# **Symbolic Logic**

 Deals with the representation and technique of algebra that separates the meaning of factual statements and from proofs of their consistency and their truth values

# **Binary Operators**

### **Common Operators**

#### **OR**

• 
$$Y = A + B$$

A	B	Y
0	0	0
0	0	0
1	0	1
1	1	1

### **NOT**

$$ullet$$
  $Y=\overline{A}$ 

A	Y
0	1
1	0

### **BUF**

$$\bullet \ Y = A$$

A	Y
0	0
1	1

#### **AND**

$$\bullet Y = AB$$

A	B	Y
0	0	0
0	0	0
1	0	0
1	1	1

### XOR

$$ullet$$
  $Y=A\oplus B$ 

A	B	Y
0	0	0
0	0	1
1	0	1
1	1	0

## NAND

• 
$$Y = \overline{AB}$$

A	B	Y
0	0	1
0	0	1
1	0	1
1	1	0

# NOR

• 
$$Y = \overline{A + B}$$

A	B	Y
0	0	1
0	0	0
1	0	0

A	B	Y
1	1	0

#### **XNOR**

 $\bullet \quad Y = \overline{A \oplus B}$ 

A	B	Y
0	0	
0	0	
1	0	
1	1	

#### **Precedence**

- Parenthesis
- NOT
- AND (AND, NAND)
- OR (OR, NOR, XOR)

#### **Truth Tables**

- Consider a Boolean function N containing n Boolean variables  $a_0, a_1, \ldots, a_{n-1}$
- A truth table may be constructed containing  $2^n$  rows which gives the value of N for every combination of truth values of the variables  $a_0, a_1, \ldots, a_{n-1}$

### **Evaluating Logical Expressions**

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- Negation
- Ex.  $\sim$ (AB) is the negation of A andB

 $\rightarrow$ 

- Implication
- ullet Ex. A o B
  - True except when *A* is true but *B* is false

### **Tautology**

• A logical expression that is true for every combination of truth values of its variables