

WRFDA-3DVar

Equation

$$J(x) = \frac{1}{2}(x - x_b)^T B^{-1}(x - x_b) + \frac{1}{2}(y - H(x))^T R^{-1}(y - H(x))$$

$J(x)$: Scalar cost function

x : The analysis: **what we're trying to find**

x_b : Background field

B : Background error covariance matrix

y : Observations

H : Observation operator: **computes model-simulated obs**

R : Observation error covariance matrix

User provided data:

$J(x)$: Scalar cost function

WRFDA output

x : The analysis

WRFDA output

x_b : Background field

User input

B : Background error covariance matrix

User input

y : Observations

User input

H : Observation operator

Included in WRFDA

R : Observation error covariance matrix

User input

Source of User-provided Data: where do the input files come from?

Symbol	Description	Source
x_b	Background ("first-guess")	real.exe or previous WRF forecast
B	Background error covariances	"gen_be" or default file provided with WRFDA
y	Observations	"obsproc" output or NCEP BUFR files
R	Observation error covariances	

WRFDA Namelist

The WRFDA namelist file includes two parts:

&wrfvar1 / &wrfvar2 / ... &wrfvar22 /	WRFDA namelist options: Running options for WRFDA code
& time_control / &fdda / ... & namelist_quilt /	WRF namelist options: WRFDA needs certain information from the WRF configuration including domain and time settings

Background Options (x_b): What's the format of my background file?

&WRFVAR3

fg_format: Format of the first guess field

fg_format = 1 : ARW regional, default

Background Error Covariance Options (B): What type of background error covariance do I want to use?

&WRFVAR7

cv_options: Background error covariance option

cv_options = 3 : global, default

cv_options = 5 : regional, generated by "gen_be"

cv_options = 5 : regional, generated by "gen_be" with multivariate moisture correlation

Observation Options (y): What's the format of my conventional observations?

```
&WRFVAR3
```

ob_format: The format of the conventional and satellite retrieval observation data going into WRFDA

ob_format = 1 : NCEP PREPBUFR (ob.bufr, gpsro.bufr)

ob_format = 2 : ASCII (ob.ascii), default

Observation Options:

```
&WRFVAR
USE_SYNOPOBS = T,
USE_SHIPSOBS = T,
USE_METAROBS = T,
USE_SOUNDOBS = T,
USE_PILOT OBS = T,
USE_AIREPOBS = T,
USE_GEOAMVOBS = T,
USE_POLARAMVOBS = T,
USE_BUOYOBS = T,
USE_PROFILEROBS = T,
USE_SATEMOBS = T,
USE_GPSZTDOBS = F,
USE_GPSPWOBS = T,
USE_GPSREFOBS = T,
USE_QSCATOBS = T,
USE_RADAROBS = F,
USE_RADAR_RV = F,
USE_RADAR_RF = F,
USE_AIRSRETOBS = T
```

What time window for my observations do I want to use?

```
&WRFVAR21
```

time_window_min = "2008-02-05_10:30:00"

```
&WRFVAR22
```

time_window_max = "2008-02-05_13:30:00"

Obs between time_window_min and time_window_max are processed

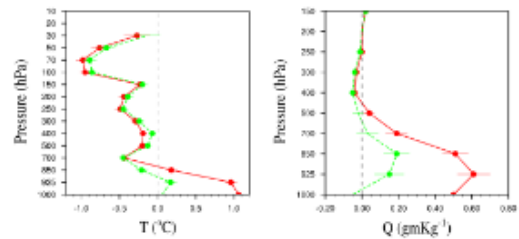
How do I want to handle surface observations?

&WRFVAR11

sfc_assi_options:

sfc_assi_options = 1 (default): The surface observations will be assimilated based on the lowest model level first guess. Observations are not used when the height difference of the elevation of observing site and the lowest model level height is larger than 100 meters

sfc_assi_options = 2: The surface observations will be assimilated based on surface similarity theory in PBL. Innovations are computed based on 10-m wind and 2-m temperature & moisture. *(Please use this option with caution, since the results could be very sensitive.)*



At what time is my analysis valid?

$$\mathbf{J}(\mathbf{x}) = \frac{1}{2}(\mathbf{x} - \mathbf{x}_b)^T \mathbf{B}^{-1}(\mathbf{x} - \mathbf{x}_b) + \frac{1}{2}(\mathbf{y} - \mathbf{H}(\mathbf{x}))^T \mathbf{R}^{-1}(\mathbf{y} - \mathbf{H}(\mathbf{x}))$$

&WRFVAR18

analysis_date = "2008-02-05_12:00:00"

(should be the same time as in your first-guess file)

How much output information do I want?

&WRFVAR1

print_detail_grad:

print_detail_grad = .false.(default)

print_detail_grad = .true. Output cost function and gradient values of every observation type each iteration into *standard output files (rsl.out)*

Before You Run

$$J(\mathbf{x}) = \frac{1}{2}(\mathbf{x} - \mathbf{x}_b)^T \mathbf{B}^{-1}(\mathbf{x} - \mathbf{x}_b) + \frac{1}{2}(\mathbf{y} - \mathbf{H}(\mathbf{x}))^T \mathbf{R}^{-1}(\mathbf{y} - \mathbf{H}(\mathbf{x}))$$

Check input files:

- Background (\mathbf{x}_b): \$DAT_DIR/rc/2008020512/wrfinput_d01
 - NETCDF format
 - For cold-start mode, (\mathbf{x}_b) is generated by WRF “real.exe”
 - For cycling mode, (\mathbf{x}_b) is generated by WRF from a previous cycle’s forecast
- Background Error Statistics (\mathbf{B}): \$DAT_DIR/be/be.dat
 - Binary format
 - Generated by “gen_be” for this specific test case domain
- Observations (\mathbf{y} , \mathbf{R}) : \$DAT_DIR/ob/2008020512/ob.ascii (conventional obs only)
 - ASCII or PREPBUFR format
 - Generated by OBSPROC from obs.2008020512, included in the tar file of the test data.
- Prepare a WRFDA namelist containing runtime options

Symbol	Description	WRFDA names
\mathbf{x}_b	Background (“first-guess”)	./fg
\mathbf{B}	Background error covariances	./be.dat
\mathbf{y}	Observations	./ob.ascii OR ./ob.bufr
\mathbf{R}	Observation error covariances	./ob.ascii OR ./ob.bufr
N/A	User-defined run-time options (namelist)	./namelist.input
N/A	Land-use table	./LANDUSE.TBL
N/A	WRFDA executable	./da_wrfvar.exe

After running you’ll find:

- **cost_fn** (cost function)
- **grad_fn** (Gradient of cost function)
- **gts_omb_oma_01** (point-by-point O, O-B, O-A information, etc.)
- **namelist.output** (Complete namelist)
- **statistics** (domain-wide O-B and O-A statistics)
- **wrfvar_output** (Analysis \mathbf{x} , the input to the WRF model)

O: Observation, A: Analysis, B: Background (first-guess)

cost_fn and grad_fn

- Contains values of the cost function and its gradient.
 - If `calculate_cg_cost_fn = .false.`, only the initial and final values of the cost and gradient functions are output as follows:

cost_fn

Outer Iter	EPS	Inner Iter	J	Jb	Jo	Jc	Je	Jp	Js	Jl
1	0.100E-01	0	24322.148	0.000	24322.148	0.000	0.000	0.000	0.000	0.000
1	0.100E-01	21	16141.946	1847.293	14284.652	0.000	0.000	0.000	0.000	0.000

grad_fn

Outer Iter	EPS	Inner Iter	G	Gb	Go	Ge	Gp	Gs	Gl
1	0.100E-01	0	543.846	0.000	543.846	0.000	0.000	0.000	0.000
1	0.100E-01	21	4.787	60.783	60.970	0.000	0.000	0.000	0.000

b: background term
 o: observation term
 c: JcDFI term
 e: alpha term
 p: radiance variational bias correction term
 s: skin temperature or cloud cover term
 l: lateral boundary conditions control variable (4dvar only)

- If `calculate_cg_cost_fn = .true.`, the cost function and its gradient at each iteration will be computed and written into **cost_fn** and **grad_fn**.

✓ WRFDA tools: `plot_cost_grad_fn.ncl`

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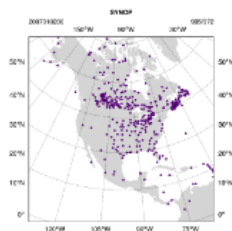
gts_omb_oma_01

- Contains complete point-by-point, detailed observation information.

obs_type	Number of obs	Number of levels	Obs index, Level index, station ID, lat, lon, pressure							
			For u: Obs, O-B, QC flag, Obs error, O-A							
synop	995									
1	176556	21.51	-104.90	89973.8836463	3.3147587	1.2193668	2	1.1000000	0.1849281	-1.5412909
-1.4225501	2	1.1000000	-1.6862257	295.5511624	2.5999150	2	2.0000000	1.3689324	89973.8836463	
-273.5464584	2	100.0000000	-236.6028635	0.0134689	0.0048657	0	0.0036749	0.0050584		

- Measured quantities for each observation type vary:

synop: u, v, t, p, q
 metar: u, v, t, p, q
 ship: u, v, t, p, q
 geoamv: u, v
 airep: u, v, t
 pilot: u, v
 satem: thickness
 qscat: u, v
 polaramv: u, v
 gpspw: tpw
 sound: u, v, t, q
 sonde_sfc: u, v, t, p, q
 profiler: u, v
 buoy: u, v, t, p, q
 airsr: t, q
 gpsref: ref



- ✓ WRFDA tools: `plot_gts_omb_oma.ncl`
- ✓ WRFDA tools: `plot_ob_ascii_loc.ncl`

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statistics

- Contains domain-wide O-B and O-A information:

Diagnostics of OI for synop

	u (m/s)	n	k	v (m/s)	n	k	t (K)	n	k	p (Pa)	n	k	q (kg/kg)	n	k
Number:	833			833			833			833			833		
Minimum(n,k):	-8.8880	172	0	-8.8880	683	0	-8.8880	833	0	-172.8880	931	0	-0.4118	719	0
Maximum(n,k):	8.8880	888	0	8.8880	630	0	8.8880	833	0	172.8880	931	0	0.4118	719	0
Average	-0.0023			-0.0023			2.1990			101.3028			0.8988		
RMSE	1.0020			1.0020			2.1990			101.3028			0.8988		

Diagnostics of AO for synop

	u (m/s)	n	k	v (m/s)	n	k	t (K)	n	k	p (Pa)	n	k	q (kg/kg)	n	k
Number:	833			833			833			833			833		
Minimum(n,k):	-8.8880	172	0	-8.8880	683	0	-8.8880	833	0	-172.8880	931	0	-0.4118	719	0
Maximum(n,k):	8.8880	888	0	8.8880	630	0	8.8880	833	0	172.8880	931	0	0.4118	719	0
Average	-0.0023			-0.0023			2.1990			101.3028			0.8988		
RMSE	1.0020			1.0020			2.1990			101.3028			0.8988		

Minimum of gridded analysis increments

Inv1	u	v	t	p	q
1	-1.0020	1.0020	-1.0020	1.0020	1.0020
2	-1.0020	1.0020	-1.0020	1.0020	1.0020

Maximum of gridded analysis increments

Inv1	u	v	t	p	q
1	1.0020	1.0020	1.0020	1.0020	1.0020
2	1.0020	1.0020	1.0020	1.0020	1.0020

Mean of gridded analysis increments

Inv1	u	v	t	p	q
1	-0.0023	0.0023	-0.0023	0.0023	0.0023
2	-0.0023	0.0023	-0.0023	0.0023	0.0023

RMSE of gridded analysis increments

Inv1	u	v	t	p	q
1	0.7990	0.7990	0.7990	0.7990	0.7990
2	0.7990	0.7990	0.7990	0.7990	0.7990

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• WRFDA Code Flow

