

Neural Network

December 14, 2020

```
[3]: ## Used train.csv and test.csv which are csv files that comprise of all the  
      →training  
      # and testing data from the MNIST handwritten Dataset  
      import numpy as np  
      import sklearn.preprocessing  
      import pandas as pd  
      from tensorflow.keras.models import Sequential  
      from tensorflow.keras.layers import Dense  
      from sklearn import linear_model  
      from sklearn.model_selection import train_test_split  
      from tensorflow.keras.utils import to_categorical, plot_model  
      import matplotlib.pyplot as plt  
      import seaborn as sns  
      # The training data has 42000 entries and 785 features  
      train_digits = pd.read_csv("train.csv")  
  
[4]: # Creating sections for training and testing data  
      # Creating training and test sets  
      # Splitting the data into train and test  
      A_matrix = train_digits.iloc[:, 1:]  
      Labels_A = train_digits.iloc[:, 0]  
  
      # Processing the images before analysis using scale function from sklearn.  
      →preprocessing  
      # Scale is used to standardise the pixels(features) in the image. This needs to  
      →be done because our dataset is sparse/widely spread out.  
      # Which can cause issues with our model being statistically skewed. Scaling the  
      →data in this manner  
      # makes the matrix entries have 0 mean and the standard variation of 1 in each  
      →field.  
      A_matrix = sklearn.preprocessing.scale(A_matrix)  
  
      # Splitting the data with 42k datapoints into 30% training data and 10% testing  
      →data  
      # The stratify property was used to ensure the data is split with even label  
      →distribution
```

```
Train_A, Test_A, Train_y, Test_y = train_test_split(A_matrix, Labels_A,
↳test_size = 0.10, train_size=0.30, random_state=10, stratify=Labels_A)
```

```
[5]: # ONEHOT ENCODING
Train_y= to_categorical(Train_y, 10)
Test_y = to_categorical(Test_y, 10)
```

0.1 Altering the Number of Hidden Layers in the Neural Network

0.2 1 hidden layer with 50 nodes and sigmoid activation function

```
[5]: # Using Sequential Keras model because we are creating a plain stack of layers
# Using Dense Layers so that our neural network is fully connected
# Using SGD as the Optimisation Algorithm because its the only one I fully
↳understand from this course
# Creating a single hidden layer with 50 nodes
# Because our model's output is one-hot encoded, I used softmax activation for
↳the output layer.
# This normalizes the values from the 10 output
# nodes such that the sum of all 10 values =1

## 1 hidden layers with 50 nodes
nn = Sequential([
    Dense(50, activation = 'sigmoid', input_shape = (784,)),
    Dense(10, activation = 'softmax')
])
```

```
[8]: # Compiling previously defined model
nn.compile(metrics=['accuracy'], optimizer="sgd",
↳loss='categorical_crossentropy')

#Using 10% of the sample size of testingvalidation
model_test = nn.fit(Train_A, Train_y, batch_size=128, epochs=30, verbose=False,
↳validation_split=.1)
loss, prediction_correctness = nn.evaluate(Test_A, Test_y)

#Printing the keys of the test model dict to see what variables to plot
print(model_test.model_test.keys())

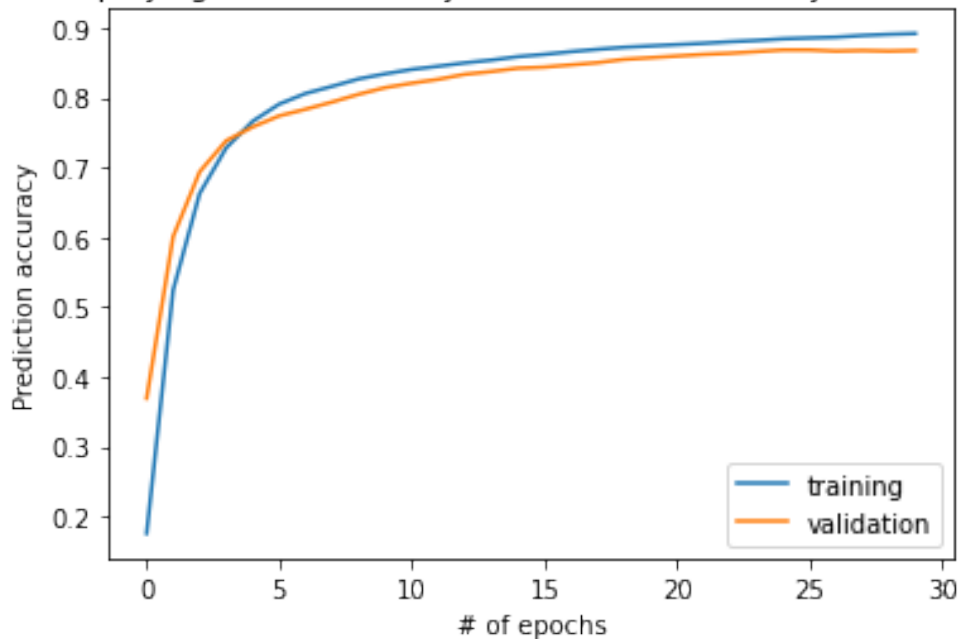
#Creating prediction and testing plot for comparison
plt.plot(model_test.model_test['accuracy'])
plt.plot(model_test.model_test['val_accuracy'])
plt.legend(['training', 'validation'])
plt.xlabel('# of epochs')
```

```
plt.ylabel('Prediction accuracy')
plt.title('Plot displaying model accuracy of NN with 1 hidden layer and 50_
↳nodes')
plt.show()

#Printing accuracy of model
print('Test accuracy: ', np.round(prediction_correctness,3))
```

```
dict_keys(['loss', 'accuracy', 'val_loss', 'val_accuracy'])
```

Plot displaying model accuracy of NN with 1 hidden layer and 50 nodes



Test accuracy: 0.888

0.3 Increasing to 2 hidden layers and 50 nodes

```
[9]: # Creating a single hidden layer with 50 nodes
nn2 = Sequential()
## 2 hidden layers with 50 nodes each
nn2 = Sequential([
    Dense(50, activation = 'sigmoid', input_shape = (784,)),
    Dense(50, activation = 'sigmoid'),
    Dense(10, activation = 'softmax')
])

nn2.summary()
```

Model: "sequential_2"

Layer (type)	Output Shape	Param #
dense_2 (Dense)	(None, 50)	39250
dense_3 (Dense)	(None, 50)	2550
dense_4 (Dense)	(None, 10)	510

Total params: 42,310
Trainable params: 42,310
Non-trainable params: 0

```
[10]: # Compiling previously defined model
nn2.compile(metrics=['accuracy'], optimizer="sgd",
            ↪loss='categorical_crossentropy')

#Using 10% of the sample size of testingvalidation
model_test = nn2.fit(Train_A, Train_y, batch_size=128, epochs=30,
            ↪verbose=False, validation_split=.1)
loss, prediction_correctness = nn2.evaluate(Test_A, Test_y)

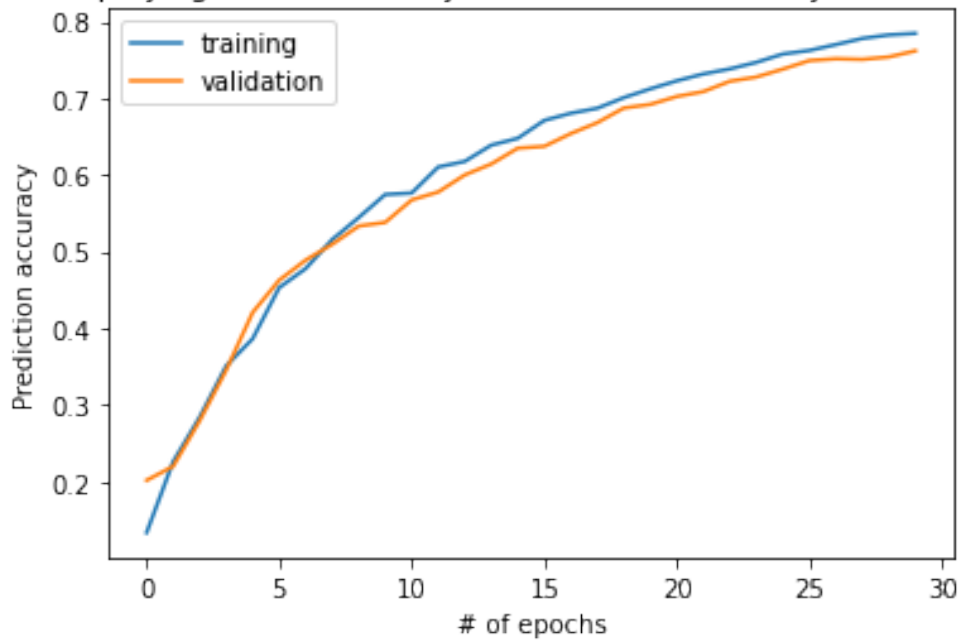
#Printing the keys of the test model dict to see what variables to plot
print(model_test.model_test.keys())

#Creating prediction and testing plot for comparison
plt.plot(model_test.model_test['accuracy'])
plt.plot(model_test.model_test['val_accuracy'])
plt.legend(['training', 'validation'])
plt.xlabel('# of epochs')
plt.ylabel('Prediction accuracy')
plt.title('Plot displaying model accuracy of NN with 1 hidden layer and 50
            ↪nodes')
plt.show()

#Printing accuracy of model
print('Test accuracy: ', np.round(prediction_correctness,3))

dict_keys(['loss', 'accuracy', 'val_loss', 'val_accuracy'])
```

Plot displaying model accuracy of NN with 2 hidden layer and 50 nodes



Test accuracy: 0.781

0.4 Increasing to 3 hidden layers and 50 nodes

```
[6]: # Creating a single hidden layer with 50 nodes
nn3 = Sequential()
## 3 hidden layers with 50 nodes each
nn3 = Sequential([
    Dense(50, activation = 'sigmoid', input_shape = (784,)),
    Dense(50, activation = 'sigmoid'),
    Dense(50, activation = 'sigmoid'),
    Dense(10, activation = 'softmax')
])
nn3.summary()
```

Model: "sequential_2"

Layer (type)	Output Shape	Param #
dense_2 (Dense)	(None, 50)	39250
dense_3 (Dense)	(None, 50)	2550
dense_4 (Dense)	(None, 50)	2550

```

-----
dense_5 (Dense)                (None, 10)                510
=====
Total params: 44,860
Trainable params: 44,860
Non-trainable params: 0
-----

```

```

[7]: # Compiling previously defined model
nn3.compile(metrics=['accuracy'], optimizer="sgd",
    ↪loss='categorical_crossentropy')

#Using 10% of the sample size of testingvalidation
model_test = nn3.fit(Train_A, Train_y, batch_size=128, epochs=30,
    ↪verbose=False, validation_split=.1)
loss, prediction_correctness = nn3.evaluate(Test_A, Test_y)

#Printing the keys of the test model dict to see what variables to plot
print(model_test.model_test.keys())

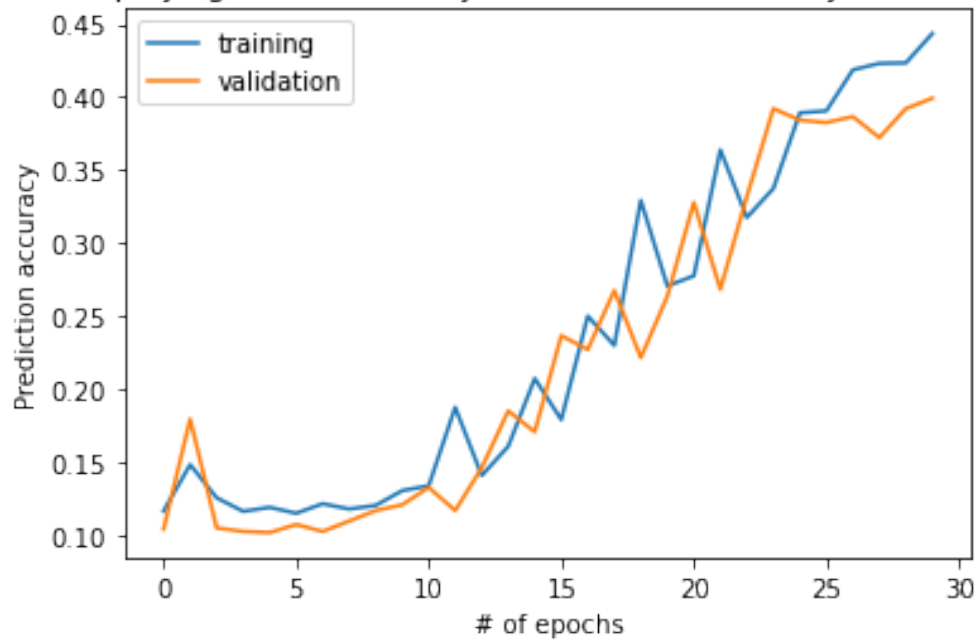
#Creating prediction and testing plot for comparison
plt.plot(model_test.model_test['accuracy'])
plt.plot(model_test.model_test['val_accuracy'])
plt.legend(['training', 'validation'])
plt.xlabel('# of epochs')
plt.ylabel('Prediction accuracy')
plt.title('Plot displaying model accuracy of NN with 1 hidden layer and 50
    ↪nodes')
plt.show()

#Printing accuracy of model
print('Test accuracy: ', np.round(prediction_correctness,3))

```

```
dict_keys(['loss', 'accuracy', 'val_loss', 'val_accuracy'])
```

Plot displaying model accuracy of NN with 3 hidden layer and 50 nodes



Test accuracy: 0.421

1 CHANGING THE # of NODES INSTEAD

1.1 1 hidden layer with 100 nodes

```
[8]: # Creating a single hidden layer with 32 nodes
nn4 = Sequential()
## 2 hidden layers with 50 nodes each
nn4 = Sequential([
    Dense(100, activation = 'sigmoid', input_shape = (784,)),
    Dense(10, activation = 'softmax')
])
nn4.summary()
```

Model: "sequential_4"

Layer (type)	Output Shape	Param #
dense_6 (Dense)	(None, 100)	78500
dense_7 (Dense)	(None, 10)	1010

Total params: 79,510
Trainable params: 79,510
Non-trainable params: 0

```
[10]: # Compiling previously defined model
nn4.compile(metrics=['accuracy'], optimizer="sgd",
            ↳loss='categorical_crossentropy')

#Using 10% of the sample size of testingvalidation
model_test = nn4.fit(Train_A, Train_y, batch_size=128, epochs=30,
            ↳verbose=False, validation_split=.1)
loss, prediction_correctness = nn4.evaluate(Test_A, Test_y)

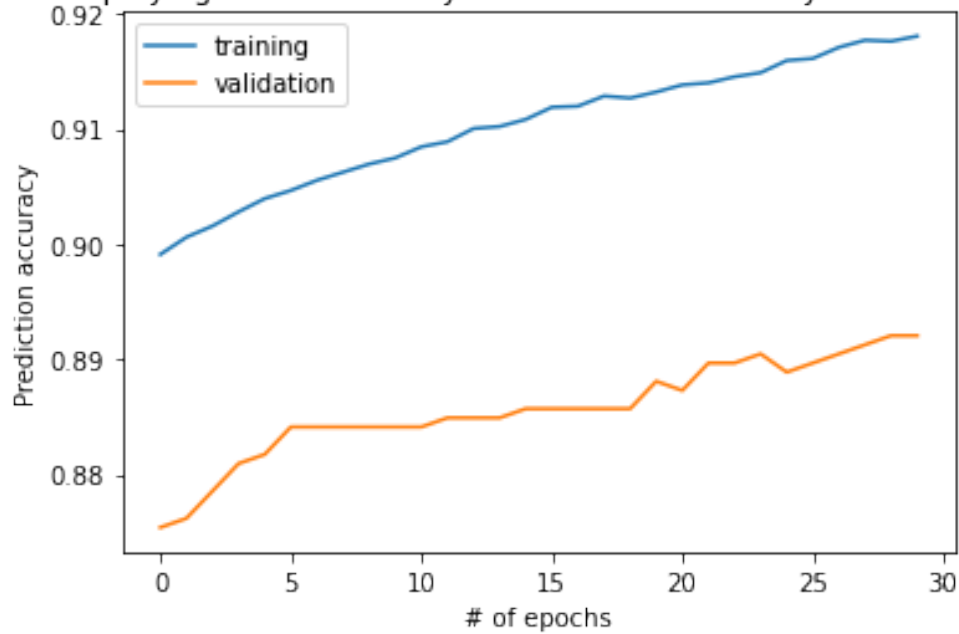
#Printing the keys of the test model dict to see what variables to plot
print(model_test.model_test.keys())

#Creating prediction and testing plot for comparison
plt.plot(model_test.model_test['accuracy'])
plt.plot(model_test.model_test['val_accuracy'])
plt.legend(['training', 'validation'])
plt.xlabel('# of epochs')
plt.ylabel('Prediction accuracy')
plt.title('Plot displaying model accuracy of NN with 1 hidden layer and 50
            ↳nodes')
plt.show()

#Printing accuracy of model
print('Test accuracy: ', np.round(prediction_correctness,3))

dict_keys(['loss', 'accuracy', 'val_loss', 'val_accuracy'])
```


Plot displaying model accuracy of NN with 1 hidden layer and 100 nodes



Test accuracy: 0.911

1.2 1 hidden layer with 500 nodes

```
[11]: # Creating a single hidden layer with 500 nodes
nn5 = Sequential()
## 2 hidden layers with 50 nodes each
nn5 = Sequential([
    Dense(500, activation = 'sigmoid', input_shape = (784,)),
    Dense(10, activation = 'softmax')
])
nn5.summary()
```

Model: "sequential_6"

Layer (type)	Output Shape	Param #
dense_8 (Dense)	(None, 500)	392500
dense_9 (Dense)	(None, 10)	5010

Total params: 397,510

Trainable params: 397,510

Non-trainable params: 0

```

[12]: # Compiling previously defined model
nn5.compile(metrics=['accuracy'], optimizer="sgd",
            ↪loss='categorical_crossentropy')

#Using 10% of the sample size of testingvalidation
model_test = nn5.fit(Train_A, Train_y, batch_size=128, epochs=30,
            ↪verbose=False, validation_split=.1)
loss, prediction_correctness = nn5.evaluate(Test_A, Test_y)

#Printing the keys of the test model dict to see what variables to plot
print(model_test.model_test.keys())

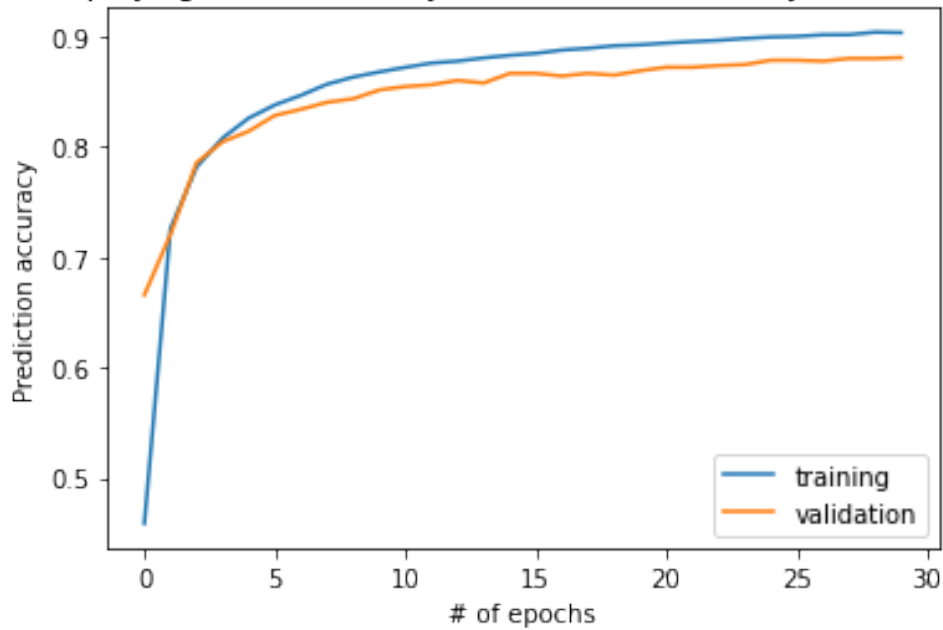
#Creating prediction and testing plot for comparison
plt.plot(model_test.model_test['accuracy'])
plt.plot(model_test.model_test['val_accuracy'])
plt.legend(['training', 'validation'])
plt.xlabel('# of epochs')
plt.ylabel('Prediction accuracy')
plt.title('Plot displaying model accuracy of NN with 1 hidden layer and 50
            ↪nodes')
plt.show()

#Printing accuracy of model
print('Test accuracy: ', np.round(prediction_correctness,3))

```

```
dict_keys(['loss', 'accuracy', 'val_loss', 'val_accuracy'])
```

Plot displaying model accuracy of NN with 1 hidden layer and 500 nodes



Test accuracy: 0.905

1.3 1 hidden layer with 1000 nodes

```
[6]: # Creating a single hidden layer with 1000 nodes
nn6 = Sequential()
## 2 hidden layers with 50 nodes each
nn6 = Sequential([
    Dense(1000, activation = 'sigmoid', input_shape = (784,)),
    Dense(10, activation = 'softmax')
])
nn6.summary()
```

Model: "sequential_1"

Layer (type)	Output Shape	Param #
dense (Dense)	(None, 1000)	785000
dense_1 (Dense)	(None, 10)	10010

Total params: 795,010
 Trainable params: 795,010
 Non-trainable params: 0

```

[7]: # Compiling previously defined model
nn6.compile(metrics=['accuracy'], optimizer="sgd",
    ↪loss='categorical_crossentropy')

#Using 10% of the sample size of testingvalidation
model_test = nn6.fit(Train_A, Train_y, batch_size=128, epochs=30,
    ↪verbose=False, validation_split=.1)
loss, prediction_correctness = nn6.evaluate(Test_A, Test_y)

#Printing the keys of the test model dict to see what variables to plot
print(model_test.model_test.keys())

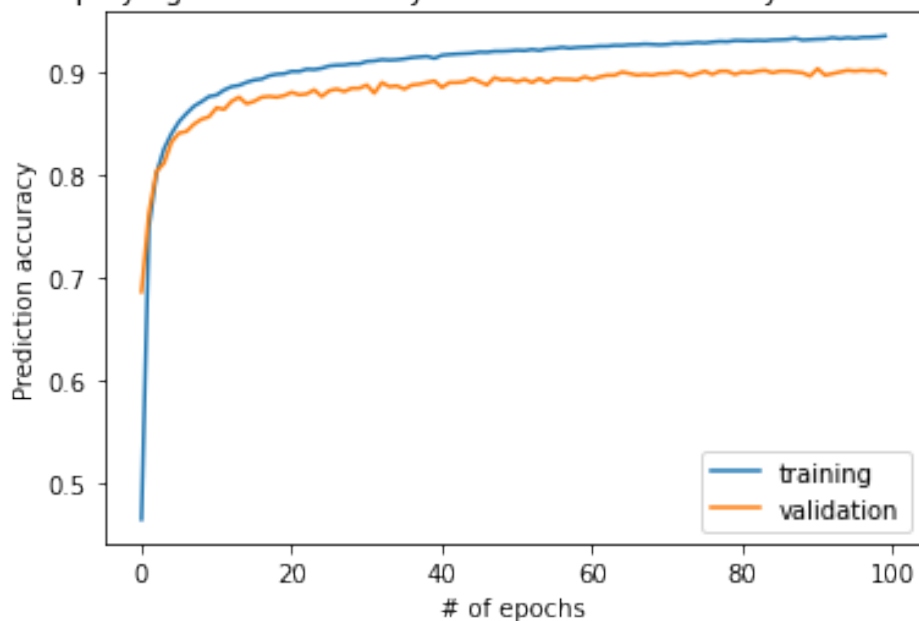
#Creating prediction and testing plot for comparison
plt.plot(model_test.model_test['accuracy'])
plt.plot(model_test.model_test['val_accuracy'])
plt.legend(['training', 'validation'])
plt.xlabel('# of epochs')
plt.ylabel('Prediction accuracy')
plt.title('Plot displaying model accuracy of NN with 1 hidden layer and 50
    ↪nodes')
plt.show()

#Printing accuracy of model
print('Test accuracy: ', np.round(prediction_correctness,3))

```

```
dict_keys(['loss', 'accuracy', 'val_loss', 'val_accuracy'])
```

Plot displaying model accuracy of NN with 1 hidden layer and 1000 nodes



Test accuracy: 0.919

1.4 Testing to find the best accuracy model

```
[12]: # Creating a single hidden layer with 32 nodes
nn7 = Sequential()
## 2 hidden layers with 50 nodes each
nn7 = Sequential([
    Dense(90, activation = 'sigmoid', input_shape = (784,)),
    Dense(10, activation = 'softmax')
])
nn7.summary()
```

Model: "sequential_5"

Layer (type)	Output Shape	Param #
dense_4 (Dense)	(None, 90)	70650
dense_5 (Dense)	(None, 10)	910
Total params: 71,560		
Trainable params: 71,560		
Non-trainable params: 0		

```
[13]: # Compiling previously defined model
nn7.compile(metrics=['accuracy'], optimizer="sgd",
            ↪loss='categorical_crossentropy')

#Using 10% of the sample size of testingvalidation
model_test = nn7.fit(Train_A, Train_y, batch_size=128, epochs=30,
            ↪verbose=False, validation_split=.1)
loss, prediction_correctness = nn7.evaluate(Test_A, Test_y)

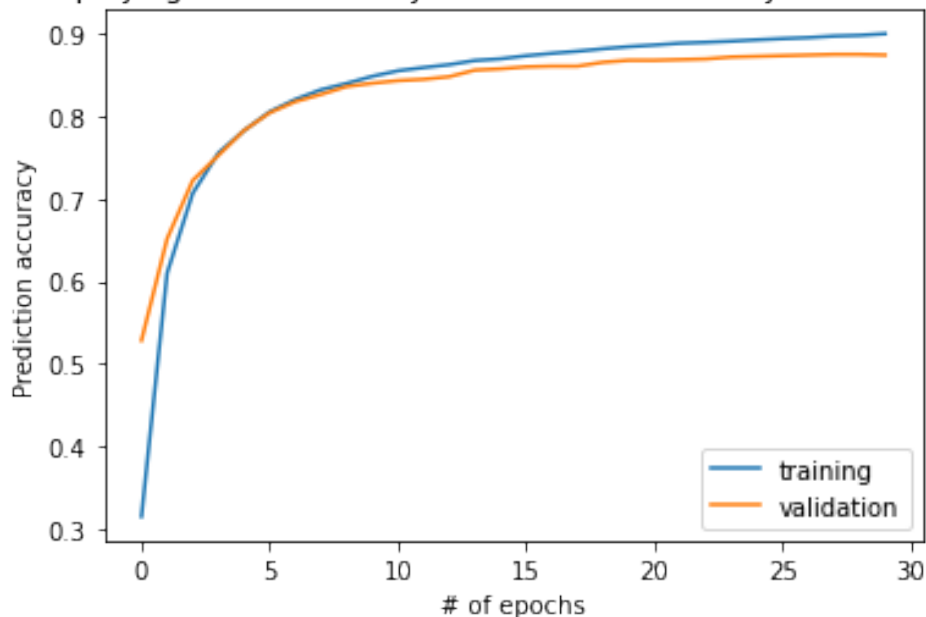
#Printing the keys of the test model dict to see what variables to plot
print(model_test.model_test.keys())

#Creating prediction and testing plot for comparison
plt.plot(model_test.model_test['accuracy'])
plt.plot(model_test.model_test['val_accuracy'])
plt.legend(['training', 'validation'])
plt.xlabel('# of epochs')
plt.ylabel('Prediction accuracy')
plt.title('Plot displaying model accuracy of NN with 1 hidden layer and 50
            ↪nodes')
plt.show()

#Printing accuracy of model
print('Test accuracy: ', np.round(prediction_correctness,3))
```

```
dict_keys(['loss', 'accuracy', 'val_loss', 'val_accuracy'])
```

Plot displaying model accuracy of NN with 1 hidden layer and 1000 nodes



Test accuracy: 0.896

```
[16]: # Creating a single hidden layer with 32 nodes
nn8 = Sequential()
## 3 hidden layers with different nodes each
nn8 = Sequential([
    Dense(800, activation = 'sigmoid', input_shape = (784,)),
    Dense(300, activation = 'relu', input_shape = (784,)),
    Dense(300, activation = 'sigmoid', input_shape = (784,)),
    Dense(10, activation = 'softmax')
])
nn8.summary()
```

Model: "sequential_12"

Layer (type)	Output Shape	Param #
dense_17 (Dense)	(None, 800)	628000
dense_18 (Dense)	(None, 300)	240300
dense_19 (Dense)	(None, 300)	90300
dense_20 (Dense)	(None, 10)	3010

Total params: 961,610
Trainable params: 961,610
Non-trainable params: 0

```
[19]: # Compiling previously defined model
nn8.compile(metrics=['accuracy'], optimizer="sgd",
    ↳loss='categorical_crossentropy')

#Using 10% of the sample size of testingvalidation
model_test = nn8.fit(Train_A, Train_y, batch_size=128, epochs=30,
    ↳verbose=False, validation_split=.1)
loss, prediction_correctness = nn8.evaluate(Test_A, Test_y)

#Printing the keys of the test model dict to see what variables to plot
print(model_test.model_test.keys())

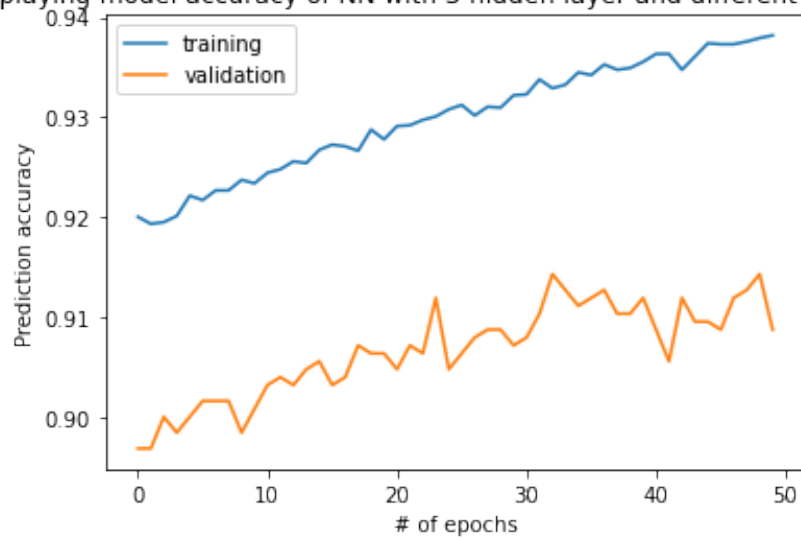
#Creating prediction and testing plot for comparison
plt.plot(model_test.model_test['accuracy'])
```

```
plt.plot(model_test.model_test['val_accuracy'])
plt.legend(['training', 'validation'])
plt.xlabel('# of epochs')
plt.ylabel('Prediction accuracy')
plt.title('Plot displaying model accuracy of NN with 1 hidden layer and 50_
↳nodes')
plt.show()

#Printing accuracy of model
print('Test accuracy: ', np.round(prediction_correctness,3))
```

dict_keys(['loss', 'accuracy', 'val_loss', 'val_accuracy'])

Plot displaying model accuracy of NN with 3 hidden layer and different nodes per layer



Test accuracy: 0.92