

## Exercise Sheet 14

### Exercise 1: Kernel Ridge Regression (10+10 P)

In the lecture, ridge regression was stated as the regularized quadratic program

$$\min_w \sum_{i=1}^n (w^\top x_i - y_i)^2 + \lambda \|w\|_2^2,$$

where  $w \in \mathbb{R}^d$  is optimized and  $x_1, \dots, x_n \in \mathbb{R}^d$  are the data points, and  $y_1, \dots, y_n \in \mathbb{R}$  are the labels.

- (a) Following the strategy outlined in the lecture slides, *give* an explicit formula for the solution of the above program.
- (b) *Kernelize* the ridge regression model, following the strategy outlined in the lecture slides.

### Exercise 2: Lagrange Multipliers (20+10+10 P)

Consider the slightly modified quadratic program

$$\begin{aligned} \min_{\xi, w} \quad & \sum_{i=1}^n \xi_i^2 \\ \text{subject to} \quad & \xi_i = w^\top x_i - y_i \text{ for } 1 \leq i \leq n \quad \text{and} \quad \|w\|_2^2 \leq C, \end{aligned}$$

where  $C$  is a regularization constant.

- (a) *Calculate* the Lagrange dual of this program, and its solution.
- (b) *Describe* how a solution for the primal program can be found from a solution of the dual.
- (c) *Explain* how the solutions relate to the original quadratic program and its solutions in ridge regression and kernel ridge regression.

### Exercise 3: Programming (40 P)

Download the programming files on ISIS and follow the instructions.