A Table of Commutation Relations

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1 A table of commutation relations for operators of a single particle.

1.1 Operators to use.

- Observables (Hermitian): $x, p_x, H, N = a^{\dagger}a, J_x, J_y, J_z, J, \Pi$
- Non-observables: a, a^{\dagger}, T ,

1.2 The table.

1.3 Operator definitions.

- $p_x = \frac{\hbar}{i} \frac{\partial}{\partial x}$ in the x-basis. Townsend p.158.
- $\Pi |x\rangle = |-x\rangle$ Townsend p.213.
- $H = \frac{p^2}{2m} + V(x)$ Sakurai p.97, (2.4.2).

1.4 References.

- 0 Any operator commutes with itself.
- $i\hbar \frac{\partial}{\partial x}V(x)$ See Townsend eq. 6.31, p. 155 or Griffiths eq. 2.51, p.55. This leads to the uncertainty principle $\Delta x \Delta p_x \geq \frac{\hbar}{2}$.
 - -a See Sakurai p.90, (2.3.10).
 - $-a^{\dagger}$ See Sakurai p.90, (2.3.11).
 - 0 By the product rule.
 - 2 A table of commutation relations for operators of two particles.