### Homework 4

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### Question 1

Reduce the following lambda terms

a) 
$$(\lambda x.(x+y))3$$

$$= [x \coloneqq 3](x+y)$$

$$= 3 + y$$

**b)** 
$$(\lambda x.(\lambda y.yx)(\lambda z.xz))(\lambda y.yy)$$

$$= [x \coloneqq \lambda y.yy](\lambda y.yx)(\lambda z.xz)$$

$$= (\lambda y.y(\lambda y.yy))(\lambda z.(\lambda y.yy)z)$$

$$= [y \coloneqq \lambda z.(\lambda y.yy)z](\lambda y.y(\lambda y.yy))$$

$$= (\lambda z.(\lambda y.yy)z)(\lambda y.yy)$$

$$=[z\coloneqq \lambda y.yy]((\lambda z.(\lambda y.yy)z))$$

$$=(\lambda y.yy)(\lambda y.yy)$$

 $=\Omega$  combinator (because of the nonterminating recursion)

### **Question 2**

Prove the following

$$+21 = 3$$

$$+21 = 2 + 1$$

$$+21 = M + N$$

$$+21 = \lambda x. \lambda y. (Mx) ((Nx)y)$$

$$+21 = \lambda x. \lambda y. (2x)((1x)y)$$

# **Question 3**

Use beta reduction to compute the following expression

$$(\lambda x(\lambda x. + (-x1))x3)9$$

$$= (\lambda x (\lambda z. + (-z1))x3)9$$

$$=(\lambda z.+(-z1))93$$

$$=(-91)3$$

$$= +83$$

$$= 3 + 8$$

$$= 11$$

## **Question 4**

Write a Scheme function named elements which counts the number of elements in a list

### **Question 5**

a)

Write a scheme function that calculates the inner producct of two vectors

b)

Implement function interleave in scheme, which expects as arguments two lists xs and ys, and returns a single list obtained by choosing elements alternately, first from xs and then from ys. When either xs or ys runs out, interleave takes the remaining elements from the other list, so that the elements of the result are exactly the elements of the two argument lists taken together.