

03.02 P3

Nº 2

$$\text{Max: } W = 15y_1 + 10y_2 + 18y_3 + 14y_4$$

$$2y_1 + y_2 + 3y_3 + y_4 \leq 9$$

$$y_1 + 3y_2 + 2y_3 + y_4 \leq 7$$

$$y_1 + 2y_2 + y_3 + 4y_4 \leq 6$$

$$y_1 + 4y_2 + 5y_3 + 2y_4 \leq 5$$

$$2y_1 + y_2 + 3y_3 + y_4 + y_5 = 9$$

$$y_1 + 3y_2 + 2y_3 + y_4 + y_6 = 7$$

$$y_1 + 2y_2 + y_3 + 4y_4 + y_7 = 6$$

$$y_1 + 4y_2 + 5y_3 + 2y_4 + y_8 = 5$$

$$y_1, \dots, y_8 \geq 0$$

B	y ₁	y ₂	y ₃	y ₄	y ₅	y ₆	y ₇	y ₈	b
y ₅	2	1	3	1	1	0	0	0	9
y ₆	1	3	2	1	0	1	0	0	7
y ₇	1	2	1	4	0	0	1	0	6
y ₈	1	4	5	2	0	0	0	1	5
Z	-15	-10	-18	-14	0	0	0	0	0

B	y ₁	y ₂	y ₃	y ₄	y ₅	y ₆	y ₇	y ₈	b
y ₅	1/5	1/5	0	1/5	1	0	0	-3/5	6
y ₆	3/5	4/5	0	1/5	0	1	0	-2/5	5
y ₇	4/5	6/5	0	18/5	0	0	1	-1/5	5
y ₈	1/5	4/5	1	2/5	0	0	0	1/5	1
Z	-5 1/2	-2 1/5	0	-3 1/5	0	0	0	18/5	18

B	y ₁	y ₂	y ₃	y ₄	y ₅	y ₆	y ₇	y ₈	b
y ₅	0	1/3	0	2/3	1	0	0	1/3	13/3
y ₆	1	1/3	0	1/3	0	1	0	-2/3	25/3
y ₇	0	0	0	0	0	0	1	0	0
y ₈	0	1	0	0	0	0	0	1	1
Z	0	10/3	0	-8/3	0	0	0	-14/3	12 1/3

B	y ₁	y ₂	y ₃	y ₄	y ₅	y ₆	y ₇	y ₈	b
y ₅	1	-1/3	0	-1/3	1	0	0	-1/3	30/3
y ₆	0	2	0	2/3	0	1	0	-1/3	11/3
y ₇	0	2	0	2/3	0	0	1	1/3	11/3
y ₈	0	1	1	1/3	0	0	0	2/3	11/3
Z	0	-7	0	-59/3	0	0	0	-9 1/3	108/3

B	y ₁	y ₂	y ₃	y ₄	y ₅	y ₆	y ₇	y ₈	b
y ₅	5	-2/3	1/3	0	2/3	0	0	1/3	13/3
y ₆	0	1/3	-2/3	0	-1/3	1	0	-1/3	11/3
y ₇	0	-20/3	-2/3	0	2/3	0	1	-1/3	11/3
y ₈	0	1/3	1/3	1	-1/3	0	0	2/3	11/3
Z	0	38/3	59/3	0	16/3	0	0	13/3	209/3

$$y_1 = 13/3 \quad y_2 = 0$$

$$y_4 = 1/3 \quad y_3 = 0$$

$$Z = 5 \cdot 13/3 + 4 \cdot 1/3 = 69 2/3$$

Optimal solution: $(y_1, y_2, y_3, y_4) = (13/3, 0, 0, 1/3)$ $Z = 69 2/3$

Nº 3

$$\text{Max: } W = 20y_1 + 16y_2 + 12y_3 + 18y_4$$

$$3y_1 + y_2 + 2y_3 + y_4 \leq 10$$

$$2y_1 + 4y_2 + 3y_3 + y_4 \leq 6$$

$$y_1 + 3y_2 + 5y_3 + 2y_4 \leq 4$$

$$y_1 + 2y_2 + y_3 + 4y_4 \leq 8$$

$$3y_1 + y_2 + 2y_3 + y_4 + y_5 = 10$$

$$2y_1 + 4y_2 + 3y_3 + y_4 + y_6 = 6$$

$$y_1 + 3y_2 + 5y_3 + 2y_4 + y_7 = 4$$

$$y_1 + 2y_2 + y_3 + 4y_4 + y_8 = 8$$

	y_1	y_2	y_3	y_4	y_5	y_6	y_7	y_8	b
y_5	3	1	2	1	1	0	0	0	10
y_6	2	4	3	1	0	1	0	0	6
y_7	1	3	5	2	0	0	1	0	7
y_8	1	2	1	4	0	0	0	1	8
Z	20	16	12	18	0	0	0	0	0

	y_1	y_2	y_3	y_4	y_5	y_6	y_7	y_8	b
y_5	0	-5	$-\frac{5}{2}$	$-\frac{1}{2}$	1	$-\frac{3}{2}$	0	0	1
y_6	1	2	$\frac{3}{2}$	$\frac{1}{2}$	0	$\frac{1}{2}$	0	0	3
y_7	0	1	$\frac{7}{2}$	$\frac{3}{2}$	0	$-\frac{1}{2}$	1	0	4
y_8	0	0	$-\frac{1}{2}$	$\frac{7}{2}$	0	$-\frac{1}{2}$	0	1	5
Z	0	24	18	-8	0	10	0	0	60

	y_1	y_2	y_3	y_4	y_5	y_6	y_7	y_8	b
y_5	0	-5	$-\frac{18}{4}$	0	1	$-\frac{1}{4}$	0	$\frac{1}{4}$	$\frac{12}{4}$
y_6	1	2	$\frac{11}{4}$	0	0	$\frac{1}{4}$	0	$-\frac{1}{4}$	$\frac{16}{4}$
y_7	0	1	$\frac{26}{4}$	0	0	$-\frac{2}{4}$	1	$-\frac{3}{4}$	$\frac{13}{4}$
y_8	0	0	$-\frac{1}{4}$	1	0	$-\frac{1}{4}$	0	$\frac{2}{4}$	$\frac{10}{4}$
Z	0	24	$\frac{118}{4}$	0	0	$\frac{62}{4}$	0	$\frac{16}{4}$	$\frac{500}{4}$

$$y_1 = \frac{16}{4} \quad y_2 = 0 \quad y_3 = 0 \quad y_4 = \frac{10}{4} \quad Z = \frac{20 \cdot 16}{4} + \frac{180}{4} = \frac{500}{4}$$

$$\text{B-geb. } (y_1, y_2, y_3, y_4) = \left(\frac{16}{4}, 0, 0, \frac{10}{4} \right) \quad Z = \frac{500}{4}$$