

# HW9-GrowthModels&CatchIndices

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## Purpose:

The purpose of this markdown document is to work through Homework 9 in Dr. Babcock's Bayesian Statistics Course at the University of Miami. Homework 9 deals with growth models and abundance indices.

## General Start to Code

```
rm(list = ls())

#####github#####
#note, only needed after 90 days from 1/16/2024

# usethis::create_github_token()
# gitcreds::gitcreds_set()

#####check for r updates#####
#note, updateing may take some time so plan accordingly

#require(installr)

#check.for.updates.R()

#updateR() #only if needed

#####check for package updates#####
#note, updateing may take some time so plan accordingly

#old.packages()

# update.packages() #make the decision to the update the packages
```

## Load packages

```
library(INLAutils)
library(INLA)
library(tidyverse)
library(R2jags)
```

```

library(rstan)
library(ggmcmc)
library(purrr)
library(magrittr)
library(here)
library(loo)
library(DHARMA)
library(lme4)
library(rstanarm)
library(shinystan)
library(BayesFactor)

theme_set(theme_bw(base_size=15))
options(mc.cores = parallel::detectCores())
rstan_options(auto_write = TRUE)

```

## Data

For problem 1) The file croakerF.csv, shows the age and total length of 204 female croakers (a fish), from the croaker data set in the FSA R library.

For problem 2) The data in marlin.csv are counts of blue marlins observed in longline sets across 5 years. Remember to code the years as 1, 2, 3 and 4 for the input data to the JAGS or STAN model.

```
#problem 1 data
```

```
croaker.data <- read_csv(here("data", "croakerF.csv"))
```

```
## Rows: 204 Columns: 2
## -- Column specification -----
## Delimiter: ","
## dbl (2): Age, ObsL
##
## i Use 'spec()' to retrieve the full column specification for this data.
## i Specify the column types or set 'show_col_types = FALSE' to quiet this message.
```

```
head(croaker.data)
```

```
#problem 2 data
```

```
marlin.data <- read_csv(here("data", "marlin.csv")) |>
  mutate(present = if_else(Count > 0, true = 1, false = 0))
```

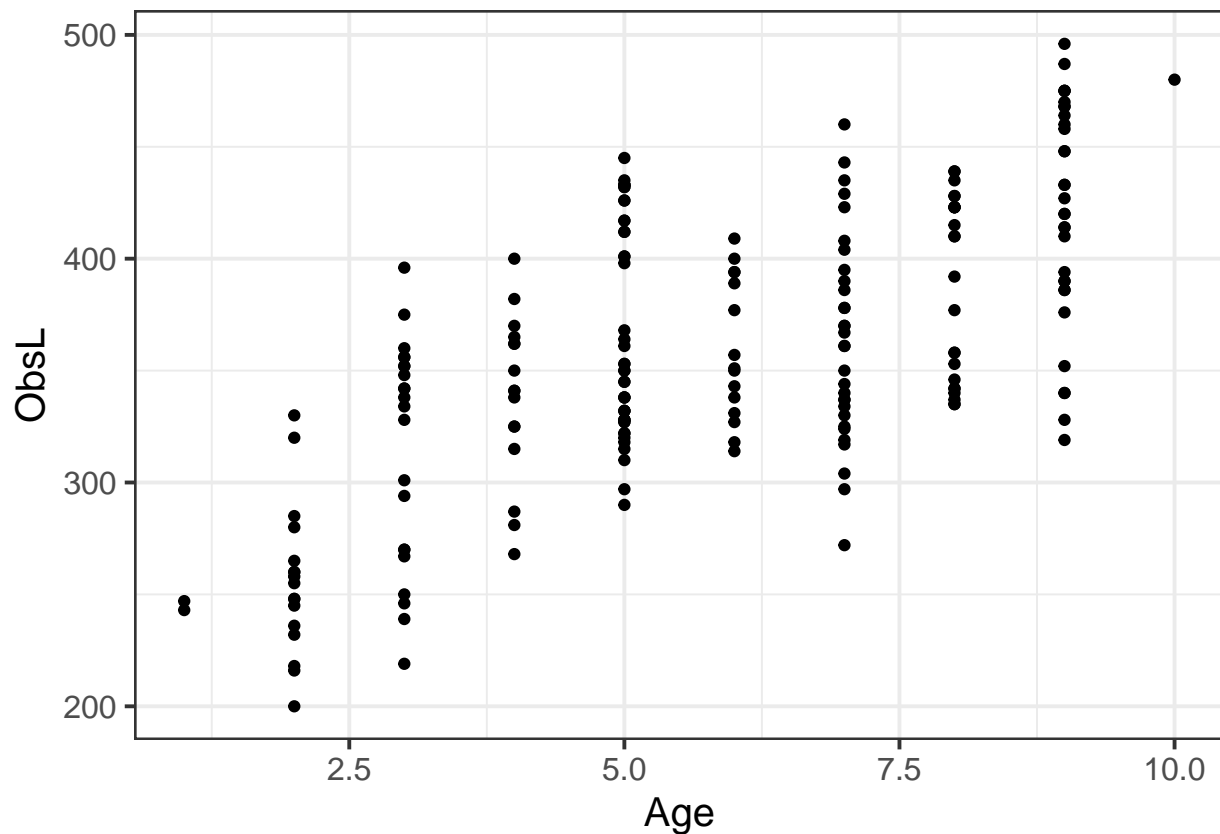
```
## Rows: 426 Columns: 2
## -- Column specification -----
## Delimiter: ","
## dbl (2): Count, Year
##
## i Use 'spec()' to retrieve the full column specification for this data.
## i Specify the column types or set 'show_col_types = FALSE' to quiet this message.
```

```
head(marlin.data)
```

## Problem 1) Growth models

```
croaker.data |>  
  ggplot(aes(x = Age, y = ObsL))+  
  geom_point()
```

A) Plot the length against age data. Is it obvious whether normal or lognormal will fit better?



It is not obvious whether the normal or lognormal will fit better. The error doesn't seem to increase with larger fish, so perhaps the normal is better.

```
write("model  
{  
  for (i in 1:N){  
    # model prediction  
    PredL[i] <- L1 +(L2-L1)* (1 - exp(- K* (Age[i] -Age1)))/(1 - exp(- K* (Age2 -Age1)))  
    logPredL[i] <- log(PredL[i])    # log-transformation of pred.value  
    ObsL[i] ~ dlnorm(logPredL[i], tau)    # lognormal likelihood
```

```

      logObsL[i] <-log(ObsL[i])      # log transfromation of observed value
      resid[i] <- logObsL[i]-logPredL[i] # residuals
      Rep[i] ~ dlnorm(logPredL[i], tau) # replicated data set
      logRep[i] <-log(Rep[i]) # replicated data set
      sresid2[i]<-(logObsL[i]-logPredL[i])*(logObsL[i]-logPredL[i])*tau
      rep.sresid2[i]<-(logRep[i]-logPredL[i])*(logRep[i]-logPredL[i])*tau
      LL[i] <- -0.5*log(2*3.14159)+0.5*log(tau)-0.5*tau*(logObsL[i]-logPredL[i])^2-logObsL[i]
    }
#priors specification
K ~ dunif(0,2)
Age1<-1
Age2<-10
L1~dunif(10,800)
L2~dunif(10,800)
tau~dgamma(0.001,0.001)
#Derived parameters
Linf<- (L2-L1*exp(-K*(Age2-Age1)))/(1-exp(-K*(Age2-Age1)))
chi.square.obs<-sum(sresid2[])
chi.square.rep<-sum(rep.sresid2[])
p.value<-step(chi.square.obs-chi.square.rep)
dev <- -2*sum(LL[])
}
",file=here("JAGS_mods","HW9_VonBertLnormSchnute_lognorm.txt"))

init1=list(tau=1,L1=200,L2=400,K=0.6)
init2=list(tau=0.5,L1=300,L2=450,K=0.4)

croaker.list <- list(N = length(croaker.data$Age),
                     Age = croaker.data$Age,
                     ObsL = croaker.data$ObsL)

HW9_SchnuteVBLG_lnorm_jags<-jags(croaker.list,list(init1,init2),
                                model.file=here("JAGS_mods","HW9_VonBertLnormSchnute_lognorm.txt"),
                                parameters.to.save=c("K","Linf","L1","L2","tau","p.value","LL","dev",
                                                       "resid","PredL","logPredL", "chi.square.obs","chi.square.rep"),
                                n.chains=2,n.iter=110000,n.burnin=10000,n.thin=10)

```

B) Fit a von Bertalanffy growth model using the Schnute formulation: with lognormal error and with uninformative priors. Set Age1 equal to 1, and Age2 equal to 10. Don't use any random effects. Note that this is a large data set, so don't save too many iterations (use a large thin) when you are saving residuals and predicted values.

Show the summaries of the parameters (L1, L2, K and precision, and the derived quantity Linf), plots of residual against predicted value and the qqnormal plot of the residuals. Does the model appear to fit the data adequately? *summary*

```

parameters <- c("L1","L2","K","tau","Linf")

res2<-HW9_SchnuteVBLG_lnorm_jags$BUGSoutput

res2$summary[parameters,]

```

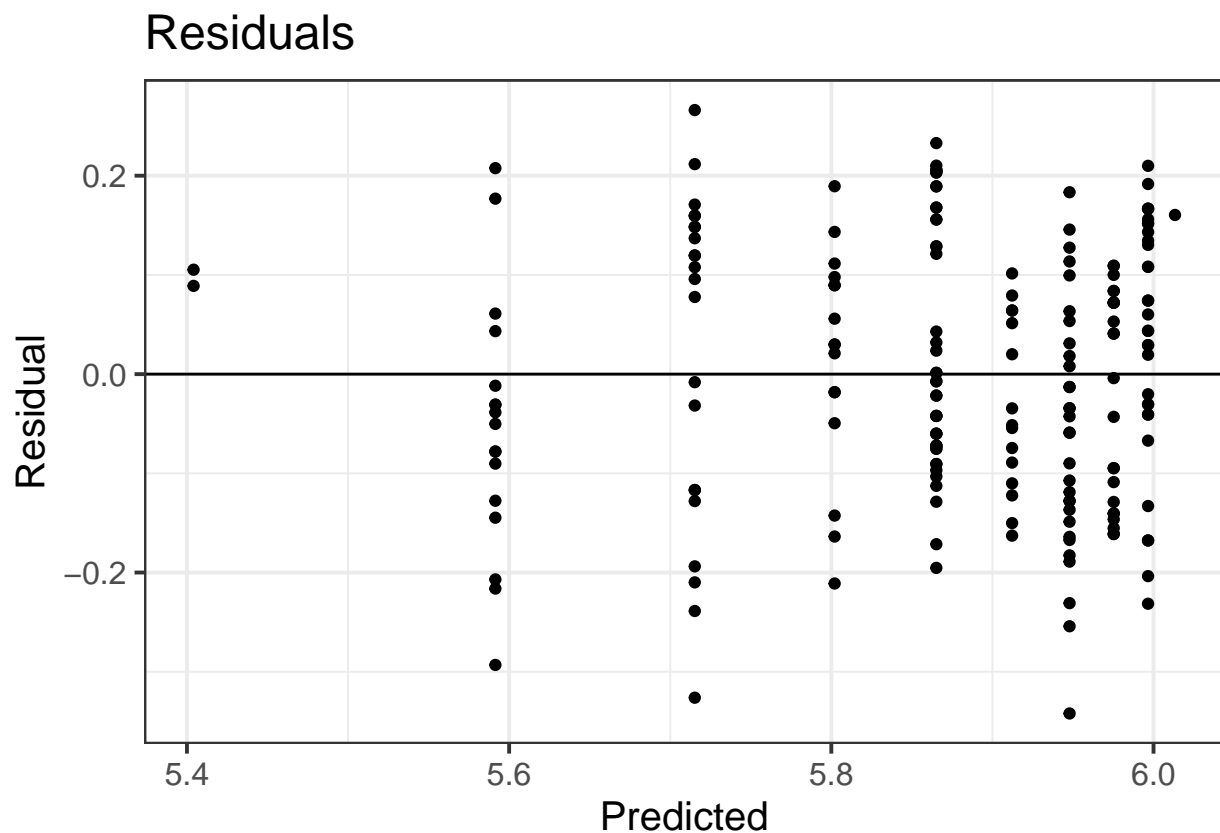
##	mean	sd	2.5%	25%	50%	75%
----	------	----	------	-----	-----	-----

```
## L1 222.7343696 13.57278587 196.0457976 213.6355879 222.7248965 231.874055
## L2 408.9415508 9.03640053 392.5124838 402.6303717 408.5262048 414.707721
## K 0.2427689 0.06859581 0.1070472 0.1970037 0.2426753 0.288493
## tau 59.8985420 5.97267944 48.6780432 55.8058438 59.7223836 63.776630
## Linf 444.8457417 354.50636937 400.2130780 418.5608087 432.3842846 451.505572
## 97.5% Rhat n.eff
## L1 249.3723566 1.001098 10000
## L2 427.9455704 1.000960 20000
## K 0.3790902 1.001108 9400
## tau 72.1606604 1.000953 20000
## Linf 536.9630098 1.001236 20000
```

*residual plots*

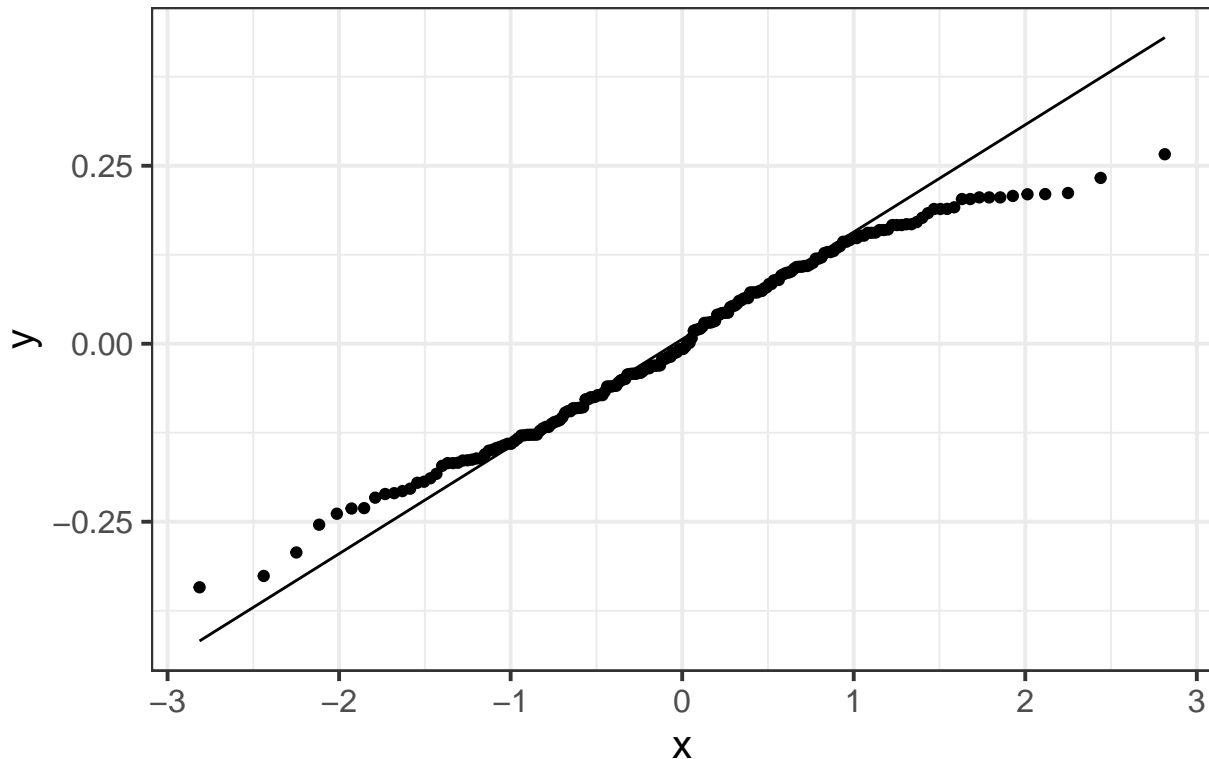
```
n<-length(croaker.data$Age)

sumtab<-res2$summary
residrows<-paste0("resid[",1:n,"]")
meanrows<-paste0("logPredL[",1:n,"]")
dfcheck<-data.frame(Predicted=sumtab[meanrows,"mean"],
  Residual=sumtab[residrows,"mean"])
ggplot(dfcheck)+
  geom_point(aes(x=Predicted,y=Residual))+
  geom_abline(intercept=0,slope=0)+ggtitle("Residuals")
```



```
ggplot(dfcheck,aes(sample=Residual))+
  geom_qq()+geom_qq_line()+ggtitle("QQNormal of Residuals")
```

## QQNormal of Residuals



C) Now fit the same model with normal error. Show the summaries of the parameters, plots of residual against predicted value and the qqnormal plot of the residuals. Does the model appear to fit the data adequately? *run the model*

```
write("model
{
  for (i in 1:N){
    # model prediction
    PredL[i] <- L1 +(L2-L1)* (1 - exp(- K* (Age[i] -Age1)))/(1 - exp(- K* (Age2 -Age1)))
    ObsL[i] ~ dnorm(PredL[i], tau)      # lognormal likelihood
    resid[i] <- ObsL[i]-PredL[i] # residuals
    Rep[i] ~ dnorm(PredL[i], tau) # replicated data set
    sresid2[i]<-(ObsL[i]-PredL[i])*(ObsL[i]-PredL[i])*tau
    rep.sresid2[i]<-(Rep[i]-PredL[i])*(Rep[i]-PredL[i])*tau
    LL[i] <- -0.5*log(2*3.14159)+0.5*log(tau)-0.5*tau*(ObsL[i]-PredL[i])*(ObsL[i]-PredL[i])
  }
#priors specification
K ~ dunif(0,2)
Age1<-1
Age2<-10
L1~dunif(10,800)
```

```

    L2~dunif(10,800)
    tau~dgamma(0.001,0.001)
#Derived parameters
    Linf<- (L2-L1*exp(-K*(Age2-Age1)))/(1-exp(-K*(Age2-Age1)))
    chi.square.obs<-sum(sresid2[])
    chi.square.rep<-sum(rep.sresid2[])
    p.value<-step(chi.square.obs-chi.square.rep)
    dev <- -2*sum(LL[])
}
",file=here("JAGS_mods","HW9_VonBertLnormSchnute_norm.txt"))

init1=list(tau=1,L1=200,L2=400,K=0.6)
init2=list(tau=0.5,L1=300,L2=450,K=0.4)

croaker.list <- list(N = length(croaker.data$Age),
                     Age = croaker.data$Age,
                     ObsL = croaker.data$ObsL)

HW9_SchnuteVBLG_norm_jags<-jags(croaker.list,list(init1,init2),
                                model.file=here("JAGS_mods","HW9_VonBertLnormSchnute_norm.txt"),
                                parameters.to.save=c("K","Linf","L1","L2","tau","p.value","LL",
                                                       "resid","PredL","chi.square.obs","chi.square.rep","dev"),
                                n.chains=2,n.iter=110000,n.burnin=10000,n.thin=10)

```

*model summary*

```

parameters <- c("L1","L2","K","tau","Linf")

res2_n<-HW9_SchnuteVBLG_norm_jags$BUGSoutput

res2_n$summary[parameters,]

```

##		mean	sd	2.5%	25%	50%
## L1		2.282425e+02	1.909225e+01	1.884407e+02	2.156532e+02	2.291927e+02
## L2		4.131163e+02	9.149843e+00	3.964258e+02	4.068167e+02	4.126032e+02
## K		2.279837e-01	8.302444e-02	6.888979e-02	1.704919e-01	2.267225e-01
## tau		4.810355e-04	4.742661e-05	3.921562e-04	4.483920e-04	4.793211e-04
## Linf		4.728097e+02	7.207494e+02	4.033281e+02	4.236028e+02	4.405706e+02
##		75%	97.5%	Rhat	n.eff	
## L1		2.417015e+02	2.630522e+02	1.001248	5000	
## L2		4.191230e+02	4.320277e+02	1.001140	7800	
## K		2.831192e-01	3.963893e-01	1.001125	8500	
## tau		5.122972e-04	5.790449e-04	1.000986	20000	
## Linf		4.673684e+02	6.282605e+02	1.001034	17000	

*residual plots*

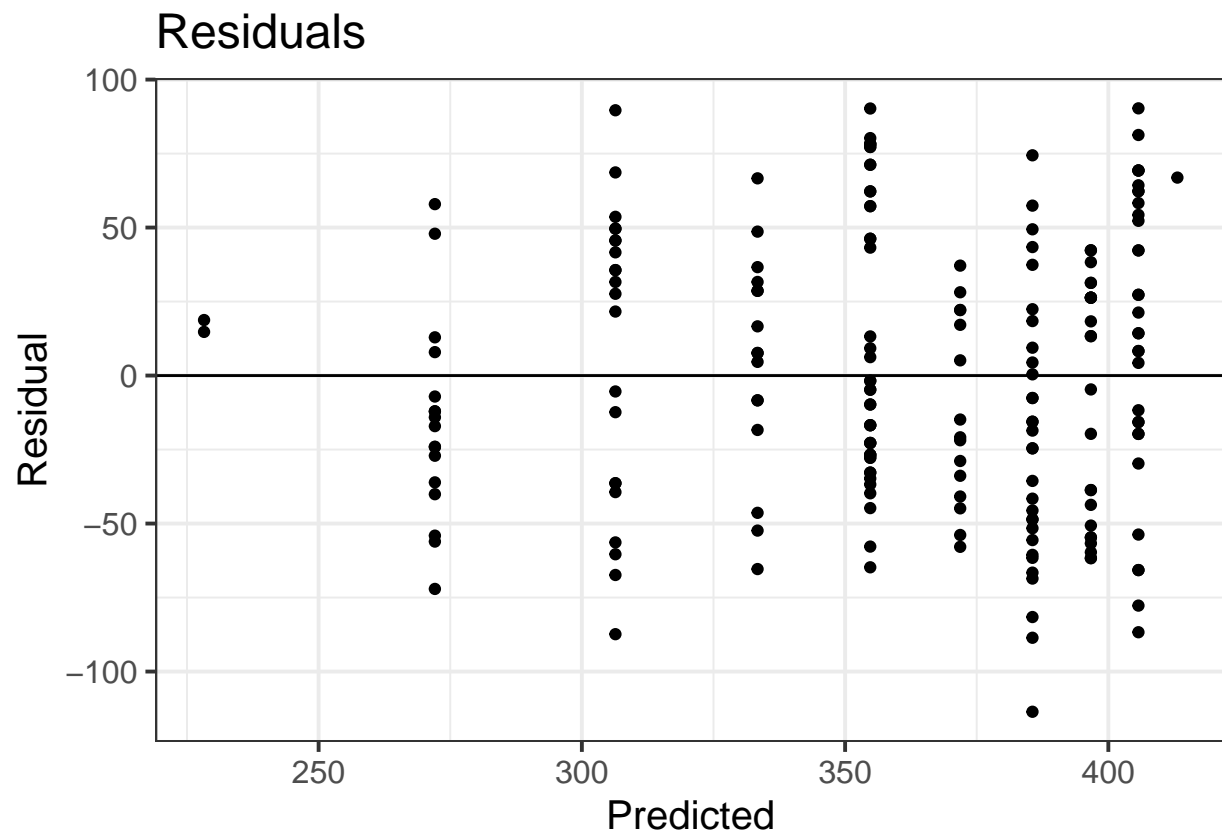
```

n<-length(croaker.data$Age)

sumtab<-res2_n$summary
residrows<-paste0("resid[",1:n,"]")
meanrows<-paste0("PredL[",1:n,"]")

```

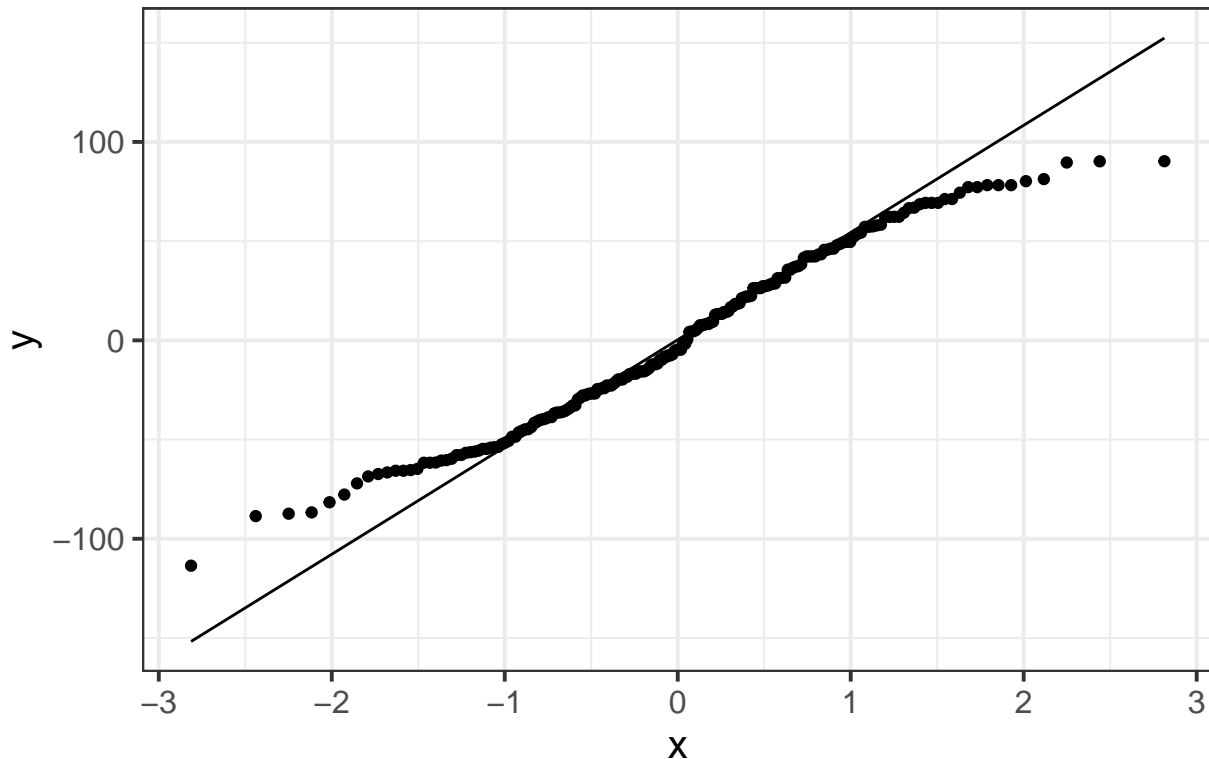
```
dfcheck<-data.frame(Predicted=sumtab[meanrows,"mean"],
  Residual=sumtab[residrows,"mean"])
ggplot(dfcheck)+
  geom_point(aes(x=Predicted,y=Residual))+
  geom_abline(intercept=0,slope=0)+ggtitle("Residuals")
```



```
ggplot(dfcheck,aes(sample=Residual))+
  geom_qq()+geom_qq_line()+ggtitle("QQNormal of Residuals")
```



## QQNormal of Residuals



D) Compare the two models with WAIC. Is normal or lognormal better? (Hint: If you are using JAGS, you calculate the deviance as  $-2 \times \text{sum}(\text{loglikelihood})$  to make sure you get the same deviance value that JAGS calculates. This is a way to check that you typed in the formula for loglikelihood correctly. STAN does this calculation of log likelihood for you so you don't need this. *check deviance*

```
#lognormal
HW9_SchnuteVBLG_lnorm_jags$BUGSoutput$summary[c("dev", "deviance"),]
```

```
##           mean      sd    2.5%    25%    50%    75%    97.5%
## dev      2138.689 2.861634 2135.121 2136.582 2138.042 2140.097 2145.701
## deviance 2138.689 2.861634 2135.121 2136.582 2138.042 2140.097 2145.701
##           Rhat n.eff
## dev      1.000952 20000
## deviance 1.000952 20000
```

```
#normal
HW9_SchnuteVBLG_norm_jags$BUGSoutput$summary[c("dev", "deviance"),]
```

```
##           mean      sd    2.5%    25%    50%    75%    97.5%    Rhat
## dev      2138.404 2.829896 2134.884 2136.318 2137.775 2139.818 2145.5 1.000954
## deviance 2138.404 2.829896 2134.884 2136.319 2137.775 2139.819 2145.5 1.000954
##           n.eff
## dev      20000
## deviance 20000
```

## WAIC Table

```
n<-length(croaker.data$Age)

WAIC.table <- tibble(model = c("Lognormal", "normal"),
  LL.ls = c(list(HW9_SchnuteVBLG_lnrm_jags$BUGSoutput$sims.matrix[,paste0("LL[",1:n
) |>
  mutate(WAIC.ls = map(LL.ls, waic),
    elpd_waic = map_dbl(WAIC.ls,c(1,1)),
    p_waic = map_dbl(WAIC.ls,c(1,2)),
    waic = map_dbl(WAIC.ls,c(1,3)),
    deltaWAIC = waic - min(waic),
    weight = round(exp(-2*deltaWAIC)/sum(exp(-2*deltaWAIC)),digits = 5))

WAIC.table |> select(-LL.ls,-WAIC.ls) |> knitr::kable(caption = "WAIC Table")
```

Table 1: WAIC Table

model	elpd_waic	p_waic	waic	deltaWAIC	weight
Lognormal	-1071.264	3.693358	2142.528	0.475448	0.2787
normal	-1071.026	3.566959	2142.052	0.000000	0.7213

Both the normal and lognormal are within 2 WAIC units so they both are adequate models. But, the normal model had the lowest WAIC.

E) Now add ageing error to the lognormal model, assuming that the input age is normally distributed around the true age with a standard deviation of 0.5. Give the true ages a uniform prior between 1 and 10. Show the summary statistics. How does this change the resulting estimates of Linf and K? (Note that you must use the estimated real age not the input age in the von Bertalanffy equation to predict length. Also, no need to calculate WAIC for this one). *run model*

```
write("model
{
  for (i in 1:N){
    z[i] ~ dunif(1,10)
    Age[i] ~ dnorm(z[i],age_tau)
    # model prediction
    PredL[i] <- L1 +(L2-L1)* (1 - exp(- K* (z[i] -Age1)))/(1 - exp(- K* (Age2 -Age1)))
    logPredL[i] <- log(PredL[i]) # log-transformation of pred.value
    ObsL[i] ~ dlnorm(logPredL[i], tau) # lognormal likelihood
    logObsL[i] <-log(ObsL[i]) # log transfromation of observed value
    resid[i] <- logObsL[i]-logPredL[i] # residuals
    Rep[i] ~ dlnorm(logPredL[i], tau) # replicated data set
    logRep[i] <-log(Rep[i]) # replicated data set
    sresid2[i]<-(logObsL[i]-logPredL[i])*(logObsL[i]-logPredL[i])*tau
    rep.sresid2[i]<-(logRep[i]-logPredL[i])*(logRep[i]-logPredL[i])*tau
    LL[i] <- -0.5*log(2*3.14159)+0.5*log(tau)-0.5*tau*(logObsL[i]-logPredL[i])^2-logObsL[i]
  }
#priors specification
```

```

K ~ dunif(0,2)
Age1<-1
Age2<-10
L1~dunif(10,800)
L2~dunif(10,800)
tau~dgamma(0.001,0.001)
#Derived parameters
age_tau <- 1/(0.5)^2
Linf<- (L2-L1*exp(-K*(Age2-Age1)))/(1-exp(-K*(Age2-Age1)))
chi.square.obs<-sum(sresid2[])
chi.square.rep<-sum(rep.sresid2[])
p.value<-step(chi.square.obs-chi.square.rep)
dev <- -2*sum(LL[])
}
",file=here("JAGS_mods","HW9_VonBertLnormSchnute_lognorm_ageerror.txt"))

init1=list(tau=1,L1=200,L2=400,K=0.6)
init2=list(tau=0.5,L1=300,L2=450,K=0.4)

croaker.list <- list(N = length(croaker.data$Age),
                     Age = croaker.data$Age,
                     ObsL = croaker.data$ObsL)

HW9_SchnuteVBLG_lnorm.zage_jags<-jags(croaker.list,list(init1,init2),
                                     model.file=here("JAGS_mods","HW9_VonBertLnormSchnute_lognorm_ageerror.txt"),
                                     parameters.to.save=c("K","Linf","L1","L2","tau","p.value","LL","dev",
                                                           "resid","PredL","logPredL", "chi.square.obs","chi.square.rep"),
                                     n.chains=2,n.iter=110000,n.burnin=10000,n.thin=10)

```

*compare summaries*

*#lognormal*

```
HW9_SchnuteVBLG_lnorm_jags$BUGSoutput$summary[c("Linf","K"),]
```

```
##              mean              sd          2.5%          25%          50%          75%
## Linf 444.8457417 354.50636937 400.2130780 418.5608087 432.3842846 451.505572
## K      0.2427689  0.06859581  0.1070472  0.1970037  0.2426753  0.288493
##              97.5%      Rhat n.eff
## Linf 536.9630098 1.001236 20000
## K      0.3790902 1.001108  9400
```

*#lognormal with age error*

```
HW9_SchnuteVBLG_lnorm.zage_jags$BUGSoutput$summary[c("Linf","K"),]
```

```
##              mean              sd          2.5%          25%          50%          75%
## Linf 426.9267524 30.20877098 394.3214792 410.184464 421.4373901 436.3379767
## K      0.2898854  0.07803393  0.1436877  0.237006  0.2867667  0.3398946
##              97.5%      Rhat n.eff
## Linf 491.5572409 1.001033 18000
## K      0.4516368 1.001113  9100
```

When including error in age, the Linf decreased and K increased when compared to the model that did not include error in age.

## Problem 2) Delta lognormal

A) Apply a zero inflated Poisson model to the data. Use a logit link to estimate the probability of a positive observation as a function of the fixed effect of year and use a Bernoulli random variable ( $z$ ) to estimate whether observations are positive or negative. Estimate the effect of year on the log of the mean count if positive as a fixed effect of year and use a Poisson likelihood for the counts. If you have trouble getting the model to run, try initializing the Bernoulli random variable for the positive catch ( $z$  in the example code) equal to 1 for all sets.

Show the summary statistics of the estimated parameters, making sure the model has converged. Plot the overall predicted mean count in each year from the model with credible intervals. *run the model*

```
write("model {
  for(j in 1:Nyear) {
    a[j]~ dnorm(0, 1.0E-6)
    a2[j]~ dnorm(0, 1.0E-6)
  }
  for(i in 1:N) {
    logit(p[i])<-a[Year[i]]
    z[i]~dbern(p[i])
    logMean[i]<-a2[Year[i]]
    Mu[i]<-z[i]*exp(logMean[i])
    count[i]~dpois(Mu[i])
  }
  for(j in 1:Nyear) {
    predmean[j] <- exp(a2[j])
    logit(predp[j])<-a[j]
    total.mean[j] <-predp[j] * predmean[j]
  }
}
",file=here("JAGS_mods","HW9_ZIP.txt"))

marlin.list <- list(N = length(marlin.data$present),
  N2 = length(marlin.data$Count),
  present = marlin.data$present,
  Year = marlin.data$Year-1994, #need the integers of year so the index in the loop
  Year2 = marlin.data$Year-1994, #need the integers of year so the index in the loop
  count = marlin.data$Count,
  Nyear = length(unique(marlin.data$Year)))

init1 <- list(z = rep(1, times = nrow(marlin.data)))
init2 <- list(z = rep(1, times = nrow(marlin.data)))

HW9_ZIP_jags <- jags(marlin.list, inits = list(init1,init2),
  parameters.to.save=c("a","a2","predmean","predp","total.mean"),
  model.file=here("JAGS_mods","HW9_ZIP.txt"),
  n.chains=2, n.iter=440000,
  n.burnin=40000,n.thin=8)

## Warning in jags.model(model.file, data = data, inits = init.values, n.chains =
## n.chains, : Unused variable "N2" in data
```

```
## Warning in jags.model(model.file, data = data, inits = init.values, n.chains =
## n.chains, : Unused variable "present" in data
```

```
## Warning in jags.model(model.file, data = data, inits = init.values, n.chains =
## n.chains, : Unused variable "Year2" in data
```

*convergence, summary and plot*

```
#convergence
range(HW9_ZIP_jags$BUGSoutput$summary[, "n.eff"])
```

```
## [1]      53 100000
```

```
range(HW9_ZIP_jags$BUGSoutput$summary[, "Rhat"])
```

```
## [1] 1.000989 1.308417
```

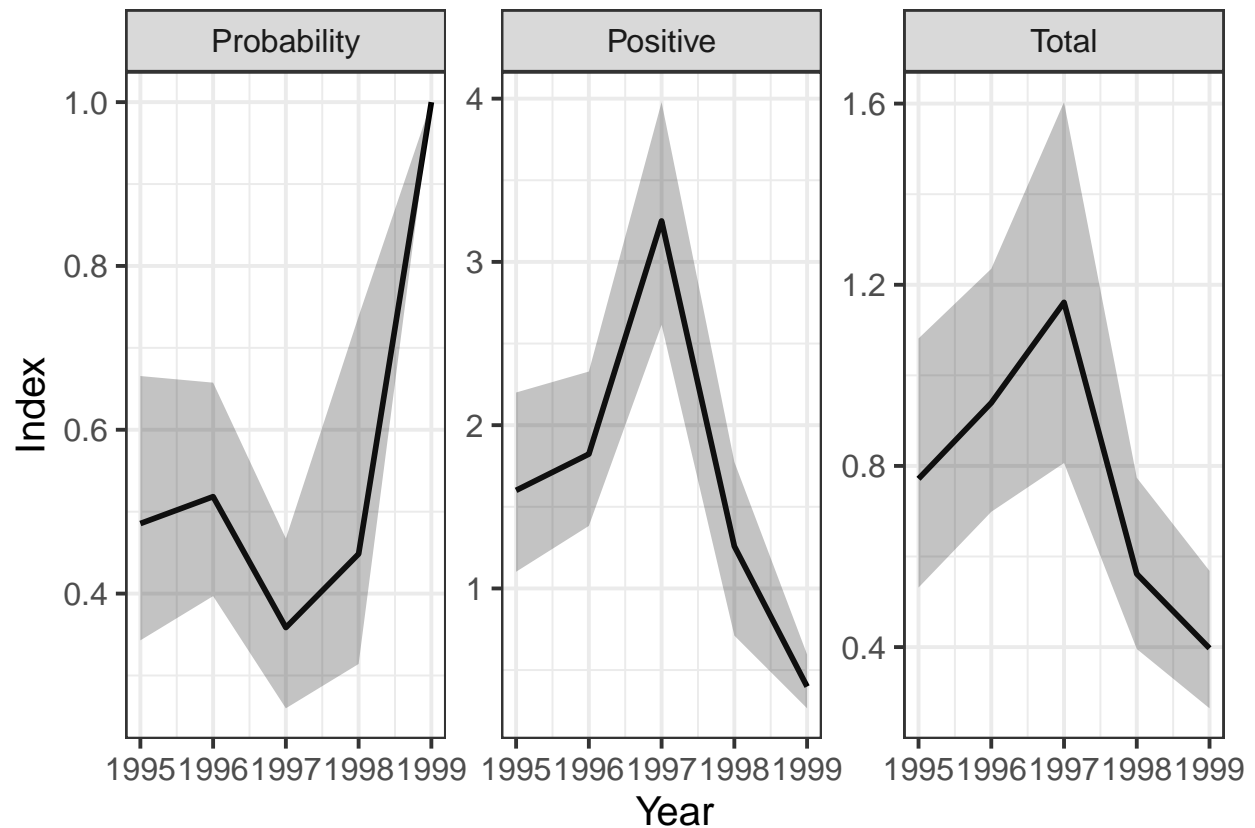
```
#summary
HW9_ZIP_jags$BUGSoutput$summary
```

##	mean	sd	2.5%	25%	50%
## a[1]	-0.03864770	0.34218218	-0.65045547	-0.26925856	-0.05794122
## a[2]	0.08342661	0.27166160	-0.41825253	-0.10192611	0.07330926
## a[3]	-0.58391278	0.23328377	-1.04640084	-0.74066485	-0.58187923
## a[4]	0.58784354	5.61481653	-0.78112066	-0.41590696	-0.20709814
## a[5]	784.65492947	606.01707596	12.34598266	302.86702765	658.96263970
## a2[1]	0.46327237	0.17576364	0.09723319	0.34971162	0.47038228
## a2[2]	0.59612667	0.13290749	0.32423642	0.50921372	0.60035097
## a2[3]	1.17679273	0.10694945	0.96102405	1.10615160	1.17895475
## a2[4]	0.20934672	0.22224769	-0.34081457	0.09440318	0.22989281
## a2[5]	-0.91800682	0.21392486	-1.32548028	-1.05365509	-0.91894109
## deviance	719.04022675	30.45652411	667.44802861	698.56588561	716.48425180
## predmean[1]	1.61366189	0.27998589	1.10211734	1.41865838	1.60060596
## predmean[2]	1.83104402	0.24143796	1.38297423	1.66398233	1.82275843
## predmean[3]	3.26247349	0.34752525	2.61437235	3.02270341	3.25097434
## predmean[4]	1.26158889	0.25789919	0.71119077	1.09900275	1.25846510
## predmean[5]	0.40903584	0.09829084	0.26567533	0.34866103	0.39894126
## predp[1]	0.49024853	0.08250885	0.34288691	0.43308913	0.48551875
## predp[2]	0.52036756	0.06637519	0.39693498	0.47454051	0.51831911
## predp[3]	0.35977435	0.05306291	0.25991684	0.32285878	0.35850030
## predp[4]	0.46472631	0.11366153	0.31407841	0.39749659	0.44840972
## predp[5]	0.99230248	0.06199873	0.99999565	1.00000000	1.00000000
## total.mean[1]	0.78069372	0.14027442	0.53147715	0.68246315	0.77152555
## total.mean[2]	0.94669816	0.13709234	0.69867877	0.85072750	0.93929282
## total.mean[3]	1.17190790	0.20365642	0.80642537	1.02820771	1.16118873
## total.mean[4]	0.56733003	0.09636125	0.39583529	0.49949734	0.56148168
## total.mean[5]	0.40241561	0.07772672	0.26479109	0.34762662	0.39726921
##	75%	97.5%	Rhat	n.eff	
## a[1]	0.16813085	0.6883908	1.000990	100000	
## a[2]	0.25574457	0.6522434	1.001020	47000	

```
## a[3]          -0.42506392   -0.1308883  1.000989 100000
## a[4]          0.02382918    1.0378461  1.308417   53
## a[5]         1141.86895010 2233.2926297 1.001174   8100
## a2[1]         0.58471938    0.7884962  1.001016  56000
## a2[2]         0.68752073    0.8452137  1.001006  86000
## a2[3]         1.25036090    1.3809188  1.001000 100000
## a2[4]         0.35515090    0.5738839  1.044353   150
## a2[5]        -0.78796027   -0.5184202  1.002646   3300
## deviance      736.06740390  790.5806883  1.021404   180
## predmean[1]    1.79448734    2.2000853  1.001016  56000
## predmean[2]    1.98877870    2.3284753  1.001006  86000
## predmean[3]    3.49160285    3.9785553  1.001000 100000
## predmean[4]    1.42639588    1.7751481  1.044353   150
## predmean[5]    0.45477146    0.5954605  1.002646   3300
## predp[1]       0.54193398    0.6656089  1.000990 100000
## predp[2]       0.56358993    0.6575158  1.001026  40000
## predp[3]       0.39530563    0.4673246  1.000989 100000
## predp[4]       0.50595701    0.7384342  1.050746   130
## predp[5]       1.00000000    1.0000000  1.072033   470
## total.mean[1]  0.86935427    1.0814194  1.001003 100000
## total.mean[2]  1.03501006    1.2352646  1.000991 100000
## total.mean[3]  1.30252202    1.6032369  1.000991 100000
## total.mean[4]  0.62851073    0.7739481  1.000989 100000
## total.mean[5]  0.45158067    0.5682931  1.001001 100000
```

```
#plot
model.bugsoutput <- HW9_ZIP_jags$BUGSoutput
Nyear= marlin.list$Nyear
rows.p1<-paste0("predp[",1:Nyear,"]")
rows.ln1<-paste0("predmean[",1:Nyear,"]")
rows.tot1<-paste0("total.mean[",1:Nyear,"]")
df1<-data.frame(model.bugsoutput$summary[rows.p1,c("2.5%", "50%", "97.5%")])
df3<-data.frame(model.bugsoutput$summary[rows.ln1,c("2.5%", "50%", "97.5%")])
df5<-data.frame(model.bugsoutput$summary[rows.tot1,c("2.5%", "50%", "97.5%")])
resdf1<-bind_rows(list(Probability=df1,Positive=df3,Total=df5),.id = "Type")>%
  mutate(Type=factor(Type,levels=c("Probability", "Positive", "Total")))
names(resdf1)[2:4]<-c(c("min", "med", "max"))
resdf1$Year<-rep(sort(unique(marlin.data$Year)),3)

#Plot
ggplot(resdf1,aes(x=Year,y=med,ymin=min,ymax=max))+
  geom_line(linewidth=1)+
  geom_ribbon(alpha=0.3)+
  facet_wrap(Type~.,scale="free")+
  ylab("Index")
```



B) Fit an integrated (i.e. all in one chunk of JAGS or STAN code) delta-lognormal model to these data, with the same model structure, i.e a fixed effect of all five years in both the binomial and lognormal parts of the model. Show the summary statistics of the estimated parameters, making sure the model has converged. Plot the overall predicted mean count in each year from the model with credible intervals. *run the model*

```
write("model {
  tau~dgamma(0.1,0.001)
  for(i in 1:Nyear) {
    a[i]~ dnorm(0, 1.0E-6)
    a2[i]~ dnorm(0, 1.0E-6)
  }
  for(i in 1:N) {
    logit(p[i])<-a[Year[i]]
    present[i]~dbern(p[i])
  }
  for(i in 1:N2) {
    logMean[i]<-a2[Year2[i]]
    count[i]~dlnorm(logMean[i],tau)
  }
  for(i in 1:Nyear) {
    mean.lnorm[i] <- exp(a2[i]+1/(2*tau))
    logit(p.year[i])<-a[i]
    total.mean[i] <-p.year[i]* mean.lnorm[i]
  }
}
```

```

}
",file=here("JAGS_mods","HW9_DeltaLognormalGLM.txt"))

marlin.list <- list(N = length(marlin.data$present),
  N2 = length(marlin.data$Count[marlin.data$present == 1]),
  present = marlin.data$present,
  Year = marlin.data$Year-1994, #need the integers of year so the index in the loop
  Year2 = marlin.data$Year[marlin.data$present == 1]-1994, #need the integers of year
  count = marlin.data$Count[marlin.data$present == 1],
  Nyear = length(unique(marlin.data$Year)))

HW9_deltaLnorm_jags <- jags(marlin.list,
  parameters.to.save=c("a","a2","mean.lnorm","p.year",
    "total.mean"),
  model.file=here("JAGS_mods","HW9_DeltaLognormalGLM.txt"),
  n.chains=2, n.iter=100000, n.burnin=5000,n.thin=2)

```

*convergence, summary and plot*

```

#convergence
range(HW9_deltaLnorm_jags$BUGSoutput$summary[, "n.eff"])

```

```
## [1] 12000 95000
```

```
range(HW9_deltaLnorm_jags$BUGSoutput$summary[, "Rhat"])

```

```
## [1] 1.000988 1.001115
```

```
#summary
```

```
HW9_deltaLnorm_jags$BUGSoutput$summary
```

```
##              mean          sd          2.5%          25%          50%
## a[1]         -0.4819409 0.24384542 -0.96959705 -0.6442266 -0.4785324
## a[2]         -0.2784829 0.20859589 -0.68849416 -0.4180404 -0.2772025
## a[3]         -0.6499916 0.22744088 -1.10637760 -0.8007442 -0.6467980
## a[4]         -0.7750823 0.21223311 -1.19932575 -0.9156936 -0.7727290
## a[5]        -1.0199120 0.27770364 -1.58018642 -1.2020303 -1.0137210
## a2[1]         0.5716638 0.11790194  0.34030848  0.4925667  0.5719047
## a2[2]         0.5385960 0.09716231  0.34831723  0.4730089  0.5387072
## a2[3]         0.9100508 0.11373704  0.68565933  0.8338564  0.9103002
## a2[4]         0.4214398 0.10851918  0.20817726  0.3484530  0.4217576
## a2[5]         0.3148609 0.14628528  0.02754184  0.2163608  0.3152615
## deviance    1004.3907247 4.76411004 997.09382207 1000.9170517 1003.7181560
## mean.lnorm[1] 2.1645534 0.26214826  1.70462032  1.9804420  2.1466338
## mean.lnorm[2] 2.0894660 0.21007301  1.71627943  1.9418149  2.0769179
## mean.lnorm[3] 3.0347168 0.35498198  2.40914620  2.7879416  3.0094125
## mean.lnorm[4] 1.8606725 0.20821987  1.49318971  1.7152723  1.8469332
## mean.lnorm[5] 1.6806233 0.25117673  1.24653735  1.5041011  1.6608182
## p.year[1]     0.3834248 0.05679241  0.27496083  0.3442917  0.3825987
```

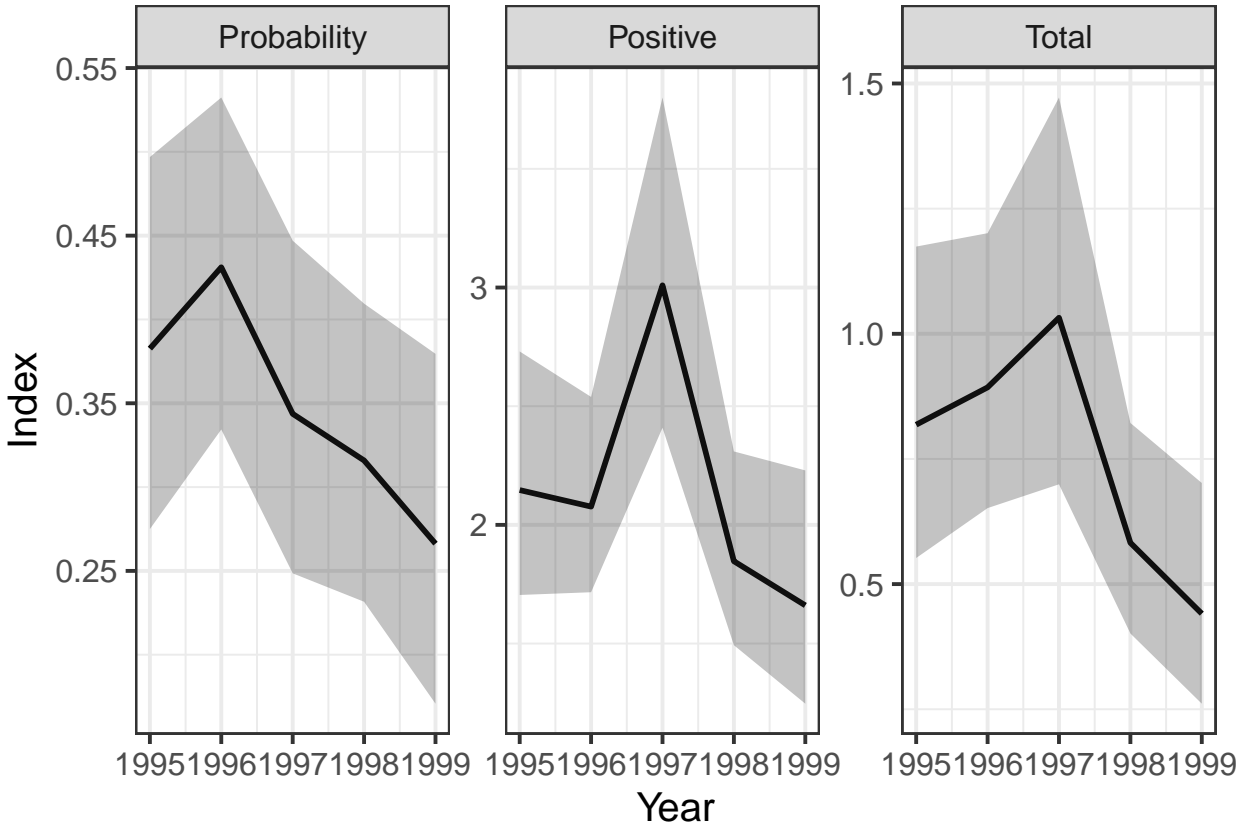


```
## p.year[2]      0.4315534 0.05062312 0.33436814 0.3969857 0.4311397
## p.year[3]      0.3447954 0.05070547 0.24854683 0.3098663 0.3437115
## p.year[4]      0.3171525 0.04544409 0.23159518 0.2858362 0.3158891
## p.year[5]      0.2685009 0.05350617 0.17076908 0.2311142 0.2662523
## total.mean[1]  0.8298769 0.15932262 0.55210592 0.7172403 0.8184047
## total.mean[2]  0.9017928 0.14029743 0.65181732 0.8041099 0.8929603
## total.mean[3]  1.0463678 0.19752208 0.69931331 0.9082506 1.0320966
## total.mean[4]  0.5900852 0.10751507 0.40136644 0.5149533 0.5825300
## total.mean[5]  0.4513093 0.11337178 0.26107567 0.3704026 0.4410080
##              75%      97.5%      Rhat n.eff
## a[1]          -0.3170453 -0.01247145 1.000990 95000
## a[2]          -0.1373711 0.12983833 1.000988 95000
## a[3]          -0.4949612 -0.21276399 1.000993 95000
## a[4]          -0.6313588 -0.36621462 1.001012 62000
## a[5]          -0.8300678 -0.49170479 1.001000 95000
## a2[1]         0.6507338 0.80256902 1.001100 13000
## a2[2]         0.6040138 0.72885297 1.000988 95000
## a2[3]         0.9859617 1.13437661 1.000989 95000
## a2[4]         0.4942592 0.63442351 1.000996 95000
## a2[5]         0.4130221 0.60096725 1.000997 95000
## deviance      1007.1379380 1015.43507278 1.000990 95000
## mean.lnorm[1]  2.3278374 2.73070588 1.001115 12000
## mean.lnorm[2]  2.2220552 2.53915495 1.000988 95000
## mean.lnorm[3]  3.2552786 3.80061216 1.000989 95000
## mean.lnorm[4]  1.9901140 2.30944159 1.000998 95000
## mean.lnorm[5]  1.8345820 2.22945350 1.000999 95000
## p.year[1]      0.4213960 0.49688218 1.000991 95000
## p.year[2]      0.4657111 0.53241406 1.000988 95000
## p.year[3]      0.3787255 0.44700875 1.000994 95000
## p.year[4]      0.3472025 0.40945602 1.001014 57000
## p.year[5]      0.3036307 0.37949205 1.001001 95000
## total.mean[1]  0.9299671 1.17420534 1.001019 48000
## total.mean[2]  0.9904314 1.20095943 1.000988 95000
## total.mean[3]  1.1707363 1.47198216 1.000995 95000
## total.mean[4]  0.6573584 0.82185223 1.001024 42000
## total.mean[5]  0.5203178 0.70197653 1.001012 63000
```

```
#plot
model.bugsoutput <- HW9_deltaLnorm_jags$BUGSoutput
Nyear= marlin.list$Nyear
rows.p1<-paste0("p.year[",1:Nyear,")")
rows.ln1<-paste0("mean.lnorm[",1:Nyear,")")
rows.tot1<-paste0("total.mean[",1:Nyear,")")
df1<-data.frame(model.bugsoutput$summary[rows.p1,c("2.5%", "50%", "97.5%")])
df3<-data.frame(model.bugsoutput$summary[rows.ln1,c("2.5%", "50%", "97.5%")])
df5<-data.frame(model.bugsoutput$summary[rows.tot1,c("2.5%", "50%", "97.5%")])
resdf1<-bind_rows(list(Probability=df1,Positive=df3,Total=df5),.id = "Type")>%
  mutate(Type=factor(Type,levels=c("Probability","Positive","Total")))
names(resdf1)[2:4]<-c(c("min","med","max"))
resdf1$Year<-rep(sort(unique(marlin.data$Year)),3)

#Plot
ggplot(resdf1,aes(x=Year,y=med,ymin=min,ymax=max))+
  geom_line(linewidth=1)+
```

```
geom_ribbon(alpha=0.3)+
facet_wrap(Type~.,scale="free")+
ylab("Index")
```



C) Which model do you think is better, a or b? Explain why you can't compare them with information criteria. Did you get the same trend across years? It is hard to tell which model is better, they both converged, though it took many more iteration for the ZIP to converge, and they both gave similar results. We can't compare the models using information criteria because the delta log normal has multiple likelihoods where as the ZIP only has one likelihood. If I had to choose, then I'd choose the delta lognormal just because it converged quicker.