**INFORMATICS INSTITUTE OF TECHNOLOGY**

**IN COLLABORATION WITH**

**UNIVERSITY OF WESTMINSTER (UOW)**

**B.Eng. (Hons) Software Engineering**

**5DATA001C.2 – Machine Learning and Data Mining**

**Module Leader: Achala Aponso**

Coursework 01

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**CLUSTERING PART**

1. **Discussion of the methodologies used in *reducing the dimensionality.***

* Since, this dataset “**vehicles.xlsx**” has a large number of features or columns (19 features), this is referred to as **a high dimensional dataset**.
* Having a large number of dimensions will lead to the **curse of dimensionality**.
* **Curse of dimensionality** means that’s as the number of dimensions (features/columns) of the dataset increases the points go further apart or data becomes extremely sparse leading the accuracy to decrease.
* **PCA** (Principal Component Analysis) is the most popular technique which can be used for dimensionality reduction, PCA helps to identify all those high correlated variables, which are not related to the target variable at all and drop them out from further analysis.
* Therefore, using PCA we can convert **a high dimension data into low dimension** without losing any of the important features which are correlated to the target class.

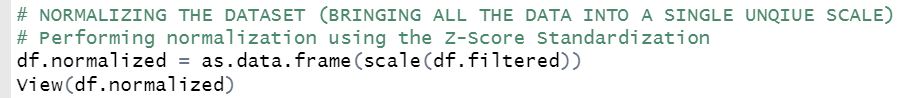
1. **What is PCA?**

* **PCA** or also known as Principal Component Analysis, is an unsupervised learning algorithm that is used specifically for dimensionality reduction in machine learning.
* When the PCA algorithm is applied it produces something called as the **Principal Components**.
* The aim of the PCA algorithm is to **lower-dimensions** from a higher dimension but still retain the quality of the data.

1. **What is Scaling and why do we need them?**

* Scaling or feature scaling is a technique which is used to standardize the data into a fixed range scale. In other words, bring all the data which belonged to different scales into a single common unique scale.
* If the data is not scaled or standardized, then a better result or a higher accuracy cannot be achieved, because all the features contribute in a different proportion not equally.

E.g.: - Price of the house sale with time, in general price of the house increase with time but time and price of house are of different scale and the difference between the values of the price and time are quite large hence data needs to be scaled down



*~ This is an image of the normalization step taken in the Kmeans clustering problem statement ~*

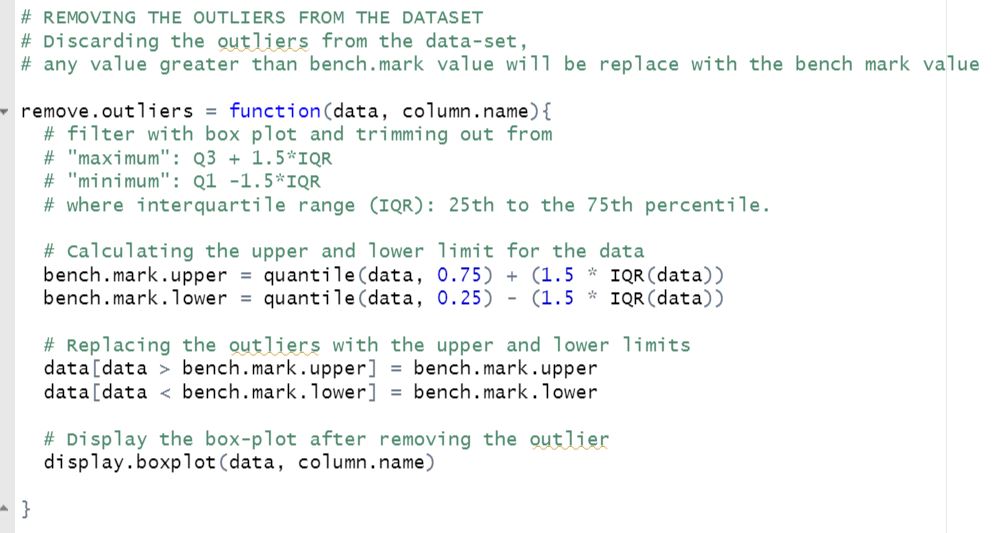
1. **What are outliers?**

* Data points or data values which are completely out of the range from what it’s expected to be in are called outliers. In other words, data collected due to some fault or error which makes it to fall way out of the range of data expected.
* Example, consider the height of students and there are 2 outliers present here which is 1ft and 8ft. (In general there are no students with the height of 1ft or 8ft so these are outliers)

Heights: **1ft**, 5ft, 5.1ft, 4.9ft, 5.7ft, 5.9ft, **8ft**

1. **Why do outliers need to be removed from the dataset?**

* The presence of an outlier can affect the accuracy of the model we create. This is because the data is not clean. With clean data only we can create a better accurate model accuracy.
* Hence, outliers need to be removed from the dataset before the training process.



*~ This is an image of the outlier removal step taken in Kmeans clustering problem statement ~*

1. **How can we find out if there are outliers in our dataset?**

* By drawing up a box plot for each feature of your dataset, you will be able to find data points which go above the maximum range and data points going below the minimum range and these are the outliers and has to be removed. You can remove the outliers by literally removing the data from the dataset or a better approach would be to replace the outlier values with the bench mark values (higher and lower) from the dataset, by doing so we don’t loose data from the dataset and also not reduce the accuracy.

**NOTE: PCA was not performed because the CW specification method NOT to. However, the code for PCA is commented in the code section for PCA reference**

1. **Explain how the Order of scaling and outlier removal is important?**

* Outliers has to be first removed from the dataset before scaling the dataset.
* If the outlier removal is not performed before normalizing the data, then the dataset won’t be efficient enough for the modal to predict, this is because the resulting data won’t be properly standardized therefore you may end up getting different variables/columns having different standard deviations which is a problem.

1. **Briefly explain the meaning of:**
2. ***Accuracy***:

* Accuracy is one an evaluation metric type for classification models.
* Accuracy is also defined by the following formula:

**Accuracy** = Total Number of correct predictions / Total Number of predictions

**Accuracy = (True Positives + True Negatives) / Total Number of predictions**

In other words, accuracy represents how close a measurement comes to its true value.

1. ***Precision***:

* Precision is another evaluation metrics which is also referred to as the spread of the measured values.
* Precision is calculated by the following formula:

**Precision** = True Positives / (True Positives + False Positives)

* The result of this equation lies between 0 to 1, 0.0 indicating that there is no precision and 1.0 for full precision.

1. ***Recall***:

* Recall is another evaluation metrics that is used to quantify the number of correct positive predictions made out of all positive predictions that could have been made.
* Unlike precision, Recall provides an indication of missed positive predictions.
* Recall is calculated by the following formula:

**Recall** = True Positives / (True Positives + False Negatives)

1. **Results and Discussion using the Confusion matrix with respect to the calculation for the accuracy/recall and precision matrices.**

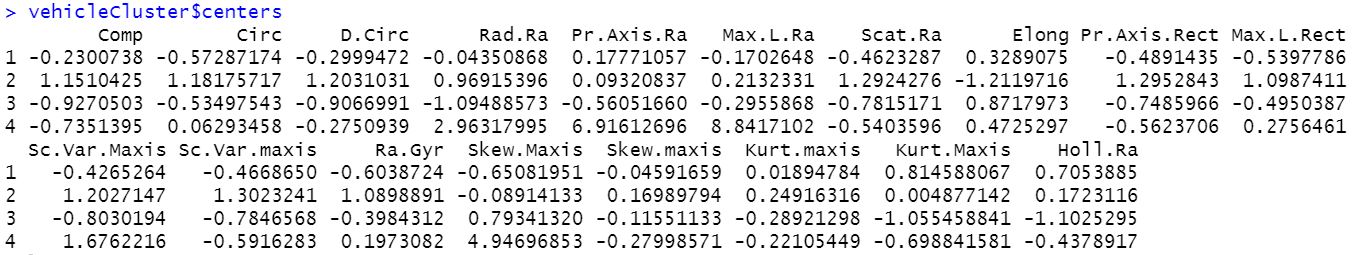
* When automated tools we used inorder to calculate the number of clusters formed these were the following results which were obtained.

**Elbow Method** (**Automated**) gave me 4 clusters as the BEST one.

**Silhouette Method** (**Automated**) gave me 2 clusters as the BEST one.

**Gap Statistics Method** (**Automated**) gave me 3 clusters as the BEST one.

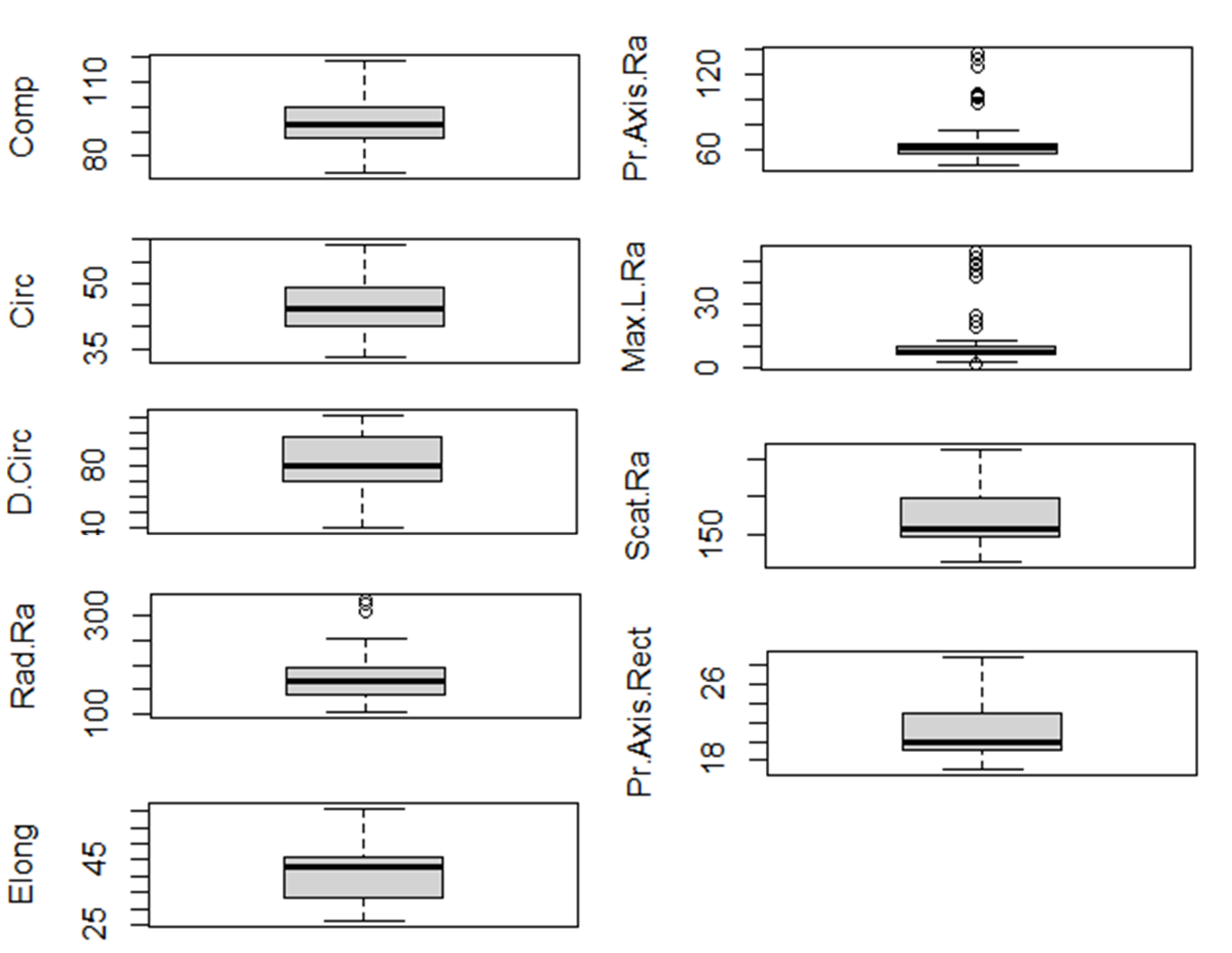
* A **manually** created **elbow method** is used to compute the best number of clusters, by looping through 1 to 10 number of clusters and performing the KMeans clustering and calculating its accuracy using the *confusion matrix*. These are the follow results given for the clusters from 1 to 10 with its accuracy, precision and its recall value.
* 1 Cluster (Accuracy: 23.5%)
* 2 Cluster (Accuracy: 12.3%)
* 3 Cluster (Accuracy: 19.5%)
* 4 Cluster (Accuracy: 35.2%)
* 5 Cluster (Accuracy: 25.5%)
* 6 Cluster (Accuracy: 9.7%)
* 7 Cluster (Accuracy: 15.2%)
* 8 Cluster (Accuracy: 13.2%)
* 9 Cluster (Accuracy: 16.0%)
* 10 Cluster (Accuracy: 11.1%)
* Since the 4-cluster have the highest accuracy, 4 clusters are considered and taken as the optimal number of clusters for this problem statement.
* These are the following coordinates of the centers of the clusters.



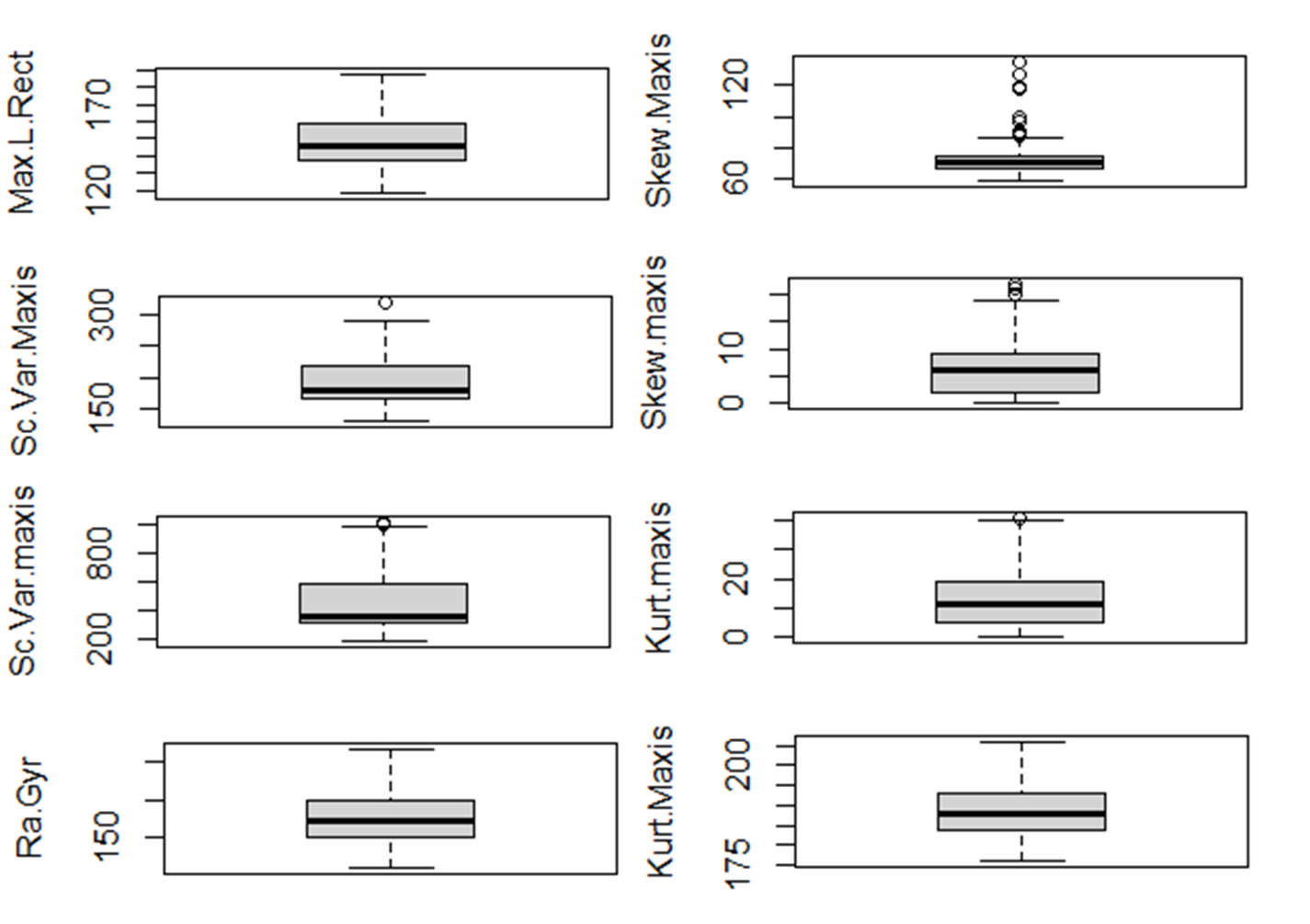
*~ Cluster centers coordinates ~*

1. **The following are graphs obtained and its respective description about the graph**

- The graphs below represent boxplots for all columns or features of the dataset which consist of outliers

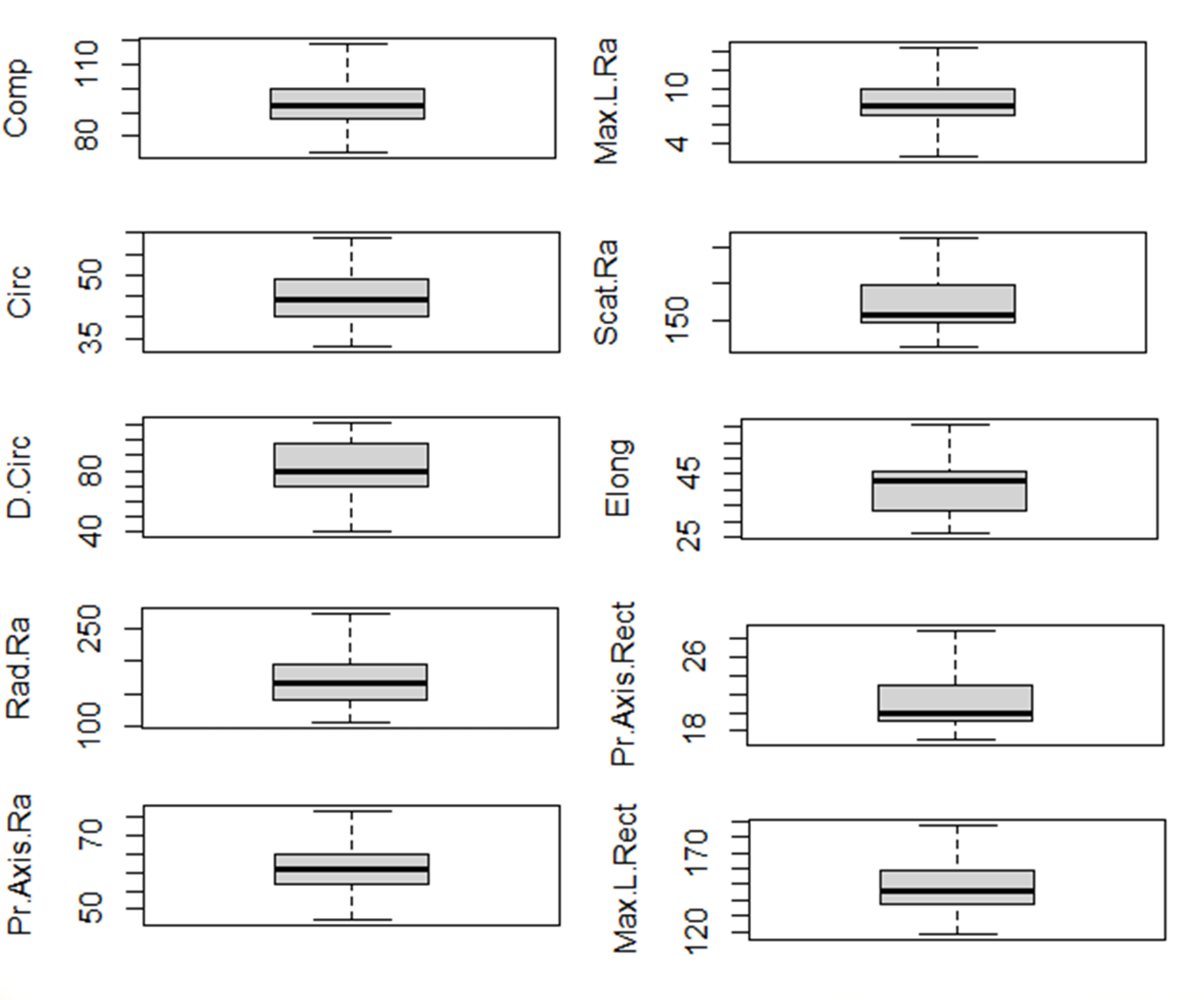


*~ Displaying outliers of the features of the dataset ~*

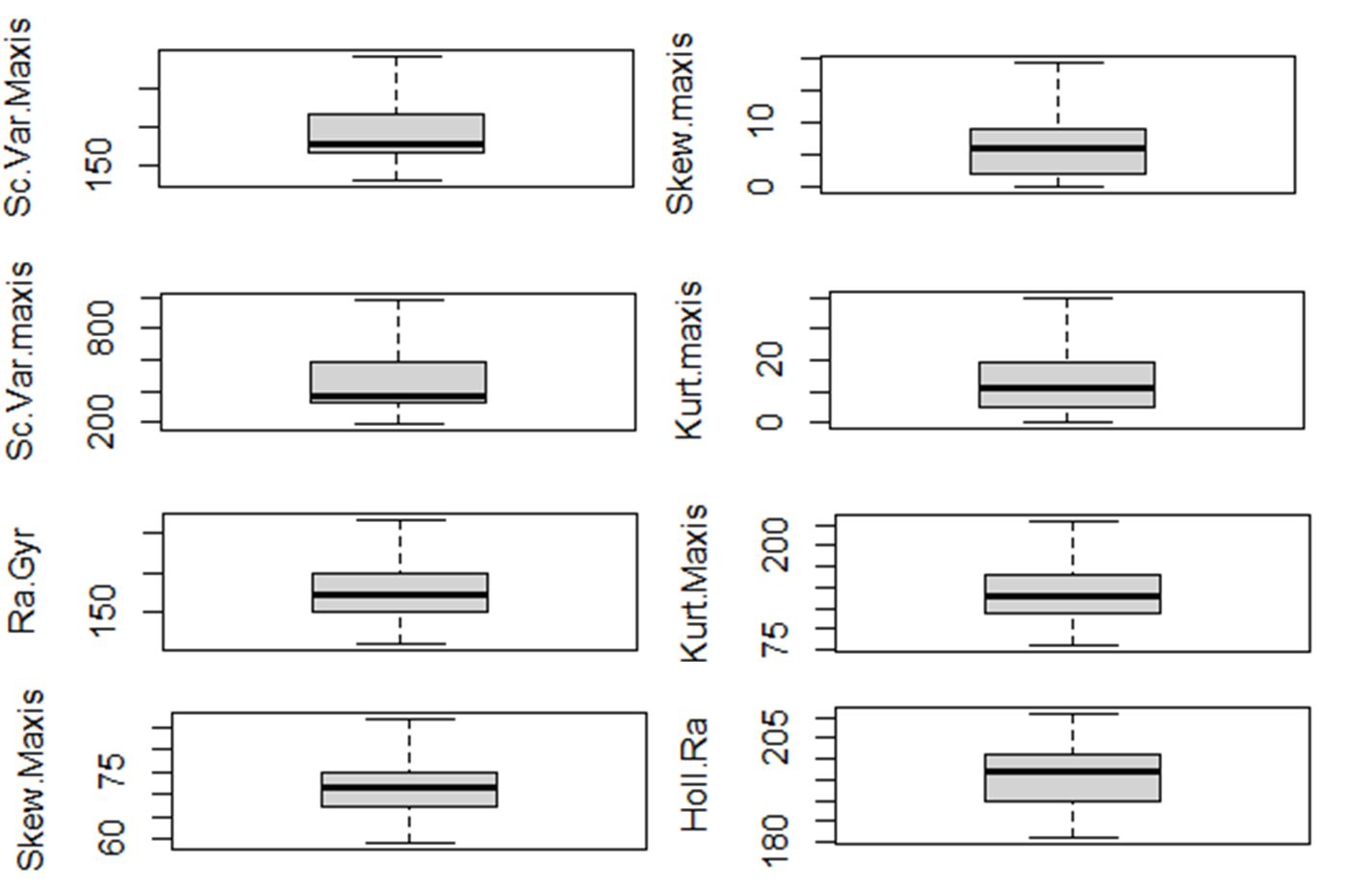


*~ Displaying outliers of the features of the dataset ~*

- The graphs below represent boxplots for all columns or features of the dataset where the outliers are removed.

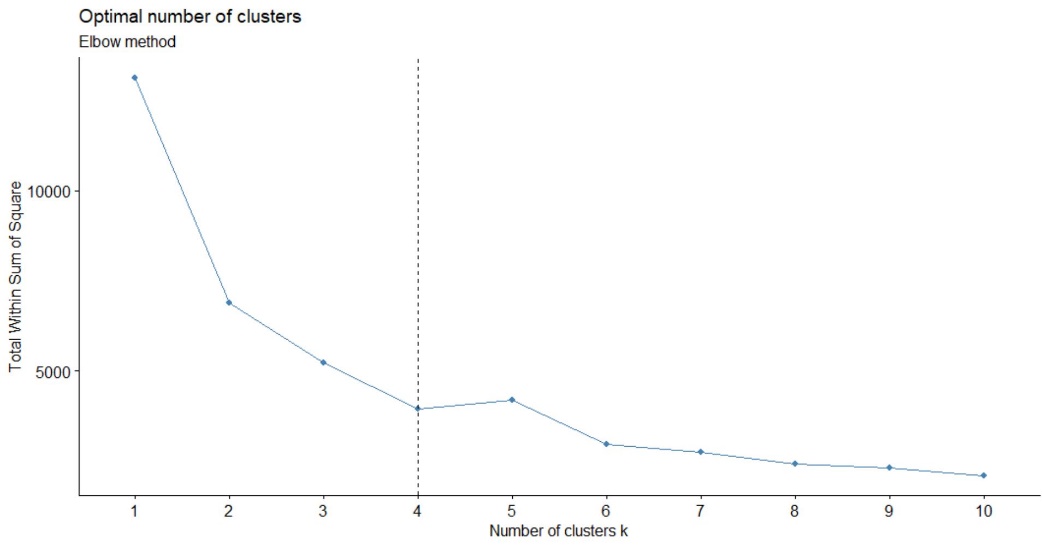


*~ Removing outliers of the features of the dataset ~*



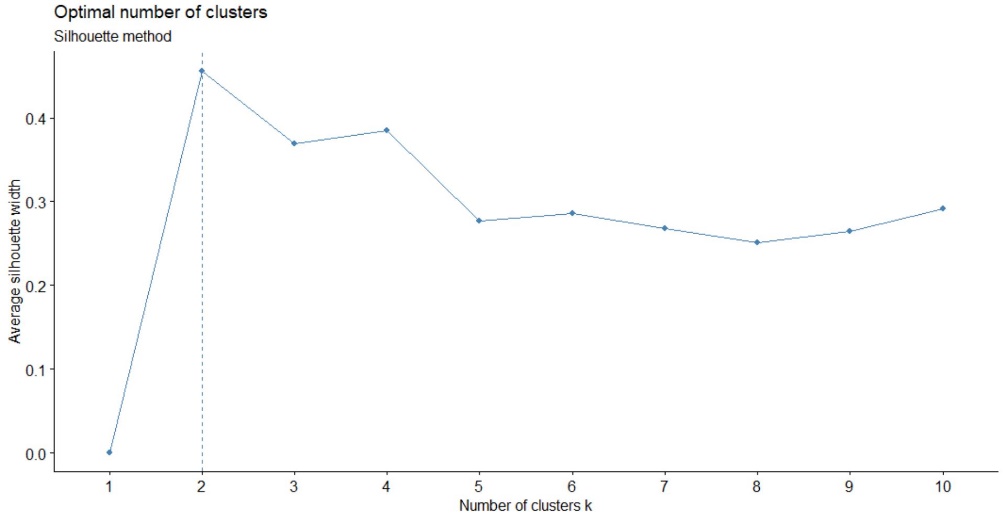
*~ Removing outliers of the features of the dataset ~*

- Using the **automated tools** to find the best number of centroids (using the **ELBOW** method)



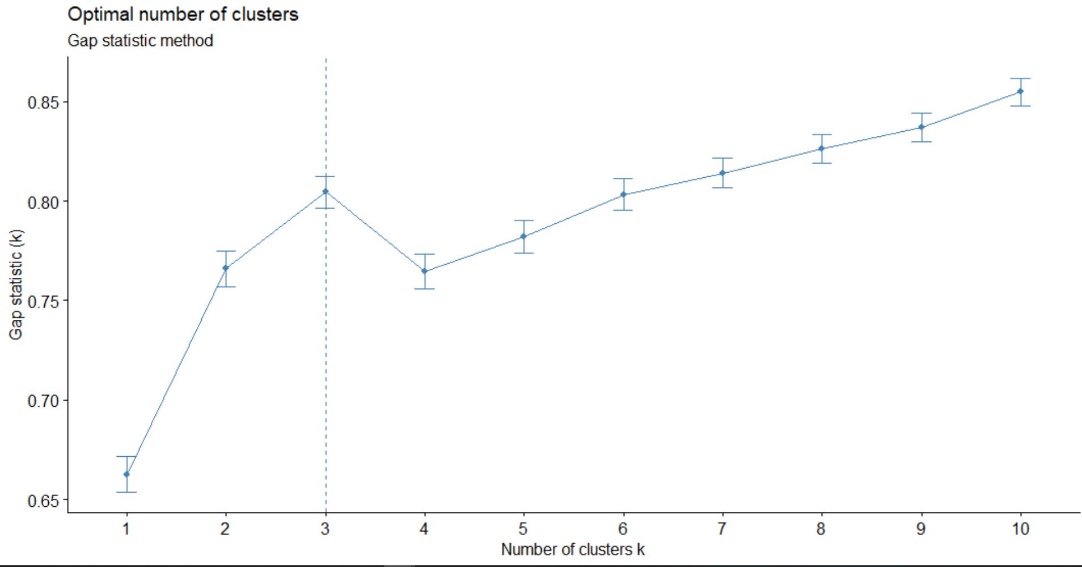
*~ Automated elbow method ~*

- Using the **automated tools** to find the best **number** of **centroids** (using the **SILHOUETTE** method)



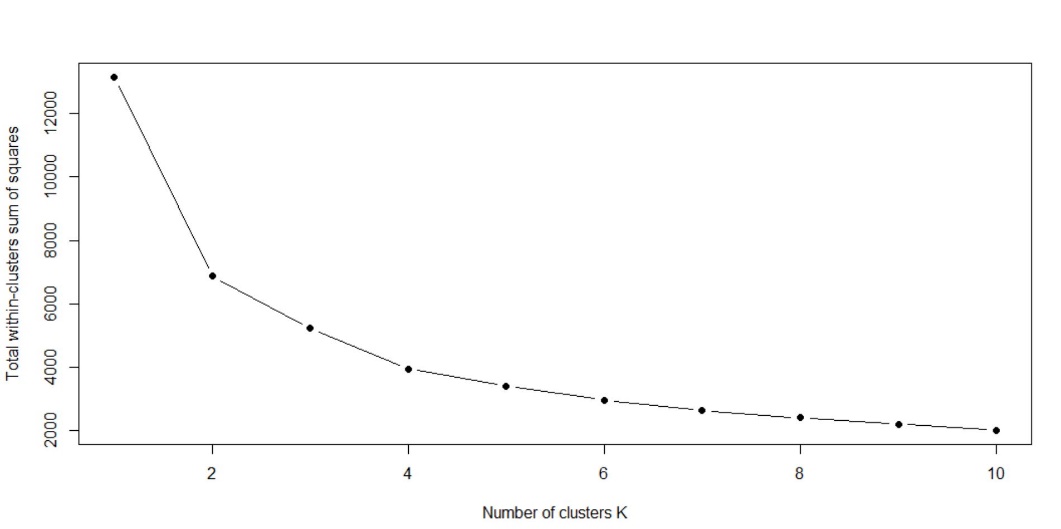
*~ Automated Silhouette method ~*

- Using the **automated** tools to find the **best** number of **centroids** (using the **GAP** **STATISTIC** method)



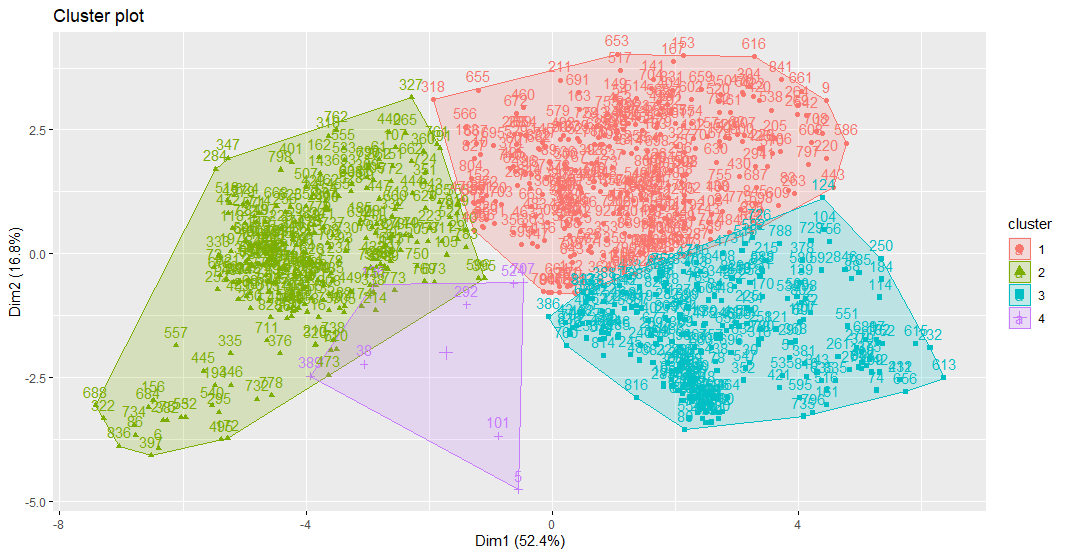
*~ Automated Gap Statistic method ~*

- Using the **manual** method to find the best number of centroids (using the ELBOW method)



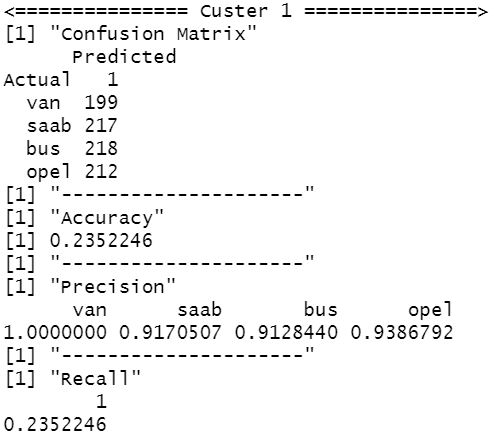
*~ Manual Elbow method to find optimal clusters~*

From the statistics, using automated elbow method the optimal clusters found was 4, using manual elbow method also the optimal number of clusters found was 4, moreover the highest accuracy recorded is achieved by 4 clusters, hence the optimal number of clusters for this problem is said to be 4, and a cluster plot related to the clustering of data is given below for visualization.

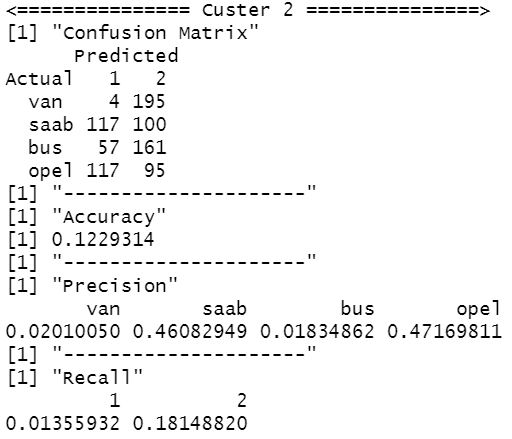


*~ Cluster Plot Visualization ~*

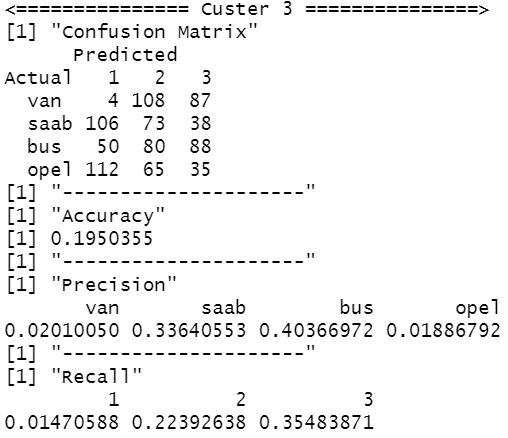
Given below are the evaluation results obtained for the first 10 clusters inorder to find the optimal cluster centroid number. (using a confusion matrix these evaluations are made)



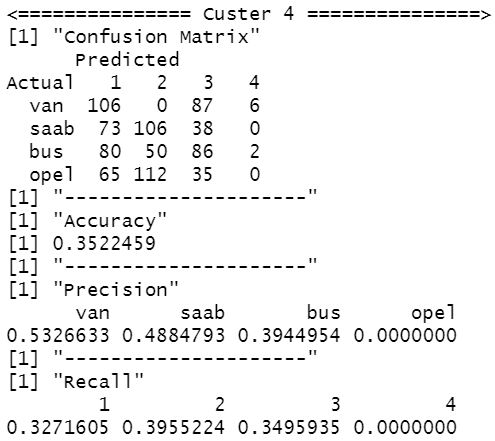
*~ Cluster 01 evaluation ~*



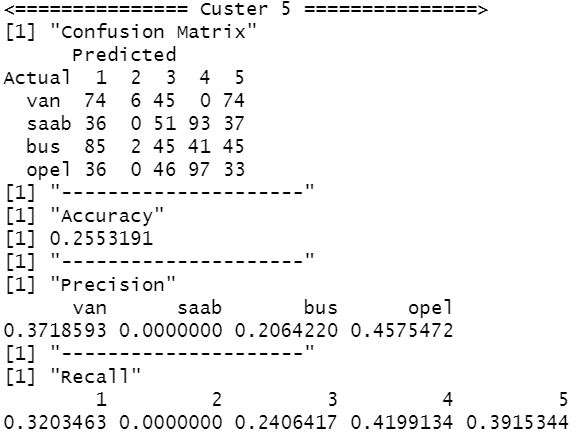
*~ Cluster 02 evaluation ~*



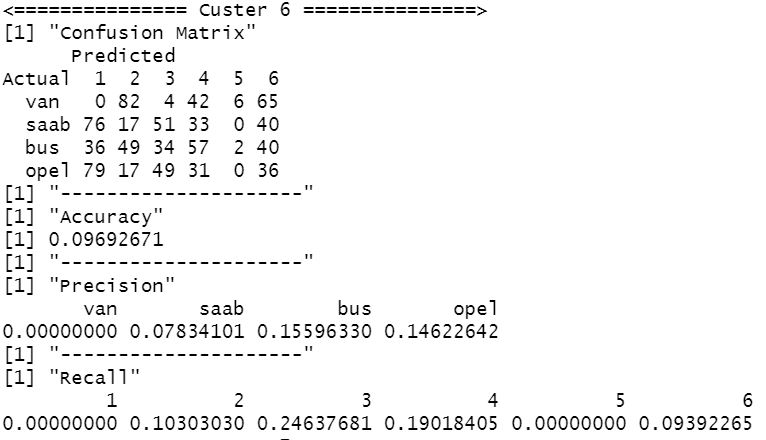
*~ Cluster 03 evaluation ~*



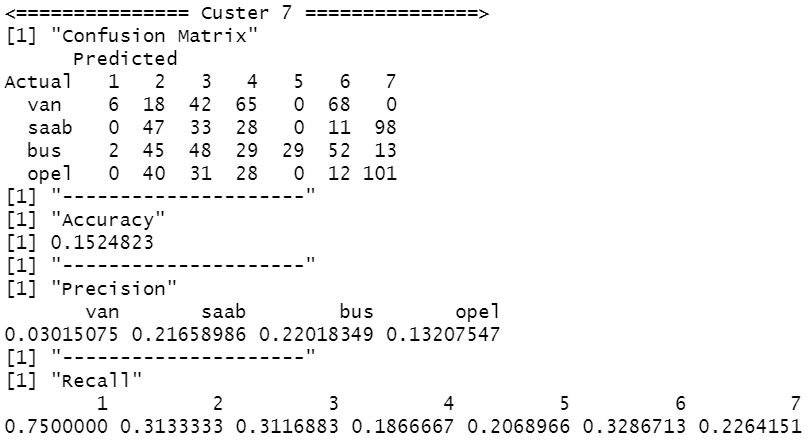
*~ Cluster 04 evaluation ~*



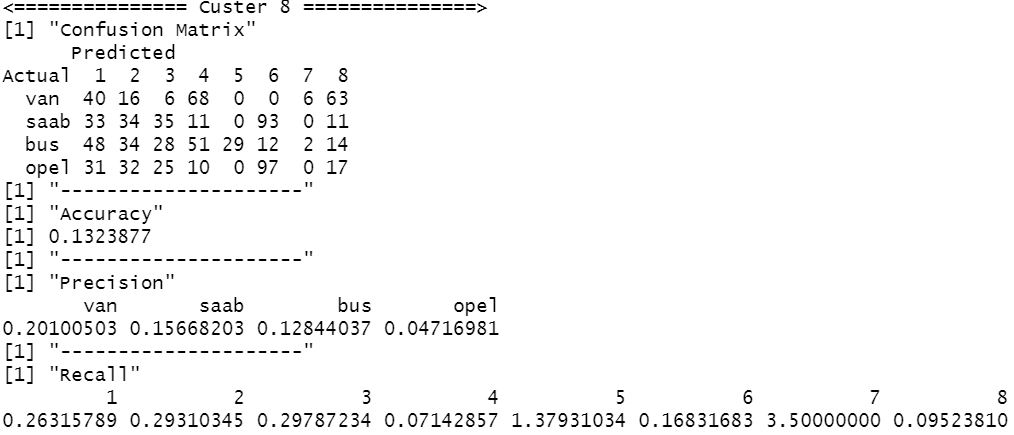
*~ Cluster 05 evaluation ~*

**

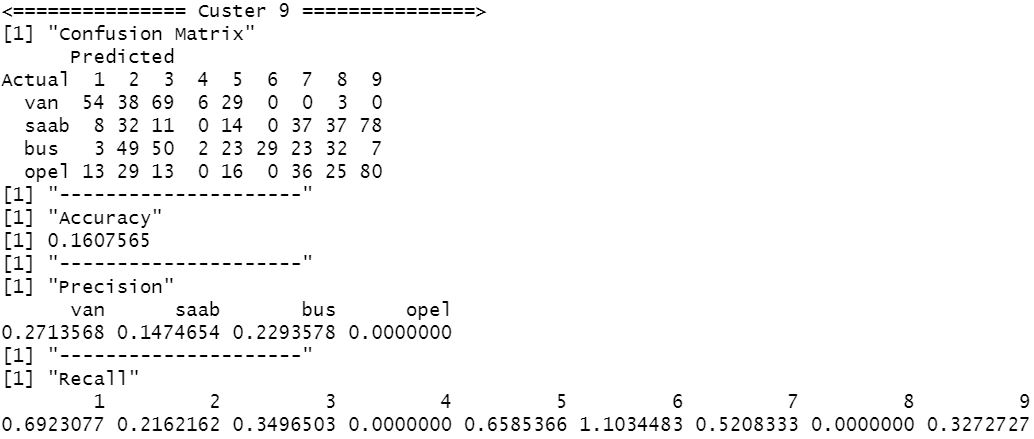
*~ Cluster 06 evaluation ~*

**

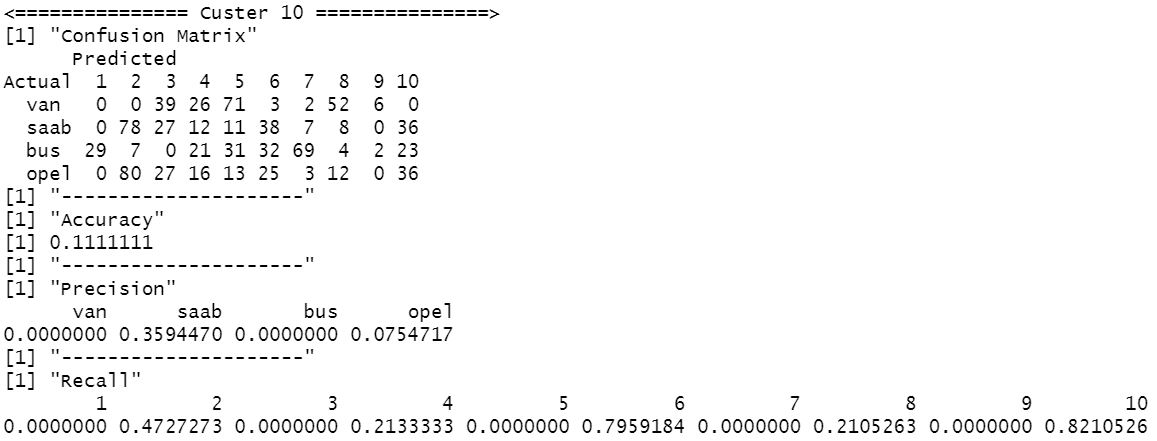
*~ Cluster 07 evaluation ~*



*~ Cluster 08 evaluation ~*

**

*~ Cluster 09 evaluation ~*

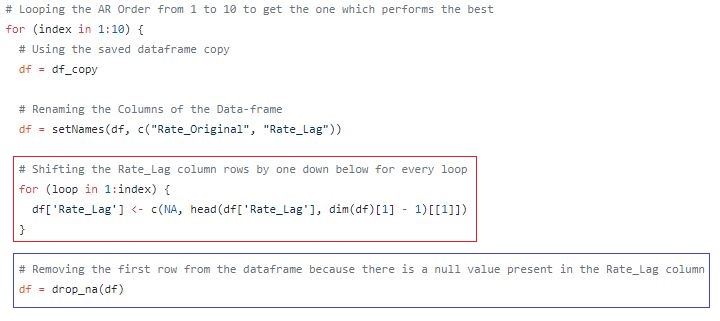
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*~ Cluster 10 evaluation ~*

**FORECASTING PART**

1. **Discussion of the various schemes used to define the input vector and related evidence.**

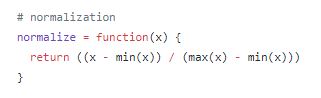
Since this problem statements requires the “autoregressive” (AR) approach, the input matrix for the model will change or vary depending on the order of AR considered when training. Suppose if AR 1 approach is considered to be applied for the model, then another duplicated column of the exchange rate column is created but the rows are shifted down by one, this is called the **lag**. Now using the lag column rates as the input for the model and output as the original rate column we perform the training process. This is repeated from AR1 to AR10 in order to find which is the best order of AR. Likewise, the input vector which is the rates lag will change when the order of AR changes (rows will get shifted with respect to the AR order). (NOTE: once rows are shifted the NULL value rows are removed before training).



In the above diagram it clearly visible that there is a looping going on to get the best order of AR from 1 to 10. In the **RED** colored box indicates that the shifting of the columns happens in order to get the lag rates and this changes as the order of AR changes. Moreover, the **BLUE** box indicates that once the shift rows are completed the top rows which contain NULL values after shifting is removed.

1. **Explain why normalization procedure is necessary for this specific type of NN.**

Since neural networks deals with a large number of layers and a large number of nodes then the TIME TAKEN for the model to train properly will take a lot of time in general, but by normalizing the data input to the neural network it SPEEDS up the learning process to a higher rate leading to faster or quicker convergence or increase the chances to reach the global minima quickly. Moreover, normalization is important give a consistence scale range for all the features there by making it more accurate for training and not making it bias to a specific feature due to its input size.



*~ Normalizing the data using MIN MAX normalization ~*

1. **Comparision table for the testing performance based on the statistical indices.**

**Input data/vector used is the AR1 rate lag data**

**Performance Table Results for 1 hidden layer**

|  |  |  |  |
| --- | --- | --- | --- |
| **PARAMETERS** | **MAE** | **RMSE** | **MAPE** |
| hidden=c(1),  act.fct = "logistic", learningrate = 0.1 | **2.204 %** | **2.9626 %** | **4.3369 %** |
| hidden=c(2),  act.fct = "logistic", learningrate = 0.1 | **2.1872 %** | **2.9313 %** | **4.3196 %** |
| hidden=c(3),  act.fct = "logistic", learningrate = 0.1 | **2.202 %** | **2.9201 %** | **4.3281 %** |
| hidden=c(4),  act.fct = "logistic", learningrate = 0.1 | **2.2107 %** | **2.9423 %** | **4.3616 %** |
| hidden=c(5),  act.fct = "logistic", learningrate = 0.1 | **2.206 %** | **2.9204 %** | **4.3337 %** |
| hidden=c(6),  act.fct = "logistic", learningrate = 0.1 | **2.1999 %** | **2.9036 %** | **4.2842 %** |
| hidden=c(7),  act.fct = "logistic", learningrate = 0.1 | **2.2146 %** | **2.9217 %** | **4.3451 %** |
| hidden=c(8),  act.fct = "logistic", learningrate = 0.1 | **2.2227 %** | **2.925 %** | **4.3579 %** |
| hidden=c(9),  act.fct = "logistic", learningrate = 0.1 | **2.2332 %** | **2.9339 %** | **4.3808 %** |
| hidden=c(10),  act.fct = "logistic", learningrate = 0.1 | **2.2386 %** | **2.9238 %** | **4.3693 %** |

**The optimal number of nodes found for the single hidden layer MLP NN is 6.**

**Now finding the optimal activation function for this MLP NN structure**

|  |  |  |  |
| --- | --- | --- | --- |
| hidden=c(6),  act.fct = "tanh", learningrate = 0.1 | **2.1921 %** | **2.9261 %** | **4.3228 %** |
| hidden=c(6),  act.fct = "logistic", learningrate = 0.1 | **2.1999 %** | **2.9036 %** | **4.2842 %** |

**It can be clearly seen that “logistic” performs much better.**

**Now finding the optimal learning rate for this MLP NN structure**

|  |  |  |  |
| --- | --- | --- | --- |
| hidden=c(6),  act.fct = "logistic", learningrate = 0.02 | **2.2184 %** | **2.9172 %** | **4.3628 %** |
| hidden=c(6),  act.fct = "logistic", learningrate = 0.04 | **2.2484 %** | **2.9625 %** | **4.4272 %** |
| hidden=c(6),  act.fct = "logistic", learningrate = 0.06 | **2.2147 %** | **2.9211 %** | **4.3637 %** |
| hidden=c(6),  act.fct = "logistic", learningrate = 0.08 | **2.2284 %** | **2.9325 %** | **4.3672 %** |
| hidden=c(6),  act.fct = "logistic", learningrate = 0.1 | **2.1999 %** | **2.9036 %** | **4.2842 %** |

**From the above results learning rate of 0.1 gave the best result, hence the best of set of parameters for 1 hidden layer MLP NN is as follows**

HIDDEN\_LAYERS = c(6)

ACTIVATION\_FUNCTION = "logistic"

LEARNING\_RATE = 0.1

**Performance Table Results for AR1 with 2 hidden layer, for the first layer 6 nodes will be used since that was the best when calculated for 1 hidden layer MLP NN, the nodes for the 2nd hidden layer will be calculated along with the learning rate, and activation function**

|  |  |  |  |
| --- | --- | --- | --- |
| **PARAMETERS** | **MAE** | **RMSE** | **MAPE** |
| hidden=c(6,1),  act.fct = "logistic", learningrate = 0.1 | **2.420 %** | **2.956 %** | **4.3451 %** |
| hidden=c(6,2),  act.fct = "logistic", learningrate = 0.1 | **2.1845 %** | **2.9546 %** | **4.3125 %** |
| hidden=c(6,3),  act.fct = "logistic", learningrate = 0.1 | **2.236 %** | **2.9236 %** | **4.3459 %** |
| hidden=c(6,4),  act.fct = "logistic", learningrate = 0.1 | **2.2512 %** | **2.9633 %** | **4.3617 %** |
| hidden=c(6,5),  act.fct = "logistic", learningrate = 0.1 | **2.226 %** | **2.9234 %** | **4.3457 %** |
| hidden=c(6,6),  act.fct = "logistic", learningrate = 0.1 | **2.1246 %** | **2.7469 %** | **4.2123 %** |
| hidden=c(6,7),  act.fct = "logistic", learningrate = 0.1 | **2.2246 %** | **2.9257 %** | **4.3421 %** |
| hidden=c(6,8),  act.fct = "logistic", learningrate = 0.1 | **2.2327 %** | **2.965 %** | **4.3539 %** |
| hidden=c(6,9),  act.fct = "logistic", learningrate = 0.1 | **2.2532 %** | **2.9379 %** | **4.3848 %** |
| hidden=c(6,10),  act.fct = "logistic", learningrate = 0.1 | **2.2686 %** | **2.9258 %** | **4.3653 %** |

**The optimal number of nodes found for the 2nd hidden layer is 6.**

**Now finding the optimal activation function for this MLP NN structure**

|  |  |  |  |
| --- | --- | --- | --- |
| hidden=c(6,6),  act.fct = "tanh", learningrate = 0.1 | **2.2547 %** | **2.9311 %** | **4.3437 %** |
| hidden=c(6,6),  act.fct = "logistic", learningrate = 0.1 | **2.2184 %** | **2.9172 %** | **4.3328 %** |

**It can be clearly seen that “logistic” performs much better.**

**Now finding the optimal learning rate for this MLP NN structure**

|  |  |  |  |
| --- | --- | --- | --- |
| hidden=c(6,6),  act.fct = "logistic", learningrate = 0.02 | **2.2184 %** | **2.9172 %** | **4.3428 %** |
| hidden=c(6,6),  act.fct = "logistic", learningrate = 0.04 | **2.2484 %** | **2.9625 %** | **4.4272 %** |
| hidden=c(6,6),  act.fct = "logistic", learningrate = 0.06 | **2.2147 %** | **2.9311 %** | **4.3437 %** |
| hidden=c(6,6),  act.fct = "logistic", learningrate = 0.08 | **2.182 %** | **2.9139 %** | **4.2749 %** |
| hidden=c(6,6),  act.fct = "logistic", learningrate = 0.1 | **2.2484 %** | **2.9211 %** | **4.333 %** |

**From the above results learning rate of 0.08 gave the best result, hence the best of set of parameters for 2 hidden layer MLP NN is as follows**

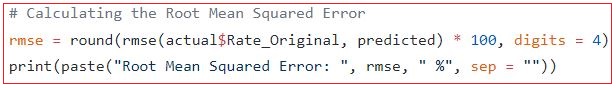
HIDDEN\_LAYERS = c(6,6)

ACTIVATION\_FUNCTION = "logistic"

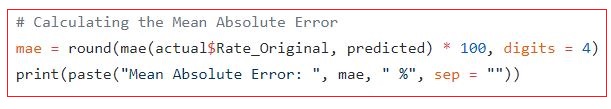
LEARNING\_RATE = 0.08

1. **Brief explanation on the statistical indices (RMSE, MAE and MAPE)**

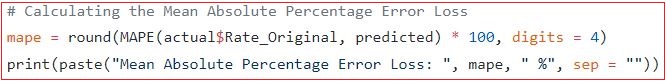
* **RMSE (Root Mean Square Error):** This is a statistical measure of the error of the model in predicting the respective data. Lower the RMSE value better the model is, better the prediction output is as well.



* **MAE (Mean Absolute Error):** This is basically the sum or total of average of the absolute difference between the predicted and actual values. So, what basically this means is that using the MAE we can get a clear picture as to how wrong the predictions are. Lower the MAE better the model



* **MAPE (Mean Absolute Percentage Error):** This is a statistical measure to define the accuracy of a model on a particular dataset or in other terms it is the percentage of average of absolute difference between predicted values and true values, divided by the true values. Lower the MAPE better the model again.



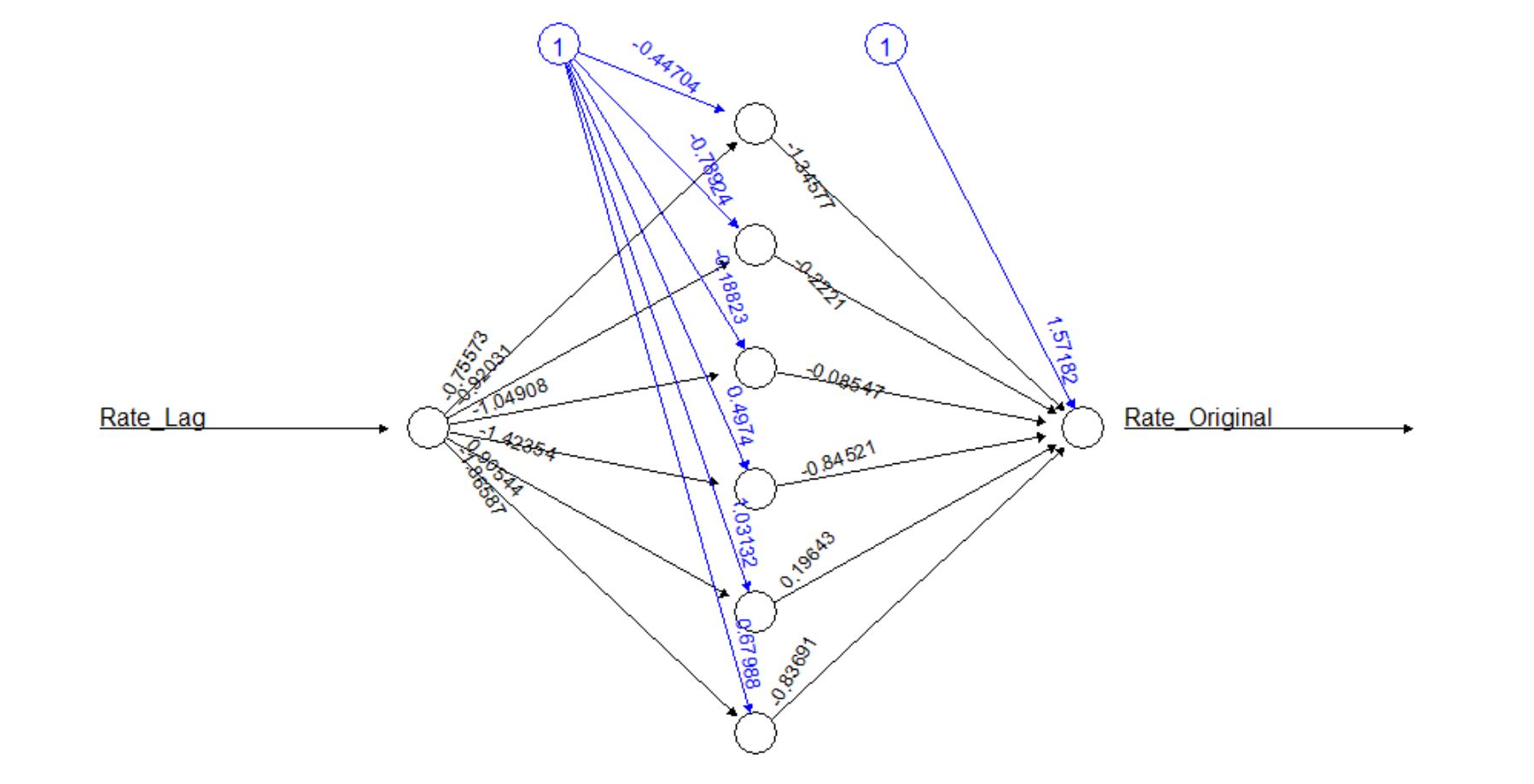
1. **Efficiency result from the best one hidden layer and two hidden layer network with their respective parameters.**

The BEST one hidden layer network

HIDDEN\_LAYERS = c(6)

ACTIVATION\_FUNCTION = "logistic"

LEARNING\_RATE = 0.1



**Number of weights between input and hidden layer:**

Number of inputs x Number of Neurons in the hidden layer = 1 x 6 = 6

**Number of weights between hidden layer and output layer:**

Number of Neurons in the hidden layer x Number of Neurons in output layer = 6 x 1 = 6

**Total Number of weight parameters = 6 + 6 = 12**

**Statistics Result (Based on AR1 input vector)**

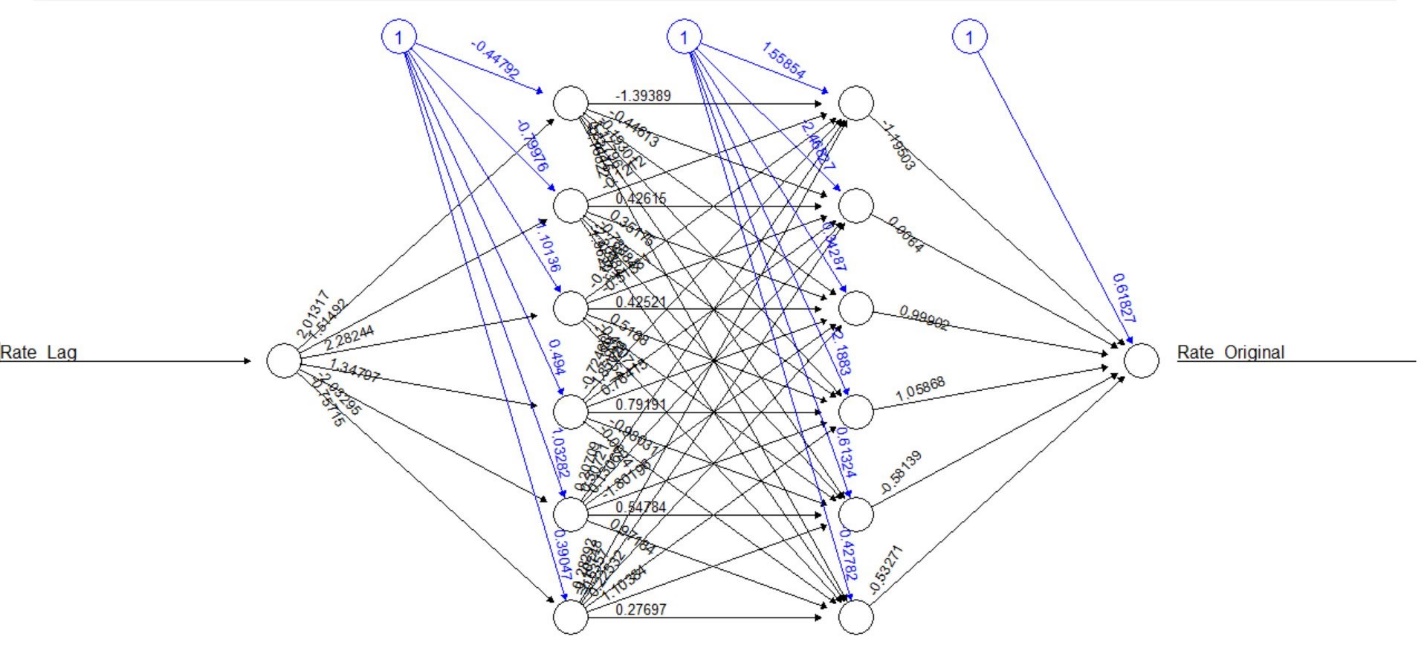
|  |  |  |
| --- | --- | --- |
| **MAE** | **RMSE** | **MAPE** |
| **2.1999 %** | **2.9036 %** | **4.2842 %** |

The BEST two hidden layer network

HIDDEN\_LAYERS = c(6,6)

ACTIVATION\_FUNCTION = "logistic"

LEARNING\_RATE = 0.08

****

**Number of weights between input and first hidden layer:**

Number of inputs x Number of Neurons in the hidden layer = 1 x 6 = 6

**Number of weights between the first hidden layer and the second hidden layer:**

Number of neurons in the first hidden layer x Number of neurons in the second hidden layer

= 6 x 6 = 36

**Number of weights between second hidden layer and output layer:**

Number of Neurons in the hidden layer x Number of Neurons in output layer = 6 x 1 = 6

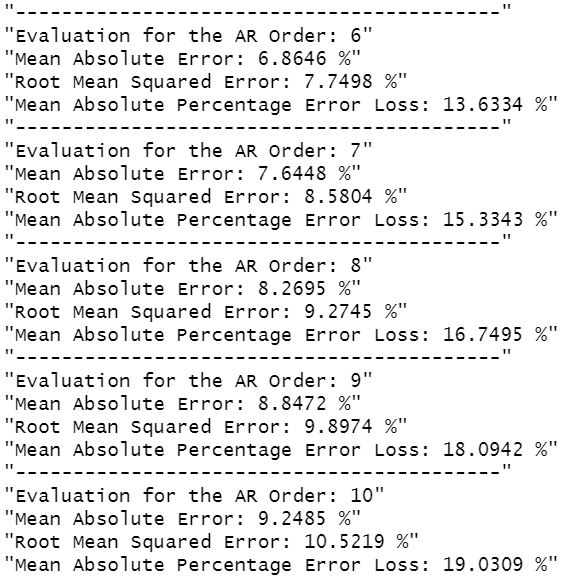
**Total Number of weight parameters = 6 + 36 + 6 = 48**

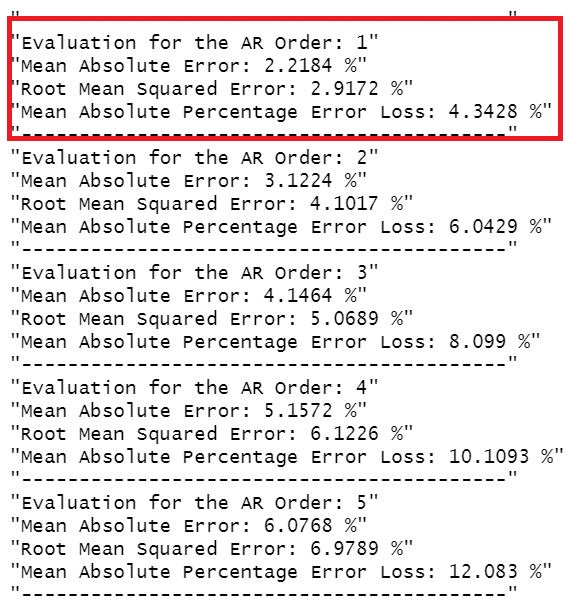
Since there is a big difference in the weight parameters between 1 hidden layer and 2 hidden layer by checking the stats of each of this model a better conclusion can be made.

**Statistics Result (Based on AR1 input vector)**

|  |  |  |
| --- | --- | --- |
| **MAE** | **RMSE** | **MAPE** |
| **2.182 %** | **2.9139 %** | **4.2749 %** |

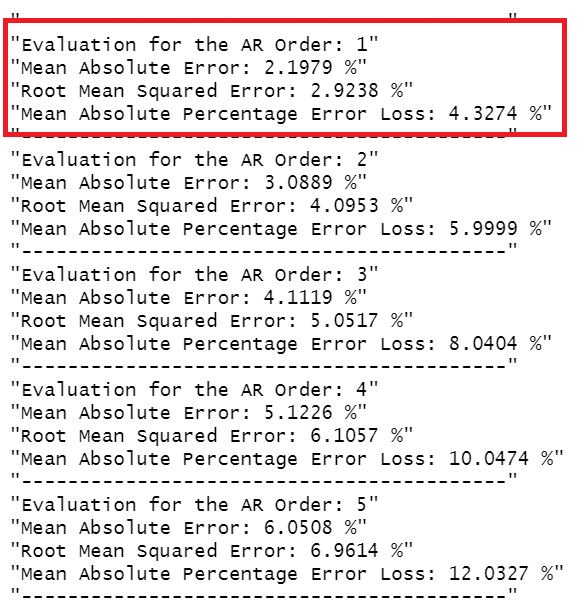
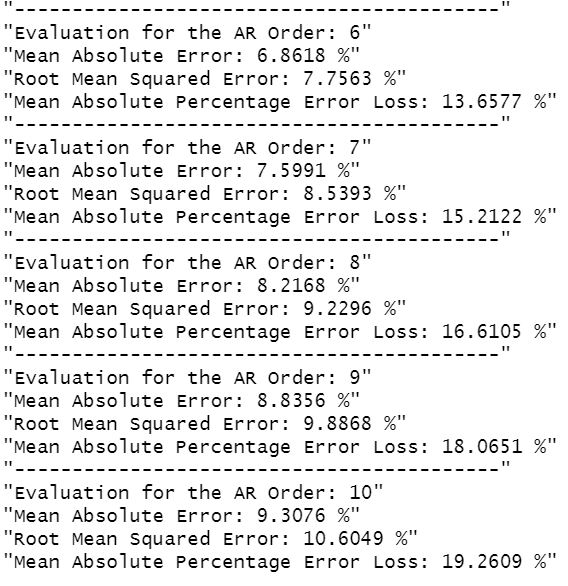
When compared both of the Statistics Result table there is only roughly 0.1 difference between the MAE, RMSE and MAPE of the single hidden layer MLP NN and 2 hidden layered MLP NN. Even though the 2 hidden layer MLP NN has a larger number of weight parameters compared to the single hidden layer, it only contributed a very small percentage to the result statistics making the 1 hidden layer MLP NN the efficient Neural Network.

1. **Discussion about the best final** MLP NN **Network by checking with the evaluation stats and with predicted VS actual result graph**

****

**~** AR order accuracy using the best 1 hidden layer MLP NN **~**

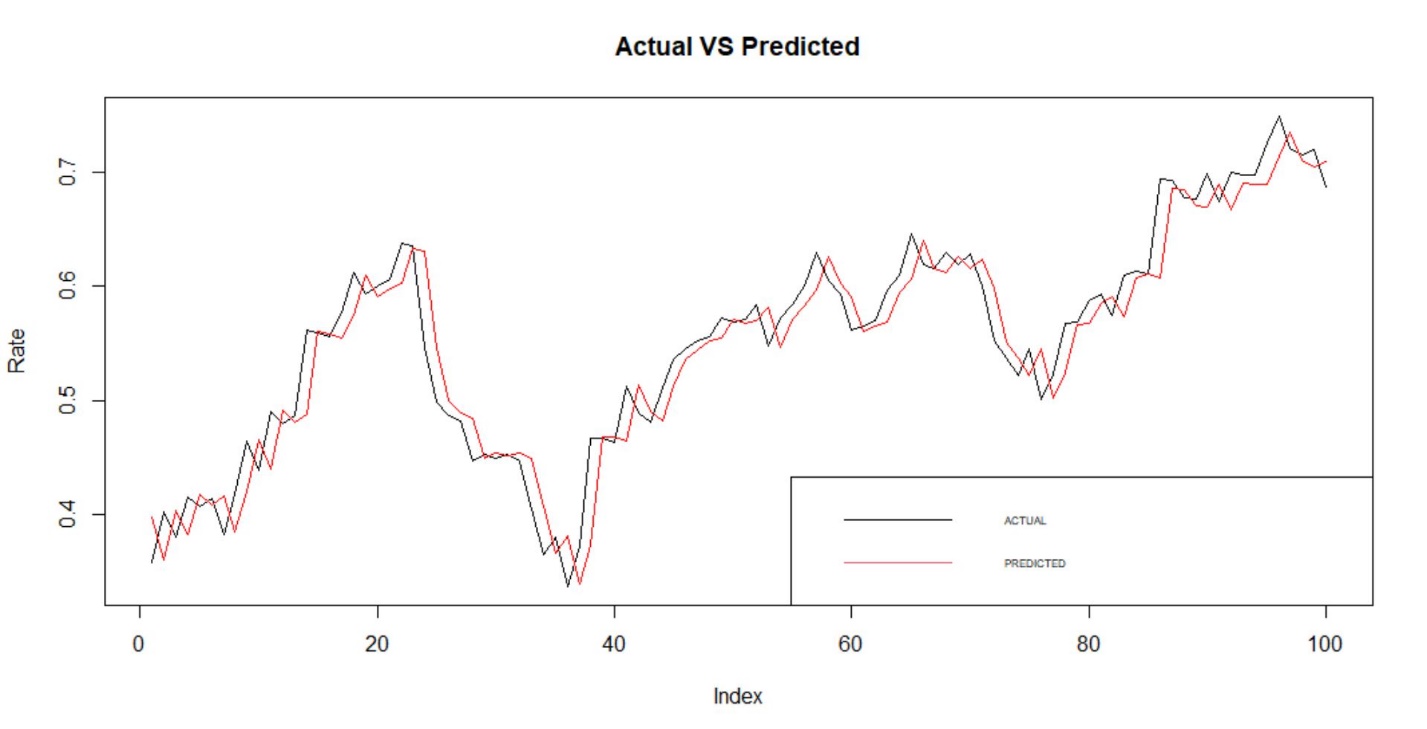
Using the BEST set of parameters for the 1 hidden layer MLP NN on input vectors varying from AR1 to AR10, we are able to see that AR1 or the 1st order of AR gives the best accuracy.

****

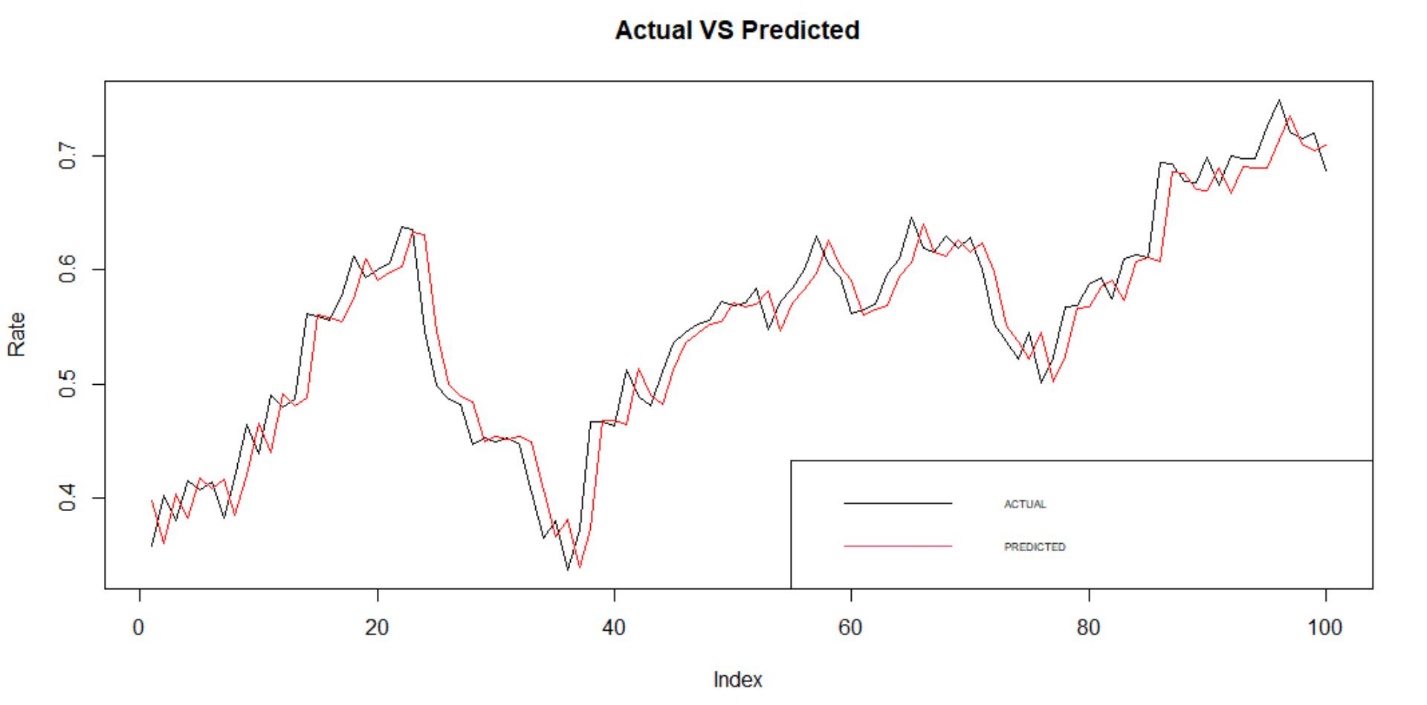
**~** AR order accuracy using the best 2 hidden layer MLP NN **~**

Using the BEST set of parameters for the 2 hidden layer MLP NN on input vectors varying from AR1 to AR10, we are able to see that AR1 or the 1st order of AR gives the best accuracy.

**Now we can come to a conclusion that AR1 is the best order, now which one out of the 2 models (neural networks) is the best to be considered is the question. Now the statistics and the graphs has to be considered in detail.**

****

*~ Prediction Output VS Desired Output for 1 hidden layer* MLP NN *~*

**

*~ Prediction Output VS Desired Output for 2 hidden layer* MLP NN *~*

**RED LINE = PREDICTED OUTPUT**

**BLACK LINE = DESIRED OUTPUT**

**Using the below performance stats we can come to a conclusion which** MLP NN **is the best.**

|  |  |  |
| --- | --- | --- |
| **MAE** | **RMSE** | **MAPE** |
| **2.1999 %** | **2.9036 %** | **4.2842 %** |

*~ Performance statistics for 1 hidden layer MLP NN~*

|  |  |  |
| --- | --- | --- |
| **MAE** | **RMSE** | **MAPE** |
| **2.182 %** | **2.9139 %** | **4.2749 %** |

*~ Performance statistics for 2 hidden layer MLP NN~*

Its very clear that there is only a very small difference in the error but however the 2 hidden layer MLP NN has a lower error rate overall when MAE and MAPE of 2 hidden layer MLP NN compared to 1 hidden layer MLP NN.

**Conclusion**

**2 HIDDEN LAYER MLP NN GAVE THE BEST ACCURACY (LOWEST ERROR) FOR THIS PROBLEM**

1. **The Code for the forecasting part problem.**

**APPENDIX**

**CODE FOR PART 01 (CLUSTERING QUESTION)**

# --------------------------------------------------

# Name: Mohammed Nazhim Kalam

# Student ID: 2019281

# UoW ID: W1761265

# --------------------------------------------------

# CLUSTERING PART

# Installing package to read Excel Data-set

install.packages("readxl") # used to read excel data files

install.packages("factoextra") # used to determine the optimal number clusters

install.packages("NbClust") # used to compute about multiple methods at once,

# in order to find the optimal number of clusters.

install.packages("factoextra") # used to plot the clusters out

# Loading the package

library(readxl)

library(knitr)

library(tidymodels)

library(janitor)

library(flexclust)

library(dplyr)

library(factoextra)

library(NbClust)

library(haven)

library(factoextra)

# Reading the data-set "vehicles.xlsx"

df = read\_excel("./vehicles.xlsx")

View(df)

# converting the class column into factors because we are not able to get its count

df = mutate(df, Class = as\_factor(df$Class))

# Displaying the types of unique classes present in the data-set

summary(df)

# Removing the Sample index column and the class column from the data-set

df.filtered = subset(df, select = -c(Samples, Class))

# Viewing the filtered data-set

View(df.filtered)

# [PRE-PROCESSING DATA] PERFORMING SCALING AND OUTLIERS REMOVAL

# Checking for any null values present in the data-set (returned 0 so no null values present)

print(sum(is.na(df.filtered)))

# Checking the Summary of the data-set (We can see the stats of the data columns eg: mean, median etc.)

df.summary = summary(df.filtered)

# Plotting a box plot graph (Box plots are useful to detect potential outliers from the data-set)

display.boxplot = function(data, column.name){

boxplot(data, ylab = column.name)

}

# calling the display.boxplot function to display the boxplot data representation for each column.

display.boxplot(df.filtered$Comp, "Comp")

display.boxplot(df.filtered$Circ, "Circ")

display.boxplot(df.filtered$D.Circ, "D.Circ")

display.boxplot(df.filtered$Rad.Ra, "Rad.Ra")

display.boxplot(df.filtered$Pr.Axis.Ra, "Pr.Axis.Ra")

display.boxplot(df.filtered$Max.L.Ra, "Max.L.Ra")

display.boxplot(df.filtered$Scat.Ra, "Scat.Ra")

display.boxplot(df.filtered$Elong, "Elong")

display.boxplot(df.filtered$Pr.Axis.Rect, "Pr.Axis.Rect")

display.boxplot(df.filtered$Max.L.Rect, "Max.L.Rect")

display.boxplot(df.filtered$Sc.Var.Maxis, "Sc.Var.Maxis")

display.boxplot(df.filtered$Sc.Var.maxis, "Sc.Var.maxis")

display.boxplot(df.filtered$Ra.Gyr, "Ra.Gyr")

display.boxplot(df.filtered$Skew.Maxis, "Skew.Maxis")

display.boxplot(df.filtered$Skew.maxis, "Skew.maxis")

display.boxplot(df.filtered$Kurt.maxis, "Kurt.maxis")

display.boxplot(df.filtered$Kurt.Maxis, "Kurt.Maxis")

display.boxplot(df.filtered$Holl.Ra, "Holl.Ra")

# REMOVING THE OUTLIERS FROM THE DATASET

# Discarding the outliers from the data-set,

# any value greater than bench.mark value will be replace with the bench mark value

remove.outliers = function(data, column.name){

# filter with box plot and trimming out from

# "maximum": Q3 + 1.5\*IQR

# "minimum": Q1 -1.5\*IQR

# where interquartile range (IQR): 25th to the 75th percentile.

# Calculating the upper and lower limit for the data

bench.mark.upper = quantile(data, 0.75) + (1.5 \* IQR(data))

bench.mark.lower = quantile(data, 0.25) - (1.5 \* IQR(data))

# Replacing the outliers with the upper and lower limits

data[data > bench.mark.upper] = bench.mark.upper

data[data < bench.mark.lower] = bench.mark.lower

# Display the box-plot after removing the outlier

display.boxplot(data, column.name)

}

# calling the remove.outliers function to remove all the outliers from each column of the data

remove.outliers(df.filtered$Comp, "Comp")

remove.outliers(df.filtered$Circ, "Circ")

remove.outliers(df.filtered$D.Circ, "D.Circ")

remove.outliers(df.filtered$Rad.Ra, "Rad.Ra")

remove.outliers(df.filtered$Pr.Axis.Ra, "Pr.Axis.Ra")

remove.outliers(df.filtered$Max.L.Ra, "Max.L.Ra")

remove.outliers(df.filtered$Scat.Ra, "Scat.Ra")

remove.outliers(df.filtered$Elong, "Elong")

remove.outliers(df.filtered$Pr.Axis.Rect, "Pr.Axis.Rect")

remove.outliers(df.filtered$Max.L.Rect, "Max.L.Rect")

remove.outliers(df.filtered$Sc.Var.Maxis, "Sc.Var.Maxis")

remove.outliers(df.filtered$Sc.Var.maxis, "Sc.Var.maxis")

remove.outliers(df.filtered$Ra.Gyr, "Ra.Gyr")

remove.outliers(df.filtered$Skew.Maxis, "Skew.Maxis")

remove.outliers(df.filtered$Skew.maxis, "Skew.maxis")

remove.outliers(df.filtered$Kurt.maxis, "Kurt.maxis")

remove.outliers(df.filtered$Kurt.Maxis, "Kurt.Maxis")

remove.outliers(df.filtered$Holl.Ra, "Holl.Ra")

# NORMALIZING THE DATASET (BRINGING ALL THE DATA INTO A SINGLE UNQIUE SCALE)

# Performing normalization using the Z-Score Standardization

df.normalized = as.data.frame(scale(df.filtered))

View(df.normalized)

# PERFORMING PCA (PRINCIPAL COMPONENT ANALYSIS) / DIMENSIONALITY REDUCTION

df.pca = prcomp(df.normalized)

summary(df.pca)

# Plotting the PCA data to find the best number of Principal Components.

# Using the elbow method of the plot below we can get the number of components which

# explain 85% or greater of the variation (BEST SET OF COMPONENTS TO TAKE)

# In this case the first 4 components are the best, because it covers the greatest

# area of the graph and has the sudden decrease after the 4th component

plot(df.pca)

plot(df.pca, type='l')

# comp.data contains the BEST PCA Component data extract

comp.data = data.frame(df.pca$x[,1:4])

View(comp.data)

# DETERMINE THE NUMBER OF CLUSTERS CENTERS (CENTROIDS) (via MANUAL and AUTOMATED TOOLS)

# AUTOMATED TOOLS TO FIND THE CENTROIDS

# USING ELBOW METHOD (Gave 4)

# The below method points out that 4 is the optimal number of centroids/clusters to be taken

fviz\_nbclust(comp.data, kmeans, method = "wss") +

geom\_vline(xintercept = 4, linetype = 2) +

labs(subtitle = "Elbow method")

# USING THE SILHOUETTE METHOD (Gave 2)

# The below method points out that 2 is the optimal number of centroids/clusters to be taken

fviz\_nbclust(comp.data, kmeans, method = "silhouette")+

labs(subtitle = "Silhouette method")

# USING GAP STATISTIC ( nboot = 50 to keep the function speedy

# recommended value: nboot= 500 for your analysis.

# Use verbose = FALSE to hide computing progression.)

# (Gave 3)

# The below method points out that 3 is the optimal number of centroids/clusters to be taken

set.seed(150)

fviz\_nbclust(comp.data, kmeans, nstart = 50, method = "gap\_stat", nboot = 50)+

labs(subtitle = "Gap statistic method")

# MANUALLY FIND THE CENTROIDS / CLUSTERS

# USING ELBOW METHOD

tot.withinss = vector(mode = "character", length = 10)

# Classification Report Function

classification\_report <- function(comparison\_table, dp = 2) {

#total counts

counts <- sum(comparison\_table)

#total sums for each column

column\_sums <- colSums(comparison\_table)

#total sums for each row

row\_sums <- rowSums(comparison\_table)

#true positive value

tp <- diag(comparison\_table)

#true negative

tn <- counts - (column\_sums + row\_sums - tp)

#false positive

fp <- row\_sums - tp

#false negative

fn <- column\_sums - tp

#precision

pr <- tp / (tp + fp)

#recall

re <- tp / (tp + fn)

#accuracy

ac <- sum(tp) / counts

# Displaying the Accuracy, Precision and Recall values

print("---------------------")

print("Accuracy")

print(ac)

print("---------------------")

print("Precision")

print(pr)

print("---------------------")

print("Recall")

print(re)

}

# Looping from 1 to the max optimal cluster to find its evaluation result

for (i in 1:10){

cat("<=============== ", "Custer ", i, " ===============>\n", sep = "")

set.seed(50)

# Performing Kmeans clustering

vehicleCluster = kmeans(comp.data, centers = i, nstart = 20)

# This is the confusion matrix

cm = as.matrix(table(Actual = df$Class, Predicted = vehicleCluster$cluster))

print("Confusion Matrix")

print(cm)

# Display Classification report

classification\_report(comparison\_table = cm)

# Total within-cluster sum of squares

tot.withinss[i] = vehicleCluster$tot.withinss

}

# plot to find the best number of clusters to be taken

plot(1:10,

tot.withinss,

type="b",

pch=19,

xlab = "Number of clusters K",

ylab = "Total within-clusters sum of squares")

# from the accuracy result we can see that we got the highest accuracy result for

# 2 clusters (33%)

set.seed(100)

vehicleCluster = kmeans(comp.data, centers = 2, nstart = 20)

fviz\_cluster(vehicleCluster, data = comp.data)

# Displaying the sizes(number of observations in each cluster) of each cluster

vehicleCluster$size

# Displaying the cluster distribution

vehicleCluster$cluster

# Getting the centers (A matrix of cluster centers).

# You get a 2 by 4 matrix representing the centers of each cluster (x,y,z,z')

# (4D coordinates) due to PCA we took 4D Data

vehicleCluster$centers

View(vehicleCluster$centers)

**CODE FOR PART 02 (FORECASTING QUESTION)**

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