Version Control Systems: Diffing with Structure Thesis

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Contents

| 1 | Intr | roduction | | |
|---|---------------|------------------------------|--|--|
| | 1.1 | Overview | | |
| 2 | Background 5 | | | |
| | 2.1 | Sum of Products | | |
| | 2.2 | Building our Universe | | |
| 3 | Typ | pe-directed diff | | |
| | 3.1 | Spine | | |
| | 3.2 | Alignment | | |
| | 3.3 | Atoms | | |
| | 3.4 | Recursive alignments | | |
| | 3.5 | Putting everything together | | |
| | 3.6 | Applying Patches | | |
| | 3.7 | Disjointedness | | |
| | 3.8 | Clojure | | |
| 4 | Heuristics 29 | | | |
| | 4.1 | Basic Oracles | | |
| | | 4.1.1 NoOracle | | |
| | | 4.1.2 NoDupBranches | | |
| | 4.2 | Oracle composition | | |
| | 4.3 | DiffOracle | | |
| | | 4.3.1 Shortcomings | | |
| | | 4.3.2 Further Shortcomings | | |
| | 4.4 | Cost | | |
| | 4.5 | Bounded Search | | |
| | 4.6 | Visualization | | |
| 5 | Ext | perimentation 45 | | |
| | 5.1 | Domain specific improvements | | |
| | 5.2 | Results | | |
| 6 | Cor | aclusion 48 | | |
| - | 6.1 | Related Work | | |
| | _ | Future Work | | |

1 Introduction

Version control systems (VCS) have been steadily becoming an ubiquitous and central tool in programming. Many big projects, with hundreds of collaborators, fundamentally rely on these kind of tools to enable different users to interact with one another and to keep a structured log of the units of change. At the heart of most modern VCS is the Unix diffutility. This tool computes a line-by-line difference between two files of text, determining the smallest set of insertions or deletions of lines that transform one file into the other. This sequence of transformations produced by diffis called an edit script. When two collaborators have modified the same source file in independent ways and the VCS wants to reconcile the two independent changes into a single one it will attempt to produce a single edit script that encompasses both changes, this is commonly referred to as a merge. This operation is clearly not always possible: if two collaborators have modified the same line the two resulting edit scripts will "overlap", it is not clear which one of the two modifications should be picked. The algorithm used to calculate these merges in most VCS is diff3, which works by calculating the two edit-scripts with diff, and attempting to merge them.

In general not all merges can be performed automatically; some conflicts will always require a manual intervention: when two people change the same thing in two different ways there is no general way of deciding which should be the resulting transformation; however the diff tool makes a big assumption in considering lines to be the basic units in which change is observable.

The shortcomings of the approach in *diff* 3 can be seen in this simple example. Suppose we have the following function in any lisp-like language:

```
(defn head [1]
  (first 1))
```

Suppose we make two independent modifications, the first of which adds a default parameter to be returned in case the list is empty, and the second one that changes the name of the function from head to fst.

```
(defn head [1, d]
  (if (nil? 1)
      (d)
      (first 1)))
(defn fst [1]
  (first 1))
```

When attempting to reconcile these two changes with the diff 3 algorithm we will run into problems; despite the two patches are modifying disjoint pieces of the actual code, the result will be a conflict. The reason is that both changes occur on the same line; this is a nuisance as manual intervention is required to solve the conflicts. Furthermore it also introduces some level of non-determinism, as the presence of conflicts may depend on things like indentation instead of being a fundamental property of the transformation.

The core idea that will be explored in this thesis is to design an alternative to *diff* which offers a finer grained control over the units of change. By attempting to extend the *diff* algorithm to operate on an AST that represents the parsed program, we are able to focus on smaller units of change; this allows us to produce more accurate patches.

The drawback of this approach is that it lifts the problem from one on strings to one on trees – computing a patch between two elements suddenly becomes computationally more expensive. Approaches similar to this one have already been explored in previous literature [5, 4, 24]. In these papers, the problem of computing the difference between two trees was always reduced to the problem of computing the difference of a flattened representation of the tree. While the flattened representation makes the problem of computing a difference easier, it makes reconstructing a valid tree from the representation more complex, and patches are more likely to generate ill-structured data. The novelty in the work of Dagand, Miraldo and Swierstra [6] lies in the idea of enforcing a structure-preserving, type-directed approach. On one hand structural information is directly encoded in the patches, so that applying a patch will always produce well-formed tree. On the other hand, the type information encoded in the grammar of the AST is exploited in the creation of a patch, making the process potentially more efficient.

The paper introduces a theoretical and practical framework to define and compute patches between structured data. This framework is generic and makes extensive use of dependent types in order to guarantee structure preserving transformations.

The main contributions of this thesis are the following

- Porting the algorithm presented by Miraldo et al. from Agda to Haskell. This requires some non-trivial setup as we need to replicate the more advanced type-level features that are present in Agda.
- The authors define a non-deterministic specification of the algorithm to compute all possible patches between two ASTs, this implies the solution space is still too large when dealing with data collected from

bigger projects. We present different heuristics which can be combined to prune the search space and make the problem tractable.

- Mining data from real-world Clojure repositories. This consists of picking suitable repositories to be investigated and devising techniques to extract real-world conflicts from their history branches.
- Finally, we want to measure the performance of our type-directed structured-diff against the standard diff. Competing against diff in terms of speed is definitely unfeasible as diff has linear complexity, in contrast to the exponential behavior of our implementation. However, we want to investigate if the quality of patches produced by our algorithm is better than the ones produced by diff. For this reason we will measure performance in terms of the conflicts that may arise when applying two patches with the same origin one after the other; intuitively more accurate patches should lead to a smaller chance of conflicts in this kind of scenario.

1.1 Overview

The chapters are structured as following: We start by showing a full Haskell implementation of the algorithm presented by Miraldo et al. [6], which is presented in Agda in the original paper. The original algorithm is implemented generically and described through dependent types in the paper; one of the main contributions of this thesis is to provide a Haskell implementation, instantiated for the Clojure language, that is suitable to run experiments on real-world data. Haskell is scheduled to land full support for dependent types in the next couple of years [9], in the meanwhile, they can only be partially supported and require some additional effort to encode. Both Generics and Dependent Types require some language extensions and machinery which are non-trivial in Haskell.

The following section starts with an introduction to dependent types in Haskell as they will be crucial in encoding the structure we want to express in our data types and their transformations. Essentially we want to characterize patches by the transformation they operate on the source code (e.g. the patch that adds an extra argument to a function) as such, we need dependent types to reflect onto the type system the action of a patch on a certain value. This will assure that any code produced by the algorithm is structurally valid by construction.

Following dependent types we will need to introduce sums of products: these give us a general way to view types and will allow us to define an algorithm that is independent of the representation of the AST for the language we are treating. In this regard there is a fine balance between having a core algorithm which is generic and can be applied to any language, and the use of domain-specific strategies to guide the generation of patches by using knowledge specific to the language in question. Despite the generality of the algorithm, we have instantiated it for the Clojure programming language [8]; this choice is motivated by the general simplicity of parsing languages that derive from LISP and by the need to select a language that is popular enough to have large active projects, available on Github, that will provide us a good sample of data to test.

After presenting the algorithm for a type-directed diff, alongside its Haskell implementation, we will analyze the performance of the non-deterministic specification and conclude that it is still to slow for real-world data. To solve this problem we will introduce different heuristics to guide the process of patch generation and analyze their performance and shortcomings. Finally we will introduce the notion of *disjointedness*, a predicate that attempts to capture the intuition that two patches that are not "overlapping" should be mergeable. We will use this predicate to run experiments on conflicts gathered from public repositories on Github and compare the amount of merge conflicts obtained by our approach compared to *diff* 3.

2 Background

With time, Haskell's type system has kept evolving from its Hindley-Miller origins and through the use of different language extensions it has gained the ability to express more complex types. In particular, many efforts have gone to add support for dependently typed programming in the latest years. A dependent type is a type whose definition depends on a value. For example, a list of Int is a standard type, but a list of Int of a fixed length n is a dependent type, as the static type depends on the dynamic information about how many elements are actually in the list.

One major stepping stone in this direction is the DataKinds [3] extension which duplicates an ordinary data type, such as

```
data Nat = Z | S Nat
```

at the kind level; this means that from this declaration we automatically get two new types, namely Z of kind Nat and S of kind Nat -> Nat.

We can use the Nat kind to index generalized algebraic data types (GADTs) in a way that allows us to create an analogue of a dependent

type. In the case of Nat, we can use it to define a GADT for vectors of a given length.

```
data Vec :: * -> Nat -> * where
    Vn :: Vec x Z
    Vc :: x -> Vec x n -> Vec x (S n)
```

Such a vector is either the empty vector, of type $\mathbf{vec} \times \mathbf{Z}$, or a vector which is built by adding an element of type \mathbf{x} in front of a vector of \mathbf{xs} of length \mathbf{n} , yielding a vector of \mathbf{xs} of length \mathbf{S} \mathbf{n} .

This allows us to define safer alternatives to some of the functions which operate on lists. The infamous **head** function will crash our program when passed an empty list; equipped with **Vec**, we can rule this out by construction.

This is how we can define a **head** function on vectors.

```
head :: Vec x (S n) \rightarrow x head (Vc h t) = h
```

Informally, we are saying that the **head** function takes as argument a vector with length strictly greater than 0. In this way, if we try to pass an empty vector to **head** we will get a compile time error instead of the usual run time one.

Another extension which plays a crucial role in dependent types is Type-Families: informally it allows us to write functions which operate on types, we will use this to define concatenation between Vecs.

The following type family can be seen as a function that takes two types of kind Nat and returns another type of kind Nat representing the result of adding those two types.

```
type family (m :: Nat) :+ (n :: Nat) :: Nat where Z :+ n = n (S m) :+ n = S (m :+ n)
```

Equipped with this type family we can now define concatenation between vectors.

```
vappend :: Vec x n \rightarrow Vec x m \rightarrow Vec x (n :+ m)
vappend Vn ys = ys
vappend (x `Vc` xs) ys = x `Vc` (vappend xs ys)
```

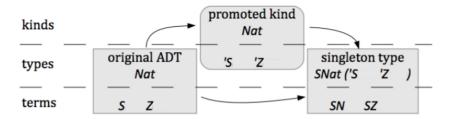
One interesting thing to note is that up to this point, we never use the Nat part of a vector at run time. That information is only used at compile time to check that everything "lines up" the way it should be, but it could actually be erased at run time.

Suppose we want to write a split function; this function takes an n of kind Nat, a vector of length n: + m and splits it into a pair of vectors, with respectively n and m elements.

The first problem is that we can not pass something of kind Nat to our split function, in fact the types Z and S have no inhabitants, so we can not construct any term of those types. Furthermore, we want to express that this n of kind Nat that we pass as a first argument, is the same n as in the vector length. The idea is to wrap this type into a singleton data type, giving us a dynamic container of the static information.

The name singleton comes from the fact that each type level value of kind Nat (namely Z or S applied to another type of kind Nat) has a single representative in the SNat type.

To sum things up: DataKinds extension promotes members of the type Nat to inhabitants of the kind Nat. Singletons allow us to take one step back in this ladder, associating to every thing of kind Nat a term from the singleton type SNat. The following picture, borrowed from Eisenberg et al. [2], gives a good representation of this process.



We can think of the DataKinds extension as a way of embedding dynamic information into the static fragment of the language. Singletons, on the other hand, are a way to reflect this static information back to the dynamic level, and make run-time decisions based on the types we obtain.

Singletons solve the two problems outlined above: they have kind * and

contain a Nat that we can later refer to in the function type. We can now define split as follows:

With these three tricks up our sleeve (data kind promotion, type level functions and singletons) we can emulate some of the features that are present in dependently typed languages such as Agda. These features allow us to emulate explicit dependent quantification. We can actually go even further in Haskell: Lindley et McBride [1] show us how to emulate implicit types via type classes and ultimately how all kinds of quantification, modulo some boilerplate, are possible in Haskell.

2.1 Sum of Products

The basic idea of the Sum of Products (SOP) approach is to define a "normal form" for all generic representations of data types and to define generic functions by induction on this form. It is, in some sense, similar to the Disjunctive Normal Form for propositional logic in the sense that every proposition can be expressed in DNF and we can write theorems (functions) which assume the expression is represented in DNF. The bulk idea is to view each type as a choice between a constructor and all the arguments that are passed to that constructor. It is useful to think about the two different levels: on the first level we make a choice about which constructor to pick; this corresponds to a sum over all the constructors of the type. On the second level, we are choosing a certain number of arguments to feed to that constructor and this can be viewed as a list, or product, of those arguments. Clearly the products will depend on the choice of constructor, each of which could take a different number of arguments of possibly different types. This motivates the need to represent the product as some sort of heterogeneous list. A constructor can also take no arguments, in which case we can simply use an empty list to represent that, but can also take an argument of the same type it is trying to construct (like the S constructor from the previous section). In this case, the recursive argument can itself be encoded as an SOP and the same encoding can be used all the way down to the leaves.

Since every data type can be encoded as an SOP, we can write functions that act on this representation. For each data type we can first convert it to the SOP representation and then pass it to the desired function. Since the SOP representation is isomorphic to the original type, we can eventually reconstruct the desired term after we are done working with the representation. This encoding is presented by Loh et al. [7] and represents one of the numerous different ways to approach generic programming in Haskell. In the remainder of this section we will try to formalize the intuition presented above by building the SOP representation of a data type.

2.2 Building our Universe

An AST consists of a family of data types, with a main one which represents the outer structure of the language, and a number of other possibly mutually recursive data types appearing as arguments to the constructors of the main data type. We can define a very simple language which consists of only one data type, IntTree which is isomorphic to binary trees of integers. This choice is just for ease of presentation, the following construction can be applied to a family of mutually recursive data types.

```
data IntTree = Node IntTree | Leaf Int
```

For each type that appears as an argument to a constructor in our family of data types, we will construct an atom representing that type. Following the example above, we will define

```
data U = KInt | KIntTree
```

Now, we can group all the constructors appearing in our original data types under the **Constr** type in a similar way as we did for the atoms.

```
data Constr :: * where
  CNode :: Constr
  CLeaf :: Constr
```

We have now deconstructed our original data type into two levels: Constructorsponding to the level of sums (the constructor) and U corresponding to the level of products (the atoms).

Since we had to define two additional data types that have no relation between each other we need a way to tie them together on the type level. To achieve this, we define the ConstrFor data type, which can be viewed as a proof that a certain constructor builds element of a certain family. In general an AST consists of a family of possibly recursive data types, hence we will need the additional information about what family the constructor Constr belongs to.

```
data ConstrFor :: U -> Constr -> * where
  NodeProof :: ConstrFor KIntTree CNode
  LeafProof :: ConstrFor KIntTree CLeaf
```

Finally we must encode one last bit of information: the "shape" of each constructor. To do so, we can use a closed type family which can be viewed as a function on types. This function takes a **Constr** and returns a list of atoms representing the arguments the constructor accepts.

```
type family TypeOf (c :: Constr) :: [U] where
  TypeOf CNode = '[KIntTree, KIntTree]
  TypeOf CLeaf = '[KInt]
```

We will also need to associate each atom with a singleton, which will allow us to relate terms of our language to their type level representation.

```
data Usingl :: U -> * where
  UInt :: Int -> Usingl KInt
  UIntTree :: IntTree -> Usingl KIntTree
```

Since TypeOf returns something of kind [U] we will define another GADT named All, that maps a type constructor k -> * over an argument of kind [k] giving us something of kind * to quantify over a list of singletons.

The definition for All is straightforward:

```
data All (k \rightarrow *) :: [k] \rightarrow * where An :: All p '[] Ac :: p \times -> All p xs \rightarrow -> All p xs \rightarrow -> All p
```

With this setup we can finally construct the View data type; this loosely corresponds to a generic view as sum of products of a data-type, and simply deconstructs each term of a type into a constructor and a list of arguments applied to that constructor

```
data View u where
  Tag :: ConstrFor u c -> All Usingl (TypeOf c) -> View u
```

An element of type View u represents an element of type u deconstructed into its SOP view; the first argument records the choice of the constructor for that datatype and the second is the heterogeneous list of arguments that are required to build that constructor, note that we are dependently relating the shape of the product to the actual choice of constructor (the c).

Finally, we want to define a pair of functions that allow us to move from an **Usingl** to a **View** and from that, back to the singleton representation.

The **view** function, defined only for the recursive elements of the language can be implemented as follows.

We parametrize this function by the IsRecEl constraint, as atomic elements can not be deconstructed into a pair of constructor and arguments.

The same holds for the inverse function inj: it will take as arguments the constructor, the list of arguments for that constructor and produce the corresponding Usingl.

In the next section we will show the implementation of the type-directed diff. Our functions will operate on the concrete type <code>Usingl</code> u which we have shown how to instantiate. It is worth noting that to achieve full-generality we could represent <code>Usingl</code> as a type-class instead of a concrete type. This would allow us to keep the implementation of the algorithm generally extensible as to new data-types other that the ones we mention it would suffice to give their <code>Usingl</code> instance. Techniques for lifting the concrete singleton data-type to a type-class are well-known and they were first showed by Eisenberg et al. [2]. Since investigating the performance across different languages was never in the scope of this thesis, the code and the presentation are tied to the concrete <code>Usingl</code> u data-type.

3 Type-directed diff

The approach presented by Miraldo, Swierstra and Dagand [6] takes advantage of the structure encoded in types to define a generic type-directed diff

algorithm between typed trees. The inspiration comes from the diff utility present in Unix; it is at the heart of the current methodologies employed by VCS to attempt to compute a patch between two different versions of the same file. The limitations of the diff algorithm, as it currently stands, is that it does not employ any structural information about the data on which it is trying to calculate a patch.

The underlying idea to the approach presented in the article is to employ the generic SOP view presented to obtain a view of any well defined program as a structured tree of data. We then try to compute a transformation, from one tree to the other, that respects the structural information we acquired.

In the process of transforming one tree into another we need to keep track of three different things:

- Transformations between constructors These are transformation between internal nodes of the trees.
- Transformations on the product level When transforming an internal node to another, we might end up in the situation where the nodes have a different number of children. We somehow have to align the children of the source node with the destination.
- Transformation between atoms The atoms can be either other internal nodes, in which case we recurse down the tree, or leaves in which case we record the pair of source and target leaf.

We will use the simple binary tree language presented in previous sections as a working example to show the construction of a patch. The transformation we will walk through is the following: given the following AST:

```
t1 = Node (Leaf 1) (Node (Leaf 1) (Leaf 1))
```

we want to characterize the patch that transforms it to

```
t2 = Node (Leaf 1) (Node (Leaf 2))
```

The first structure we will employ is the *spine*, this can be thought of as a common skeleton between the two trees which captures the parts that do not change under the transformation.

3.1 Spine

We will define Spines only between two elements of the same sum-type, and defer to later the discussion on how to perform transformation between elements of different sum-types. Calculating a spine for two elements of the same sum-type loosely corresponds to calculating the longest common prefix between two strings. Recall that the two elements x and y are viewed as SOP, in this sense calculating the spine between x and y corresponds to capturing the common co-product structure between them. Let x and y be two such elements, we will have three cases to consider.

- \bullet x = y
- \bullet x and y have the same constructor on the sum level but differ in the arguments
- \bullet x and y have different constructors

This gives rise to the following three different constructors for the Spine GADT, each corresponding to one of the cases described above.

If the two elements are the same, the spine is a copy. If the top level constructors match, the spine consists of this information and a function to transform the constructor fields pairwise. Lastly, if two constructors don't match, the spine must record this and also contain a function to transform the list of source fields into the list of destination fields.

The Scp constructor corresponds to the first case, in which we need to record no additional information other than the fact that the two elements are equal. Before looking at the other two constructors, let us focus our attention for a moment to the three arguments that a spine takes: the third parameter of the spine (the U) represents the underlying type for which we are trying to compute a patch, the sum-type to which x and y both belong. The other two, al and at are respectively a function between products that describes what to do with the different constructor fields and a function between atoms which describes what to do with the paired fields in case we have the same constructor. These functions are needed for the remaining constructors: the Scns constructor corresponds to the case where the constructor is left untouched but some of the arguments have changed. For this

reason its second argument consists of the predicate at applied to the list of arguments which describes how to transform them.

Finally, Schg represents a change of constructor on the sum level: the first two arguments record the source and destination constructors, the third argument is the all function applied to the constructor fields of the source and destination constructor respectively.

Let's not worry about the al and at parameters for the time being, these will later be used to close the recursive knot and generate the full patch by interleaving the construction showed here and in the following sections. For now we can simply observe that if we were to calculate a spine between the two programs introduced above we would proceed by constructing their view as presented in 2.1 obtaining the following

```
v1 = Tag NodeProof (UIntTree (Leaf 1) `Ac` UIntTree (Node

→ (Leaf 1) (Leaf 1)))

v2 = Tag NodeProof (UIntTree (Leaf 1) `Ac` UIntTree (Leaf 2))
```

These views are not completely equal, but their first argument is. This represents the outer choice of constructor and we are after all ultimately transforming an Node into another one. The spine produced by these two views will then start with an Scns recording the fact that the outer constructor has stayed the same but there are some changes in its arguments.

```
spine = Scns NodeProof _
```

We ignored the second argument up to this point (representing it as an underscore); let's turn our attention to that now: since we know that the constructor is unchanged in the transformation, we also know that both for the source and destination tree, the number and types of its arguments will be the same. For this reason we can simply pair up the corresponding arguments and calculate the diff between every pair. The second argument to Scns can be read as: the function at applied to a list of pairs of elements of the same type. The type of each pair is specified by TypeOf s, which in our working example is equal to [KIntTree, KIntTree]. Essentially we have a list of **UIntTree** pairs and are left with the problem of calculating patches between the elements contained in each pair. We can easily see that the first pair of our example will give rise to an Scp, the two sub-trees are in fact the same and we can simply copy the information along the transformation. The second pair is more interesting though: this is the case where we have a change on the constructor level and the spine we produce will be the following

Schg NodeProof LeafProof _

However the remaining argument to fill is not as simple as the Scns case since Node and Leaf expect completely different arguments. In the case where the constructor had remained the same, we could pair up the arguments and proceed from there; however, when the external constructor has changed, there is no obvious way of pairing up the arguments. Indeed they might be completely in different numbers and types, which motivates the following definition of alignments.

3.2 Alignment

The spine takes care of matching the constructors of two trees, alignments handle the products packed within the constructors. Recall that this alignment has to work between two heterogeneous lists corresponding to the fields associated with two distinct constructors. The approach presented below is inspired by the existing algorithms based on the edit distance between two strings. The problem of finding an alignment of two lists of constructor fields can be viewed as the problem of finding an edit script between them. An edit script is simply a sequence of operations which describes how to change the source list into the destination. In the case of diff the source and destination lists are the lists of lines in the source and destination files; in our context the source and destination lists are the products of fields of the source and destination constructors respectively. To compute an edit script we simply traverse the lists, from left to right, considering one element from each list. At each step we are presented with three choices:

- We can match the two elements (Amod) of the list and continue recursively aligning the rest
- We can insert the destination element before the current element in the source list (Ains) and recursively compute an alignment between whatever we have in the source list and the tail of the destination.
- We can delete the element from the source list (Adel) and recursively compute the alignment between the rest of the source and the destination.

The following GADT models the sequence of operations that represent an alignment.

```
data AL (at :: U -> *) :: [U] -> [U] -> * where
  AO :: Al at '[] '[]
Ains :: Usingl u -> AL at xs ys -> AL at xs (u : ys)
Adel :: Usingl u -> AL at xs ys -> AL at (u : xs) ys
Amod :: at u -> AL at xs ys -> AL at (u : xs) (u : ys)
```

AL is parametrised by the same type-level function introduced in the spine. AO represents the empty alignment, Ains and Adel take as first argument a singleton representing the element being inserted or deleted. These two, together with an alignment for the rest of the list, give us the alignment with an insertion (resp. deletion) as explained in the section above. In the Amod case the first argument is the predicate on the underlying atom that describes how to transform it and the second one, as for the case of insertions and deletions, represents an alignment between the rest of the lists.

One key difference to keep in mind, between the edit scripts produced by diff and the alignments is the atomicity of the elements being aligned (lines and sub-trees respectively). In the case of strings we can assume deletions and insertions to be somewhat equivalent in cost thus we can safely try to minimize one of the two. However, in our case, the elements we are inserting or deleting are sub-trees of arbitrary size, therefore it is not obvious if we should try and prune insertions or deletions.

This poses the problem that when enumerating alignments we have no guiding heuristic to cut the number of solutions, for the time being we will simply ignore the problem and resort to enumerate all possible alignments, to not skew the algorithm into preferring insertions over deletions or viceversa.

Let's walk through calculating the alignment for our running example: we have to produce an alignment between [KSExpr, KSExpr] and [Kint] (recall that these are the shapes of the Node and Leaf constructors). Because of the way we define the Amod constructor, more precisely because of the at function that describes how to transform an atom into the other, we restrict ourselves to only attempt an Amod between two singletons of the same underlying type.

This means that in a case like this one, we will only be able to transform one list into the other by repeated applications of Ains or Adel. It is worth noticing that this restriction is not mandatory and we could in principle allow these transformations as well, the choice here is purely pragmatical and the underlying reason is, this will be a recurring theme, to reduce the sheer amount of combinations that must be checked. What we are left with are the three possible alignments that can be formed by inserting the Uint

and deleting the two **UIntTrees**, we will generate all of them.

3.3 Atoms

Having figured out all the alignments between two lists of constructor fields, we still have to decide what to do in the case where we match two elements. We need to make a distinction between the possibly recursive fields and the constant ones. In the case of constant fields like Ints or Strings, a transformation between two values of this type consists of a pair recording the source value and the destination value. In the case of a recursive datatype we are essentially left with the problem we started from: transforming a value of a data type into another. To do so, we simply start all over again, recursively computing a spine and an alignment between constructor fields.

To represent pairs of constant atoms we introduce a helper Diagonal datatype which lifts f over a pair of xs.

```
newtype Diagonal (f :: k -> *) (x :: k)
= Diagonal { unDiag :: (f x , f x) }
```

To distinguish between recursive and non recursive elements of the language we define a typeclass with no additional methods, and add instances of this typeclass only for the recursive atoms.

Once again, borrowing the language definition from the previous section, we will have the following class and instances defined

```
class IsRecEl (u :: U) where
instance IsRecEl KSExpr where
```

With this we can define the following datatype to represent diffs between atoms of our language.

```
data At (recP :: U -> *) :: U -> * where
  Ai :: (IsRecEl u) => recP u -> At recP u
  As :: Diagonal Usingl u -> At recP u
```

Here the At datatype is parametrised by a predicate that describes how to transform the recursive atoms. The first constructor, Ai, which represents the recursive case is parametrised by this predicate, the constraint is added to ensure by construction that when we build an Ai we can only do so for the elements of the language that actually are recursive. The other case is covered by the As constructor, recall that in this case Diagonal simply lifts

Using l to a pair of elements of type l, so the first parameter can be read as: a pair of Using l l.

In our example we have already seen the case for Ai, the atoms paired by the first spine were all Kexprs which we recursively calculated spines on. The As will be produced when we match two Leafs that contain different integers, in that case we produce a pair of Usingl Kint that record the transformation from one Int to the other.

3.4 Recursive alignments

Starting by computing the spine is not necessarily the optimal choice, this can be seen from the following simple example between lists:

```
[1, 2, 3, 4] \rightarrow [2, 3, 4]
```

Clearly the optimal patch will proceed to delete the first element and then copy over any remaining one. Our definition, however, does not allow for such deletions. Deletions (resp. insertions) are only handled by alignments. To handle such cases we can extend our spines and alignments with the datatype Almu that allows insertions or deletions to happen on the sum level.

A match of constructors will be represented as a spine while insertions and deletions will record the constructor being inserted (resp. deleted) and a Ctx which records which fields are associated to that constructor. Ctxs are inspeired by Huet zippers [10]: they can be thought as a representation of a type with a hole somewhere; the hole represents the place where we plug in the rest of the tree to continue the computation.

```
data Ctx (r :: U -> *) :: [U] -> * where

Here :: (IsRecEl u) => r u -> All Usingl l -> Ctx r (u : l)

There :: Usingl u -> Ctx r l -> Ctx r (u : l)
```

The Here constructor represents the hole, or the recursive position in which we want to carry on the computation. With this definition of contexts, we can finally define Almu $u\ v$, the datatype that represents structured patches between u and v

```
data Almu :: U -> U -> * where
   Alspn :: Spine (At AlmuH) (AL (At AlmuH)) u -> Almu u u
Alins :: ConstrFor v s -> Ctx (AtmuPos u) (TypeOf s) -> Almu u v
Aldel :: ConstrFor u s -> Ctx (AtmuNeg v) (TypeOf s) -> Almu u v
```

The AlmuH, AtmuPos and AtmuNeg are wrappers around Almu s to make source and destination types line up correctly. This gives rise to another occasion for non-determinism, as Almu has the same shortcomings of AL meaning that we have no obvious choice of what operation should be maximized over the others. As for alignments we decide to proceed non-deterministically and compute every possibly choice.

3.5 Putting everything together

Now that we have defined all the types we need to represent our patches we are ready to define a function that given two $\tt Usingl u$ and $\tt Usingl v$ produces an $\tt Almu u v - a$ patch that describes how to transform an $\tt u$ into a $\tt v$. We can write this function from the "bottom up", starting from the atoms and working our way up through spines and recursive alignments. Notice how all these functions return a list of results, as non-determinism comes into play at every step. The signatures have been slightly simplified from the actual implementation where, for example, the result is parametrised by a monad, making it more general.

We will only present the signatures of the functions in this section as it allows us to simplify some details of the implementation. The bodies of each function will be replaced by a short description which, given the types introduced up to this point and the supplied signature, will hopefully make it easy to fill in the gaps. The diff function for atoms should have the following signature

This function is parametrised by a function that describes the treatment for recursive atoms. By inspecting the first singleton we learn whether the atom is recursive or not; if that is the case, the function that deals with the recursive elements can be used to build the corresponding At. In the other case, when the element is non recursive, we can simply pair up the two constant atoms with a Diagonal and build the non-recursive At.

We need to define a function that given a pair of singletons produces all the spines between those two singletons. Remember that spines are parametrised by the alignment that handles the product structure, for this reason we will end up with as many spines as the number of valid alignments. Recall that in a Spine al at u, al and at are respectively two functions that respectively describe how to handle the paired atoms in case the external constructor hasn't changed (Scns), and how to handle the products in the case where the external constructor has changed (Schg). These parameters are of kind at :: $U \rightarrow *$ and al :: $[U] \rightarrow [U] \rightarrow *$. In the most simple case we can imagine that the treatment of atoms and products consists of simply pairing them up. We can define "trivial" alignments for atoms and products which simply consist of this pairing up. For atoms we can reuse the <code>Diagonal</code> type we introduced earlier, for products we need to define a custom <code>Pair</code> type.

```
type TrivialA = Diagonal Usingl
data TrivialP :: [U] -> [U] -> * where
Pair :: All Usingl 1 -> All Usingl r -> TrivialP 1 r
```

We compute the diff in two steps: first we produce a single spine parametrised by the trivial alignments, then we will map over this spine with our diffAt, and another function to generate all the alignments to obtain all of the different spines. We can start by defining the function that computes the trivial spine.

Here zipP is a function that simply zips the two lists together by constructing a Diagonal for each pair. In the Scns branch, we use the Pair constructor to record the two lists of arguments. Recall an AL at s d is also parametrised by a function that describes how to handle the atoms. We can start by defining the trivial alignment that uses TrivialA to simply pair up elements with Diagonal, as for the spine, we will then map over this trivial alignment with a function that takes the pair of recorded elements and produces all patches between them, thus closing our recursive loop.

The implementation is straight forward as we simply non-deterministically explore all the possible choices, the only exception being that we choose to pair-up two elements only if the testEquality test succeeds. Finally we can define diffs. The definitions of mapAlM and mapSpineM are omitted, these combinators are used to map the recursive functions over their trivial counterparts.

We finally have to define a function that computes the diff in terms of Almus. This will call diffS in case of two matching constructors from which we can compute the spine wrapping that with the corresponding Alspn constructor. In the other cases it will attempt the insertion (resp. deletion) at the constructor level by recording the constructor being inserted (deleted) and producing a Ctx which describes where the original tree is attached in respect to the added (deleted) constructor.

This function will have the following signature

```
diffAlmu :: (IsRecEl u, IsRecEl v) => Usingl u -> Usingl v -> [Almu u v]
```

As is the case for the alignment between products, here we will simply proceed by enumerating all possible recursive alignments, attempting at each

level the alignment of spines, insertions and deletions. One shortcoming of this approach lies in the great combinatorial explosion of possibilities that arises in computing the alignments for constructors and products. We will see in the next sections what we will employ different techniques to keep this in check.

3.6 Applying Patches

Now that we have constructed these type-safe patches we can define how to apply them to an expression to produce a transformed expression.

Application will be defined between a patch of type Almu u v and a singleton Usingl u. Again, we will proceed defining our functions from the atoms all the way up to recursive alignments. As before, our functions will be parametrised by one or more functions to deal with the recursive elements.

If we are dealing with a recursive element we can apply the supplied function and proceed the recursive application with that. If the element is non-recursive, we check if it is a copy, in which we can return whatever argument we got. If it is a change instead, we will check if the argument matches the source and return the target.

Alignments will be applied to heterogeneous list of Usingl u. The function is parametrised by the previous function we defined over atoms.

```
Refl <- testEquality x k
applyAl appAt a xs</pre>
```

Applying an alignment is straightforward, the types guarantee that we can only apply lists of <code>Usingls</code> and alignments which are compatible. This is reflected by the fact that the supplied alignment has type <code>AL</code> at <code>p1 p2</code> which matches the type in <code>All Usingl p1</code> and the result produced by applyAl has type <code>All Usingl p2</code>. We step through the alignment applying each <code>AL</code> to the head of the list until we are done.

```
applyS :: IsRecEl r =>
          (forall a . at a -> Usingl a -> Maybe (Usingl a))
       -> (forall p1 p2 . al p1 p2 -> All Usingl p1
          -> Maybe (All Usingl p2))
       -> Spine at al r
       -> Usingl r
       -> Maybe (Usingl r)
applyS appAt appAL Scp x = pure x
applyS appAt appAL (Schg i j p) x = case view x of
  Tag c d -> do
    Refl <- testEquality c i</pre>
    inj j <$> appAL p d
applyS appAt appAL (Scns i p) x = case view x of
  Tag c d -> do
    Refl <- testEquality c i</pre>
    inj i <$> sAll appAt p d
```

Application for spine is parametrised by a function to apply atoms and one to apply alignments. We inspect the spine and proceed accordingly. If it is an Scp we return the argument, if it is an Schg we need to inspect the argument and convert it to the SOP view. If the constructor on the sum level matches the source constructor of the Schg then we can construct the element with the target constructor and the result of the application on the alignment. Finally, if the constructor is an Scns, we start by peeling the argument and turning it into its SOP view. If the constructors match, then we can construct the element with the old constructor plus the result of applying appAt to every pair of atoms found by pairing the product in the Scns and the view of x.

Finally, for the case of recursive elements, we can give the following implementation.

The case of Alspn amounts to simply calling the function we have defined to apply spines with the correct arguments. In case of an Alins, we still have to construct an element, it will be obtained by an injection of the inserted constructor and the context. ctxIns walks through the context collecting all the singletons and calling the application recursively when it finds the hole. In case of a deletion, we don't have to build anything. We check if the element matches the constructor we intend to delete and simply carry on if it does. ctxDel walks through the context, throwing away every singleton it finds and only calling the recursive application once it finds the corresponding hole.

3.7 Disjointedness

We can define a predicate to decide disjointedness between patches. We want to define this notion only for pair of patches that share the same source, as patches from completely different sources are incomparable to each other. The idea that we want to capture with disjointedness is that two disjoint patches should always commute; this means that we can apply them in any order to the source and always get the same result. This property is crucial in reconciling patches coming from two different branches. When trying to compute a three way merge, if we can determine that the two patches are disjoint, then we know we can pick an arbitrary order to apply them, and will not end up with a conflict.

In the case of diff3, two patches are not disjoint when they modify the same line in two different ways. If that is the case, then the two patches must not commute, as whatever patch is applied last, will overwrite the conflicting line with it's own version.

We can start by attempting to define what disjointedness is on the recursive level. Disjointedness should model the fact that two patches are acting on different parts of the source. This suggests we want to impose the condition that any patch different from the trivial one, is disjoint from itself. Following this line of though we can start by defining

When matching an Alins with anything else, we extract the focus from the context, and recursively call the disjointedness predicate on the focus and whatever the other argument is. In other words, insertions are always allowed.

When we match an Aldel with an Alspn, we will inspect the spine contained in the Alspn. If it is an Scp then the two are trivially disjoint.

If it is an Scns then they are disjoint if the recursive changes within the Scns do not change the deleted context and the focus of the context is disjoint from the corresponding changes in the Scns product.

If the spine is an **Schg** then they are not disjoint: as one patch is deleting a constructor, where the other one is trying to change it to something else.

The only case left is when we have two Alspn. In this case we have to look into the pair of spines to decide whether they are disjoint. As before, we can walk through all the cases. Scp is disjoint from any other node.

A pair of Scns is disjoint if the constructor they fix is the same, and if their fields are pairwise disjoint.

A pair of Schg is never disjoint, as the two patches are trying to modify the same constructor in two different ways. Finally, when we have an Scns and a Schg: they are disjoint if the constructor fixed by Scns is the source constructor for the Schg and if the fields of the Scns are disjoint from the alignment in Schg.

Since we learned that the constructor of the Scns and the source constructor of Schg are the same, we know that p and p' are acting on the same product of arguments. The predicate disjAtAl follows the same pattern outlined up to this point, we step through the elements of the alignment and the list of paired atoms, considering them in pairs. Insertions are always fine as long as the rest of the patches are disjoint. If we find an Adel we have to check that the patch on the field being deleted is the identity patch.

Lastly, when the alignment contains an Amod we can check if the argument of the Amod is disjoint from the field.

To do so we need to introduce a function that tells us when two atoms are disjoint, the recursive case can be dealt with a function which will be taken as the first argument to close the recursive loop. Finally, two non-recursive atoms are disjoint if either one of them is the identity (represented by a pair containing the same element).

3.8 Clojure

Having developed a general framework to compute patches between typed trees, we know want explore its performance in the context of a real programming language. To test this, we developed a parser for Clojure; the implementation of this parser can be somewhat different to one designed to interpret and run Clojure code, this is because in this context we are more concerned with capturing the syntactical structure rather than the semantical one. One further consideration is that the parser should try to capture as much syntactical information as possible, in order to produce code that strives to respect any syntactical convention embraced by the authors.

The AST will be composed by a family of data-types, with the Expr type representing the "entry point" for each parse.

```
| Cons Expr Sep SepExprList

data Term = TaggedString Tag String

data Sep = Space | Comma | NewLine | SEmpty
data FormTy = Quote | SQuote | UnQuote | DeRef
data CollType = Vec | Set | Parens
data Tag = String | Metadata | Var
```

This is enough to parse all Clojure code obtained from the test data that we collected; it can actually parse even more than legal Clojure as it does not consider the semantical correctness of the parsed code, only its syntactical coherence. The definition of SepExprList can represent lists of expressions separated by either newlines, commas or spaces, which are all legal legal and interchangeable separators in Clojure, we also have an SEmpty separator for the Nil case.

We can apply the same procedure outlined before to generate the required singletons and type families. The only difference from before is that in this case is that our language is represented by a family of mutually recursive datatypes. If you recall from section 2 we introduced ConstrFor to relate our singleton constructors to the type they were constructing. In case of a single data-type representing the whole AST there was no real necessity for this type, and we could have resorted so simply passing Constr around. In the case of the Clojure AST we need this additional information, and the ConsrFor type becomes (slightly) more interesting.

```
data ConstrFor :: U -> Constr -> * where
  NilProof :: ConstrFor KSepExprList Nil
  ConsProof :: ConstrFor KSepExprList Cons

SpecialProof :: ConstrFor KExpr Special
  DispatchProof :: ConstrFor KExpr Dispatch
  CollectionProof :: ConstrFor KExpr Collection
  TermProof :: ConstrFor KExpr Term
  CommentProof :: ConstrFor KExpr Comment
  SeqProof :: ConstrFor KExpr Seq
  EmptyProof :: ConstrFor KExpr Empty

[...]
```

As the constructor name suggests, we can think of these as proofs that

that a certain **Constr** maps to a specific **U**. These are straightforward to generate manually, but can also be generically derived.

Finally we will have to add <code>IsRecEl</code> instances for the recursive elements of the family, we can define these instances for <code>Expr</code>, <code>SepExprList</code> and <code>Term</code> only, and treat all the other types as atoms.

4 Heuristics

When moving from our toy language to a more complex one like Clojure, we soon run into the limitations of our non-deterministic approach. Non-determinism sneaks in when we have to compute an alignment, either on the recursive or on the atomic level.

It is easy to see that in some cases, prioritizing deletions can be more profitable and in other it may be better to do the opposite; this uncertainty stems from the fact that at the time we are calculating the alignment we have no information about the size of the sub-trees we are considering.

Since we don't know a priori which alignment is more efficient, in the original specification we simply decide to enumerate all possible ones. This number can grow very quickly and, to make things worse, we are dealing with alignments of arbitrarily large subtrees, which prevents us from optimising towards insertions or deletions.

In this section we will define some heuristics we can use to guide this process of enumeration in order to trim down the amount of computations that need to be carried on. These heuristics fall under two categories.

1. One is to explore the possibility of using the standard unix diff3 algorithm as an oracle to prune the alignment trees that are being generated. The idea is that instead of enumerating all possible alignments between two trees, we can check and see how diff3 treats the sequence of lines in which that tree resides in the source. This can allow us to prune the search space based on the information we can derive from diff3 and may be able to speed up the computation to handle larger inputs. This idea can be taken a step further. We can generalise the approach to add an Oracle which, based on some internal state, generates the next branches that should be explored.

We can define different Oracles and explore different strategies to reduce the combinatorial explosion. One of the upsides of this approach is that it will allow us to test different kinds of optimisations in a clean and flexible way; we could even imagine an oracle that interacts with

the user, occasionally asking her for guidance into which branches to pursue. Furthermore, we could define a notion of composition between oracles that will give us the chance to combine different optimisations into one.

2. Another approach that we could take in the attempt to speed up the algorithm is to define an heuristic to score patches which will allow us to greedily prune the search space. With this approach, the question that arises is: what are the properties of patches for which we can compare and score them? The answer is not clear yet. Informally we want to prefer patches that make minimal modifications and encourage copying as much as possible. This is because if a patch consists of a copy on a certain sub-tree, we can be sure that we can safely merge this with any patch that modifies that same sub-tree. In other words, want to define an heuristic that picks the patch that maximises the chances of it being disjoint from any other patch from the same source.

4.1 Basic Oracles

The goal for Oracles is to be able to have a uniform interface to implement different kinds of optimisations, heuristic and possibly even human interaction in the process of generating all the possible patches.

The key idea, is to extend the algorithm to perform a monadic action at each non-deterministic "junction". The result of this action will be a list that encodes which branches should be explored and which should be cut from the enumeration of patches.

We can start by observing that in both places where we have a nondeterministic choice, we always have to pick between three possible paths: namely to insert or delete something or to match source and destination in a pair. We can model this with a very simple datatype

```
data Path = I | M | D
```

Where the three constructors respectively stand for: Insert, Modify and Delete. We want to give our oracles the possibility to inspect the history of issued paths on each branch, this can be modeled with a reader monad.

```
type HistoryM = ReaderT [Path]
```

We can now define our Oracle class

The Oracle class has two functions, one for the choice on the constructor level (callF) (we call this the *Fixpoit* too, hence the 'F' in the suffix) and one for the choice on the product level (callP). At each choice, the oracle has access to the history of paths issued on the branch via the history monad, and has also access to it's internal state (the o type).

Notice that the signatures differ in the arguments they take, callP is meant to handle alignments on the product level, as such it takes the two heterogeneous lists that are being aligned. The function callF on the other hand, is meant to handle the recursive alignments on the constructor level and takes two singletons as input.

4.1.1 NoOracle

To warm up we can start by defining the "unit" oracle.

This oracle will not contain any global information and will ignore the history of issued paths. It will simply output all possible choices in any non-trivial case.

4.1.2 NoDupBranches

The first optimisation we want to encode is to limit the duplicate branches being explored: we avoid performing an insertion if the last step was a deletion and vice-versa. It is easy to see that an insertion followed by a deletion is equivalent to a deletion followed by an insertion, furthermore – if we can match two elements – then the match will never be worst than an insertion followed by a deletion.

We can define the following function that looks at the history of issued paths to avoid performing an insertion if the last step was a deletion and vice-versa. The last step is attached in front of the list as it is more efficient that traversing the list every time to add it at the end.

```
nextPaths :: [Path] -> [Path]
nextPaths (I:_) = [I, M]
nextPaths (D:_) = [D, M]
nextPaths (M:_) = [I, M, D]
```

Given this function we can implement the NoDupBranches oracle

data NoDupBranches = NoDupBranches

4.2 Oracle composition

With the oracles we gain the possibility to tweak the run-time behaviour of the algorithm without have to change any parts of the actual implementation. An advantage of this is that we can define a notion of composition between oracles; this way we can layer different processes, each of which is independent of the other in terms of implementation.

The composition we define wants to model a stack of oracles, the oracles are consulted in the order in which they appear on the stack. When an oracle is called, only if the answer is an empty list we will go down the stack and ask the oracle underneath.

This means that we can build other optimisations on top of NoDupBranches, these optimisations can also be partial or based on heuristics, as long as we have a "safe" oracle at the bottom of the stack we can always fallback to the ones below in the cases when it is not clear which choice should be done.

```
data ComposeOracle a b = ComposeOracle a b
-- Give it a nice constructor
```

4.3 DiffOracle

A considerable speedup can be obtained by using diff to prune the search space. We can define a datatype, which mirrors the definition of a path and identifies which lines are copied, which are deleted and which are inserted according to diff.

We will call this data type ${\tt DiffAction}$ and it will have the following definition.

```
data DiffAction =
   OMod LineRange LineRange
| OIns LineRange
| ODel LineRange
```

Where LineRange is a pair of Int which represent the first and last line of the corresponding region. We can think of DiffAction as some sort of Edit Script, with the difference that in addition to copies, insertions and deletions we introduce modifications. We will produce an OMod every time we have two contiguous regions of insertions or deletions between the source and destination file. The regions tagged by an OMod are the ones where we attempt to produce a more accurate patch than diff.

Note that regions that are not covered by any **DiffAction** are implicitly considered copies. For example, given this pair of source and destination

```
1 (defn function 1 ;; A comment
2 [a b] 2 (defn function
3 return a) 3 [a b]
4 doSomethingElse
5 return b)
```

The preprocessing will produce the list [OIns (1,1), OMod (3,3) (4,5)]. The first line can be definitely ruled as an insertion, as it is adjacent to a copy on both the source and destination. *Diff* records line 3 of the source as a deletion and lines 4 and 5 of the destination as insertions. This gives us two contiguous regions of insertions and deletions between source and destination and are accordingly recorded as a modification.

Since traversing the whole list of **DiffAction** every time we want to call the oracle is not very efficient we can encode the same information in a pair of maps from **Int** to **Path** (one for the source and one for the destination files). Given this pair of maps, the oracle will extract the **LineRange** contained in each **Usingl** u and lookup the line that corresponds to the beginning of the **LineRange** in the corresponding map. We want to only look at the beginning of the **LineRange** as we want to locally exploit the global solution provided by diff. An alternative approach might be to look at the whole **LineRange** and observe how diff behaves on the corresponding set of lines. This however, introduces too much noise at the top-level, not giving us enough chances to prune the tree early on which is where we gain the most from the heuristic. We can define the following helper predicate

with the corresponding isIns and isDel, we can finally define the giveAdvice function.

```
giveAdvice :: DelInsMap -> Usingl u -> Usingl v -> [Path]
giveAdvice (srcMap, dstMap) src dst =
  if (isMod srcRange srcMap && isMod dstRange dstMap)
    then []
  else if (isDel srcRange srcMap || isMod srcRange srcMap)
    then [ D ]
  else if (isIns dstRange dstMap || isMod dstRange dstMap)
    then [ I ]
```

```
else [ M ]
where
   srcRange = fromJust $ extractRange src
   dstRange = fromJust $ extractRange dst
```

In case in which the ranges do not match with anything in our maps, we simply want to emit an M, as these expressions lie in lines that diff3 identified as copies (we will later see how this may give rise to some problems, as diff can copy in a way that our algorithm does not support). When changes in the source and destination overlap, we are essentially in a range where we know that diff can not reconcile the changes between them; it will simply delete everything in the source and insert everything in the destination. This is the case where we can attempt to generate a more efficient patch, so we return an empty list to fall back to any underlying oracle that will compute a more precise solution in that range.

Alternatively, if the source is marked as a deletion, or the destination is marked as an insertions, we will emit the corresponding instruction. In the else cases we also check if either the source or the destination is marked as modification (but the other one isn't as the first check was already showed to be false at this point). We have to handle the case that when transforming a source into the destination, we end up on a branch that has inserted (resp. deleted) everything it had to, and it simply needs to delete (rep. insert) the remaining range.

Finally, the full oracle can be defined as follows:

```
instance (Monad m) => Oracle DiffOracle m where
  callF o s d = return (askOracle o s d)
  callP _ An
                     An
                                = return []
                     (_ `Ac` _) = return [ I ]
  callP _ An
  callP _ (_ `Ac` _) An
                               = return [ D ]
  callP o (s `Ac` _) (d `Ac` _) = return (askOracle o s d)
askOracle :: DiffOracle -> Usingl u -> Usingl v -> [Path]
askOracle (DiffOracle diffActions) src dst
  = case (extractRange src, extractRange dst) of
      (Nothing, Nothing)
                                 -> [ M ]
      (Just sRange, Nothing)
                                 -> [ D ]
                                 -> [ I ]
      (Nothing, Just dRange)
      (Just sRange, Just dRange) -> giveAdvice diffActions src dst
```

With this definition, we exploit the fact that the LineRange is only defined for the recursive elements of the family, which means that in the case we can not extract it, we can short-circuit the computation since we never pair up non-recursive elements with recursive ones.

4.3.1 Shortcomings

One of the issues with this optimisation is that not every modification between source and destination file is correctly identified by this procedure. Some problems arise when changes in the resulting AST are invisible to diff. Suppose that we didn't include empty expressions in our AST and modeled the top-level parse as either a single expression or a sequence of multiple ones. What happens when try to compute the patch between the following files?

```
1 (keep
1 (keep
2 new keep)
2 old keep) 3 (new new)
```

The preprocessing will produce the following list of DiffAction: [OMod (2,2) (2,3)]. However, to perform the optimal patch between these two programs we clearly want to insert a Seq on the first line and proceed calculating the diff from there, but our DiffAction does not contain any insertion there. By following the diff instead, we realize we had to change the external node when it is too late, we are now looking at line 2 and have already decided to copy over the first line. At its core, the problem lies in the fact that the external change is invisible to diff, since it only deals with lines, and the addition of lines at the end does not influence in any way the lines at the beginning of the file. In our case, we have the whole expression tree, and adding a line at the end of the file does not necessarily only trigger changes on the leaves of the tree, but changes may bubble up to the root, as in the example shown.

Possible Solutions

There are different ways we can solve this problem. One is to carefully think about which nodes have this "non-local influence" and treat them in a special way. For example, the problem presented in the previous snippet arises from the fact that – when transforming a top level expression from a single Expr to a Seq – we can only realize that this change has to be made when we get to the second Expr. Whenever we change a single expression

to a sequence of two by adding one at the end, we will inevitably mark the first expression as a copy, and the second as an insertion. This means it will be "too late" when we get to the inserted line: we already decided to copy a node which leaves us no space to insert the new expression.

One solution is to design the AST in a way that prevents this problem from ever coming up. If we modelled the top-level of a program so that the top level is always a Seq, and we add an Empty constructor to Expr an example like the previous one, would not be problematic anymore. Indeed, when we get to the second line, we don't have to change the previous constructor anymore, as the source will conveniently contain an Empty expression slot in which we can insert our new expression. This solution has the problem of being very ad-hoc. We have to modify the parser and add support for the new constructors throughout the implementation. Empty expressions turned out to be useful in any case, as we need them to model the patch that inserts into an empty file, but the solution is clearly not satisfactory as it requires us to model our AST in a very specific way which breaks our claim to generality.

A better solution would be to design oracles that can deal with the problematic cases. Sticking to the example presented earlier, we could define a simple oracle which ignores everything, except the case when it gets as input a single expression from the source and a sequence of multiple ones in the destination. In that case we know that – no matter what the other oracles say – we must insert a **Seq** node on the top-level; in that situation we can directly return **I** and skip the other oracles.

This solution is better than the previous one, as it is less invasive. It is still troublesome however that the correctness of the oracle depends on an oracle being present before it. Also, if we want to add support for other languages in the future we will have to carefully re-implement the ad-hoc oracles for the new languages. To solve these last lingering issues, we can adopt a different strategy.

Ultimately the problem lies in the fact that there are two distinct actors at play: on one hand we have the AST, on the other the actual lines of code, which can be thought of as a pretty-printed representation of the AST. We are using the line based solution over the pretty-printed AST to derive a solution on the original AST. Our problems come from the fact that changes to the pretty-printed AST don't always map one-to-one to changes in the AST. If we could somehow run the line based diff on the AST directly there would be no discrepancies. To do so, we can print the AST to a file and, since every constructor is annotated with a line range which tell us on what line it appears, we can print each sub-tree on the lines the elements

it contains appear in. We can now run diff to preprocess the ASTs printed in this way. Each change that was detected by running on the original files will also be detected by looking at the ASTs, as they are representations of the content of those files. The converse, is not true though, by running diff on the AST we know exactly on which levels of the tree, modifications on certain lines reflect. The problematic case we showed earlier will now be correctly recognized. Indeed, by printing the ASTs of the two files showed earlier, we will immediately detect that on line 1 the constructor has changed from Collection to Seq.

4.3.2 Further Shortcomings

Another problem, perhaps even more troubling, is that diff can mark some parts as copies even though these copies are illegal for our algorithm. Imagine a case where we have this pair of source and destination files

```
1 ((keep
2 del 2 ins)(
3 keep)) 3 keep))
```

In this case, according to diff3 we are supposed to copy lines 1 and 3 and modify line 2. The problem is that – in the source file – we have a Cons node that contains all the copied lines in one of its children. In the destination however, some of these lines are copied to the left child of a Cons, and others to the right. In the example above this can be seen on the keep appearing on line 3, which will end up in a different expression than the one on the first line. What happens is that diff3 can copy nodes across adjacent sub-trees, but our algorithm does not: we have to pick one of the two sub-trees and attempt the copies only into that.

When we are transforming a Cons a Nil into a Cons c d the only option we have is to insert d in the place of Nil. However, according to diff, lines in the sub-tree a get copied both to c and d. In practice this means that when we are at the step in which we have to calculate the patch between a and c, we are left with inconsistent information, in particular we marked some nodes as copies into d when we actually want to delete them.

Possible Solutions

To solve this problem we must find a way of detecting when a situation like the one described above arises. We can formulate the problem as follows: given the following source and destination nodes

```
src = Seq a b
dst = Seq c d
```

- Let CopyPairs(P) be the set of pairs of lines (s,t) that are marked as copies by diff 3 in the program P.
- Let CopySet(e) be the function that extracts all the lines marked as copies contained in an expression e (A line is marked as copy if it appears in one of the pairs resulting from CopyPairs(P)).

Then, if we can find an $s \in CopySet(a)$ such that $t \in CopySet(c)$, where $(s,t) \in CopyPairs(P)$ and we can find $s' \in CopySet(a)$ such that $t' \in CopySet(d)$, where $(s',t') \in CopyPairs(P)$ then we know we are in a conflicting situation.

This condition deals with the case where we had to insert a sub-tree which contains at least one expression marked as copy, to deal with the deletion as well, we must also check that the converse condition does not hold going from c to a and b.

Once we detected the conflicting copy across sub-trees, we can simply remove pairs from the set CopyPairs(P) until the previous condition is satisfied. In other words, after we detect that a node contains copies over sub-trees, we pick one of the sub-trees and remove all the copies contained in it.

The only step that is still missing is about which criteria can be used to pair up the nodes we must check. One way to formulate the problem is the following: we run into this issue whenever we have a pair of candidate nodes that are marked as copy on their outer level (resulting in an Scns in our case), but would then later attempt to copy across subtrees. The crucial observation is that the candidate nodes to check will always start on a line that diff will have marked as copies (this is exactly the issue, diff can issue a copy there and move across sub-trees later, our algorithm can not).

One solution could be to extend the oracles to add support for a De-optimise operation. The oracle should be able to perform some computation on each branch and decide if it should keep operating on subsequent computations that follow from that branch. This could very well consist in performing the check we described earlier to detect when the information contained in the DiffOracle is not trustworthy anymore, and proceed the process ignoring the oracle which is marked as de-opt. Supporting this interface might be also very useful if we plan to write a human-interaction oracle, where we could have it work on the top levels of the tree (e.g. user matches top level

expressions) and then turn off as the program takes care of the deeper levels.

Another solution, could be to try and solve the problem with some preprocessing. This criteria identified to match nodes suggests an enumeration strategy that we could use to break any eventual conflicts in the [DiffAction]. The idea is to identify which lines diff marked as copies and collect all the sub-trees on those lines (from the source and destination respectively) so that we can perform the check on them. The final observation we need is that, when collecting sub-trees starting on a pair of lines (s,r) — where s is a copied line from the source file that ends up on line d in the destination — then we will collect the same number of sub-trees from s and d. This happens because, since the line is a copy, it must contain the same number of sub-trees starting from it, both in the source and destination file.

Moreover, since the whole line is marked as copy, our algorithm will end up only considering the respective pairs of sub-trees, meaning that we can zip up the two lists and check each pair. Given, a function CollectST(P,s) that takes as input a program P and collects all sub-trees starting on line s in P. For each pair $(s,t) \in CopySet(P)$ we can perform the following steps:

```
let src = CollectST(P,s)
let dst = CollectST(P,t)
map check (zip src dst)
```

Where check is the predicate we defined earlier to check if two expressions are conflicting. At this point, if check fails, we have a pair (s,t) of lines which diffidentified as copies but our algorithm can not. Once identified the critical pairs of lines we can remove pairs from CopySet(P) until the predicate is true.

4.4 Cost

Up to this point we have seen how the algorithm generates a list of patches, we have explored some techniques to reduce the size of this output list but we still have never considered the problem of which patch choosing from the output. Given the notion of application defined in 3.6, we can consider patches as partial functions. That is: a patch Almu u v is a partial function where the domain is the set of values of type Usingl u and the codomain is Maybe (Usingl v, where the function is obtained through patch application. A partial function is more accurate than an other, if it succeeds in producing a result to more input data — if one domain is a subset of the

other. We can lift the canonical partial order on Maybe a to functions by point-wise comparison over their domain. More formally, we obtain

```
\forall x. \text{ Nothing} \leq p x Just p1 < \text{Just } p2 \iff \forall x. \ p1 \ x \equiv p2 \ x
```

This definition – while capturing our intuition faithfully – is too extensional to be practical. The approach we will take is to assign a natural number to every patch, representing its cost. In this way we can compute this value by just traversing the patch, ideally this ordering should respect the extensional definition. Intuitively the best patch between x and y is the one that fixes as little elements as possible in the domain and range of its application.

We will count the elements that are fixed by performing insertions, deletions or replacement of non-recursive atoms. With this in mind we can start defining the cost function for trivial patches.

```
costK :: TrivialA u -> Int
costK c = if old == new then 0 else 2
  where (old, new) = unDiag c
```

If the patch is a copy then no element is fixed, if it contains a replacement instead we fix one item in the domain and one in the range giving a cost of 2

In the general case of atoms, we just need to distinguish between recursive and non-recursive elements and call the appropriate function.

With this function we can now define the cost for alignments.

Here we need a cost function over <code>Usingl</code> s, intuitively we want to assign a higher cost to a patch that deletes (resp. inserts) bigger elements. We can assign a cost to each <code>Usingl</code> and to each type in the family that constitute our target language by counting the number of choices that are fixed by each element. In the case of BinaryTrees – which have been our running example – this translates to

```
costUsingl :: Usingl u -> Int
costUsingl (UInt u) = 1
costUsingl (UIntTree t) = costIntTree t

costIntTree :: IntTree -> Int
costIntTree (Node t1 t2) = costIntTree t1 + costIntTree t2
costIntTree (Leaf i) = 1
```

We can now define cost for spines.

The definition for the function **sumAll** is omitted: it simply computes **costAt** over each pair of elements and sums all these together.

Finally, we are only left with the recursive alignments to handle. The case of Alspn has been handled already, if we match on an Alins or an Aldel, then we want to add 1, which represents fixing the choice of the external constructor being inserted or deleted, and the cost of the context.

The cost of the context, as in the case for alignments, sums the cost of all the <code>Usingls</code> in the context with the result of recursively calling <code>costAlmu</code> when we reach the hole.

4.5 Bounded Search

The last optimisation we are going to present is very simple but will allow us to gain just enough benefit to be able to handle the majority of our test data. Bounded search is a widespread technique employed when we have an exponential number of solutions to a problem and a *quality* function which assigns a value to any (possibly partial) solution. We can start the search process by establishing an upper bound to the quality of solutions we want to consider.

As we move through the solution space we want to keep track of the current quality of the solution, and prune every branch that exceeds the imposed bound. This process is not guaranteed to generate a solution, the upper bound to the solution quality might be too low. For this reason, bounded search implementations usually have some strategy to restart the search in such cases, increasing the bound by a suitable amount. On the other hand, if the bounded search terminates, we know that the optimal solution (where optimal means minimal according to the quality function) must be in the produced results.

A perfect candidate for the quality function is the notion of cost defined above. However we want to adapt it so that it can work on partial solutions, furthermore we want to be sure to apply the pruning as soon as possible and reduce the number of steps performed in a branch that will be pruned.

We can extend our History monad to store an **Int** which will represent the cost of each branch. Now we just have to change the algorithm to update this local cost at every step and check if the bound hasn't been exceeded at each step.

We can omit the details of how this cost is assigned, as it mirrors exactly the definition of the cost function over patches presented in 4.4.

We will thread the current cost across the computation at each alignment step (recursive and non-); we will add the cost of performing that step to the total and, if we exceed the supplied upper bound, prune the branch immediately.

4.6 Visualization

Patch objects produced by the algorithm are isomorphic to trees. For this reason, inspecting them by hand is often slow and error-prone. To make the inspection of these objects easier we wrote a simple interactive visualizer. The visualization relies on treant JS [11], a library for the creation and manipulation of tree structures. To take advantage of the library we only

have to define ToJSON instances for our patch type and – depending on how we want to represent insertions and deletions in the tree – possibly for each type in the family that constitutes our language.

Deletion and insertion nodes (both recursive and in alignments) are color-coded to be respectively red and green – and this coloration is inherited by child nodes and edges. Patches on non-recursive elements are represented as a single element if the patch was a copy, or by the pair of elements in the other case. Finally, nodes are collapsible, and the visualization defaults to collapse every node that only contains copies among its children. This allows us to keep the size of the visualized tree restrained, and allows us to read off the important information contained in a patch with ease.

This tool has proven to be very useful in the development process, allowing quick analysis and comparison of the produced patches. Deriving ToJSON instances can also be automated, making the visualization easily extensible to the treatment of other target languages.

Figure 1 shows a representation of the patch constructed through section 3.

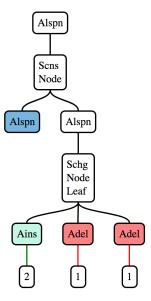


Figure 1: A patch between Binary Trees

The produced patch correctly shows a copy on the left sub-tree and an Schg on the right one: from a Node containing two leaves, to a single Leaf

containing a 2. The alignment produced must change the pair of 1s supplied to the source Node to the single 2 that is the argument to Leaf. It does so by inserting the 2 and deleting the 1s.

5 Experimentation

5.1 Domain specific improvements

Before presenting the results we want to introduce a relaxation of the definition of disjointedness. Many of the conflicts appearing in the collected test data share a common pattern. These are conflicts that arise from modifications to configuration files, which in Clojure are often expressed in the language itself via the defproject macro.

For example:

```
(defproject project-name "1.2.3"
  :description "The description of the project"
  :dependencies [[dependency-1 "0.0.1"]
       [dependency-2 "1.1.0"]]
  :dev-dependencies [[dev-dependency-1 "1.5.1"]])
```

It is very common for these files to give rise to conflicts due to modifications in the required version of the different dependencies by commits which are either merged into, or rebased on top of the development branch.

We can define two patches to be structurally-disjoint if they only differ on non-recursive atoms. Given a pair of structurally disjoint patches we can employ some domain specific merging strategies which may automate or drastically reduce the user effort required to perform the merge. In a case like the one described above, most of the conflicts are resolved by picking the highest version number every time there is a conflict consisting of a choice between two strings encoding version numbers. Nowadays, most projects adhere to SEMVER [12] which defines a standard total-ordering for strings representing versions which partially encode the semantics of the change.

This suggests that conflicts arising from structurally-disjoint patches can often be automatically resolved via some user-defined partial ordering between the atoms of the language. For the case of SEMVER specifically, we could imagine encoding different specific resolution strategies; e.g. we could decide to automatically resolve conflicts between PATCH or MINOR version changes and still notify the user when there is a conflict on a MAJOR version change.

There is another relaxation of the disjointedness predicate which we may consider. The current definition of disjointedness imposes that every patch p – that is different from the trivial patch \mathbf{Scp} — is not disjoint from itself. We can attempt to relax the definition from disjointedness to compatibility: two compatible patches may modify the same elements, as long as they do so in the same way. It is easy to see that every patch is compatible with itself.

Because of the current practices in how branches and the development process is managed, it is not so rare that we may need to merge a pair of patches which both contain the same changes. These common changes can come from cherry-picking another commit, rebasing, merging or any similar operation between branches of the same repository. Compatible patches can still not be applied in commuting order with the same result unless we relax the definition of application as well. However, it is easy to see that given two patches from the same source, and a proof that they are compatible, we can produce a single patch which encompasses the same changes and is independent of the order in which the two patches are supplied to the function. To put it another way: two patches are compatible if we can combine the into one without throwing away any information and the function that combines them is commutative in its arguments. Clearly disjointedness implies compatibility by picking the merging function to be the lication we defined earlier.

5.2 Results

In order to test the framework in a real world context we need to find some suitable data. To acquire this we explored all the Clojure repositories on Github and extracted the ones with the best combination of stars and collaborators. A high number of collaborators will possibly imply a higher chance for conflicts in the source tree, the high number of stars is a good indicator of the quality of the Clojure code and hopefully provides a selection of repositories from different domains.

We have collected data from twenty popular Clojure repositories. For each repository, we counted the number of *merge points*. A merge point indicates that files have been changed in two different ways, requiring a merge to reconcile the changes. Merge commits are identified by the simple fact of being commits that have more than one parent, we will restrict our attention to the case of two parents. This is the most common and sensible case for our scenario, as most teams will develop features on different

branches and eventually merge each branch into master. This process will generate a merge commit with exactly two parents: one of which is the master branch and the other is the feature branch.

- 1. For each of these commits we reproduced the process of performing the merge within branches and extracted any Clojure files that were marked as conflicts from this merge.
- 2. For each of these files we want to extract three different versions of it. The original version O.clj represents the snapshot of the file at the moment the branches initially diverged. It is the last version the two branches agreed on. We also want to extract the versions A.clj and B.clj, which capture the current state of the file on each of the two branches.

From this process we obtained 452 folders – each containing the three different snapshots of the conflicting file. These files have been shrunk with a pre-processing that relies on diff3 to remove all top level expressions that are are not involved in a conflict in any way. Each test consists in generating the pair of patches (OA,OB) and checking if they are disjoint. The patch OA is the best patch generated between O.clj and A.clj according to the cost function, and OB is generated in the same way but with B.clj as destination. Out of 452 conflicts, 18 timed out either while constructing the OA or the OB patch; the rest are reported in the following table, showing results of running the tests for disjointedness and compatibility, both in the full and the structurally-respecting variations.

Table 1 shows the results of our experiment. The first columns describe the number of contributors (Contributors), lines of Clojure code (LOC), the total number of commits (Commits), the number of conflicts that diff 3 has encountered (Conflicts). Note that for some repositories, only counting the Clojure code present leads to skewed statistics. For example, the circleci/frontend repository contains only a fraction of Clojure code, compared to the other languages used.

The relatively small size of test data, especially when compared to the impressive amount of research that has gone in a renowned algorithm as diff3, suggests caution in interpreting these results.

Having said this, it is certainly encouraging to observe that, given this specific set of conflicts, we perform approximately 20% better than diff3 in producing patches that can be safely and automatically merged. We can also see that these numbers drastically increase if we are willing to relax the notion of disjointedness we are investigating. This points to the fact

| Name | Contributors | LOC | Commits | Conflicts | A | В | С |
|---|--------------|------------|------------|-----------|-----|-----|-----|
| marick/Midje | 35 | 14,693 | 2,416 | 18 | 8 | 2 | 8 |
| ztellman /aleph | 62 | $4,\!557$ | 1,064 | 17 | 6 | 5 | 6 |
| ${f boot\text{-}{f clj}}/{f boot}$ | 66 | $9,\!370$ | $1,\!271$ | 8 | 2 | 2 | 4 |
| ${f nathanmarz}/{f cascalog}$ | 43 | 8,028 | 1,366 | 46 | 17 | 14 | 15 |
| $\mathbf{dakrone}/\mathrm{clj}	ext{-http}$ | 109 | $5,\!193$ | 1,111 | 5 | 1 | 0 | 4 |
| metosin/compojure-api | 36 | 6,604 | 1,818 | 12 | 1 | 4 | 7 |
| wit-ai/duckling-old | 65 | 28,790 | 586 | 12 | 3 | 2 | 7 |
| $\mathbf{cemerick}/\mathrm{friend}$ | 33 | 803 | 227 | 1 | 1 | 0 | 0 |
| $\mathbf{circleci}/\mathrm{frontend}$ | 92 | 894 | $18,\!857$ | 27 | 5 | 2 | 20 |
| incanter/incanter | 82 | 16,478 | 1,282 | 40 | 9 | 22 | 9 |
| jonase /kibit | 47 | 1,099 | 401 | 4 | 2 | 0 | 2 |
| bhauman/lein-figwheel | 86 | $6,\!515$ | 1,464 | 6 | 4 | 0 | 2 |
| ${f technomacy}/{ m leiningen}$ | 315 | 10,669 | 4,484 | 28 | 12 | 4 | 12 |
| clojure-liberator /liberator | 42 | 2,965 | 347 | 8 | 6 | 1 | 1 |
| $\mathbf{onyx}	ext{-}\mathbf{platform}/\mathbf{onyx}$ | 46 | 23,778 | 6,641 | 90 | 46 | 11 | 33 |
| overtone/overtone | 55 | 27,935 | 2,996 | 50 | 21 | 6 | 23 |
| $\mathbf{pedestal}/\mathbf{pedestal}$ | 59 | $1,\!1206$ | 1,403 | 24 | 13 | 5 | 6 |
| quil /quil | 34 | 1,341 | 960 | 10 | 1 | 8 | 3 |
| riemann/riemann | 114 | $16,\!586$ | 1,654 | 6 | 3 | 0 | 3 |
| ring-clojure/ring | 99 | 4,909 | 958 | 40 | 4 | 31 | 5 |
| Total | | | | 452 | 165 | 117 | 170 |

Table 1: The results collected

that another strong advantage of this approach – alongside improving the number of patches which can be automatically merged – is in the quality of the conflicts that can be produced. Given more accurate information about what is changing between two files enables us to employ stronger conflict resolution rules, which would have been cumbersome, or almost impossible, to express given the "opaque" representation of conflicts from *diff3*

6 Conclusion

6.1 Related Work

In this thesis we focus on converting the theoretical approach presented in [6] into a practical implementation that can be tested against real-world

data. Previous attempts to tackle this problems with similar approaches had, nonetheless, some key differences. The Untyped approach has been extensively studied: with authors focusing both on the linear [16, 17] and the tree [15, 18, 19, 20, 21, 22] variation.

In recent years other authors explored the typed approach [24, 23] in a generic setting. However they restricted their attention to the linear variation, by considering a flattening of the tree consisting in a pre-order traversal. The downside is that this flattening makes it harder to guarantee that the transformation encoded in a patch is structurally preserving and thus correct.

Several pieces of related work exist in the literature: from VCS systems built on strong theoretical foundations like Darcs and Pijul, respectively based on work by Roundy [13] and Mimram [25]. In our experimentation we have used Git to extract the information required for a merge (e.g. picking the common ancestor between two files). It is interesting to note how O'Connor [26] and other authors point out how the strategy adopted by Git in identifying and picking merge points, is inherently inconsistent and can lead to some surprising outcomes compared to other Version Control Systems.

Remarkably there is a formalization of the theory of patches through the lens of Homotopy Type Theory, which gained a lot of popularity in recent years and offers a new and interesting view on type theory. This has been explored by Licata et al. [14] with the key idea of modeling patches as paths in a suitable topological space.

Finally, Swierstra et al. [5] showed how separation logic and Hoare calculus can be used to reason about patches, in particular in terms of characterizing the relationship between patches and defining safe ways in which they can be combined.

6.2 Future Work

The goal of this work was to explore the performance of the typed, treestructured diff between datatypes. The result we managed to obtain are surely encouraging, but are still too sparse and specific when confronted with one of the venerable Unix tools as *diff*.

Strategies for automatic or semi-automatic conflict resolution where just hinted to in this thesis, exploring them in full generality is probably one of the most important and substantial next steps that can be taken. The definition of application should be modified to convey more information, namely the reason why a certain application failed. As mentioned in the previous section regarding SEMVER, we could imagine that some classes of conflicts could be automatically resolved with a custom set of directives specified by end users. Identifying the key use-cases, designing and integrating a framework which allows these custom user-supplied rules is definitely a non-trivial, but possibly very fruitful task.

Finally one of the remaining pieces to fill the puzzle is to explore the level of generality that can be achieved with this approach; while the algorithm is presented generically, the implementation is concretely tied to a specific language: both for convenience of presentation and efficiency. Regardless, for each language, we still need a custom parser to obtain the abstract representation we operate on, which hinders our claim to generality. Of course we can always use a generic strategy to parse a language for which we don't have a more specific parser; in particular one of these generic parsers could be the parser that consumes all characters until a newline. We can imagine that, presented in this context, the original diff can be collocated at the left end of a scale; by moving to the right we add structural information, which enables us to characterize transformations, and produce more accurate patches. The cost we pay for this is some loss of generality and the added computational complexity. Thus, the final question is ultimately about investigating this balance, the trade-off between adding information and complexity and the (possibly several) "sweet spots" that can be identified in this spectrum.

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