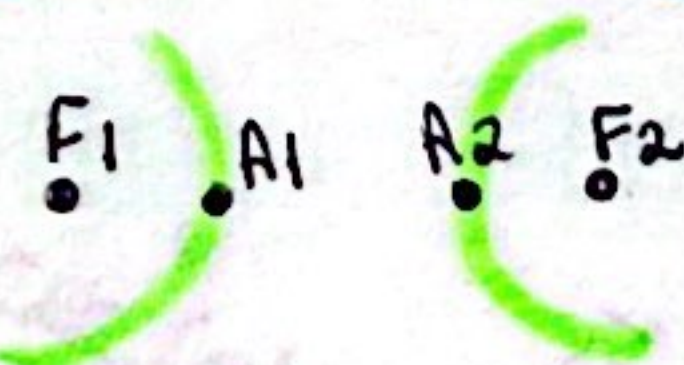
amp. focal

$$cc' = \frac{2b^2}{a}$$

$$e < 1$$

HIPÉRBOL

$$\frac{(x - x_0)^2}{a^2} - \frac{(y - y_0)^2}{b^2} = 1$$



$$\frac{(y - y_0)^2}{a^2} - \frac{(x - x_0)^2}{b^2} = 1$$



$$cc' = \frac{2b^2}{a}$$

$$e > 1$$

Usar completamente de quadras em equações gerais

$$Ax^2 + Bxy + Cy^2 + Dx + Ey + F = 0$$

CIRCUNFERÊNCIA

+ superfície esfera

$$(x - x_0)^2 + (y - y_0)^2 = r^2$$

parabolóide Hiperbólico
cela de coval

$$\frac{x - x_0}{a} = \frac{(y - y_0)^2}{b^2} + \frac{(z - z_0)^2}{c^2}$$

negativo

elipsóide

$$\frac{(x - x_0)^2}{a^2} + \frac{(y - y_0)^2}{b^2} + \frac{(z - z_0)^2}{c^2} = 1$$



Hiperbolóide de uma folha
um sinal negativo

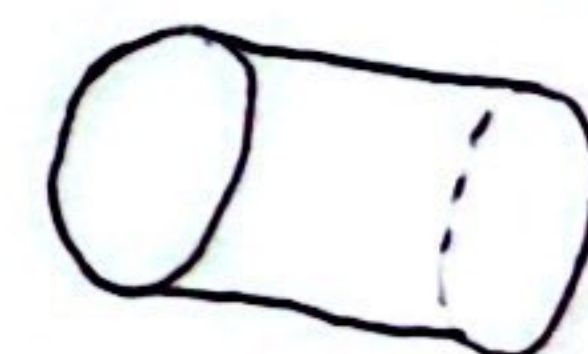


Hiperbolóide de duas folhas
dois sinais negativos

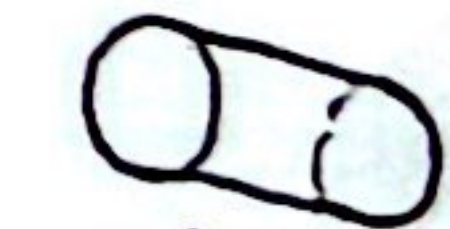


|| os eixos sinal +

cilindros elípticos

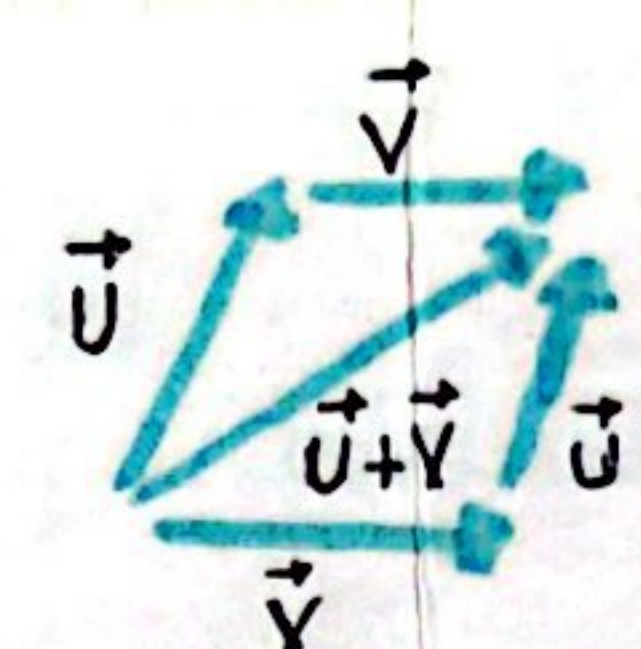
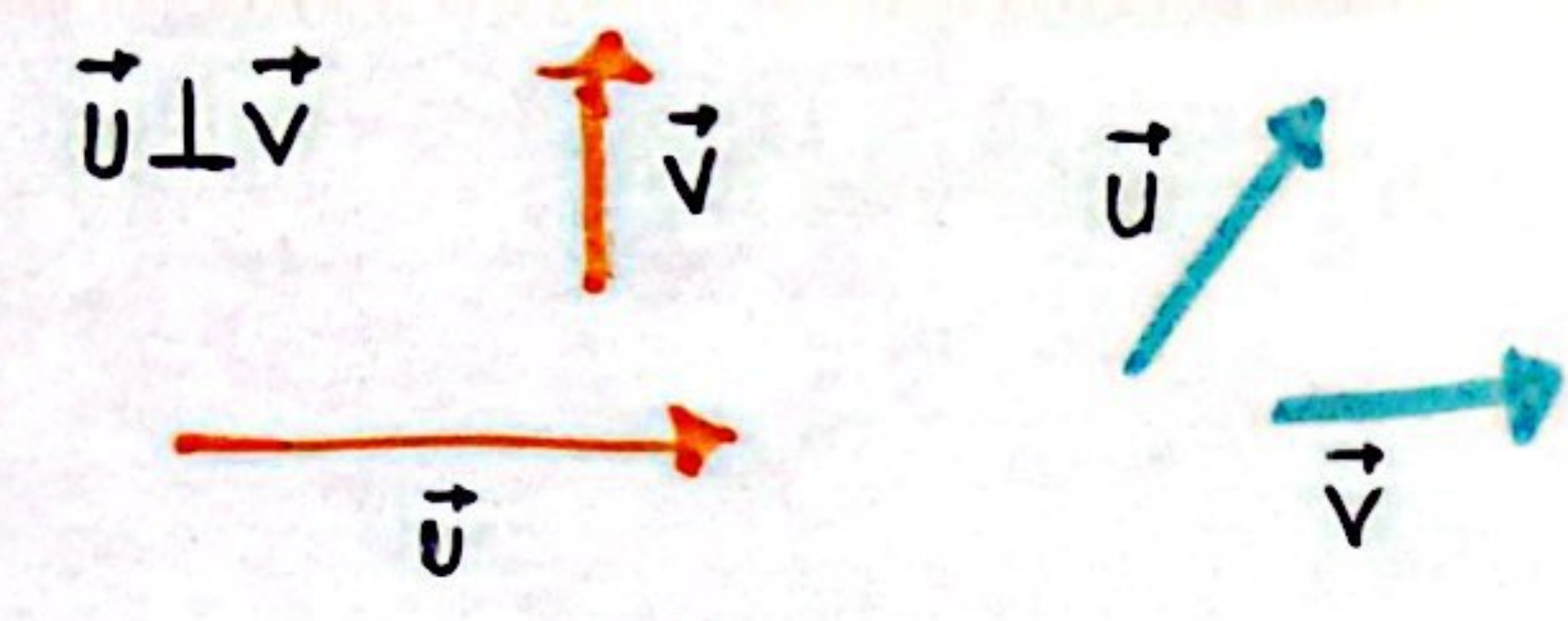
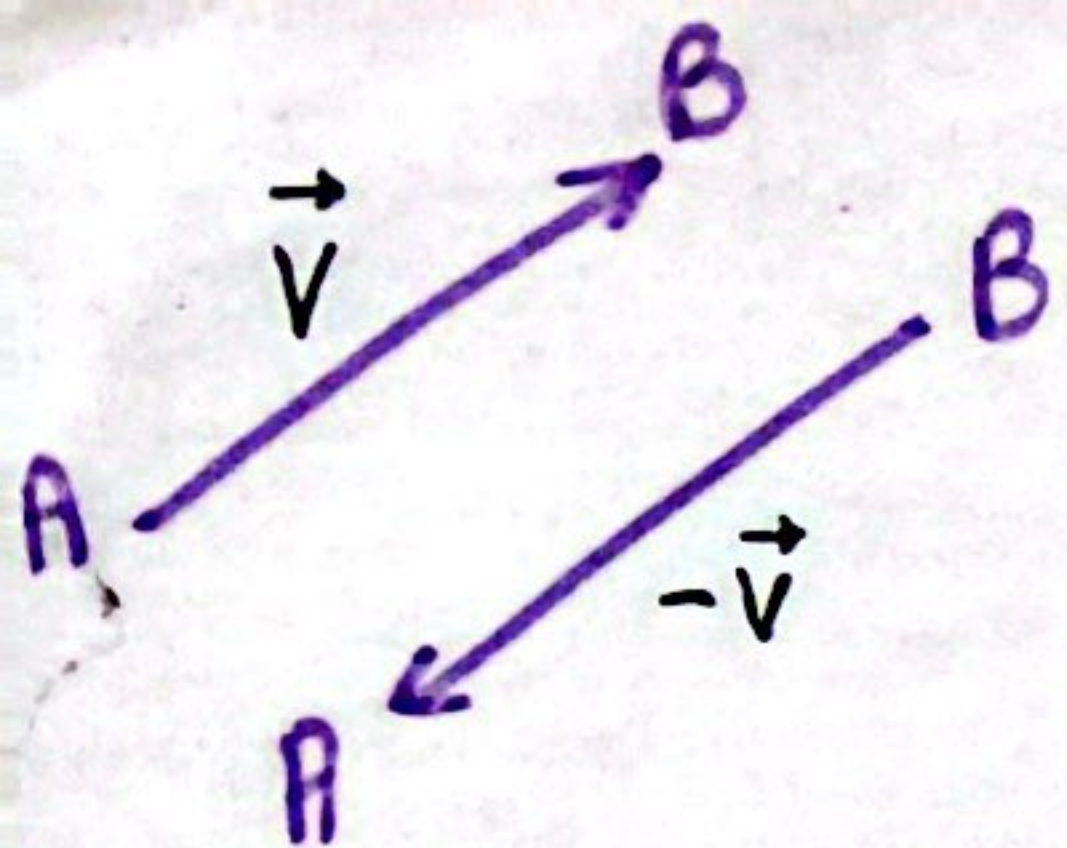


cilindros de revolução



$$\frac{x - x_0}{a} = \frac{(y - y_0)^2}{b^2} + \frac{(z - z_0)^2}{c^2}$$





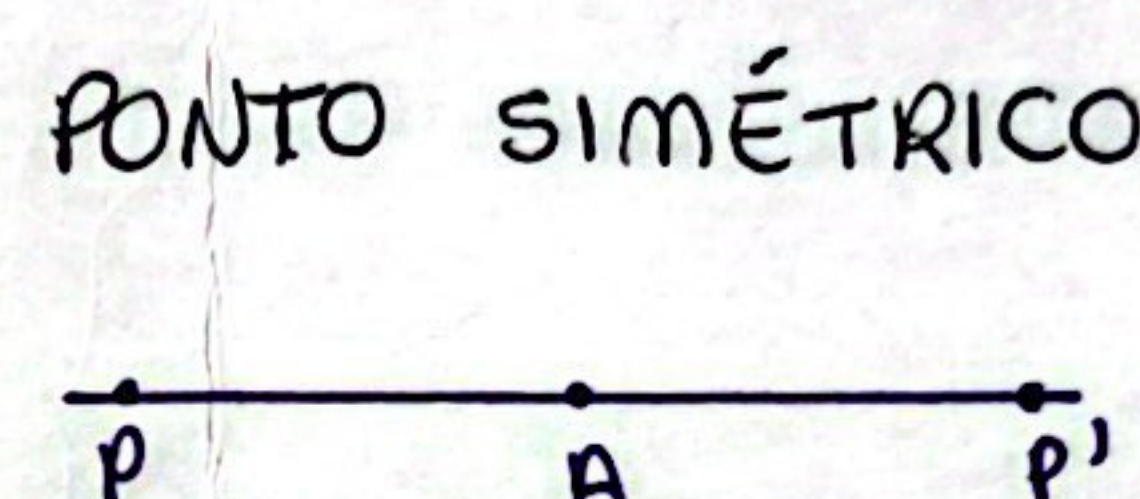
$u // v \rightarrow u = \alpha v$
PARALELISMO
PROPORCIONALIDADE

versor

$$\frac{\vec{v}}{\|\vec{v}\|}$$

$$\vec{u} = \vec{PQ} = Q - P$$

colineares - mesma reta
 $A, B, C \Rightarrow \vec{AB} = \alpha \vec{AC}$



$$\vec{u} + \vec{v} = (x_1 + x_2, y_1 + y_2, z_1 + z_2)$$

$$\|\vec{v}\| = \sqrt{x^2 + y^2 + z^2}$$

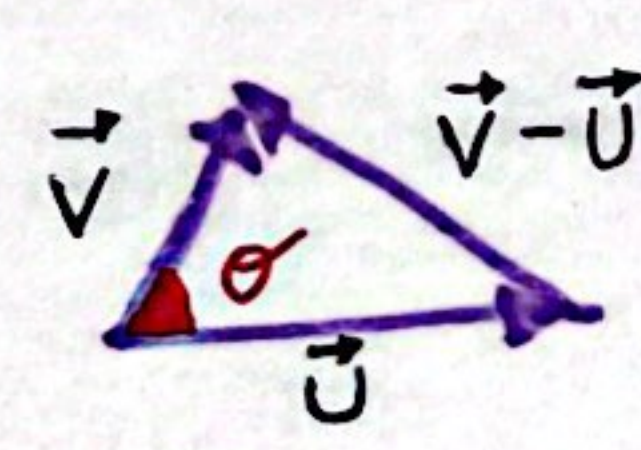
PRODUTO ESCALAR

números $\in \mathbb{R}$

$$\vec{u} \cdot \vec{v} = x_1 x_2 + y_1 y_2 + z_1 z_2$$

$$\alpha (\vec{u} \cdot \vec{v}) = (\alpha \vec{u}) \cdot \vec{v} = \vec{u} \cdot (\alpha \vec{v})$$

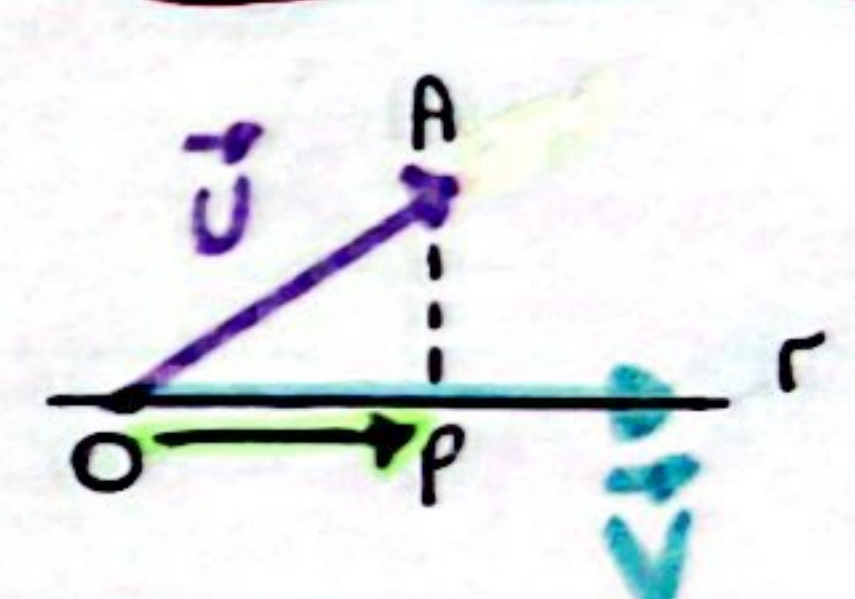
ÂNGULO θ ENTRE VETORES



$$\vec{u} \cdot \vec{v} = \|\vec{u}\| \cdot \|\vec{v}\| \cdot \cos(\theta)$$

$\vec{u} \perp \vec{v} \leftrightarrow \vec{u} \cdot \vec{v} = 0$
 $\vec{u} \cdot \vec{v} = \|\vec{u}\|^2$

VETOR PROJEÇÃO ORTOGONAL

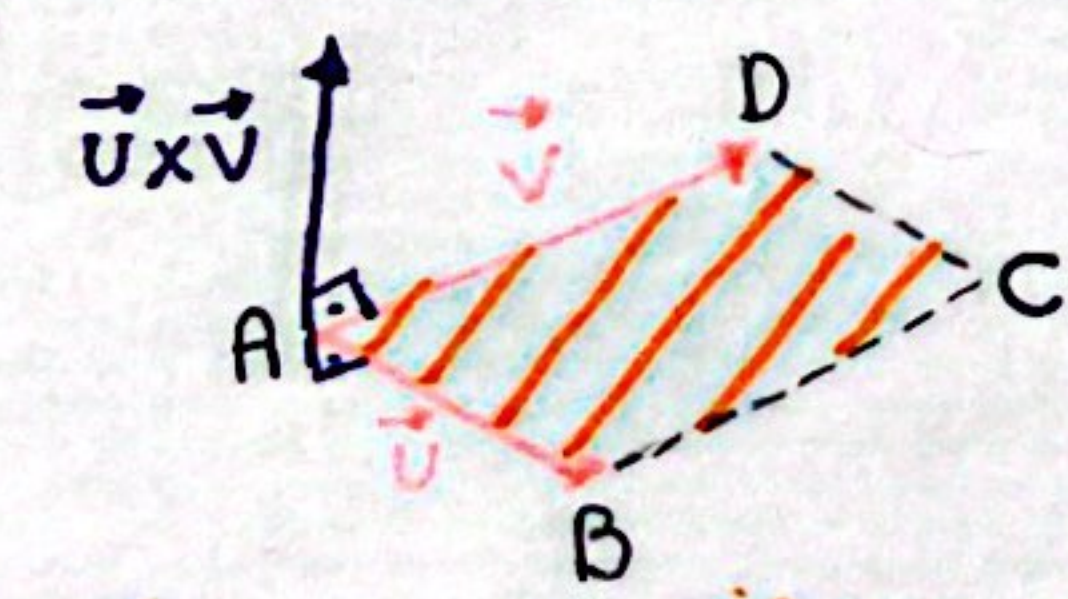


$$\text{proj}_{\vec{v}} \vec{u} = \frac{\vec{u} \cdot \vec{v}}{\|\vec{v}\|^2} \vec{v} \Rightarrow \text{vetor}$$

PRODUTO VETORIAL

vetor

$$\vec{u} \times \vec{v} = \det \begin{bmatrix} \vec{i} & \vec{j} & \vec{k} \\ x_1 & y_1 & z_1 \\ x_2 & y_2 & z_2 \end{bmatrix}$$



$$A(ABCD) = \|\vec{u} \times \vec{v}\|$$

$$\vec{w} \cdot (\vec{u} \times \vec{v}) = (\vec{w} \times \vec{u}) \cdot \vec{v}$$

$\|\vec{u} \times \vec{v}\| = \|\vec{u}\| \cdot \|\vec{v}\| \cdot \sin(\theta)$
 medida θ entre \vec{u} e \vec{v}

$$\alpha (\vec{u} \times \vec{v}) = (\alpha \vec{u}) \times \vec{v} = \vec{u} \times (\alpha \vec{v})$$

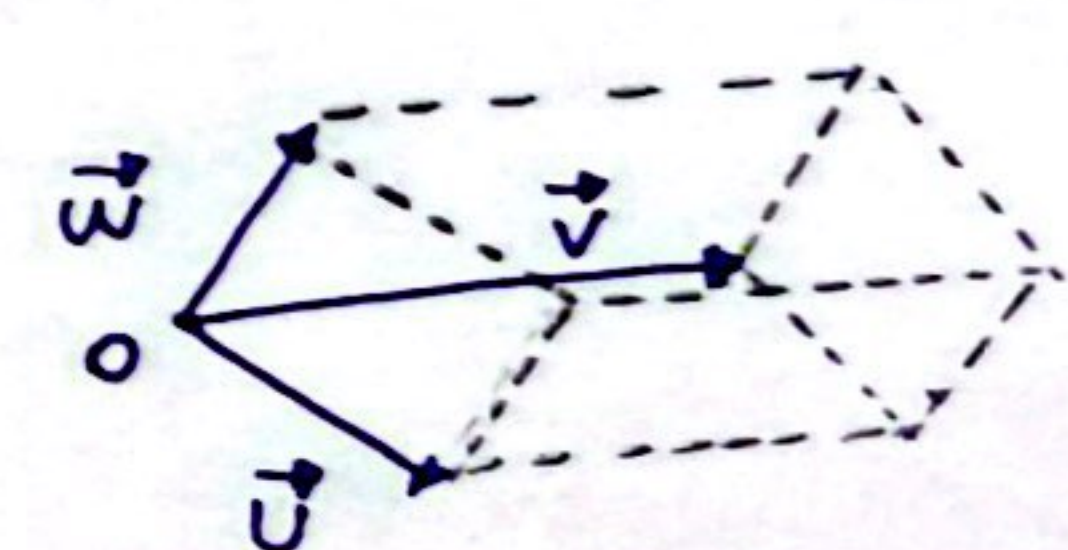
PRODUTO MISTO

números $\in \mathbb{R}$

$$\vec{u} \cdot \vec{v} \times \vec{w} = \det \begin{bmatrix} x_1 & y_1 & z_1 \\ x_2 & y_2 & z_2 \\ x_3 & y_3 & z_3 \end{bmatrix}$$

VOLUME

$$V = |\vec{u} \cdot \vec{v} \times \vec{w}|$$

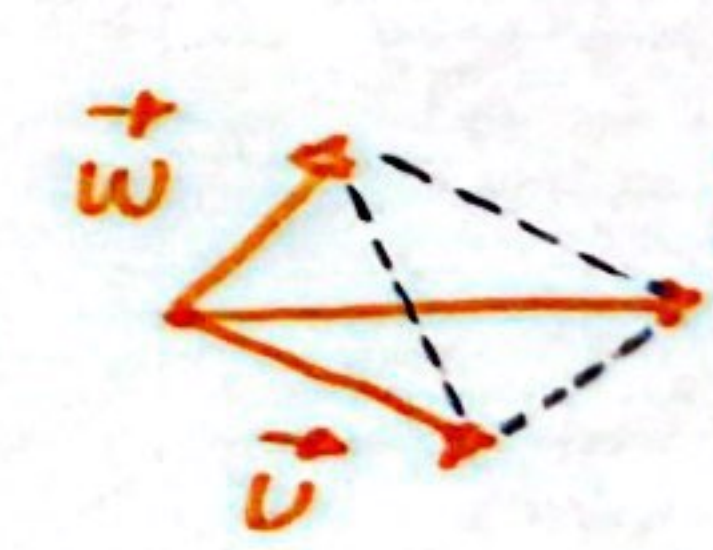


VECTORES

&

COORDENADAS CARTESIANAS

A, B, C, D
COPLANARES
 $\vec{AB} \cdot \vec{AC} \times \vec{AD} = 0$
 mesma origem



$$V = \frac{|\vec{u} \cdot \vec{v} \times \vec{w}|}{6}$$

VOLUME TETRAEDRO