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Astrea

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Chapter 1

Matlab Codes

1.1 Satellite Footprint

```
1  %----ASTREA CONSTELLATION----
2  %PROJECTS - 220028
3  %Aerospace Engineering Barchelor's Degree
4  %ESEIAAT - UPC
5  %Autumn 2016-2017
6
7  % ORBIT DESIGN TEAM
8  % COMPUTATION OF A SATELLITE FOOTPRINT
9
10 clc
11 clear all
12 close all
13
14 %% PHISICAL CONSTANTS AND PARAMETERS
15
16 Re = 6378;           %Earth's Radius [Km]
17 Se = 4*pi*Re^2;      %Earth's Surface [Km^2]
18 h = 500:100:1000;   %Satellte height [Km]
19 eo = 0:5:40;         %Elevation angle [deg]
20
21 %% SOLVER
22
23 for i = 1:length(h)
24     for j = 1:length(eo)
25
26         d(i,j) = Re*(sqrt(((h(i)+Re)/Re)^2-(cosd(eo(j)))^2))-sind(eo(j)));
27         Bo(i,j) = asind( d(i,j)*cosd(eo(j)) / (h(i)+Re) );
28
29         S(i,j) = 2 * pi * Re^2 * ( 1-cosd(Bo(i,j)) );
```

```

30
31     R(i,j) = sqrt( d(i,j)^2 - h(i)^2 );
32
33     %Satellite coverage expressed as a fraction of Earth's Area (%)
34     Cov(i,j) = ( S(i,j) / Se ) * 100;
35
36     %Number of satellites needed
37     nsat(i,j) = ( Se / S(i,j) );
38
39     end
40 end
41
42 %% PLOTS
43
44 figure
45 for k = 1:length(h)
46     plot ( eo , Cov(k,:) )
47     hold on
48 end
49
50 title('Coverage vs Elevation')
51 xlabel('Elevation [deg]') % x-axis label
52 ylabel('Coverage [%]') % y-axis label
53 legend(num2str(h(1)),num2str(h(2)),num2str(h(3)),...
54         num2str(h(4)),num2str(h(5)),num2str(h(6)))
55
56 figure
57 for k = 1:length(h)
58     plot ( eo , nsat(k,:) )
59     legend ('h(j)')
60     hold on
61 end
62
63 title('Num.Satellites vs Elevation')
64 xlabel('Elevation [deg]') % x-axis label
65 ylabel('Num.Satellites') % y-axis label
66 legend(num2str(h(1)),num2str(h(2)),num2str(h(3)),...
67         num2str(h(4)),num2str(h(5)),num2str(h(6)))
68
69 figure
70 for k = 1:length(h)
71     plot ( eo , 2*Bo(k,:) )
72     hold on
73 end
74
75 title('Angle vs Elevation')
76 xlabel('Elevation [deg]') % x-axis label
77 ylabel('Angle between satellites[deg]') % y-axis label
78 legend(num2str(h(1)),num2str(h(2)),num2str(h(3)),...
79         num2str(h(4)),num2str(h(5)),num2str(h(6)))

```

1.2 Minimum Plane Inclination

```

1  %---ASTREA CONSTELLATION---
2  %PROJECTS - 220028
3  %Aerospace Engineering Barchelor's Degree
4  %ESEIAAT - UPC
5  %Autumn 2016-2017
6
7  % ORBIT DESIGN TEAM
8  %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
9  % MINIMUM INCLINATION - To provide Full coverage %
10 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
11
12 %PROBLEM:
13 % Given: - Minimum Elevation over the horizon to contact the satellite
14 %         - Height of the orbit
15 % Compute the minimum elevation to ensure visual contact
16 clear; clc;
17
18 %% Key variable
19 min_elevation_pole=5; %Initially set by @lfore as 32;
20
21 %% Previous Calculation: Visibility(latitude)
22
23 R = 6371;
24 N = 180;
25 deg = 180;
26 x = linspace(0,90,N);
27
28 %%% Minimum angle of elevation due to atmospheric conditions at given
29 %%% latitudes. 0 km represents the poles whereas 6371 km represents the
30 %%% Earth's equator taking as reference point the south pole.
31
32 elvlat = zeros (1,deg);
33 for i = 1:deg/5
34     elvlat(i) = min_elevation_pole-(min_elevation_pole-15)/(2*(90-75))*i;
35 end
36 for i = deg/5+1:4*deg/10
37     elvlat(i) = elvlat(deg/5);
38 end
39 for i = 4*deg/10+1:6*deg/10
40     elvlat(i) = elvlat(2*deg/5)+3/15*(i-4*deg/10);
41 end
42 for i = 6*deg/10+1:8*deg/10
43     elvlat(i) = elvlat(6*deg/10)-3/15*(i-6*deg/10);
44 end
45 for i = 8*deg/10+1:10*deg/10
46     elvlat(i) = elvlat(8*deg/10)-1/15*(i-8*deg/10);

```


Minimum Plane Inclination

```

47 end
48 elvlat=flipplr(elvlat); %Sets the first value to the value in the equator
49 %The first value matches 0 latitude
50
51 %% Minimum i computation
52
53 h = 400:100:1000; %Satellite height [Km]
54 L = 0:5:90; %Latitude angle [deg]
55 e = (interp1q(x',elvlat',L'))'; %Minimum elevations interpolation [deg]
56
57 figure(1)
58 subplot(1,2,1)
59 plot(x,elvlat)
60 subplot(1,2,2)
61 title('Interpolation Verification')
62 plot(L,e)
63
64 inc=zeros(length(h),length(L)); %Inclinations preallocation
65
66 for i = 1:length(h)
67     for j = 1:length(L)
68
69         A=cosd(e(j))/(1+h(i)/R);
70         theta=acosd(A)-e(j); %Earth Central Angle
71         inc(i,j)=L(j)-theta;
72         if inc(i,j)<0
73             inc(i,j)=0;
74         end
75     end
76 end
77
78 %% 3. Results Plotting
79
80 figure(2)
81 colors=['r','b','y','g','m','k','c'];
82 for k = 1:length(h)
83     hold on
84     plot ( L , inc(k,:),colors(k))
85 end
86
87 grid on
88 title('Minimum inclination required to fulfill global coverage')
89 xlabel('Latitude [deg]')
90 ylabel('Inclination [deg]')
91 legend(num2str(h(1)),num2str(h(2)),num2str(h(3)),...
92         num2str(h(4)),num2str(h(5)),num2str(h(6)),num2str(h(7)))
93
94 %% Bonus!!!
95
96 L=90;

```

```

97 e=5.33;
98 h=500:1:600;
99 inc=zeros(1,length(h));
100 for i = 1:length(h)
101     A=cosd(e)/(1+h(i)/R);
102     theta=acosd(A)-e; %Earth Central Angle
103     inc(i)=L-theta;
104     if inc(i)<0
105         inc(i)=0;
106     end
107 end
108
109 figure(3)
110 plot(h,inc)
111 xlabel('Heights')
112 ylabel('Inclination')
113 grid on
114 axis([min(h) max(h) 45 90])

```

1.3 Satellite Number Computation for Polar Orbits

```

1  %----ASTREA CONSTELLATION----
2  %PROJECTS - 220028
3  %Aerospace Engineering Barchelor's Degree
4  %ESEIAAT - UPC
5  %Autumn 2016-2017
6
7  % ORBIT DESIGN TEAM
8  % POLAR ORBITS Number of satellites computation
9
10 %PROBLEM:
11 % Given: - Elevation over the horizon to contact the satellite
12 %         - Height of the orbit
13 % Compute the final number of satellites
14 % Through the "Streets of coverage" method.
15
16 clear; clc;
17
18 %% 1. Input data
19 % PHYSICAL CONSTANTS AND PARAMETERS
20
21 Re = 6378;           %Earth's Radius [Km]
22 Se = 4*pi*Re^2;      %Earth's Surface [Km^2]
23 h = 500:20:600;      %Satellite height [Km]
24 eo = 20;             %Elevation angle [deg]
25

```

```

26 %% 2. Number of satellites computation
27
28 d=zeros(length(h),length(eo));
29 nsats_opt=d;
30
31 for i = 1:length(h)
32     for j = 1:length(eo)
33
34         d(i,j)= Re*(sqrt(((h(i)+Re)/Re)^2-(cosd(eo(j)))^2)-sind(eo(j)));
35         Bo = asind( d(i,j)*cosd(eo(j)) / (h(i)+Re) );
36         Sup = 2 * pi * Re^2 * ( 1-cosd(Bo) );
37
38         Nspp_min=ceil(360/(2*Bo));           %Number of satellites per plain
39         Nsatspp=Nspp_min:1:Nspp_min+50;     %Array of sats/plain to optimize
40
41         S=360./Nsatspp;
42
43         Lstreet=acosd(cosd(Bo)./cosd(S/2));
44
45         DmaxS=Lstreet+Bo;
46         DmaxO=2*Lstreet;
47
48         Nplains=ceil(1+((180-DmaxO)./DmaxS));
49         Nsats=Nplains.*Nsatspp;
50         [row,col]=find(min(Nplains));
51         Nplains_opt(i,j)=Nplains(row,col);
52         nsats_opt(i,j)=Nsats(row,col);
53
54         %Number of satellites needed
55         nsat(i,j) = ( Se / Sup );
56
57     end
58 end
59
60 %% 3. Results Plotting
61
62 figure(2)
63 colors=['r','b','y','g','m','k','c'];
64 for k = 1:length(eo)
65     subplot(1,2,1)
66     hold on
67     semilogy ( h , nsats_opt(:,k),colors(k) )
68     subplot(1,2,2)
69     hold on
70     semilogy ( h , Nplains_opt(:,k),colors(k) )
71 end
72
73 subplot(1,2,1)
74 title('Num.Sats vs Height')
75 xlabel('Height [km]') % x-axis label

```

```

76 ylabel('Num.Satellites') % y-axis label
77 %legend(num2str(eo(1)),num2str(eo(2)),num2str(eo(3)),...
78 %      num2str(eo(4)),num2str(eo(5)),num2str(eo(6)),num2str(eo(7)))
79 axis([400 900 0 1000])
80 grid on
81
82 subplot(1,2,2)
83 title('Num.Planes vs Height')
84 xlabel('Height [km]') % x-axis label
85 ylabel('Num of Orbital Planes') % y-axis label
86 % legend(num2str(eo(1)),num2str(eo(2)),num2str(eo(3)),...
87 %      num2str(eo(4)),num2str(eo(5)),num2str(eo(6)),num2str(eo(7)))
88 axis([400 900 0 30])
89 grid on
90
91 %% Single detailed analysis
92
93 figure(1)
94 plot(h,nsats_opt)
95 title('Num.Sats vs Height - Streets of coverage Method')
96 xlabel('Height [km]') % x-axis label
97 ylabel('Num.Satellites') % y-axis label
98 grid on
99
100 %% Multianalysis variation with height
101
102 figure(3)
103 colors=['r','b','y','g','m','k'];
104 for k = 1:length(h)
105     subplot(1,2,1)
106     hold on
107     plot ( eo , nsats_opt(k,:),colors(k))
108     subplot(1,2,2)
109     hold on
110     plot ( eo , Nplains_opt(k,:),colors(k))
111 end
112
113 subplot(1,2,1)
114 title('Num.Sats vs Elevation - Streets of coverage Method')
115 xlabel('Elevation [deg]') % x-axis label
116 ylabel('Num.Satellites') % y-axis label
117 legend(num2str(h(1)),num2str(h(2)),num2str(h(3)),...
118        num2str(h(4)),num2str(h(5)),num2str(h(6)))
119 axis([0 40 0 700])
120 grid on
121
122 subplot(1,2,2)
123 title('Num.Planes vs Elevation - Surfaces Method')
124 xlabel('Elevation [deg]') % x-axis label
125 ylabel('Num.Orbital Planes') % y-axis label

```

```

126 legend(num2str(h(1)),num2str(h(2)),num2str(h(3)),...
127         num2str(h(4)),num2str(h(5)),num2str(h(6)))
128 axis([0 40 0 30])
129 grid on

```

1.4 Orbit Parameters

```

1  %----ASTREA CONSTELLATION----
2  %PROJECTS - 220028
3  %Aerospace Engineering Barchelor's Degree
4  %ESEIAAT - UPC
5  %Autumn 2016-2017
6
7  % ORBIT DESIGN TEAM
8  % ORBIT PARAMETERS
9
10 % This routine calculates the minimum number of plans and satellites
11 % to guarantee global coverage.
12 % -----
13 % _v2 --> Computes angles with arccosine
14 % _v3 --> Also iterates in f
15
16 clc
17 clear all
18 close all
19
20 tic
21
22 %% DATA INPUT
23
24 Re = 6371;           %Earth's Radius [Km]
25 Se = 4*pi*Re^2;      %Earth's Surface [Km^2]
26 h = 500:5:600;       %Height vector [km]
27 in = 75:3:90;         %Inclination vector [deg]
28 pmin = 5; p=12;       %Minimum number of plans
29 pmax = 20;            %Maximum number of plans
30 sppmin = 10; spp=10;  %Minimum number of satellites each plane
31 sppmax = 24;          %Maximum number of satellites each plane
32 typeWD = 2;          %Defines:
33                       % 1- Semi-Walker-Delta
34                       % 2- 3/4 of Walker-Delta
35                       % 3- Full Walker-Delta
36 plaunch = 5.76e6;     %Launch price
37 psat = 250e3;         %Price per satellite
38 eo = 20;              %Vison angle
39 q=0;                  %Variable used as counter

```

```

40 nplanes_win=0;
41 %Boolean, Indicates a succesful combination with that number of planes
42
43 %% COMPUTATIONS
44 %result=zeros(6,100);
45
46 for j=1:length(h)
47     fprintf('\n\nH = %g km',h(j))
48     Bo = visibleangle(h(j),eo); %Footprint angle
49
50     for k=1:length(in)
51         fprintf('\ni=%g: ',in(k))
52
53         for p=pmin:pmax
54             F=0:1:p-1; nF=length(F); anglesp_f=zeros(1,nF);
55
56             for spp=sppmin:sppmax
57                 angles = 360/spp; %Angle between satelllites of same plane
58
59                 for kf=1:nF
60                     % We look for the optimum f for this spp,npp,inc,h
61                     anglesp_f(kf)=distance_opt_f(in(k),h(j),p,spp,typeWD,F(kf));
62                     %Angle between satelllites of different planes
63                 end
64
65                 [anglesp,kf_min]=min(anglesp_f);
66
67                 if (angles ≤ 2*Bo) && (anglesp ≤ Bo)
68
69                     q=q+1;
70                     result(:,q)=[h(j) in(k) spp p spp*p F(kf_min)];
71                     fprintf(['Solution %g: h=%gkm - i=%g - '...
72                             '%gspp - %gplanes - %g sats - f=%g'],q,result(:,q))
73                     nplanes_win=1;
74                     break %Stop iteration in satelllites per plain
75
76                 end
77
78             end
79             if nplanes_win %If a combination with that num of planes
80                 nplanes_win=0; %works, then jump to the next inclination
81                 break
82             end
83         end
84     end
85 end
86
87 %% Optimum Results
88 % Minimum number of cubesats
89 numsat = result (5,1:q);

```

```

90 [minsat,index] = min(numsat);
91
92 disp(sprintf('\nMINIMUM SATELLITES\nheight: %d', result(1,index)))
93 disp(sprintf('inclination: %d',result(2,index)))
94 disp(sprintf('number of satellites in each plane: %d',result(3,index)))
95 disp(sprintf('number of planes: %d',result(4,index)))
96 disp(sprintf('minimum number of satellites: %d',result(5,index)))
97
98 % Minimum number of planes
99 numplane = result(4,1:q);
100 [minplane,index]= min(numplane);
101
102 disp(sprintf('\nMINIMUM PLANES\nheight: %d', result(1,index)))
103 disp(sprintf('inclination: %d',result(2,index)))
104 disp(sprintf('number of satellites in each plane: %d',result(3,index)))
105 disp(sprintf('number of planes: %d',result(4,index)))
106 disp(sprintf('minimum number of satellites: %d',result(5,index)))
107
108 % Price Optimization
109 TCost = plaunch*result(4,:) + psat*result(5,:); TCost = TCost/(1e6);
110 [CostOpt,index] = min(TCost);
111 height = result(1,:);
112
113 disp(sprintf('\nMINIMUM PRICE\nprice[M]: %d', TCost(index)))
114 disp(sprintf('height: %d', result(1,index)))
115 disp(sprintf('inclination: %d',result(2,index)))
116 disp(sprintf('number of satellites in each plane: %d',result(3,index)))
117 disp(sprintf('number of planes: %d',result(4,index)))
118 disp(sprintf('minimum number of satellites: %d',result(5,index)))
119
120 fprintf('\n\n MORE THAN ONE SOLUTION COULD HAVE THE SAME MIN NUMBER\n')
121
122 %% Plots
123
124 x=0:q-1;
125 plot(x,numplane,x,numsat,x,TCost,x,height)
126 strValues = strtrim(cellstr(num2str([x(:) numplane(:)],'(%d, %d)')));
127 text(x,numplane,strValues,'VerticalAlignment','bottom');
128 strValues = strtrim(cellstr(num2str([x(:) numsat(:)],'(%d, %d)')));
129 text(x,numsat,strValues,'VerticalAlignment','bottom');
130 strValues = strtrim(cellstr(num2str([x(:) TCost(:)],'(%d, %.1f)')));
131 text(x,TCost,strValues,'VerticalAlignment','bottom');
132 strValues = strtrim(cellstr(num2str([x(:) height(:)],'(%d, %d)')));
133 text(x,height,strValues,'VerticalAlignment','bottom');
134 legend('number of planes','number of satellites','Total Cost (M)')
135
136
137
138 toc

```

```

1 function [Bo] = visibleangle (h, eo)
2
3 d=zeros(length(h),length(eo));
4 nsats_opt=d;
5 Re = 6371;
6
7 for i = 1:length(h)
8     for j = 1:length(eo)
9
10         d(i,j)= Re * ( sqrt( ( (h(i)+Re)/Re )^2 - ( cosd(eo(j)) )^2 ) - sind(eo(j)) );
11         Bo = asind( d(i,j)*cosd(eo(j)) / (h(i)+Re) );
12
13     end
14 end
15
16 end

```

```

1 function [anglesp] = distance_opt_f (i,a,p,s,typeWD,F)
2 %% Data input
3
4 % i: Inclination angle [deg]
5 % a: Height of the orbit [km]
6 % p: Number of planes
7 % s: Number of satellites per plane
8
9 %% Walker Delta type of geometry
10 WD=[180 225 360];
11 degreegenerate = WD(typeWD);
12 % Walker Delta 360 deg, SemiWalker Delta 180 deg,
13 % other constellations range between 180 and 360
14
15 m = degreegenerate/180;
16 % generates Walker Delta Constellation
17 % (m=2 -> 2*180 generated constellation),
18 % Semi Walker (m=1 -> 1*180) or other 1<m<2.
19
20 % Phasing between adjacent planes
21 %f = F*p*cosd(i); % parameter defined graphically
22 f = F; % Whereas F is a number 0 < f < (p-1)
23     % According to Astrodynamics notes
24
25 REarth = 6371; % [km]
26 h = (REarth+a)/REarth; %radius of the orbit
27 % (in terms of the sphere radius) R=h*r;
28
29 %% Distribution of Coordinates of the satellites
30 Omega = zeros(1,p);
31 nu = zeros(s,p);

```



```

32 angle = zeros(1,p);
33 X = zeros(3,s,p);
34
35 for j = 1:p
36     Omega(j) = m*pi*(j-1)/p;
37     angle(j) = f*2*pi*(j-1)/(s*p); %Phasing due to f between planes
38     for k = 1:s
39         % True anomalies of the s satellites
40         nu(k,j) = 2*pi*(k-1)/s+angle(j);
41         X(:,k,j) = cartesian(h,0,i,Omega(j),0,nu(k,j));
42         % h[adim] --> X[adim]
43     end
44 end
45
46 %% Fast comprovation
47 % Does the adjacent phasing exceed pi
48 % THIS MEANS
49 % The minimum might be between
50
51
52 %% Angle between different satellites
53
54 c=zeros(s,p); %General aproach. Where is the minimum angle?
55
56 for j=2:p
57     for i=1:s-1
58
59         % We need to assess the angles between the last and first plane
60         % Specially in Semi-Walker configurations. That's why we add this
61         % auxiliar variables.
62
63         p1=j;
64         if j==1
65             p2=p;
66         else
67             p2=j-1;
68         end
69
70         % Angles a2 and a3 could be used to increase de reliability of the
71         % constellation, allowing greater possibilities of communication
72         % between planes. (not only between (i,p1) and (i,p2)
73
74         % Angle between satellite (i,p1) and satellite (i,p2)
75         a1=acosd((X(:,i,p1)'*X(:,i,p2))/(norm(X(:,i,p1))*norm(X(:,i,p2))));
76
77         % Angle between satellite (i,j) and satellite (i+1,j-1)
78         a2=acosd((X(:,i,p1)'*X(:,i+1,p2))/(norm(X(:,i,p1))*norm(X(:,i+1,p2))));
79
80         % Angle between satellite (i,j) and satellite (i-1,j-1)
81         a3=acosd((X(:,i,p1)'*X(:,i-1,p2))/(norm(X(:,i,p1))*norm(X(:,i-1,p2))));

```

```

82
83     % Among the computed angles, choose the minimum
84     [angle(i,j),c(i,j)]=min([a1 a2]);
85
86     % Why minimum? Then we know that at least it will be able to
87     % cover the angle with one of the two adjacent close nodes.
88
89     end
90 end
91
92 anglesp = max(max(angle));
93 %Maximum angle between satellites of different planes

```

1.5 Walker Delta Testing

```

1  %----ASTREA CONSTELLATION----
2  %PROJECTS - 220028
3  %Aerospace Engineering Barchelor's Degree
4  %ESEIAAT - UPC
5  %Autumn 2016-2017
6
7  % ORBIT DESIGN TEAM
8  % ORBIT SMART WALKER-DELTA
9
10 % This routine compute the WD possible configurations that give global
11 % coverage by having the distance between planes matches the planes
12 % rotation
13
14 p=[12 15 18];
15 S=360./p; S=S*pi/180;
16
17 re=6378.01e3;
18 u=3.986012e14;
19 J2=1.0826e-3;
20
21 we=2*pi/(24*3600);
22
23 syms a;
24 inc=75; inc=inc*pi/180;
25 a_sol=zeros(1,length(inc));
26
27 for i=1:length(inc)
28     dOmega=-1.5*J2*(re/a)^2*sqrt(u/a^3)*cos(inc(i));
29     P0=2*pi*sqrt(a^3/u);
30     Pn=P0*(1-1.5*J2*(re/a)^2-0.75*J2*(4-5*sin(inc(i))^2)*(re/a)^2);
31     eq=S(2)-Pn*(we-dOmega);

```

```

32     sol=vpasolve(eq,re*1.15);
33     if imag(sol)==0
34         a_sol(i)=sol;
35     end
36 end
37
38 plot(inc*180/pi, (a_sol-re)/1000)
39 h=(a_sol-re)/1000
40
41 %% Satellites computation
42
43 emin=20*pi/180;
44 Lstreet=5*pi/180;
45
46 rho=re/(re+h*1000);
47 etha=asin(sin(rho)*cos(emin));
48 Lmax=pi/2-emin-etha;
49 S=2*acos(cos(Lmax)/cos(Lstreet));
50 N=ceil(2*pi/S)

```

1.6 Orbit Plotter

```

1  %----ASTREA CONSTELLATION----
2  %PROJECTS - 220028
3  %Aerospace Engineering Barchelor's Degree
4  %ESEIAAT - UPC
5  %Autumn 2016-2017
6
7  % ORBIT DESIGN TEAM
8  % ORBIT PLOTTER - Influential phenomena computation
9
10 % This matlab routine plots the position of the satellites of a Walker
11 % Delta / SemiWalker Delta or other generated configurations.
12
13 clc, clear, close all;
14 %-----
15 %% 0. Data Input
16 %add the subfolder programs to the current path
17 addpath(genpath('./auxiliar'));
18
19 %_____Physical input_____
20
21 global h, h = 542; % [km]
22 degreegen = 225; % Walker Delta 360 deg, SemiWalker Delta 180 deg,
23 % other constellations range between 180 and 360 deg
24 in = degtorad(72); % inclination of the planes

```

```

25 s = 21;           % satellites per plane
26 p = 9;           % number of planes
27 f=8;             % f = 1.25*p*cos(i); % parameter defined graphically
28 eo=degtorad(20); % elevation angle [rad]
29
30 %___Numerical Input_____
31 r = 1;           %radius of the sphere
32 n = 50;          %number of cells of the sphere generated
33 N = 50;          %number of points used to print the orbit
34 nn = 100;        %number of points used to compute the footprint
35
36 %___Physical Constants_____
37 global Re, Re = 6371; %Earth's Radius [Km]
38 %% 1. Preprocessing
39
40 global m, m = degreeen/180;
41         % generates Walker Delta Constellation (m=2 -> 2*180)
42         % generated constellation), Semi Walker (m=1 -> 1*180)
43         % or other 1<m<2.
44
45 global a, a = (Re+h)/Re;
46         %radius of the orbit (in terms of the sphere radius) R=h*r;
47
48 %% 2. Main Process
49
50 %compute the sat RAAN and some sat. parameters (Laura)
51 Omega = zeros(1,p);
52 nu = zeros(s,p); %true anomaly of the satellites
53 angle = zeros(1,p); %angle between satellites
54 for i = 1:p
55     Omega(i) = m*pi*(i-1)/p; %orbits
56
57     angle(i) = f*2*pi*(i-1)/(s*p); %sats
58     for k = 1:s
59         nu(k,i) = 2*pi*(k-1)/s+angle(i);
60     end
61 end
62
63 % Compute the satellite coordinates (Laura)
64 X = zeros(3,s,p);
65 for i = 1:p
66     for k = 1:s
67         X(:,k,i) = cartesian(a,0,in,Omega(i),0,nu(k,i));
68     end
69 end
70 sCOOR=reshape(X,3,p*s)'; %put the data in a more friendly structure
71
72 %compute the radius of the footprint
73 %SATELLITE_FOOTPRINT_COMPUTATION.m
74 d=Re*((((h+Re)/Re)^2-cos(eo)^2)^.5-sin(eo));

```

```

75 Bo=asin(d*cos(eo)/(h+Re));
76 S=2*pi*Re^2*(1-cos(Bo));
77 R=(S/pi)^.5;
78
79 %create the footprint of each satellite
80 SATfp=[];
81 for i=1:s*p
82     %unitary vector pointing to the sat from the earth's center
83     u=-sCOORD(i,:)/norm(sCOORD(i,:));
84     %Generate the circle coordinates (2D)
85     [satfp(:,1),satfp(:,2),satfp(:,3)]=circle3D(sCOORD(i,:),u, R/Re, nn);
86     satfp=satfp+repmat(u*h/Re,nn,1); %move the circle to be tg to Earth
87
88     for j=1:size(satfp,1)
89         v=sCOORD(i,:)-satfp(j,:); v=v/norm(v);
90         %unitary vector sat->footprint
91
92         %verify if the footprint intersect with the earth's surface
93         tol=satfp(j,1)^2+satfp(j,2)^2+satfp(j,3)^2-r^2;
94         while tol>1e-2
95             satfp(j,:)=satfp(j,:)-0.01*v;
96             tol=satfp(j,1)^2+satfp(j,2)^2+satfp(j,3)^2-r^2;
97         end
98     end
99     %store the footprint
100     SATfp=[SATfp; satfp];
101 end
102
103
104 %% 3. Plots
105
106 %3D plot
107 [COORD]=Orbitplot3D( in,r, X,n, SATfp, nn );
108 %Ground track
109 x=zeros(size(COOR,1),size(COOR,2)/3); y=x; z=x;
110 for i=1:size(COOR,2)/3
111     x(:,i)=COORD(:,3*(i-1)+1);
112     y(:,i)=COORD(:,3*(i-1)+2);
113     z(:,i)=COORD(:,3*(i-1)+3);
114 end
115 GroundTrackPlot( x, y, z, sCOORD, SATfp, nn);

```

```

1 function [x,y,z]=circle3D(center,normal,radius,n)
2 %This matlab function generates the points of a circle normal to a 3D
3 %vector
4 %In:
5 %   center: center of the circle (x, y, z)
6 %   normal: vector normal to the circle
7 %   radius: radius of the circle

```

```

8 %   n: number of points (small number can make the circle not smooth)
9 %Out:
10 %   x, y z: vectors containing the coord.
11 %-----
12
13 theta=linspace(0,2*pi,n);
14 v=null(normal);
15 points= repmat(center',1,size(theta,2))+...
16     radius*(v(:,1)*cos(theta)+v(:,2)*sin(theta));
17 x=points(1,:); y=points(2,:); z=points(3,:);
18 end

```

```

1 function [COOR] = Orbitplot3D( in,r, X,n, sCOOR, N )
2 %Orbitplot3D is a function that creates a 3D representation of a
3 %constellation and plots the satellites. It can be also configured to plot
4 %their footprint
5 %In:
6 %   in: inclination angle [rad]
7 %   r: sphere radius [-]
8 %   X: Coordinates of the sats (3,spp,p)
9 %   n: number of points used to draw thhe sphere
10 %   sCOOR
11 %   COOR: coordinates of the footprints
12 %   N: number of points used to compute the footprint
13 %-----
14 p=size(X,3);
15 s=size(X,2);
16 global a m;
17
18 % Earth
19 %Create the earth instance as an sphere
20 [x,y,z]=sphere(n); %Generate the sphere
21 surf(r*x,r*y,r*z,'FaceColor','interp','EdgeColor','none'); %plot the sphere
22 colormap(linspace(0,1,n)'.*[0 0.6 1]); %custom colormap (blue tones);
23 axis equal;
24 box off;
25 hold on;
26 rotate3d on;
27
28 % Orbits
29 %Generate the circle coordinates (2D)
30 coor=zeros(N+1,3);
31 for i=1:N
32     coor(i,:)=[a*r*cos(2*i*pi/N), a*r*sin(2*i*pi/N), 0];
33 end
34 coor(N+1,:)=coor(1,:);
35
36 %Rotation Matrices
37 Ry=[ cos(in) 0 sin(in)

```

```

38         0      1      0
39     -sin(in) 0 cos(in)];
40
41 Rz= @(Omega) [-sin(Omega) cos(Omega) 0
42               cos(Omega) sin(Omega) 0
43               0          0          1]; % he modificat aquesta matriu
44
45 coor=coor*Ry; %Rotate the circle in the y axis (inclination)
46
47 %rotate the plane to get the other planes
48 COOR=zeros(N+1,3*p);
49 for i=1:p
50     COOR(:,(1+(i-1)*3):(3+(i-1)*3))=coor*Rz(m*(i-1)*pi/p);
51 end
52 for i=1:p
53     plot3(COOR(:,1+(i-1)*3),COOR(:,2+(i-1)*3),COOR(:,3+(i-1)*3),...
54           'linewidth',1.5);
55 end
56
57 % Satellites (Laura)
58 for i = 1:p
59     for k = 1:s
60         scatter3(X(1,k,i),X(2,k,i),X(3,k,i),25,'square','k','filled');
61         hold on;
62     end
63 end
64
65 %Plot also the footprint if the number of input variables is bigger than 4
66 if nargin > 4
67     for i=1:p*s
68         b=1+N*(i-1); c=N+N*(i-1);
69         fill3(sCOOR(b:c,1),sCOOR(b:c,2),sCOOR(b:c,3),[1 0 0],...
70             'FaceAlpha','.3','LineStyle','none');
71     end
72 end
73 end

```

```

1 function [] = GroundTrackPlot( x, y, z, coor, fp_coor, N)
2
3 %GroundTrackPlot is used to plot the ground
4 %track of the constellation orbits
5 %given their coordinates (cartesian).It has two variants, only introducing
6 %the first 3 inputs will plot the orbits and if you introduce all the
7 %inputs it plots the satellites and their footprint.
8 %In:
9 %   x: matrix containing the x coordinate of the orbits to plot
10 %   y: matrix containing the y coordinate of the orbits to plot
11 %   z: matrix containing the z coordinate of the orbits to plot
12 %   ---

```

```

13 %   coor: satellite coordinates (nx3)
14 %   fp_coor: satellite footprint coordinates ((n*nn)x3)
15 %   N: number of points used to compute the footprint
16 %-----
17 p=size(x,2); %n of planes
18 s=size(coor,1)/size(x,2); %n of spp
19
20 %% Set the background image for the ground track plot
21 figure('name','Constellation Ground Track');
22 tit=[ 'Num. of planes: ' num2str(p) ' Num. of spp: ' num2str(s)];
23 ground='World-satellite-map.png';
24 im=imread(ground);
25 imagesc([-180,180],[-90,90],im);
26 grid on;
27 axis([-180 180 -90 90]);
28 title(tit);
29 hold on;
30 %set the plot lines color
31 c = ['r','y','m','g','w']; C=[];
32 for i=1:ceil(size(x,2)/5)
33     C=[C c];
34 end
35
36 %% Main process
37 for i=1:size(x,2)
38     %convert the cartesian coordinates to spherical
39     [lon,lat]=cart2sph(x(:,i),y(:,i),z(:,i));
40     %get the coordinates of the orbit in spherical coord.
41     lon=radtodeg(lon); %pass to degrees
42     lat=radtodeg(lat);
43     Lon=[lon(end); lon(1:end-1)];
44
45     %Plot the sat ground track
46     [j,j]=max(abs(lon-Lon));
47     plot(lon(1:j-1),lat(1:j-1),C(i),'linewidth',1.2);
48     plot(lon(j:end),lat(j:end),C(i),'linewidth',1.2);
49 end
50
51 if nargin > 3
52     [slon,slat]=cart2sph(coor(:,1),coor(:,2),coor(:,3));
53     %get the coordinates of the sats in spherical coord.
54     slon=radtodeg(slon); %pass to degrees
55     slat=radtodeg(slat);
56
57     %plot the sats
58     scatter(slon,slat,30,'square','w','filled');
59
60     %get the coordinates of the sats footprint in spherical coord.
61     [fplon,fplat]=cart2sph(fp_coor(:,1),fp_coor(:,2),fp_coor(:,3));
62     fplon=radtodeg(fplon); %pass to degrees

```



```

63     fplat=radtodeg(fplat);
64
65     %Plot their footprint
66     for i=1:p*s
67         b=1+N*(i-1); c=N+N*(i-1);
68         fpLon=[fplon(c); fplon(b:c-1)];
69
70         %get the maximum values (plotting purposes)
71         [sorted, I]=sort(abs(fplon(b:c)-fpLon));
72         M=sorted(end-1:end);
73         j=I(end-1:end); j(2)=j(2)-1;
74
75         if M(1) > 300
76             if j(1) < j(2)
77                 auxlon=fplon(b+j(1):b+j(2)-1); %negative lon. part
78                 auxlat=fplat(b+j(1):b+j(2)-1);
79
80                 auxlon2=[fplon(b+j(2):c); fplon(b:b+j(1)-2)]; %+ lon. part
81                 auxlat2=[fplat(b+j(2):c); fplat(b:b+j(1)-2)];
82             else
83                 auxlon2=fplon(b+j(2):b+j(1)-2); %negative lon. part
84                 auxlat2=fplat(b+j(2):b+j(1)-2);
85
86                 auxlon=[fplon(b+j(1):c); fplon(b:b+j(2)-1)];
87                 %positive lon. part
88                 auxlat=[fplat(b+j(1):c); fplat(b:b+j(2)-1)];
89             end
90
91             fill(auxlon,auxlat,[1 0 0],'FaceAlpha','.2','LineStyle','none');
92             fill(auxlon2,auxlat2,[1 0 0],'FaceAlpha','.2','LineStyle','none');
93         else
94             fill(fplon(b:c),fplat(b:c),[1 0 0],...
95                 'FaceAlpha','.3','LineStyle','none');
96
97         %%%%%%%%%%%
98         pause(.05); %
99         %%%%%%%%%%%
100     end
101
102
103     end
104 end
105 end

```

```

1  % This function converts kepler orbit elements to cartesian coordinates
2
3  % a: semimajor axis
4  % e: eccentricity
5  % i: inclination [rad]

```

```

6 % Omega: longitude of the ascending node [rad]
7 % w: Argument of periapsis [rad]
8 % nu: True anomaly [rad]
9
10 function [X] = cartesian(a,e,i,Omega,w,nu)
11
12 % Position in cylindrical coordinates
13 r = a*(1-e^2)/(1+e*cos(nu));
14
15 % Position components
16 X = [r*(cos(Omega)*cos(w+nu)-sin(Omega)*sin(w+nu)*cos(i));
17      r*(sin(Omega)*cos(w+nu)+cos(Omega)*sin(w+nu)*cos(i));
18      r*sin(i)*sin(w+nu)];
19
20 end

```

1.7 Perturbations

```

1 %----ASTREA CONSTELLATION----
2 %PROJECTS - 220028
3 %Aerospace Engineering Barchelor's Degree
4 %ESEIAAT - UPC
5 %Autumn 2016-2017
6
7 % ORBIT DESIGN TEAM
8 % ORBIT PERTURBATIONS - Influential phenomena computation
9
10 %PROBLEM:
11 % Given: - Initial orbital parameters
12 % Compute the final orbital parameters after each orbit
13 %clear; clc;
14
15 %% 1.A Input data physical constants
16 % PHYSICAL CONSTANTS AND PARAMETERS
17 %Physical data
18 RE=6.378e6; %Earth Radius [m]
19 u=3.986e14; %GM Earth
20 J2=1082.6e-5; %J2 coefficient;
21
22 %% 1. Input data Orbit parameters
23 % SPACECRAFT DATA
24 m=4; % Satellite mass [kg]
25 Cd=2.2; % Drag Coefficient
26 A=0.1; % Satellite surface [m^2] --> 3U pointing to Earth
27 Bc=m/(Cd*A); % Ballistic coefficient of the satellite;
28

```

```

29 % ORBIT DATA
30 H0=542e3;      % Altura inicial [m]
31 e0=0.0001;     % Excentricity
32 i0=72*pi/180;  % Inclination [deg]
33 a0=RE+H0;
34
35 % INITIAL PARAMETERS
36 P=2*pi*(a0^3/u)^.5; % Orbit Period [s]
37 v=sqrt(u/a0);     %satellite velocity [m/s]
38 n=(2*pi/P)*86400; %number of revolutions/day
39
40
41 % SIMULATION PARAMETERS
42 N=10000000;
43
44 %% 2. Perturbations propagation
45 %Outputs de la funcio Perturbation:
46 %   Pert: matrix (4x5) with the perturbations causes at the rows (J2,Drag,
47 %   Moon,Sun) and the orbital elements in the columns (a,e,i,omega,Omega)
48 %       a  e  i  w  Omega
49 %   [                ]J2
50 %   [                ]Drag
51 %   [                ]Moon
52 %   [                ]Sun as 3rd Body
53
54
55
56 t=zeros(1,N); t(1)=0;
57 a=t; a(1)=a0;
58 e=t; e(1)=e0;
59 i=t; i(1)=i0;
60
61 w_sun=zeros(1,N-1); w_moon=w_sun; w_J2=w_sun;
62 Om_sun=w_sun; Om_moon=w_sun; Om_J2=w_sun;
63
64 w0=0; Omega0=0;
65 w=t; w(1)=w0;
66 Omega=t; Omega(1)=Omega0;
67
68 tic
69 for n=2:N
70
71     a0=a(n-1);
72     e0=e(n-1);
73     i0=i(n-1);
74     w0=w(n-1);
75     Omega0=Omega(n-1);
76
77     P=2*pi*(a0^3/u)^.5; % Orbit Period [s]
78

```

Perturbations

```

79     [Pert_i rho]=Perturbation(a0,e0,i0,Bc);
80
81     a(n)=a0+sum(Pert_i(:,1));
82     e(n)=e0+sum(Pert_i(:,2));
83     i(n)=i0+sum(Pert_i(:,3));
84     w(n)=w0+sum(Pert_i(:,4));
85     Omega(n)=Omega0+sum(Pert_i(:,5));
86
87     w_sun(n-1)=Pert_i(4,4);
88     w_moon(n-1)=Pert_i(3,4);
89     w_J2(n-1)=Pert_i(1,4);
90
91     Om_sun(n-1)=Pert_i(4,5);
92     Om_moon(n-1)=Pert_i(3,5);
93     Om_J2(n-1)=Pert_i(1,5);
94
95     % We don't want angles bigger than 360!
96     w(n)=w(n)-360*floor(w(n)/360);
97     Omega(n)=Omega(n)-360*floor(Omega(n)/360);
98
99     if Omega(n)>2*pi
100         Omega(n)=Omega(n)-2*pi;
101     end
102
103     t(n)=t(n-1)+P;
104
105     if a(n)<(RE+180e3)
106         fprintf('Your satellite succesfully burned in the atmosphere.\n\n')
107         break
108     end
109
110 end
111
112 %% Post processing and results plotting
113
114 time=toc;
115 fprintf('Time to do %g iterations = %g s.\n ',n,time)
116
117 figure(1)
118 plot(t(1:n)/(3600*24),(a(1:n)-RE)/1000)
119 ylim([100 500])
120 grid on
121 ylabel('Orbit height [km]')
122 xlabel('Time [days]')
123 tfin=floor(t(n)/(3600*24));
124 days = num2str(floor(tfin/365));
125 titulaso=['Orbit decay in ' num2str(tfin) ' days = ' days 'years'];
126 title(titulaso)
127
128

```

Perturbations

```

129 figure(2)
130 subplot(1,2,1)
131 plot(t(1:n)/(3600*24),w(1:n))
132 grid on
133 ylabel('Perigee Argument [deg]')
134 xlabel('Time [days]')
135 title('Perigee Argument deviation in 100 days')
136 axis([0 100 0 360])
137
138 subplot(1,2,2)
139 plot(t(1:n)/(3600*24),Omega(1:n))
140 grid on
141 ylabel('Ascenent Node Argument [deg]')
142 xlabel('Time [days]')
143 tfin=t(n)/(3600*24);
144 title('Ascendent Node deviation in 100 days')
145 axis([0 100 0 360])
146
147 %% Modulus Analysis
148
149 figure(3)
150
151 subplot(1,2,1)
152 semilogy(t(2:n+1)/(3600*24),abs(w_sun(1:n)),'b','LineWidth',2);
153 hold on
154 semilogy(t(2:n+1)/(3600*24),abs(w_moon(1:n)),'r','LineWidth',2)
155 semilogy(t(2:n+1)/(3600*24),abs(w_J2(1:n)),'k','LineWidth',2)
156 legend('Sun','Moon','J2')
157 xlabel('Time (days)');
158 ylabel('Modulus of Perturbation []');
159 title('Effects on Argument of the Perigee');
160 grid on
161 axis([0 t(n)/(3600*24) 1e-8 1])
162
163 subplot(1,2,2)
164 semilogy(t(2:n+1)/(3600*24),abs(Om_sun(1:n)),'b','LineWidth',2);
165 hold on
166 semilogy(t(2:n+1)/(3600*24),abs(Om_moon(1:n)),'r','LineWidth',2)
167 semilogy(t(2:n+1)/(3600*24),abs(Om_J2(1:n)),'k','LineWidth',2)
168 legend('Sun','Moon','J2')
169 xlabel('Time (days)');
170 ylabel('Modulus of Perturbation []');
171 title('Effects on Argument of Ascendent Node');
172 axis([0 t(n)/(3600*24) 1e-8 1])
173 grid on
174
175 print -depsc ModulusAngulars

```

```

1 function [pert rho] = Perturbation( a,e,i,Bc)

```

```

2 %% Perturbations
3 % This matlab is used to compute the perturbations in the classical orbital
4 % elements due to:
5 % J2 (non spherical earth)
6 % Atmospheric drag
7 % Third body (Moon and Sun)
8 %Inputs:
9 % a: semi-major axis [m]
10 % e: eccentricity [-]
11 % i: inclination [rad]
12 % m: mass of the satellite [kg]
13 % Cd: drag coefficient [-]
14 % A: Area of the satellite [m^2]
15 %Outputs:
16 % Pert: matrix (4x5) with the perturbations causes at the rows (J2,Drag,
17 % Moon,Sun) and the orbital elements in the columns (a,e,i,omega,Omega)
18 % incP/revolution
19 % incv/revolution
20 %TO DO:
21 %Les perturbacions degudes a J2 i 3rd body no se si son en pert/dia o no,
22 %cal mirar-ho per tal de tenir totes les pertrubacions escalades igual
23 % ~~~~~
24 %% Previous calculations and PreAllocation
25 %Physical data
26 RE=6.378e6; %Earth Radius [m]
27 u=3.986e14; %GM Earth
28 J2=1082.6e-5; %J2 coefficient;
29
30 P=2*pi*(a^3/u)^.5; % Orbit Period [s]
31 v=sqrt(u/a); %satellite velocity [m/s]
32 n=(2*pi/P)*86400; %number of revolutions/day
33
34
35 % ATMOSPHERIC MODEL
36 %get the density from MSISE model (extracted as a list from
37 %http://omniweb.gsfc.nasa.gov/vitmo/msis_vitmo.html
38 % h[km] rho[kg/m^3]
39 % filename1='msis_26371.lst'; filename2='msis_2226.lst';
40 % formatSpec='%f %f';
41 % size=[2 Inf];
42 % fileID=fopen(filename1,'r');
43 % rho_h=fscanf(fileID,formatSpec,size);
44 % fclose(fileID);
45 % fileID=fopen(filename2,'r');
46 % rho_h=[rho_h fscanf(fileID,formatSpec,size)];
47 % fclose(fileID);
48 % rho=interp1(rho_h(1,:),rho_h(2,:), (a-RE)/1000);
49
50 H = (a - RE)*1e-3;
51 % Compute exospheric temperature [K]

```

Perturbations

```

52     T = 900 + 2.5*(120-70);
53     % Compute effective atmospheric molecular mass [km/K], valid 180<H<500
54     M = 27 - 0.012 * (H - 200);
55     % Compute atmospheric scale height [km]
56     SH = T / M;
57     % Compute atmospheric density [kg/m3]
58     rho = 6E-10 * exp(-(H - 175) / SH);
59
60
61     pert=zeros(4,5);
62
63     %% Computation
64
65     %J2 perturbation_____ PER REVOLUCIO
66     j=1;
67     pert(j,5)=-1.5*n*J2*(RE/a)^2*cos(i)*(1-e^2)^-2;
68     pert(j,4)=0.75*n*J2*(RE/a)^2*(4-5*(sin(i))^2)*(1-e^2)^-2;
69
70     %Atmospheric Drag_____ PER REVOLUCIO
71     %Perturbations/revolution
72     j=2;
73     pert(j,1)=-2*pi*rho*a^2/Bc;
74
75     % incP=-6*pi^2*a^2*rho/(v*Bc);
76     % incv=pi*a*rho*v/Bc;
77
78     %Moon Perturbation_____ /DIA --> /REV
79     j=3;
80     pert(j,5)=-0.00338*cos(i)/n;
81     pert(j,4)=0.00169*(4-5*(sin(i))^2)/n;
82
83     % Fins aqui son /dia,
84     % Canviem unitats + apliquem periode actual
85     pert(j,5)=pert(j,5)*P/(24*3600);
86     pert(j,4)=pert(j,4)*P/(24*3600);
87
88     %Sun Perturbation_____ /DIA --> /REV
89     j=4;
90     pert(j,5)=-0.00154*cos(i)/n;
91     pert(j,4)=0.00077*(4-5*(sin(i))^2)/n;
92
93     % Fins aqui son /dia,
94     % Canviem unitats + apliquem periode actual
95     pert(j,5)=pert(j,5)*P/(24*3600);
96     pert(j,4)=pert(j,4)*P/(24*3600);
97
98
99     end

```

1.8 Orbit Decay

```

1  %----ASTREA CONSTELLATION----
2  %PROJECTS - 220028
3  %Aerospace Engineering Barchelor's Degree
4  %ESEIAAT - UPC
5  %Autumn 2016-2017
6
7  % ORBIT DESIGN TEAM
8  % ORBIT DECAY
9
10 % This routine computes the orbital decay of an spacecraft with time
11 % using the cowell's method.
12 % The differential equations are integrated using "ode45"(Runge-Kutta 4th,
13 % 5th order)
14
15
16 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
17 %%
18 clear all;
19 clc;
20 close all;
21
22 %% Initialization %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
23 global mu mmu smu re rs rm omega J2;
24
25 %_____Physical Variables_____
26 mu=3.986004418e14; % earth gravitational constant [m^3/s^2]
27 mmu=4902.800076e9; %moon gravitational constant [m^3/s^2]
28 smu=132712440040.944e9; %sun gravitational constant [m^3/s^2]
29
30 re=6378136.3; %earth radius [m]
31 rs=696e6; %sun radius [m]
32 rm=1730e3; %moon radius [m]
33
34 omega=7.292115e-5; %earth angular velocity [rad/s]
35 J2=0.001081874; %earth oblateness gravity coeff []
36
37 au=149597870691; %astronomical unit [m]
38 c=2.99792458e8; %[m/s] speed of light
39
40 %_____Numerical variables_____
41 hlim=180; %minimum height for considering the decay [km]
42 dt=15*60; %timestep of the simulation [s]
43 t0=0; %initial time of the sim
44 tf=dt;
45
46 %% User Input %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

```



```

47  %__Orbital elements_____
48  a=re+542e3; %[m] semimajor axis
49  e=0.0001; % eccentricity
50  i=deg2rad(72); %[rad] inclination
51  w=0; %[rad] argument of periapsis
52  Omega=0; %[rad] RAAN
53  nu=0; %true anomaly
54
55  date=datetime(2017,2,4); %datetime array [Y, M, D]
56
57  %__Oblateness parameters_____
58  znls=0; %zonals [0-18]
59  tssrls=0; %tesserals [0-18]
60
61  %__Drag perturbation inputs_____
62  Cd=2.2; %Drag coefficient (Typical for sats, various ref.)
63  Adrag=.09; %[m^2] Wet area for the drag
64  m=4.1; %[kg] Cubesat mass
65
66  Bc=Adrag*Cd/m; %Ballistic coeff.
67
68  %__SRP perturbation inputs_____
69  Cr=2; %reflectivity ct.
70  Asrp=.5; %[m^2] Area for the SRP
71
72  % Ws (@Dap) = 1361/(1+0.0334*cos(2*pi*Dap/365));
73  Ws=1361; %W/m^2 approximation for the solar irradiance
74
75  srp=Ws/c*Cr*Asrp/m*au^2; %Solar radiation pressure ct.
76
77  %% Main Process %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
78  display('Computing...');
79  f=@(q) q*((3+3*q+q^2)/(1+(1+q)^3/2)); %richard Battin's function
80
81  aobl=zeros(3,1);
82  adrag=aobl; asun=aobl; amoon=aobl; asrp=aobl;
83
84
85  y=cartesian2(a,e,i,Omega,w,nu); %obtain the state vector (r,V)
86  jdate0=juliandate(date); %compute the julian date
87
88  tic
89  iter=0; tt=[]; xx=[];
90
91  h=(norm(y(1:3))-re)*1e-3;
92  while h>hlim
93      jdate=jdate0+tt/86400;
94      %      GMST=JD2GMST(jdate);
95      %
96      %      %Acceleration due to oblateness

```

```

97 %      aobl=Oblat((t0+tf)/2,y,znls,tssrls,GMST);
98 %
99 %      %Acceleration due to the 3rd body pert.
100 %      rsun=planetEphemeris(jdate,'Earth','Sun');
101 %      %geocentric pos of the Sun
102 %      rmoon=planetEphemeris(jdate,'Earth','Moon');
103 %      %geocentric pos of the Moon
104 %      rsun=rsun'; rmoon=rmoon';
105 %
106 %      rs2s=y(1:3)-rsun; %vector sun-sat
107 %      rm2s=y(1:3)-rmoon; %vector moon-sat
108 %
109 %      qs=dot(y(1:3),(y(1:3)-2*rsun))/dot(rsun,rsun);
110 %      qm=dot(y(1:3),(y(1:3)-2*rmoon))/dot(rmoon,rmoon);
111 %
112 %      asun=-smu/norm(rs2s)^3*(y(1:3)+f(qs)*rsun);
113 %      amoon=-mmu/norm(rm2s)^3*(y(1:3)+f(qm)*rmoon);
114 %
115 %      %Acceleration due to the solar radiation presure.
116 %      usun=rsun/norm(rsun); %unit vector of the pos of the sun
117 %      us=y(1:3)/norm(y(1:3)); %unit vector of the pos of the sat
118 %
119 %      shadow=random('Normal',0.5,.1); %shadow factor
120 %
121 %      asrp=srp*rs2s/norm(rs2s)^3;
122
123 %Acceleration due to the drag force
124 % Compute exospheric temperature [K]
125 T = 900 + 2.5*(100-70);
126 % Compute effective atmospheric molecular mass [km/K], valid 180<H<500
127 M = 27 - 0.012 * (h - 200);
128 % Compute atmospheric scale height [km]
129 SH = T / M;
130 % Compute atmospheric density [kg/m3]
131 rho = 6E-10 * exp(-(h - 175) / SH);
132
133 atmosV=y(4:6)+omega*[y(2); -y(1); 0];
134 %relative vel between sat and atmos
135
136 adrag=-.5*rho*Bc*atmosV*norm(atmosV);
137
138 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
139 acc=aobl+asun+amoon+asrp+adrag;
140
141 ode=@(t,y)[y(4);
142             y(5);
143             y(6);
144             acc(1)-mu/norm(y(1:3))^3*y(1);
145             acc(2)-mu/norm(y(1:3))^3*y(2);
146             acc(3)-mu/norm(y(1:3))^3*y(3)

```

```

147         ]; %function to integrate (6eqn)
148
149         [t,x]=ode45(ode,[t0 tf], y);
150
151         y=x(size(x,1),:);
152         %save one value each 12 hours
153         if mod(t(length(t)),12*3600)==0
154             tt=[tt; t(length(t))]; xx=[xx; y];
155         end
156         y=y';
157
158         %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
159         %End of the timestep
160         t0=tf;
161         tf=tf+dt;
162
163         h=(norm(y(1:3))-re)*1e-3;
164
165         iter=iter+1;
166         if mod(iter,300)==0
167             fprintf('Days elapsed: %0.1f \nH=%0.3f km\n',(jdate-jdate0),h);
168         end
169     end
170     toc
171     %% Post Process %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
172     fprintf('The satellite decays in %0.0f days',tf/86400);
173
174     h=zeros(size(xx,1),1);
175     for i=1:size(xx,1)
176         h(i)=(norm(xx(i,1:3))-re)*1e-3;
177     end
178
179     plot(tt/86400,h);

```

```

1  % This function converts kepler orbit elements to cartesian coordinates
2
3  % a: semimajor axis
4  % e: eccentricity
5  % i: inclination [rad]
6  % Omega: longitude of the ascending node [rad]
7  % w: Argument of periapsis [rad]
8  % nu: True anomaly [rad]
9
10 function [y] = cartesian2(a,e,i,Omega,w,nu)
11 global mu;
12 % Position in cylindrical coordinates
13 r = a*(1-e^2)/(1+e*cos(nu));
14
15 % Position components

```

```

16 X = [r*(cos(Omega)*cos(w+nu)-sin(Omega)*sin(w+nu)*cos(i));
17       r*(sin(Omega)*cos(w+nu)+cos(Omega)*sin(w+nu)*cos(i));
18       r*sin(i)*sin(w+nu)];
19
20 A = sin(Omega)*cos(i)*(e*cos(w)+cos(w+nu));
21 v(1)=-sqrt(mu/(a*(1-e^2)))*(cos(Omega)*(e*sin(w)+sin(w+nu))+A);
22
23 B = cos(Omega)*cos(i)*(e*cos(w)+cos(w+nu));
24 v(2)=-sqrt(mu/(a*(1-e^2)))*(sin(Omega)*(e*sin(w)+sin(w+nu))-B);
25
26 v(3)=sqrt(mu/(a*(1-e^2)))*(e*cos(w)+cos(w+nu))*sin(i);
27
28 y=[X;v'];
29 end

```

1.9 Performance Evaluator

```

1  %----ASTREA CONSTELLATION----
2  %PROJECTS - 220028
3  %Aerospace Engineering Barchelor's Degree
4  %ESEIAAT - UPC
5  %Autumn 2016-2017
6
7  % ORBIT DESIGN TEAM
8  % PERFORMANCE EVALUATOR
9
10 clear all;
11
12 %% Input Data
13
14 a=6378.01e3;
15 u=3.986012e14;
16 h=(a+546.5101e3)/a;
17 ap=h*a;
18 J2=1.0826e-3;% J2=0;
19
20 ws=sqrt(u/ap^3); % Satellite mean motion
21 we=2*pi/(24*3600); % Earth mean motion
22 dOmega=-1.5*J2*(a/ap)^2*sqrt(u/ap^3)*cosd(75);
23
24 At=1/6; % [min] % Every 10 seconds
25 t=0:At:60*24; t=t*60; % Time array in seconds
26
27 i=72*pi/180;
28
29 p=9;

```

```

30 spp=21;
31 N=p*spp;
32 %f=floor(0.25*spp);
33 f=0;
34 fprintf('\ni=%gdeg, p=%g, spp=%g, N=%g\n',i*180/pi,p,spp,N);
35
36 latGS=57.5*pi/180;
37 longGS=(17.73-60)*pi/180; longGS=0;
38
39 fprintf('GS Coordinates: Lat=%g, Long=%g \n',latGS*180/pi, longGS*180/pi)
40
41 f1=pi/2-latGS; f2=longGS;
42 R1=[cos(f1) 0 -sin(f1);0 1 0;sin(f1) 0 cos(f1)];
43 R2=[cos(f2) sin(f2) 0; -sin(f2) cos(f2) 0; 0 0 1];
44 RotGS=R1*R2;
45
46 % Rotation Matrix:
47 % From ECEF - To SEZ
48 % Where:
49 % ECEF = Earth Centered Earth Fix - Coordinate System
50 % SEZ = Topocentric Horizon - Coordinate System
51
52 emin=20*pi/180;
53
54 %% Le simulasion
55 %Omega = 0:30:240; Omega=Omega*pi/180;
56 Omega = 0:225/(p-1):225; Omega=Omega*pi/180;
57 %Omega=0:360/p:360-360/p; Omega=Omega*pi/180;
58
59 nu = zeros(spp,p);
60 angle = zeros(1,p);
61 X = zeros(3,spp*p);
62
63 flight_time=zeros(1,1000); % Length of the flyby of a satellite
64 links_at_time=zeros(1,1000); % Number of links when one sat has finished
65 time_end_flyby=zeros(1,1000); % When did this flyby end?
66
67 contact=zeros(1,length(t)); % Number of links
68
69 quality_time=zeros(1,length(t));
70 %If a flyby lasts longer than 3 minutes,
71 % then the previous 3 minutes were successfully covered.
72
73 time_record=zeros(1,N); % Accumulates Timesteps being on the GS
74 before_tracking=zeros(1,N);
75 % Boolean to know which ones are already passing by
76 now_tracking=zeros(1,N); % Boolean to know which ones are now passing by
77 Nflyby=0; % Number of flight paths computed
78
79 for n=1:length(t)

```

```

80
81     % J2 deviation
82     Omegat=Omega+dOmega*t(n);
83
84     % Ground Station Coordinates
85     f1=we*t(n)+longGS;
86     f2=latGS;
87     RGS=cos(f2);
88     XGS=[RGS*cos(f1);RGS*sin(f1);sin(f2)];
89
90     R2=[cos(f1) sin(f1) 0; -sin(f1) cos(f1) 0; 0 0 1];
91     RotGS=R1*R2;
92
93     % Constellation Coordinates
94     nu_t=ws*t(n);    % True anomaly due to time passing by
95     for j = 1:p
96         angle(j) = f*2*pi*(j-1)/(spp*p); %Phasing due to f between planes
97         for k = 1:spp
98             % True anomalies of the s satellites
99             A = spp*(j-1)+k; % Number of the satellite
100             nu(k,j) = 2*pi*(k-1)/spp+angle(j);
101             X(:,A) = cartesian(h,0,i,Omegat(j),0,nu(k,j)+nu_t);
102         end
103     end
104
105     % Contact Evaluation
106     win=0;    % Counter to know number of links
107     now_tracking=zeros(1,N);
108     for sat=1:N
109         X_hor=RotGS*(X(:,sat)-XGS);
110         % fprintf('%g,%g,%g --> |r|=%g\n',X_hor(1),X_hor(2),X_hor(3),norm(X_hor))
111         ang=asin(X_hor(3)/norm(X_hor));
112         if ang >= emin
113             win=win+1;
114             time_record(sat)=time_record(sat)+1;
115             now_tracking(sat)=1;
116         end
117
118         % Flight time computation and reset of this satellite flyby
119         if before_tracking(sat)==1 && now_tracking(sat)==0
120             Nflyby=Nflyby+1;
121             flight_time(Nflyby)=At*time_record(sat);
122
123             links_at_time(Nflyby)=contact(n-1);
124             time_end_flyby(Nflyby)=t(n);
125
126             % THE KEY QUESTION
127             % Was this flyby useful?
128             if flight_time(Nflyby)>3
129                 start=n-time_record(sat);

```

```

130             finish=n;
131             quality_time(start:finish)=quality_time(start:finish)+1;
132         end
133         time_record(sat)=0;
134     end
135 end
136 before_tracking=now_tracking;
137 contact(n)=win;
138 end
139
140 %% Post-Processing
141 % PLOT 1: NUMER OF LINKS
142 figure(1)
143 title('Links vs Time')
144 plot(t/(3600),contact)
145 axis([min(t)/(3600) max(t)/(3600) 0 max(contact)+1]);
146 fails=length(find(contact==0));
147 ratio=fails/length(contact);
148 fprintf('Links on GS           : %g percent of the time\n',(1-ratio)*100)
149
150 % PLOT 2: LENGTH OF THE LINKS
151 figure(2)
152 plot(flight_time(1:Nflyby));
153 titola=['Length of the ' num2str(Nflyby) ' flyby s. Mean time = '...
154         num2str(mean(flight_time(1:Nflyby))) 'min'];
155 title(titola)
156 ylabel('Length (minutes)')
157 xlabel('Contact')
158 %xlim([1 Nflyby])
159
160 % PLOT 3: ANALYSIS OF THE FLYBYS
161 figure(3)
162 index=1:Nflyby; % X variable to the following plots
163 plot(time_end_flyby(index)/3600,flight_time(index),...
164       time_end_flyby(index)/3600,links_at_time(index),...
165       t/3600,quality_time);
166
167 titola='Flybys Analysis';
168 title(titola)
169
170 legend('Length of flybys','Links by end of flyby',...
171        'Num of sats @flybys longer than 3 min')
172 xlabel('Time (h)')
173
174 epic_wins=length(find(quality_time>=1));
175 ratio_covered=epic_wins/length(t);
176 fprintf('Quality flybys on GS: %g percent of the time\n',ratio_covered*100)
177 fprintf('Mean flyby time = %g minutes\n',mean(flight_time(1:Nflyby)))
178
179

```

Thrust

```

180 %% MAXIMUM GAP SEARCH
181 gap=0;
182 at_gap=0;
183 gap_record=zeros(1,100);
184 ngap=0;
185
186 for n=1:length(t)
187     if quality_time(n)==0
188         at_gap=1;
189         gap=gap+1;
190     end
191
192     if quality_time(n)>0 && at_gap==1
193         at_gap=0;
194         ngap=ngap+1;
195         gap_record(ngap)=gap*At;
196         gap=0;
197     end
198 end
199
200 max_gap=max(gap_record);
201 fprintf('Maximum gap = %g minutes\n',max_gap)
202 fprintf('Number of gaps = %g\n\n',ngap)

```

1.10 Thrust

```

1  %----ASTREA CONSTELLATION----
2  %PROJECTS - 220028
3  %Aerospace Engineering Barchelor's Degree
4  %ESEIAAT - UPC
5  %Autumn 2016-2017
6
7  % ORBIT DESIGN TEAM
8  % THRUST
9
10 % This function computes the  $\Delta V$  and propellant mass necessary to
11 % maintain an orbit between to heights
12
13 %function [mp, $\Delta V$ ,tHoh] = thrust(hmax,hmin,ms,Isp,Thr)
14
15 % This function computes the  $\Delta V$  and propellant mass necessary to
16 % maintain an orbit between to heights
17
18 % Input variables:
19 % - hmax: maximum height [m]
20 % - hmin: minimum height [m]

```


Thrust

```

21 % - ms: dry mass of the spacecraft [kg]
22 % - Isp: specific impulse of the spacecraft [s]
23 % - Thr: thrust of the spacecraft [N]
24
25 % Output variables:
26 % - mp: array of propellant mass necessary for every Hohmann transfer [kg]
27 % - ΔV: array of ΔVs necessary for every Hohmann transfer [m/s]
28 % - tHoh: array of time necessary to do a Hohmann transfer [s]
29
30 % Proposed values:
31 hmax = 550e3;
32 hmin = hmax-8;
33 ms = 3.95;           % Dry mass [kg]
34 Isp = 2150;
35 Thr = 100e-6;
36
37 %% Data
38
39 % PHYSICAL CONSTANTS AND PARAMETERS
40 RE = 6.378e6; %Earth Radius [m]
41 mu = 3.986e14; %GM Earth
42 g0 = 9.81;
43
44 % SPACECRAFT DATA
45 m = 4;             % Satellite mass [kg]
46 Cd = 2.2;          % Drag Coefficient
47 A = 0.1*0.3;       % Satellite surface [m^2] --> 3U pointing to Earth
48
49 % ORBIT DATA
50 H0 = hmax;          % Altura inicial [m]
51 E0 = 0.01;          % Excentricity
52 IO = 80*pi/180;     % Inclination [deg]
53 A0 = RE+H0;
54
55 % SIMULATION PARAMETERS
56 N=100000;
57 M = 10000;
58
59 %% 2. Perturbations propagation
60
61 % Creation of the matrices
62 temp=zeros(M,N);
63 temp(1,1)=0;
64 H = zeros(M,N);
65 H(1,1) = H0;
66 % ΔV = zeros(2,N);
67
68 % Assign initial values
69 W0=0; OMEGA0=0;
70 a=zeros(1,N); a(1)=A0;

```

```

71 e=a; e(1)=E0;
72 i=a; i(1)=I0;
73 t=a; t(1)=0;
74 w=a; w(1)=W0;
75 Omega=a; Omega(1)=OMEGA0;
76
77 for j = 1:M
78
79     n = 1;
80     while a(n) ≥ (RE+hmin)
81
82         n = n+1;
83
84         a0=a(n-1);
85         e0=e(n-1);
86         i0=i(n-1);
87         w0=w(n-1);
88         Omega0=Omega(n-1);
89
90         P=2*pi*(a0^3/mu)^.5; % Orbit Period [s]
91
92         Bc = m/(Cd*A); % Ballistic coefficient of the satellite
93         Perti=Perturbation(a0,e0,i0,Bc);
94
95         a(n)=a0+sum(Perti(:,1));
96         e(n)=e0+sum(Perti(:,2));
97         i(n)=i0+sum(Perti(:,3));
98         w(n)=w0+sum(Perti(:,4));
99         Omega(n)=Omega0+sum(Perti(:,5));
100
101         % We don't want angles bigger than 360!
102         w(n)=w(n)-360*floor(w(n)/360);
103         Omega(n)=Omega(n)-360*floor(Omega(n)/360);
104
105         if Omega(n)>2*pi
106             Omega(n)=Omega(n)-2*pi;
107         end
108
109         t(n)=t(n-1)+P;
110
111     end
112
113     % Hohmann
114     [ΔV1,ΔV2,mpit,tHohit] = Hohmann(a(n)-RE,hmax,m,Isp);
115     m = m-mpit;
116
117     if m≤ms
118         break
119     end
120

```

Thrust

```

121     ΔV(1,j) = ΔV1; % first row of the column -> ΔV1
122     ΔV(2,j) = ΔV2; % second row of the column -> ΔV2
123     mp(j) = mpit;
124     tHoh(j) = tHohit;
125
126     a(1)=A0;
127     e(1)=E0;
128     i(1)=I0;
129     w(1)=W0;
130     Omega(1)=OMEGA0;
131     altura = a-RE;
132
133     H(j,:) = altura;
134     temp(j,:) = t;
135
136 end
137
138 %% Post process
139
140 mfr = Thr/(g0*Isp);
141
142 for i = 1:N
143     if H(1,i) ≤ 0
144         break
145     end
146 end
147 for j = 1:M
148     if H(j,1) ≤ 0
149         break
150     end
151 end
152 H = H(1:(j-1),1:(i-1));
153
154 for i = 2:N
155     if temp(1,i) ≤ 0
156         break
157     end
158 end
159 for j = 2:M
160     if temp(j,2) ≤ 0
161         break
162     end
163 end
164 temp = temp(1:(j-1),1:(i-1));
165 for j = 2:size(temp,1)
166     temp(j,:) = temp(j,:)+tHoh(j-1)+temp(j-1,size(temp,2));
167 end
168
169 % Convert matrix to vector
170 H = reshape(H.',1,size(H,1)*size(H,2));

```

Thrust

```

171 temp = reshape(temp.',1,size(temp,1)*size(temp,2));
172
173 figure(1)
174 plot(temp/(3600*24),H/1000)
175 grid on
176 ylabel('Orbit height [km]')
177 xlabel('Time [days]')
178 tfin=floor(temp(length(temp))/(3600*24));
179 days=num2str(floor(tfin/365));
180 titulaso=['Orbit decay in ' num2str(tfin) ' days = ' days ' years'];
181 title(titulaso)
182
183 %% Final calculations
184
185 % % Perimeter of the ellipse
186 % r1 = RE+hmax; % semimajor axis
187 % r2 = RE+hmin; % semiminor axis
188 % h = (r1-r2)^2/(r1+r2)^2;
189 % % Ramanujan approximation
190 % C = pi*(r1+r2)*(1+3*h/(10+sqrt(4-3*h)));
191 %
192 % % Check if ΔV is possible for the given thruster
193 % OK = true;
194 % for j = 1:length(mp)
195 %     for i = 1:2
196 %         mfrnecessary = ΔV(i,j)*mp(j)/(C/2);
197 %         if mfrnecessary>mfr
198 %             OK = false;
199 %         end
200 %     end
201 % end
202 %
203 % if OK ==true
204 %     fprintf('The trajectory is possible\n\n');
205 % else
206 %     fprintf('Trajectory not possible\n\n');
207 % end
208 if length(mp)<M
209     fprintf('There is still propellant left ._. \n\n')
210 end

```

```

1 function [ΔV1,ΔV2,mp,t] = Hohmann(hinicial,hfinal,m,Isp)
2
3 % Hohmann transfer orbit between two circular orbits
4 % - hinicial: height of the first orbit [m]
5 % - hfinal: height of the second orbit [m]
6 % - m: mass of the satellite (total) [kg]
7 % - Isp: Specific impulse [s]
8 % - mp: fuel mass [kg]

```

```

 9 % - t: time needed to do the maneuver [s]
10
11 mu = 3.986004418e14; % Standard gravitational parameter (Earth)
12 REarth = 6.371e6; % [m]
13 g0 = 9.81; % Earth's gravity [m/s^2]
14
15 % First orbit
16 r1 = REarth+hinicial; % [m]
17 v1 = sqrt(mu/r1); % [m/s]
18
19 % Second orbit
20 r2 = REarth+hfinal; % [m]
21 v2 = sqrt(mu/r2); % [m/s]
22
23 % Transfer orbit (ellipse)
24 vp = sqrt(2*mu*r2/(r1*(r1+r2))); % [m/s]
25 va = sqrt(2*mu*r1/(r2*(r1+r2))); % [m/s]
26 a = (r1+r2)/2;
27 T = sqrt(2*pi^2*a^3/mu);
28
29 % ΔV 1 -> p(transfer orbit)
30 ΔV1 = vp-v1;
31 % ΔV a(transfer orbit) -> 2
32 ΔV2 = v2-v1;
33 % Total
34 ΔV = ΔV1+ΔV2;
35
36 % Fuel mass
37 mp = m*(1-exp(-ΔV/(g0*Isp)));
38
39 % Time
40 t = T/2;
41
42 end

```

1.11 Satellites Datasheet

```

1 %----ASTREA CONSTELLATION----
2 %PROJECTS - 220028
3 %Aerospace Engineering Barchelor's Degree
4 %ESEIAAT - UPC
5 %Autumn 2016-2017
6
7 % ORBIT DESIGN TEAM
8 % SATELLITES DATASHHET
9

```

```

10 % Writing the constellation characteristics
11
12 a=6378.01e3;
13 u=3.986012e14;
14 h=(a+542e3)/a;
15 ap=h*a;
16 J2=1.0826e-3;% J2=0;
17
18 ws=sqrt(u/ap^3); % Satellite mean motion
19 i=72*pi/180;
20
21 p=9;
22 spp=21;
23 N=p*spp;
24 %f=floor(0.25*spp);
25 f=0;
26 fprintf('\ni=%gdeg, p=%g, spp=%g, N=%g\n',i*180/pi,p,spp,N);
27
28
29 %Omega = 0:30:240; Omega=Omega*pi/180;
30 Omega = 0:225/(p-1):225; %Omega=Omega*pi/180;
31 %Omega=0:360/p:360-360/p; Omega=Omega*pi/180;
32
33 P=2*pi/ws/60;
34
35 %% Excel IMPORT
36
37 D=zeros(N,9);
38 for sat=1:N
39
40     Om=ceil(sat/spp); ID_p=sat-(Om-1)*spp;
41     ph=(ID_p-1)*360/spp;
42     %[ID Plane h P i e Omega phase per]
43     D(sat,1:9)=[sat Om (ap-a)/1000 P i*180/pi 0 Omega(Om) ph 0];
44
45 end
46 NameCells=['B2:I' num2str(N)];
47 xlswrite('SatsDatasheet.xls',D,NameCells)
48
49 %% Latex IMPORT
50
51 for sat=1:N
52
53     Om=ceil(sat/spp); ID_p=sat-(Om-1)*spp;
54     ph=(ID_p-1)*360/spp;
55     %[ID Plane h P i e Omega phase per]
56     D(sat,1:9)=[sat Om (ap-a)/1000 P i*180/pi 0 Omega(Om) ph 0];
57
58 end
59

```

```

60 [rows,cols]=size(D);
61 file=fopen('Autotable.txt','w');
62
63 for i=1:rows
64     Text=['AstreaSAT ' num2str(i) ' $ '];
65     for j=2:cols
66         if j≠cols
67             Text=[Text num2str(D(i,j-1)) ' $ '];
68         else
69             Text=[Text num2str(D(i,j-1)) ' \\\ '];
70         end
71     end
72     fprintf(file,[Text '\n']);
73 end
74
75 fclose(file);

```

1.12 Ground Station Localization

```

1  %----ASTREA CONSTELLATION----
2  %PROJECTS - 220028
3  %Aerospace Engineering Barchelor's Degree
4  %ESEIAAT - UPC
5  %Autumn 2016-2017
6
7  % COMMUNICATION TEAM
8  % GROUND STATIONS LOCALIZATION
9
10 clc; clear;
11
12 %% Input Data
13 N_sat=21;    %number of sats in a plane
14 N_planes=9; %number of orbital planes
15 h=542;      %high of the sats in km
16 I=72;       %inclination of the orbits in degrees
17 phase=210/(N_planes-1); %Angle between planes in the equator
18 At=0.1;     %time step in minutes
19 T=48;       %time to simulate in hours
20 t=0:At:T*60; %array of time in minutes
21 e_min=7.5;  %minumum elevation in degrees
22 lambda=57.5; %latitudes to simulate in degrees
23 lat=length(lambda);
24 mu=0;       %longitudes to simulate in degrees
25 long=length(mu);
26 l=length(t);
27

```

Ground Station Localization

```

28 %% Solver
29
30 Xs=Orbitalposition(N_sat,N_planes,h,I,phase,t);
31 L=zeros(lat,1);
32
33 for i=1:lat
34     Xg=Groundposition(lambda(i),mu,t);
35     [L(i,:)]=Links(Xs,Xg,e_min);
36 end
37
38 %% Plots
39
40 figure;plot(t/60,L);legend 0 30 60 90;xlabel('time (h)');ylabel('links');

```

```

1 function [X] = Orbital_position(N_sat,N_planes,h,I,mu,t)
2 %N_sat: number of sats per plane
3 %N_planes: number of planes
4 %h: Orbit high in km
5 %I: inclination of the orbital plane in degrees
6 %mu: Angle between two adjacent orbital planes at the equatorial plane in
7 %degrees
8 %t: array of time in minutes
9
10 I=I*pi/180; %I in rad
11 mu=mu*pi/180; %mu in rad
12 Omega=0:mu:(N_planes-1)*mu;
13 %longitude of the ascending node respect the inertial X axe [rad]
14
15 %for defining the orbits are defined a system of
16 %local axes X_o in which the y_o is the rotation axe and x_o is
17 %contained in the equatorial plane. The transformation for the inertial
18 %system X_I to the local system 2 rotations are defined.
19 %FIRST ROTATION: it defines a intermediate system X_1. The inertial system
20 %rotates around z_I an Omega angle.
21 %SECOND ROTATION: The X_1 system is rotated (90deg-I) around x_1
22
23 L_1o=[1 0 0; 0 sin(I) cos(I); 0 -cos(I) sin(I)]; %1st rotation matrix.
24 %It transform a vector from local coordinates X_o to intermediate
25 %coordinates X_1. This matrix is the same for every orbital plane
26 %since all orbits have the same inclination
27
28 Re=6371; %Earth radius km.
29 %The distances are going to be refered to the earth radius
30 h=h/Re; %high in earth radius
31 GM=6.474e-11*5.972e24*3600/Re^3;
32 %Gravitational constant*earth mass [(Re^3)/min^2]
33 Ro=1+h; %orbital radius in earth radius
34
35 w=sqrt(GM/(Ro^3)); %sat's angular speed [rad/min]

```



```

36 phi=0:2*pi/N_sat:(N_sat-1)*2*pi/N_sat;
37 %relative angle between every sat of a plane respect the first one
38 f=8;
39 %factor to module the relative desfase of the first sat of one plane
40 %to the first sat of the next plane
41 l=length(t);
42
43 for p=1:N_planes    %going through each plane
44
45     phi_0(p)=f*2*pi*(p-1)/(N_planes*N_sat);
46     %relative desfase of the first sat of one plane to the
47     %first sat of the next plane
48
49     One = cos(Omega(p));
50     Two = sin(Omega(p));
51     L_I1=[One -Two 0; Two One 0; 0 0 1];
52     %2nd rotation matrix. It transforms a vector from
53     %intermediate coordinates X_1
54     %to inertial coordinates X_I. This matrix is characteristic of every
55     %plane since every plane has a different longitude of the ascending node
56     %(Omega)
57
58     L_eo=L_I1*L_1o;
59     %Global rotation matrix from local coordinates to inertial coordinates
60
61     for s=1:N_sat    %going through every sat of the plane
62
63         for k=1:l    %going through every time step
64
65             First = Ro*cos(w*t(k)+phi(s)+phi_0(p));
66             Second = -Ro*sin(w*t(k)+phi(s)+phi_0(p));
67             X_loc=[First;0;Second];
68             %Coordinates of the sat at the given time in
69             %local coordinates X_o.
70             %It defines a circumference at the plane x_o-z_o with an angular
71             %velocity w, an initial phase respect the first sat and an
72             %initial phase respect the first sat of the previous orbit
73             %first sat.
74
75             X(:,(p-1)*N_sat+s,k)=L_eo*X_loc;
76             %Coordinates of the sat in inertial system
77             %(Coordinate [x y z], Sat number, instant(time))
78         end
79     end
80 end
81 end

```

```

1 function [X] = Ground_position(lambda,long,t)
2 %Ground_position calculates the position of a place of the earth, with a

```

Ground Station Localization

```

3 %given longitude and latitude, in an inertial system of coordiantes X_I in
4 %a given period of time
5
6 %lamda: is the latitude of the place in degrees[-90,90]
7 %long: is the longitude of the place iin degrees [0,360)
8 %t: is a array of time in minutes
9
10 long=long*pi/180;    %longin radians
11 lambda=lambda*pi/180;    %lambda in radians
12
13 Rg=cos(lambda);
14 %distance between the Earth point to the rotation axis of the Earth [0,1]
15 hg=sin(lambda);
16 %distance between th Earth point to the equatorial plane [0,1]
17 %this 2 distances are measured in earth radius.
18
19 w=2*pi/(24*60); %angular velocity of the Earth [rad/min]
20
21 X=[Rg*cos(w*t+long);Rg*sin(w*t+long);hg*ones(1,length(t))];
22 %position of the point in X_I
23 %for the given time. The point describes a cicumference
24 %with a Rg radius in the horizontal
25 %plane x_I-y_I with an angular velocity w and a initial phase long. The
26 %coordinate z_I is allways hg. It is expresed in earth radius.
27 %X(coordinates, instant (time)
28
29 end

```

Chapter 2

Bibliography