

2 — Palindromic Mirror Eliminates One-Way Bias (and How to

A 1-page, hand-verifiable rationale with falsifiers, receipts, and a paper worksheet

One-line claim

If a workflow passes a palindromic mirror test—forward transform T , then inverse T^{-1} , returning to the same rest P within tolerance ϵ —then one-way bias cannot accumulate between views; failures localize as repairable deltas (Δ -lifts) without contaminating meaning.

Setup

Objects: input x , view operators $\{V_1 \dots V_8\}$, forward transform T , inverse T^{-1} , palindromic rest P , metric $\|\cdot\|$ (e.g., L_2 , TV, KL). Invariants: determinism under replay, lockstep parity (two lanes), idempotent canonicalization $C(C(z))=C(z)$.

The palindromic test

Core check: $\|T \cdot P \cdot T^{-1} - P\| \leq \epsilon$. Edge checks (octet): for each view V_i , $\|V_i \cdot T \cdot P \cdot T^{-1} - V_i \cdot P\| \leq \epsilon_i$ with $\epsilon_i \leq \epsilon$. Interpretation: forward•back leaves the rest unchanged in every view.

Why bias is annihilated

Any asymmetric drift d inserted by T shows up as a commutator residual $[T, P] := TPT^{-1} - P$. If residual $\leq \epsilon$ (strict ratchet shrinks ϵ after each pass), then persistent one-way moves cannot accumulate. Non-zero residuals are localized and become Δ -lift targets.

Receipts (what to ledger)

• Residual norms: $r_0 = \|TPT^{-1} - P\|$, $r_i = \|V_i TPT^{-1} - V_i P\|$. • Votes: mirror_votes (e.g., 22/24 probes), view_votes ($\geq 6/8$). • Four-bit commit: e.g., 1011 for {mirror, octet, Δ -lift, strict} passes. • Merkle-ish page hash over $\{P, T, \text{thresholds, receipts}\}$ for replay.

Δ -lift cookbook (local repairs)

Admissible moves that reduce r_0 and all r_i without increasing any: • Re-parameterize T (units, scaling, pose). • Replace fragile step with identity-equivalent form (algebraic or numerical). • Insert parity guard (swap lanes) where asymmetry leaked. Monotone rule: accept only if all residuals non-increase; otherwise annihilate.

Minimal falsifiers (to keep us honest)

F1: Exhibit a pipeline that passes A/B accuracy but fails the palindromic check (large r_0). F2: Show a case where $r_0 \approx 0$ but r_i explode in ≥ 2 views (octet gap). F3: Show replay with identical seeds produces divergent receipts (breaks determinism). Any F1-F3 breaks the claim; fix requires tightening views or redefining P .

Paper worksheet (evening exercise)

1) Choose P (a canonical 'rest' object) and metric. 2) Draw the palindrome rail: $P \rightarrow (T) \rightarrow \bullet \rightarrow (T^{-1}) \rightarrow P$. 3) Compute r_0 ; then place 8 small boxes (views $V_1 \dots V_8$) around it and compute r_i . 4) If any $r_i > \epsilon$: mark in red, propose one Δ -lift, recompute, and verify monotone decrease. 5) Ledger: write four-bit, votes, and thresholds used. Tip: start with symbolic identities (e.g., FFT/iFFT, encode/decode) before numeric runs.

Tiny live example (toy number)

Let P be a normalized image; $T = \text{FFT}$, $T^{-1} = \text{iFFT}$; metric=relative L_2 . $r_0 = 3.1e-12$, $(r_1 \dots r_8) \leq 5e-12 \rightarrow$ pass. After injecting $\frac{1}{N}$ unit leak (forgot N in iFFT) $r_0 = 1.0$, views fail. Δ -lift: add $1/N \rightarrow r_0$ back to $\sim 1e-12$; strict: tighten ϵ by $\times 0.3$.

Why this belongs in every loop

Without the palindrome, you can 'win' on a forward metric while quietly accumulating bias. With it, every improvement must survive the round-trip in all views, turning progress into stable receipts.

