

# Digital Image Processing

## Introduction

Erchan Aptoula

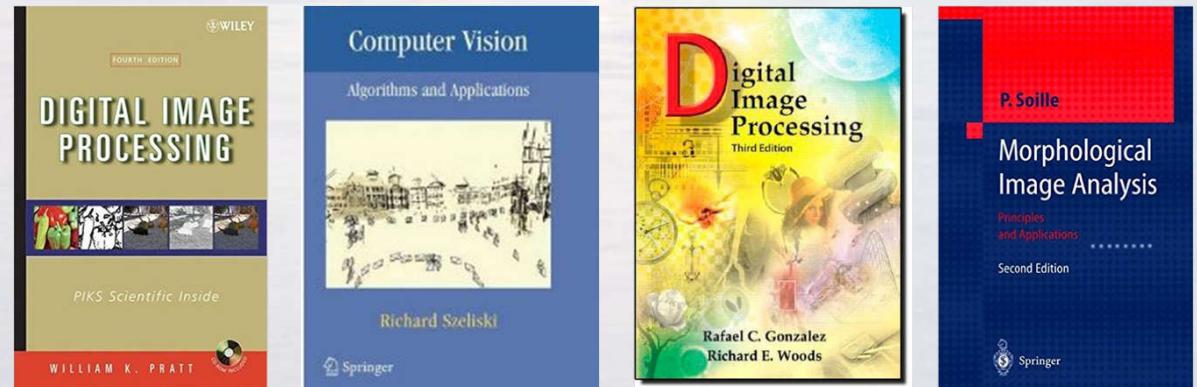
Spring 2016-2017

## Contact

- Office #253; only at office hours.
- Faster responses through email: [eaptoula@gtu.edu.tr](mailto:eaptoula@gtu.edu.tr)
- All course related communication will run through moodle.

## Popular textbooks

- R. Gonzalez & R. Woods, Digital image processing, 3<sup>r</sup> ed. 2008.
- W. K. Pratt, Introduction to digital image processing, 4<sup>th</sup> ed. 2007
- R. Szeliski, Computer vision: algorithms and applications, 2010
- P. Soille, Morphological image analysis, 2004



## Introduction

- Grading

|              | Undergraduates | Graduates |
|--------------|----------------|-----------|
| Homework     | 30%            | 30%       |
| Midterm      | 30%            | 25%       |
| Final Exam   | 30%            | 25%       |
| Presentation | 10%            | 20%       |

- Attendance is mandatory.
- Plagiarism will be **punished**.
- Late arrivals are not allowed.

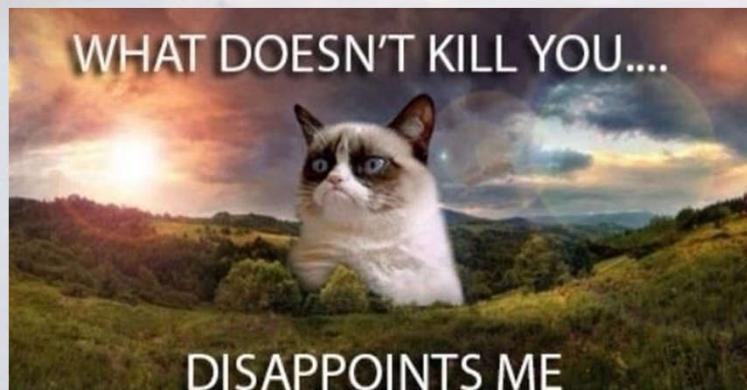
| AA     | BA    | BB    | CB    | CC    | DC    | DD    | FF   |
|--------|-------|-------|-------|-------|-------|-------|------|
| 100-90 | 89-80 | 79-70 | 69-60 | 59-50 | 49-45 | 44-40 | 39-0 |

## Course objectives **are...**

- To provide an introduction to the principles of digital image processing
- To provide an insight into digital image analysis
- To teach the use and properties of basic digital image processing/analysis tools
- To prepare you for the computer vision course

## Course objectives **are NOT...**

- To teach you photoshop/coreldraw/autocad
- To teach you digital painting/drawing



## Requirements

- Linear algebra
  - Matrices, matrix operations
  - Systems of linear equations
  - Eigenvalues, eigenvectors
- Statistics and probability
  - Probability density function
  - Mean, variance, co-variance
  - Gaussian distribution
- Programming skills (Java | C/C++/OpenCV | Matlab)

**Digital image processing is about processing digital images;  
i.e. an image stored in a digital medium.**

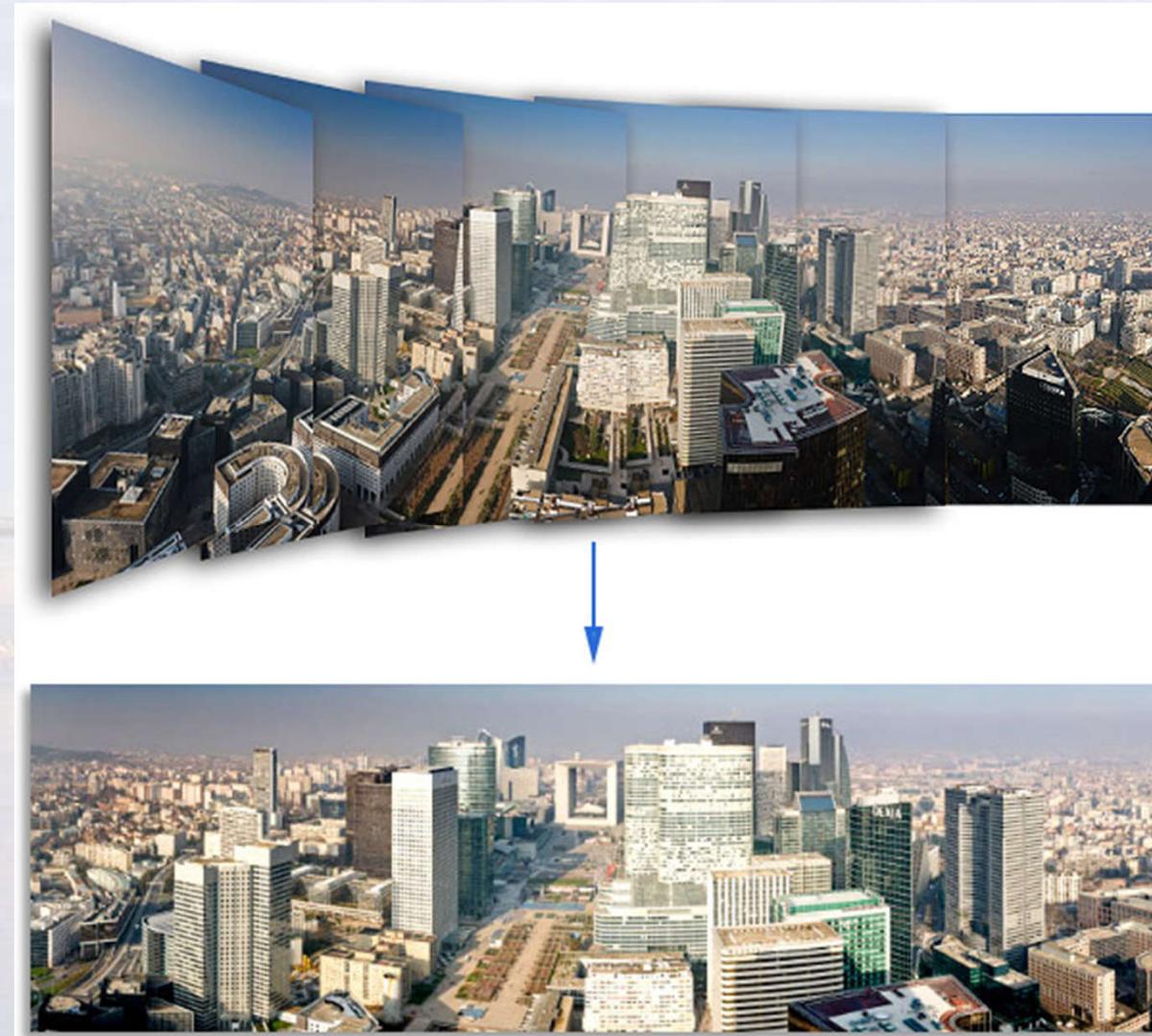


And why process digital images?

- Acquisition: color balance correction
  - Display or printing: color mapping, gamma-correction, half-toning
  - Storage/transmission: compression
  - Enhancement/restoration: noise reduction
  - Information extraction: content description
- etc.

# Introduction – image processing examples

Image stitching



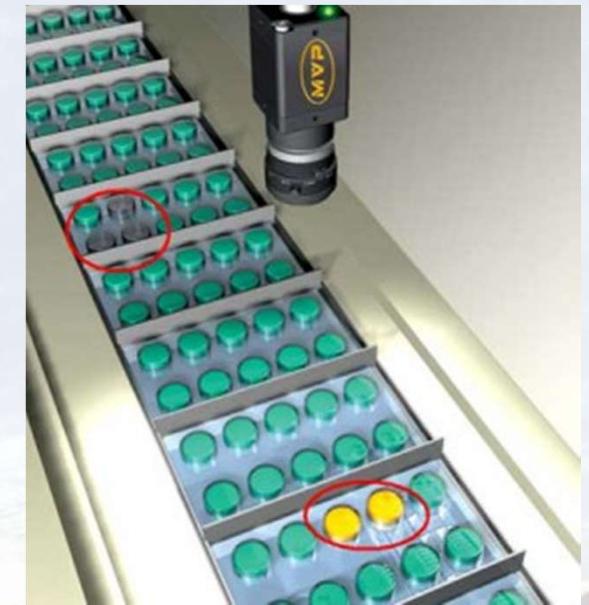
## Introduction – image processing examples

### Image restoration



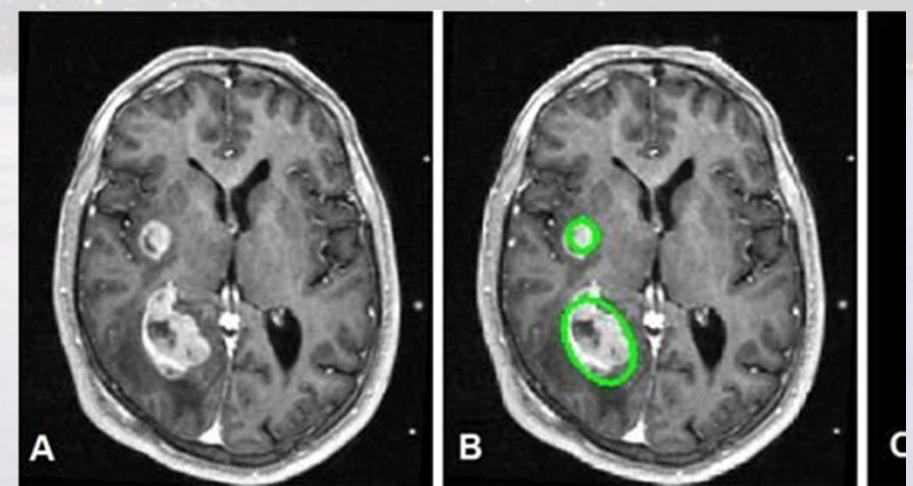
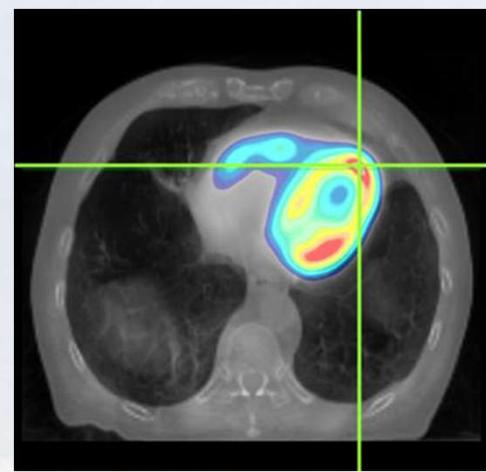
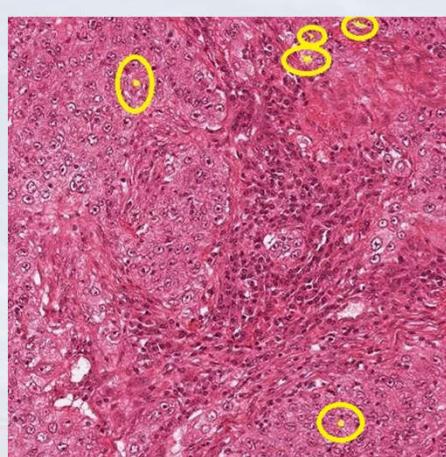
# Introduction – image processing examples

## Automated visual industrial inspection



# Introduction – image processing examples

## (Bio)Medical image processing



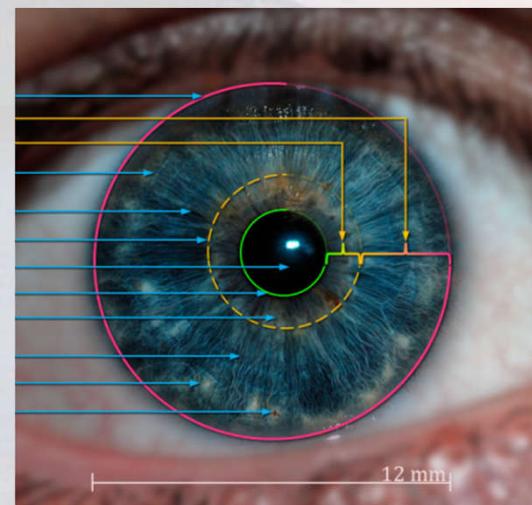
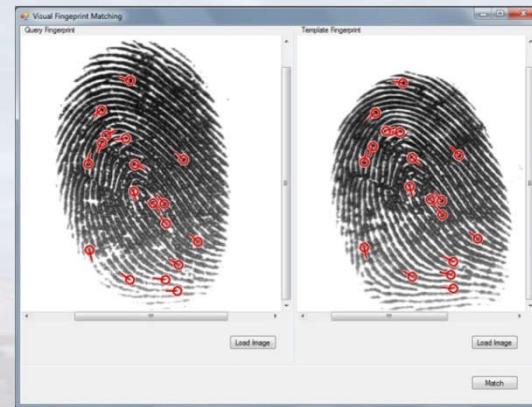
# Introduction – image processing examples

## Autonomous vehicles



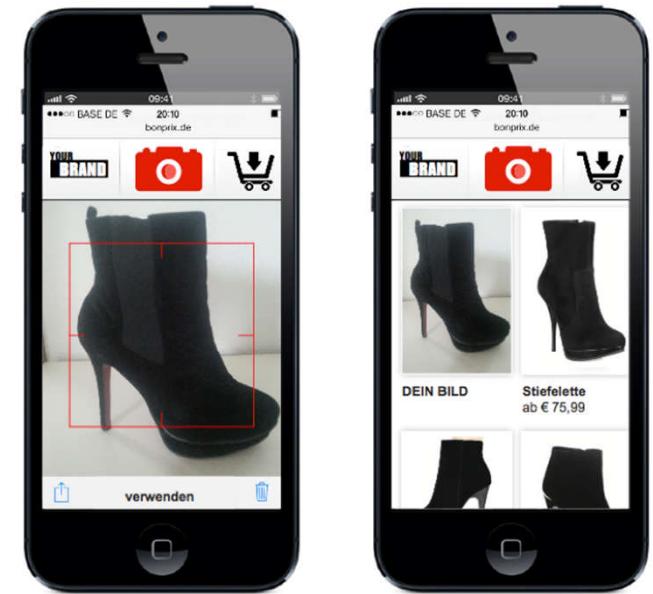
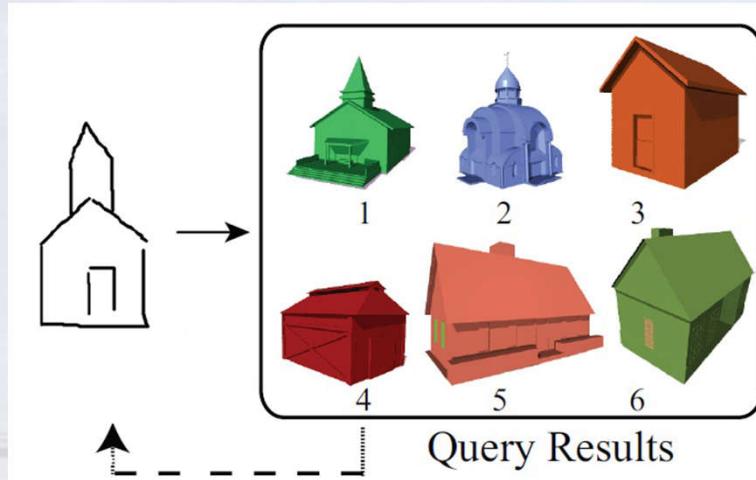
# Introduction – image processing examples

## Biometrics and forensics



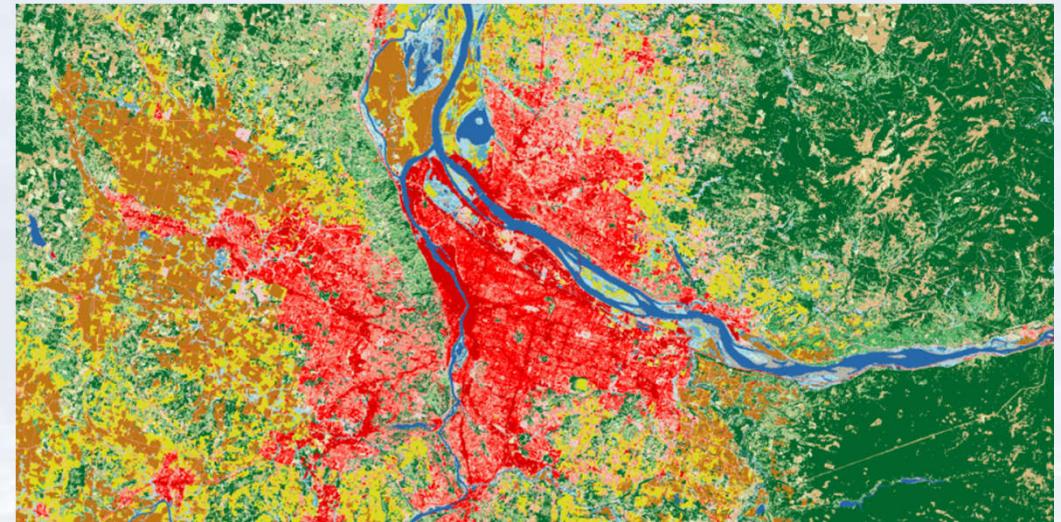
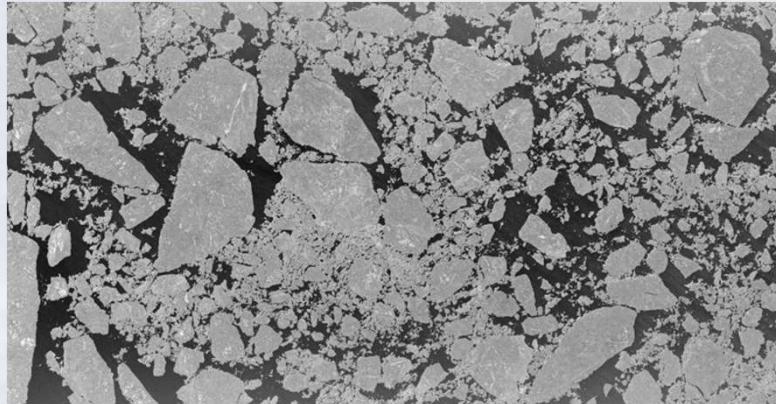
# Introduction – image processing examples

## Content based image retrieval

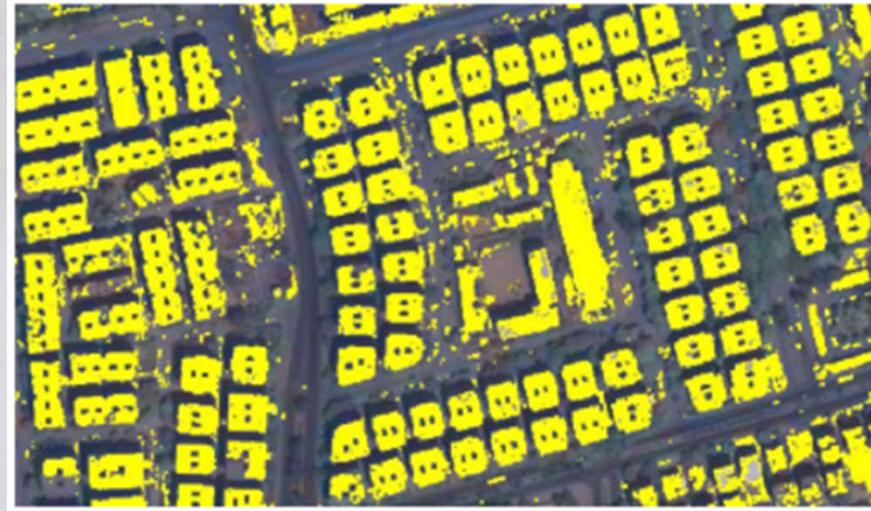


# Introduction – image processing examples

Remote sensing

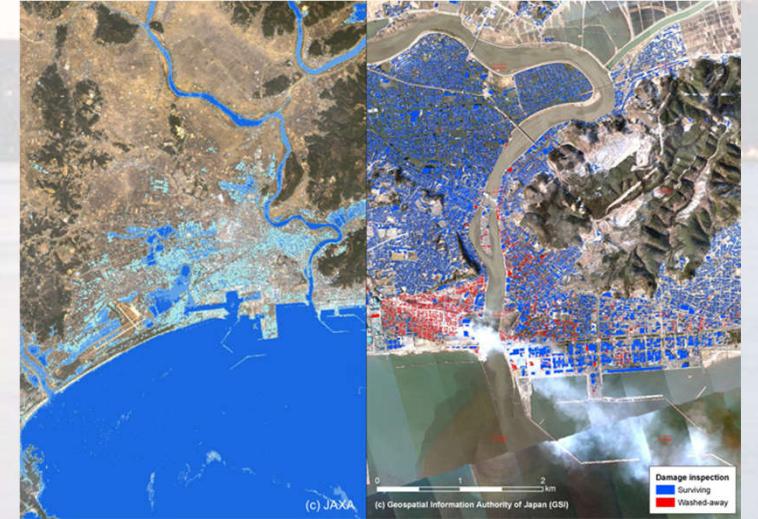


Environmental monitoring



Building detection

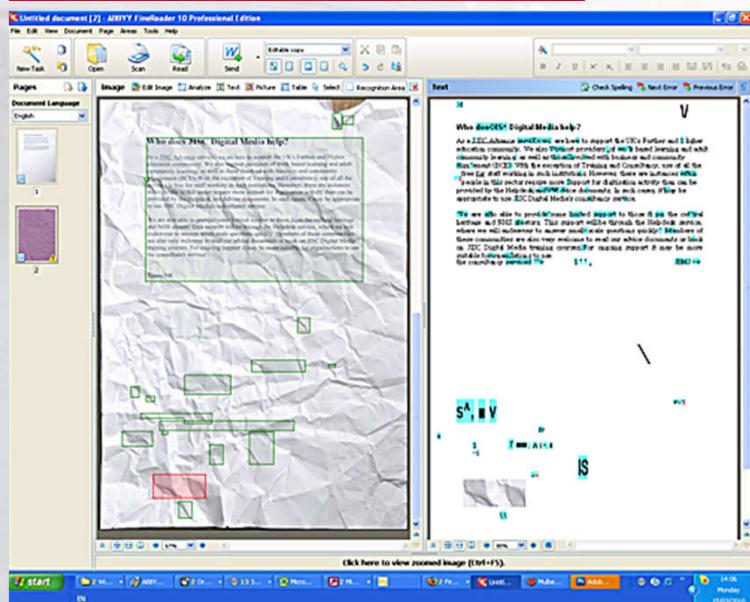
Landcover classification



Disaster management

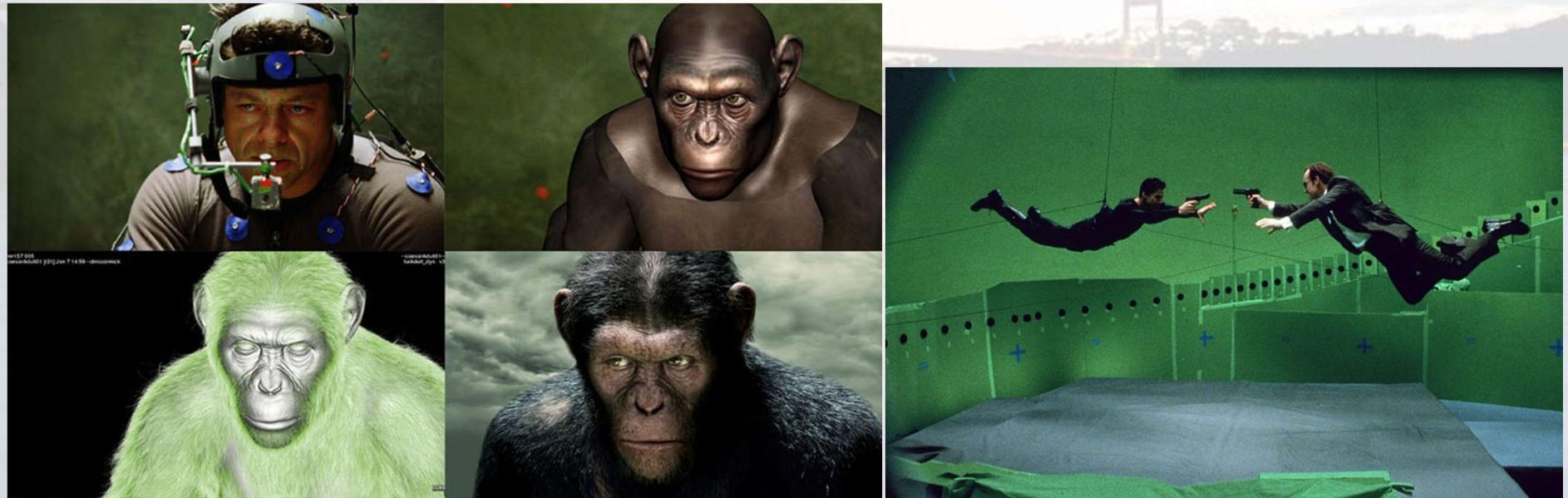
# Introduction – image processing examples

## Optical character recognition



# Introduction – image processing examples

## Visual arts

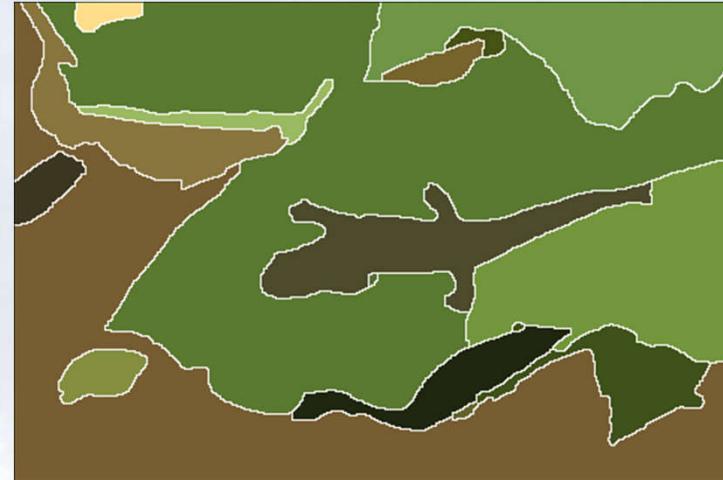


Most of the aforementioned applications involve multi-level processing.

- Low-level (~**image processing**): both input and output are **often** images
- Mid-level (~**image analysis**): aims to extract useful information from images; constructs feature vectors, computes partitions, etc.
- High-level (~**computer vision**): aims to enable machines to “see”; to recognize and perceive concepts/objects, to interpret visual data semantically.



Low-level processing: edge detection



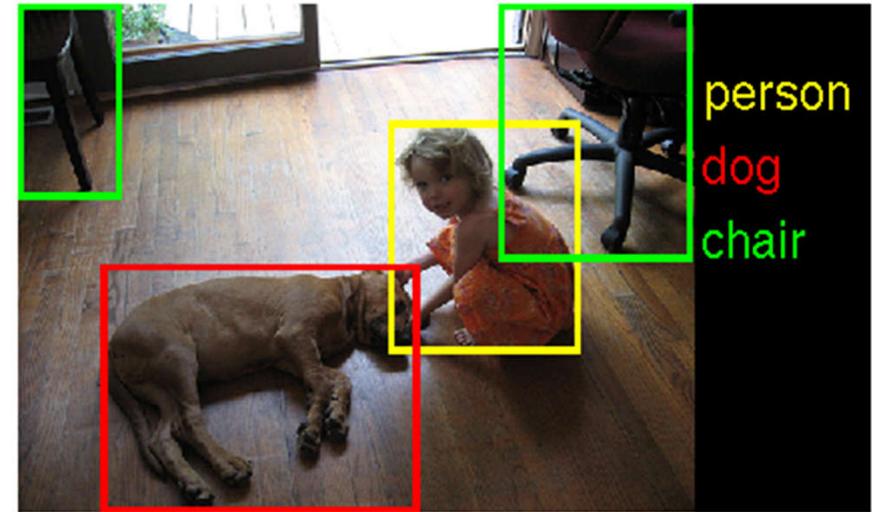
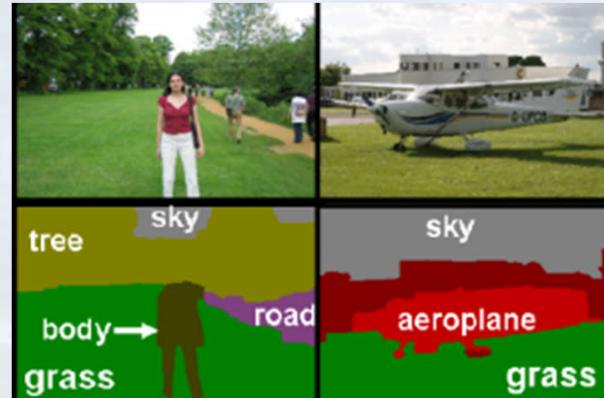
**Mid-level processing: segmentation**



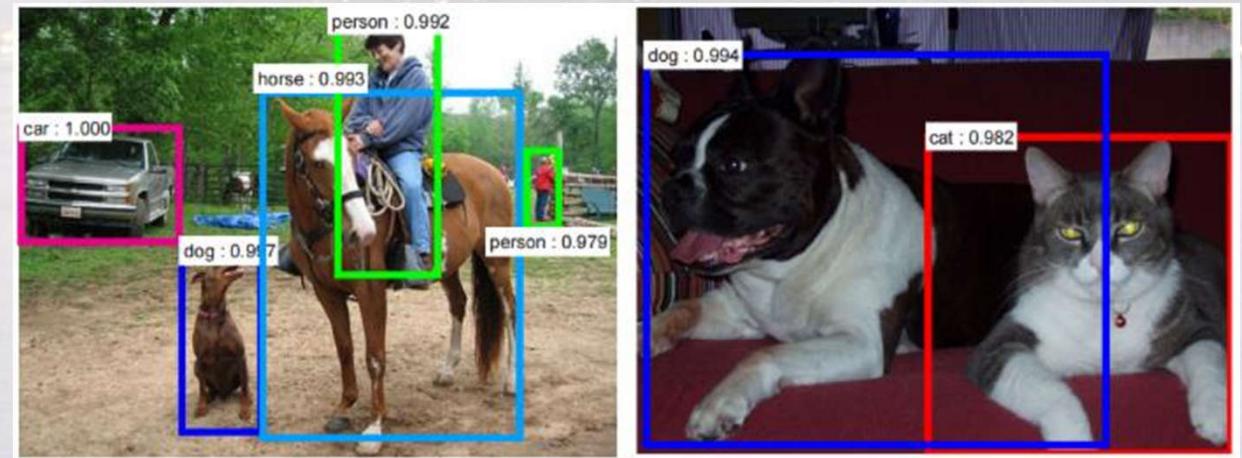
$[0.1, 0.5, 0.07, 0.55, 0.72]^T$



**Mid-level processing: feature extraction**



## High-level processing: event recognition and object categorization



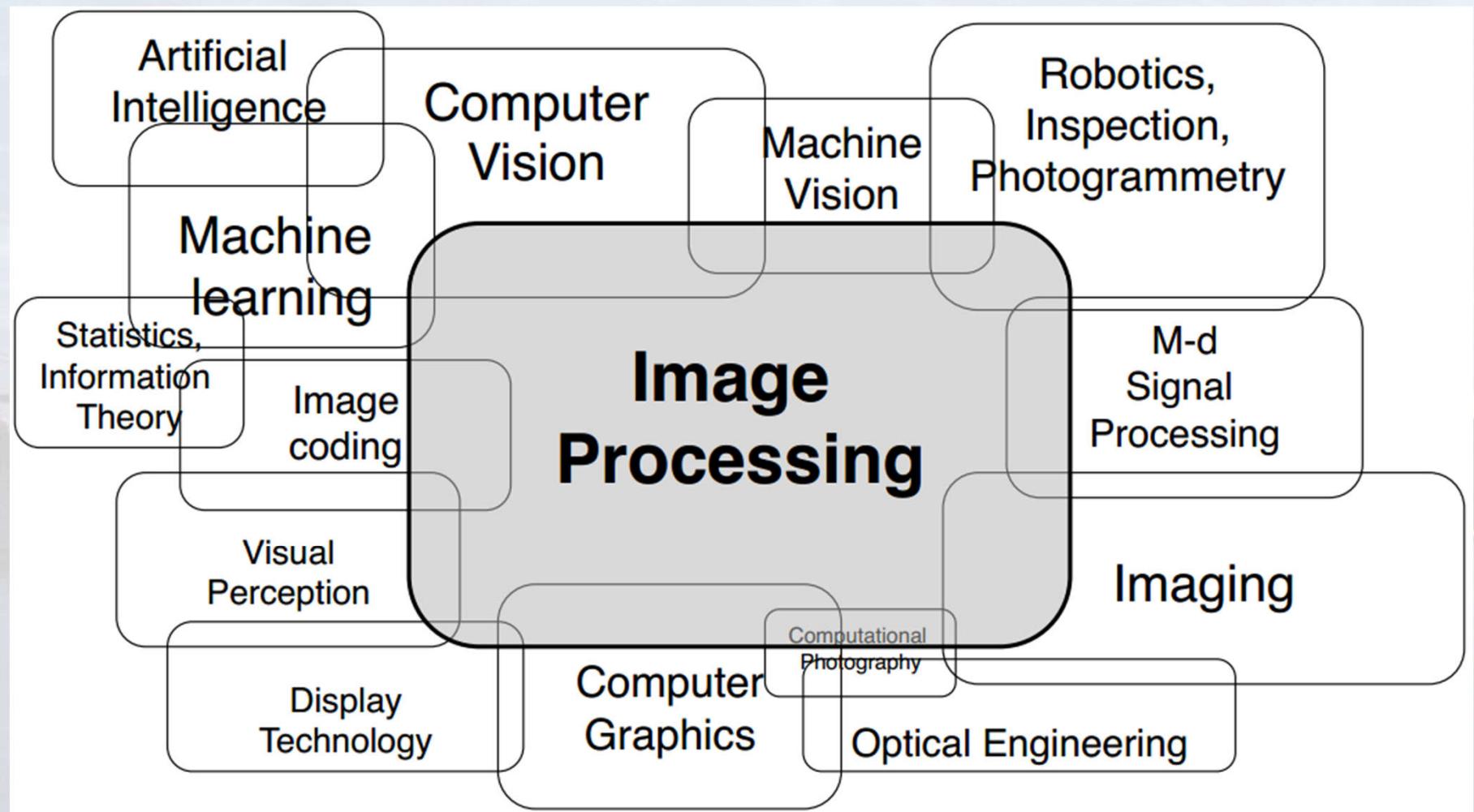


Image from Bernd Girod, Stanford

## Introduction – A tentative schedule

1. Introduction to digital image processing/analysis
2. Point processing
3. Binary image analysis
4. Spatial domain linear filtering
5. Frequency domain linear filtering
6. Non-linear filtering: mathematical morphology
7. Color image processing
8. Midterm
9. Content description
10. Case study 1
11. Segmentation
12. Case study 2
13. Student presentations
14. Case study 3

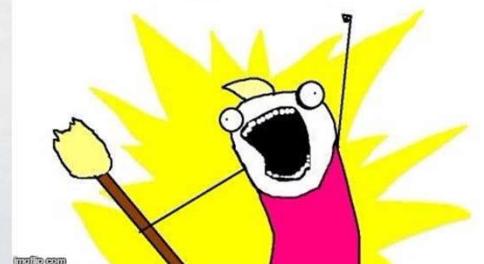
A mixture of image analysis  
and image processing

For the latest developments in this field:

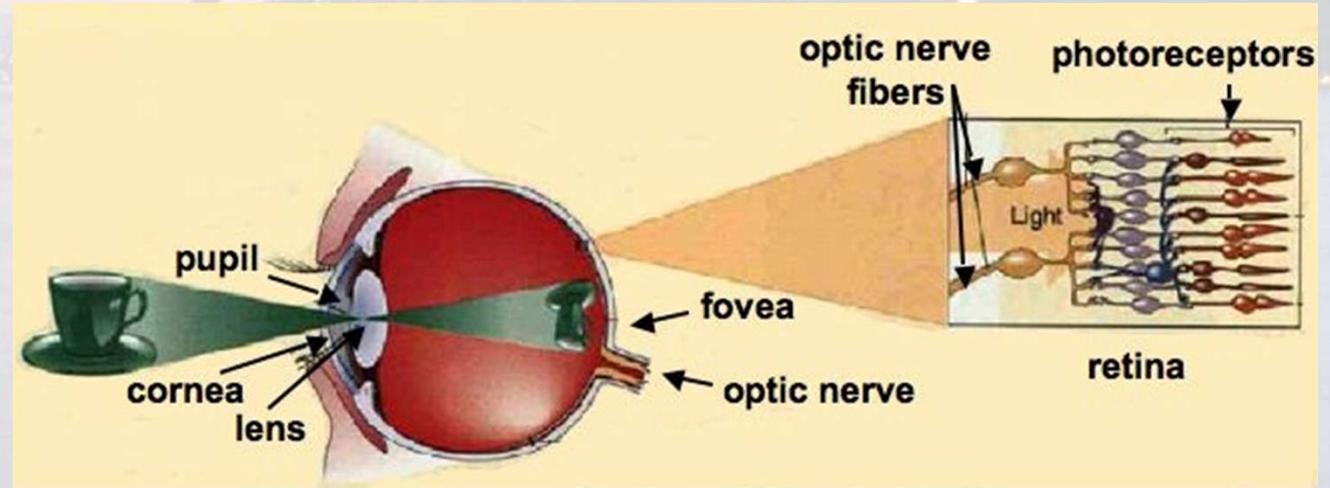
- IEEE Transactions on Image Processing
- IEEE Transactions on Pattern Analysis and Machine Intelligence
- International Journal of Computer Vision
- Pattern Recognition
- Image and Vision Computing
- Computer Vision and Image Understanding
- International Conference on Computer Vision (ICCV)
- European Conference on Computer Vision (ECCV)
- Computer Vision and Pattern Recognition Conference (CVPR)
- International Conference on Image Processing (ICIP)

etc.

**READ ALL THE ARTICLES**



- When the eye is properly focused, light from an object outside the eye is imaged on the **retina**
- There are discrete light receptors on the retina.
- They transform light into electric signals, that are subsequently sent to the visual cortex for processing.
- There are two classes of receptors: **Cones and Rods**



## Cones

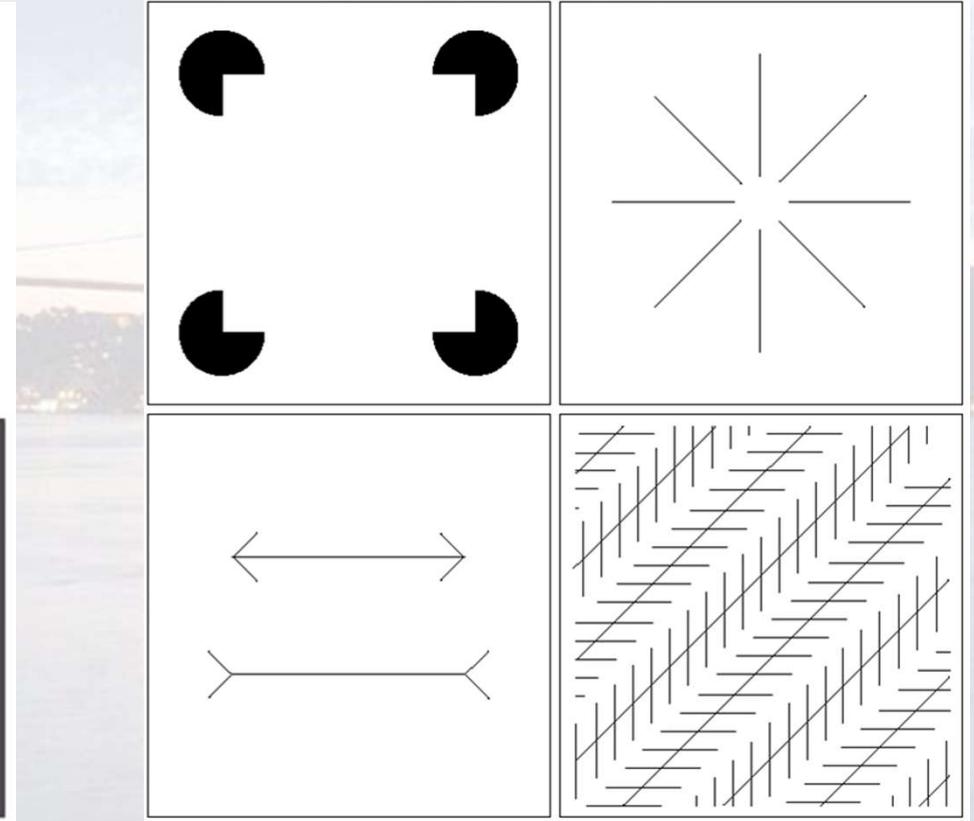
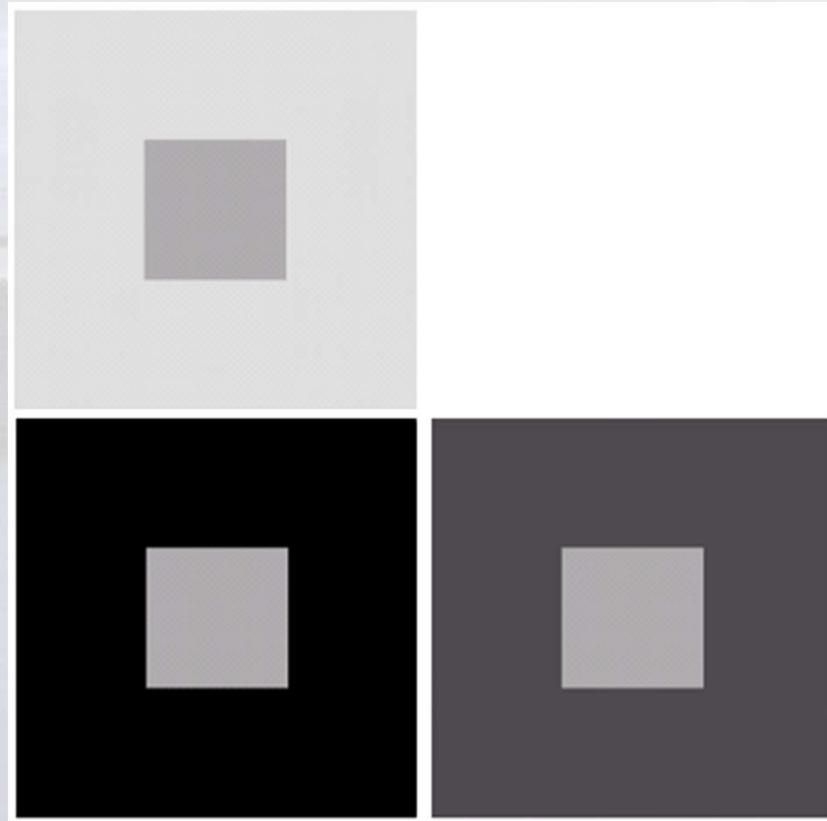
- ~6 - 7 million cells, in the central portion of retina (fovea)
- Highly sensitive to color, we can see fine details with them
- Cone vision is called photopic or bright-light vision
- Women have more than men (we'll talk about them in a few weeks)

## Rods

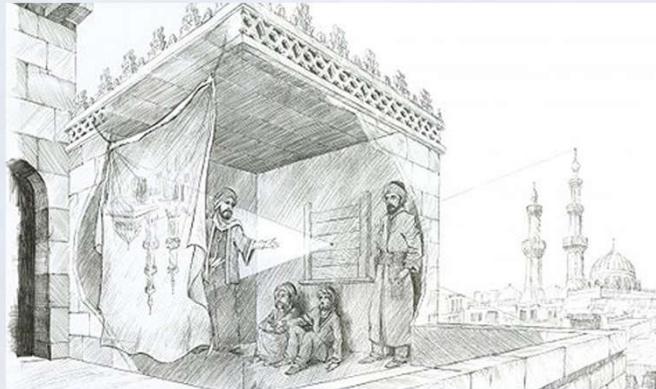
- ~75-150 million cells
- Less detail is discernible by them, they provide an overall picture of the FoV
- Sensitive to low-level illumination, rod vision is called scotopic or dim-light vision
- Men have more than women

## Wonders of the human eye

- Very high adaptation capability to brightness variations
- Perceived brightness depends on context
- Very little is known about higher human vision

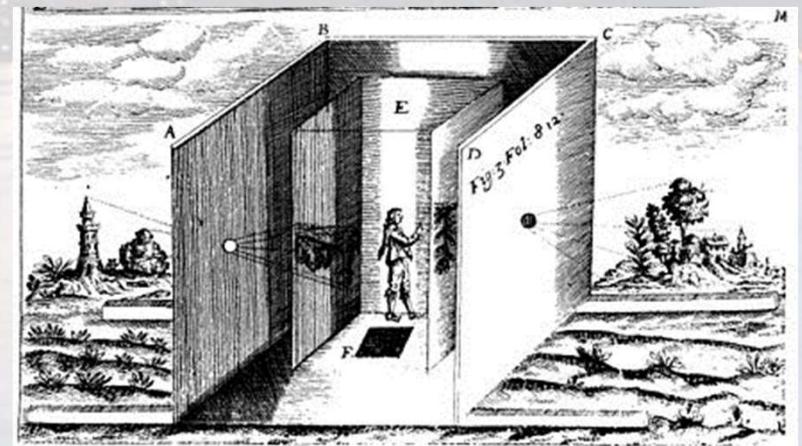


# Introduction – A short history of image acquisition



İbn-i Heysem, 10<sup>th</sup> century, author of the “Book of Optics”, inventor of the scientific method

The “camera obscura”, 16<sup>th</sup> century.

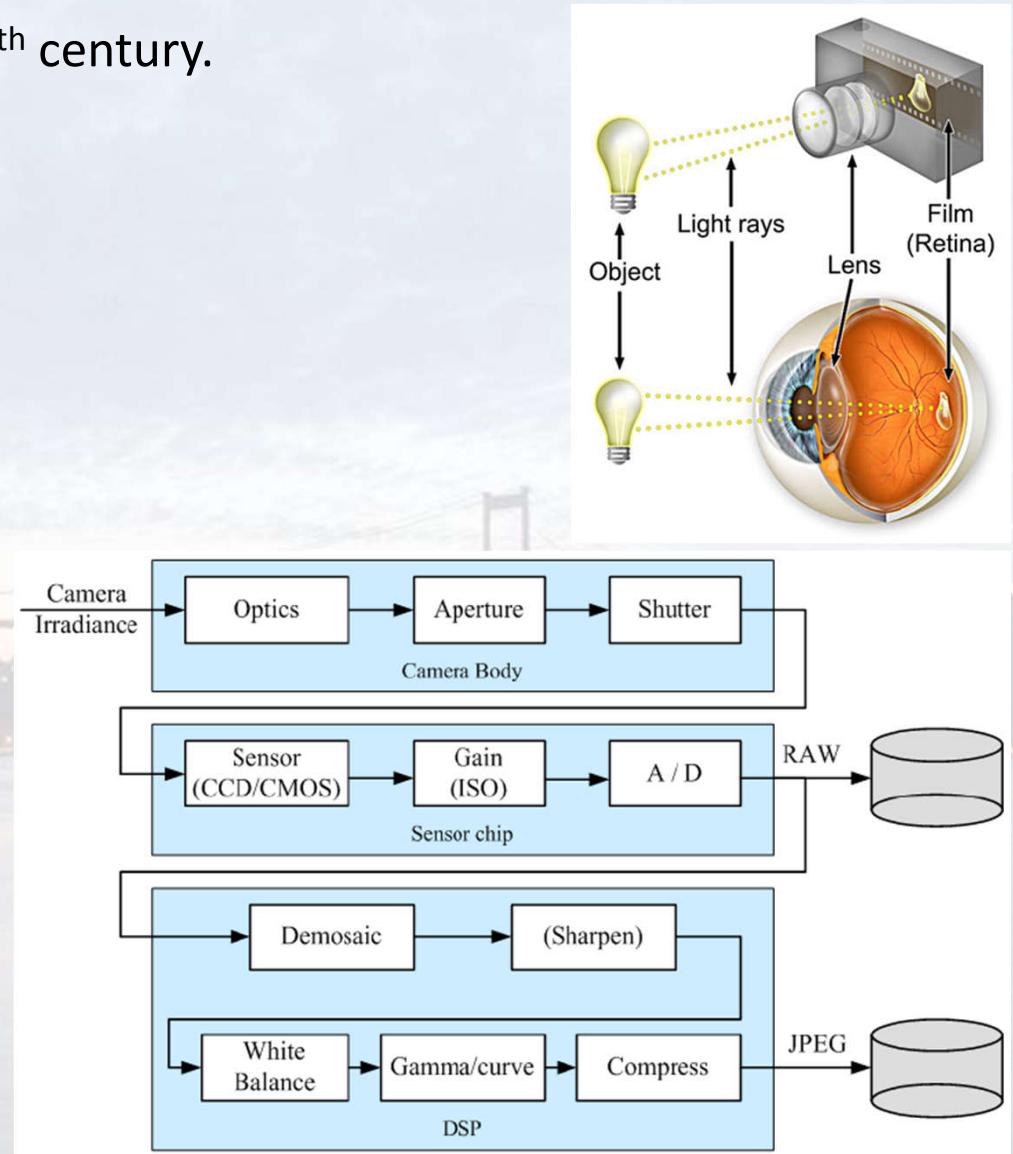


## Introduction – A short history of image acquisition

Nicéphore Niépce; first photograph, 19<sup>th</sup> century.



From analog to digital, invention of the Charged Coupled Device (CCD) in 1969 by Boyle & Smith; Physics Nobel Prize, 2009.



- A 2D **image** or a visual scene, can be modeled through a function  $f(x, y)$  where  $f$  represents the “brightness intensity or color” at location  $(x, y)$ .
- $f$  is a continuous function in both amplitude and space.



A **digital image** refers to a discretized version of  $f(x, y)$ , represented as  $f[x, y]$  in the form of a 2D array. Every element of this array is referred to as a **pixel**, and the digitized brightness value is called a **gray level**.

$$f[x, y] = \begin{bmatrix} f[0,0] & \dots & f[W, 0] \\ \vdots & \ddots & \vdots \\ f[0, H] & \dots & f[W, H] \end{bmatrix}, \text{ where } 0 \leq f[x, y] \leq G-1, \text{ and } G \text{ is a power of 2.}$$

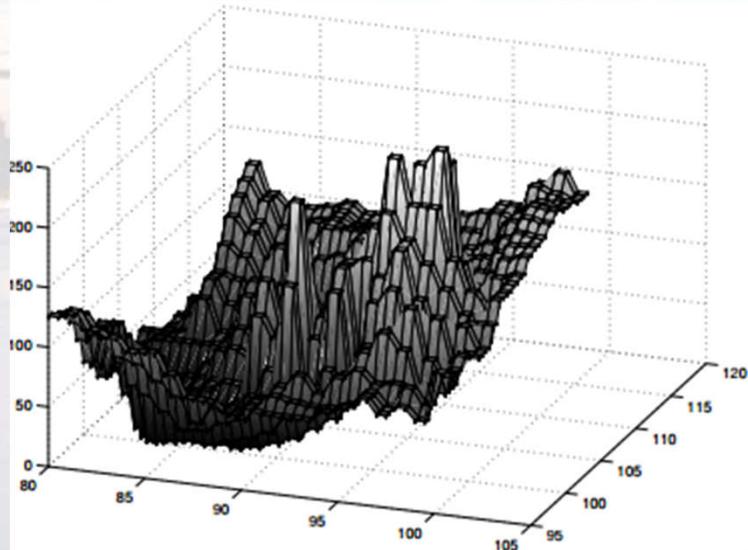
## Introduction – Image acquisition



Discrete grid

|     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |    |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|----|
| 126 | 132 | 118 | 114 | 104 | 105 | 89  | 71  | 70  | 64  | 68  | 85  | 65  | 65  | 73  | 79  | 88  | 77  | 85  | 76  |    |
| 122 | 124 | 113 | 93  | 89  | 77  | 66  | 46  | 60  | 56  | 68  | 75  | 72  | 70  | 71  | 76  | 88  | 78  | 96  | 84  |    |
| 117 | 107 | 102 | 88  | 58  | 46  | 34  | 34  | 42  | 47  | 61  | 78  | 89  | 76  | 91  | 99  | 90  | 92  | 82  | 96  |    |
| 105 | 96  | 93  | 58  | —   | —   | —   | —   | —   | 33  | 46  | 64  | 65  | 88  | 109 | 127 | 115 | 84  | 83  | —   |    |
| 85  | 100 | 70  | 77  | —   | —   | —   | —   | —   | 34  | 34  | 44  | 61  | 88  | 123 | 144 | 103 | 84  | —   | —   |    |
| 61  | 94  | 36  | —   | —   | —   | 77  | 48  | 41  | 40  | 40  | 49  | 60  | 69  | 88  | 129 | 132 | 99  | —   | —   |    |
| 52  | 89  | 32  | —   | —   | —   | 30  | 42  | 66  | 139 | 42  | 72  | 59  | 96  | 101 | 64  | 90  | 117 | 122 | —   |    |
| 38  | 73  | 30  | —   | —   | —   | 10  | 104 | 88  | 204 | 91  | 132 | 56  | 127 | 140 | 99  | 75  | 86  | 119 | —   |    |
| 39  | 61  | 56  | —   | —   | —   | 31  | 39  | 38  | 128 | 95  | 144 | 104 | 147 | 77  | 143 | 167 | 128 | 100 | 90  | 95 |
| 37  | 55  | 46  | —   | —   | —   | 33  | 62  | 56  | 94  | 59  | 77  | 75  | 146 | 150 | 191 | 170 | 152 | 133 | 114 | 92 |
| —   | —   | —   | —   | —   | —   | 46  | 53  | 73  | 64  | 78  | 84  | 120 | 172 | 232 | 194 | 194 | 152 | 128 | 116 | —  |
| 35  | 44  | 44  | 44  | 45  | 55  | 102 | 101 | 68  | 76  | 70  | 93  | 128 | 171 | 203 | 195 | 221 | 121 | 120 | 146 | —  |
| 34  | 43  | 47  | 76  | 50  | 61  | 95  | 127 | 83  | 77  | 72  | 97  | 143 | 142 | 148 | 137 | 145 | 109 | 127 | 152 | —  |
| 32  | 43  | 54  | 87  | 68  | 56  | 74  | 98  | 86  | 71  | 73  | 95  | 116 | 119 | 128 | 121 | 120 | 121 | 139 | 157 | —  |
| 37  | 61  | 87  | 83  | 61  | 58  | 70  | 76  | 81  | 95  | 110 | 123 | 126 | 128 | 120 | 125 | 127 | 146 | 164 | —   | —  |
| —   | 56  | 105 | 97  | 80  | 70  | 85  | 103 | 108 | 122 | 125 | 127 | 121 | 125 | 110 | 115 | 120 | 154 | 169 | —   | —  |
| 37  | 63  | 123 | 111 | 92  | 96  | 109 | 123 | 124 | 124 | 115 | 110 | 114 | 109 | 107 | 110 | 131 | 156 | 167 | —   | —  |
| 43  | 65  | 135 | 115 | 97  | 107 | 121 | 125 | 121 | 118 | 108 | 104 | 107 | 112 | 115 | 121 | 139 | 153 | 161 | —   | —  |
| —   | 87  | 143 | 128 | 107 | 115 | 117 | 126 | 119 | 116 | 113 | 113 | 113 | 123 | 123 | 141 | 138 | 167 | 163 | —   | —  |

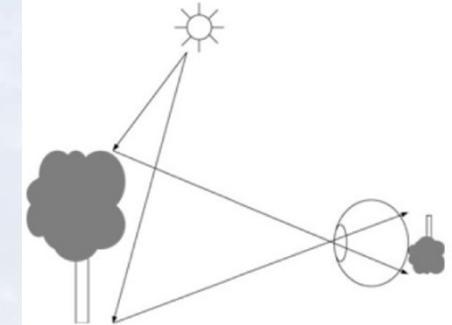
Gray values/levels



But how is the **gray level** calculated?

In short (assuming zero noise):

- 1 – An object is illuminated with light
- 2 – The light is partly absorbed and partly reflected
- 3 – The reflected photon of energy  $E_{\lambda_a}$  at wavelength  $\lambda_a$  reaches a sensor with a sensitivity curve  $s(\lambda)$
- 4 – The product  $E_{\lambda_a} \times s(\lambda_a)$  is computed and accumulated.
- 5 – The total energy collected by the sensor (during the exposure) is used in order to calculate the gray level/intensity corresponding to that sensor.



The intensities of pixels are significant only **relatively** to each other, and are **meaningless** in absolute terms. Pixel values of different images, can be compared only if either the acquisition conditions were identical, or if the images have been normalized to remove the effect of different physical processes; in which case we say the sensors have been **calibrated**.

### Example

You possess a single sensor and its sampled sensitivity. You also have (in some units) the energy amounts  $E_{\lambda_i}$  corresponding to wavelength  $\lambda_i$ . The shutter of the camera is open long enough for 5 photons to reach the sensor. The wavelengths of the photons are:  $\lambda_0, \lambda_3, \lambda_3, \lambda_0, \lambda_2$ . Calculate the value recorded by the sensor. Assume zero noise.

$$\begin{aligned}f(0,0) &= 2E_{\lambda_0} \times 0.0 + E_{\lambda_2} \times 0.2 + 3E_{\lambda_3} \times 0.3 \\&= 0.85 \times 0.2 + 2.28 \times 0.3 = 0.17 + 6.84 = 7.01\end{aligned}$$

| Wavelength  | Sensor | Energy |
|-------------|--------|--------|
| $\lambda_0$ | 0.0    | 1.00   |
| $\lambda_1$ | 0.1    | 0.95   |
| $\lambda_2$ | 0.2    | 0.85   |
| $\lambda_3$ | 0.3    | 0.76   |
| $\lambda_4$ | 0.1    | 0.66   |
| $\lambda_5$ | 0.0    | 0.59   |

## Terminology

**Radiance:** total amount of energy flowing from a light source, measure in Watts (W).

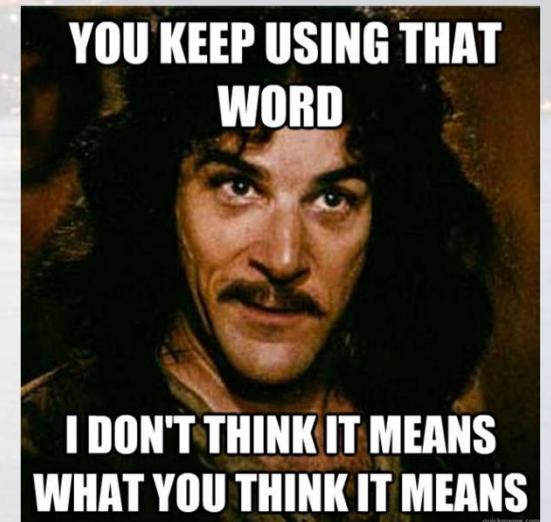
**Luminance:** the amount of energy an observer perceives from a light source; measures in lumens (lm). For instance, a radiator, radiates a lot in infrared wavelengths, but we, as observers perceive very little of it.

**Brightness:** a subjective descriptor of light perception; impossible to measure.

Wavelength  $\lambda$  (nm), frequency  $\nu$  (Hz), speed of light c:

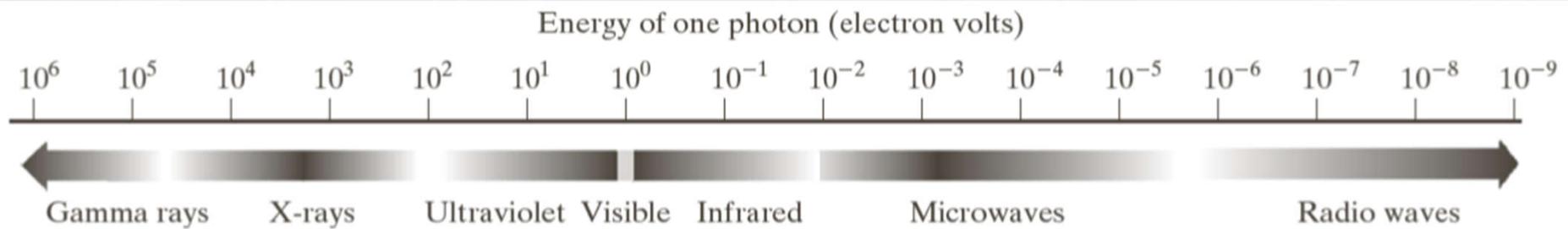
$$\lambda = \frac{c}{\nu}$$

And energy  $E = \nu h$ , with  $h$  the Planck constant.



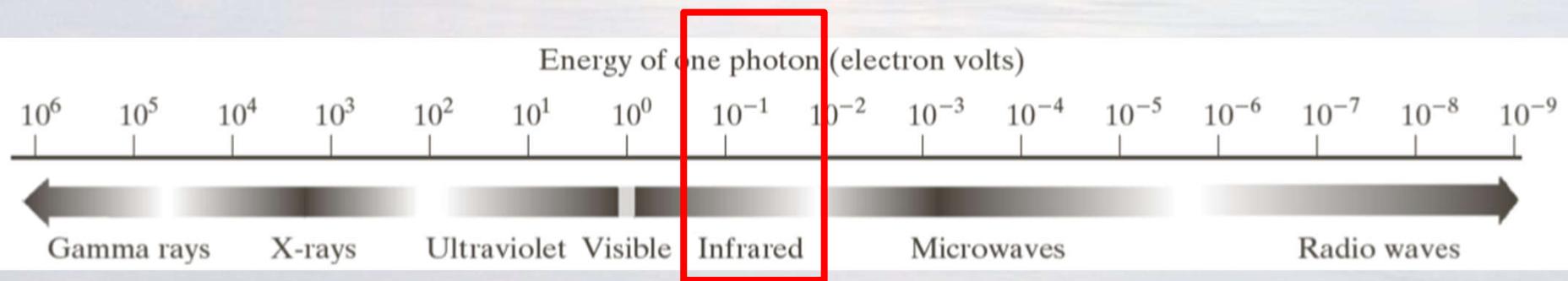
Human eyes have a sensitivity curve too, we can sense only the wavelengths between approximately 390 and 700nm; i.e. the **visible spectrum**.

For the rest, we have cameras ☺



- **Gamma-ray imaging:** nuclear medicine and astronomical observations
- **X-rays:** medical diagnostics, industry, and astronomy, etc.
- **Ultraviolet:** lithography, industrial inspection, microscopy, lasers, biological imaging, and astronomical observations
- **Visible and infrared bands:** light microscopy, astronomy, remote sensing, industry, and law enforcement
- **Microwave band:** radar
- **Radio band:** medicine (such as MRI) and astronomy

Infrared, i.e. thermal imaging; **often noisy!**

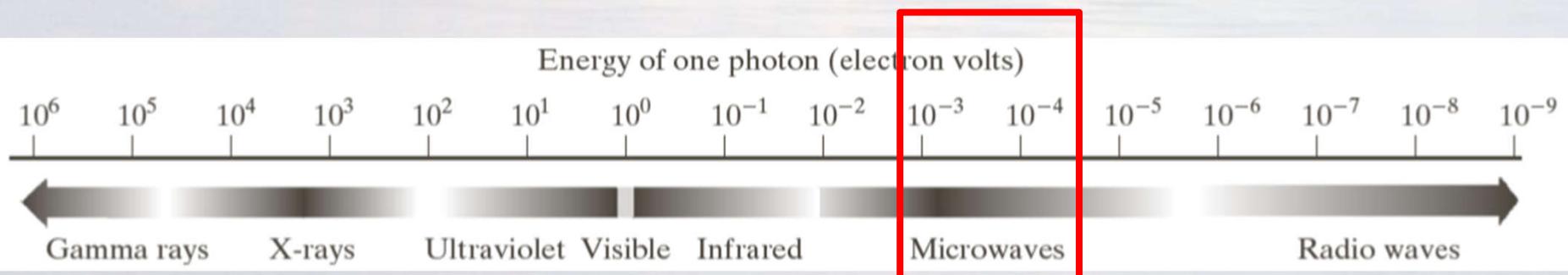
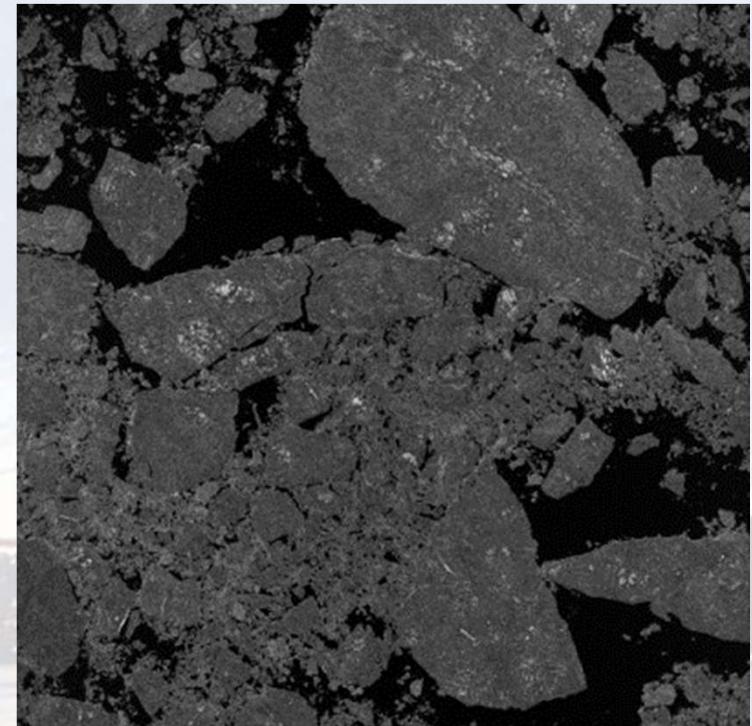


Radar imaging; synthetic aperture radar (SAR) – Göktürk 3, 2019.

Acquired using the Doppler principle.

~Unaffected by clouds or weather conditions.

Can be acquired **day or night**.



## Magnetic resonance imaging (MRI);



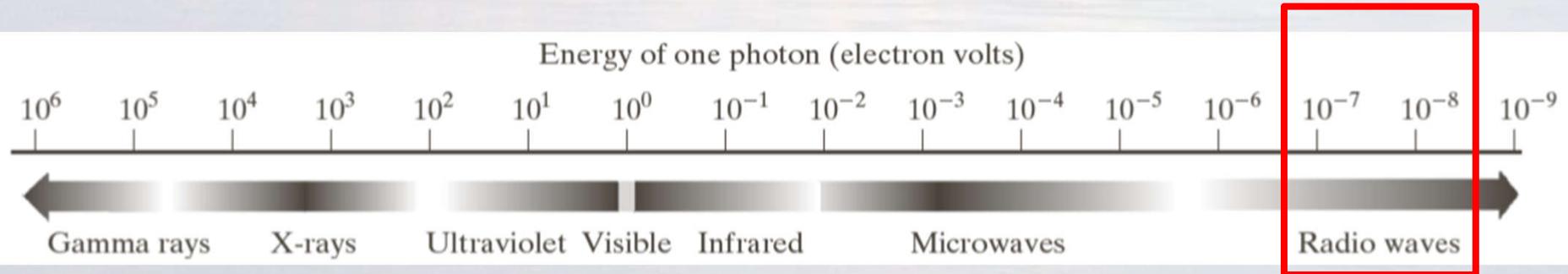
knee



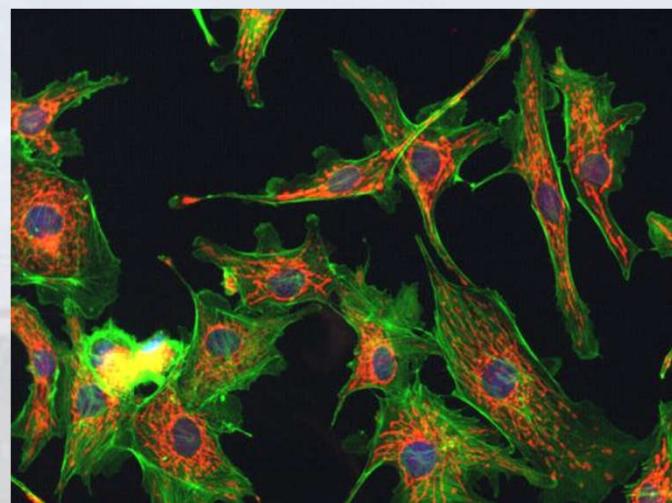
spine



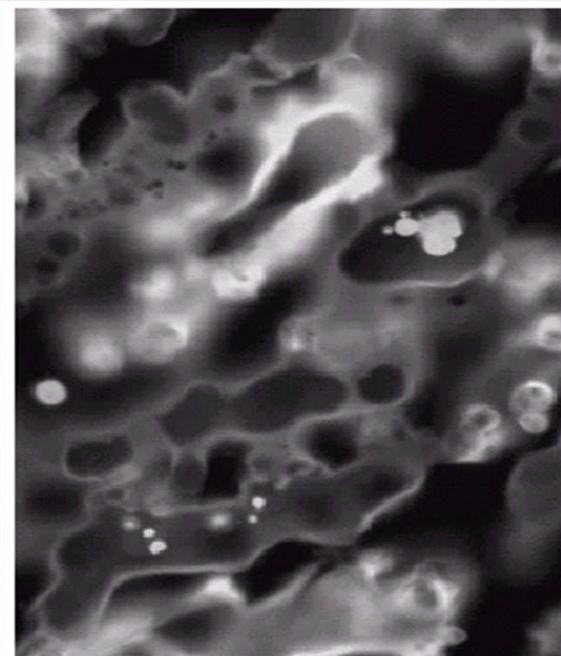
head



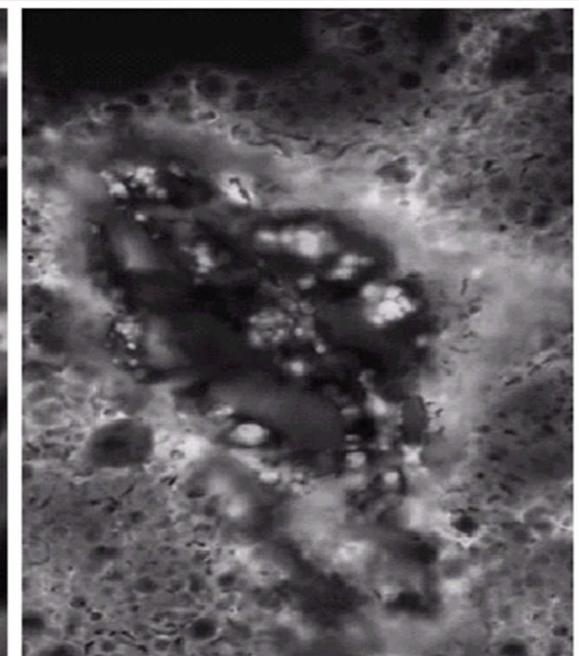
## Fluorescence microscopy imaging;



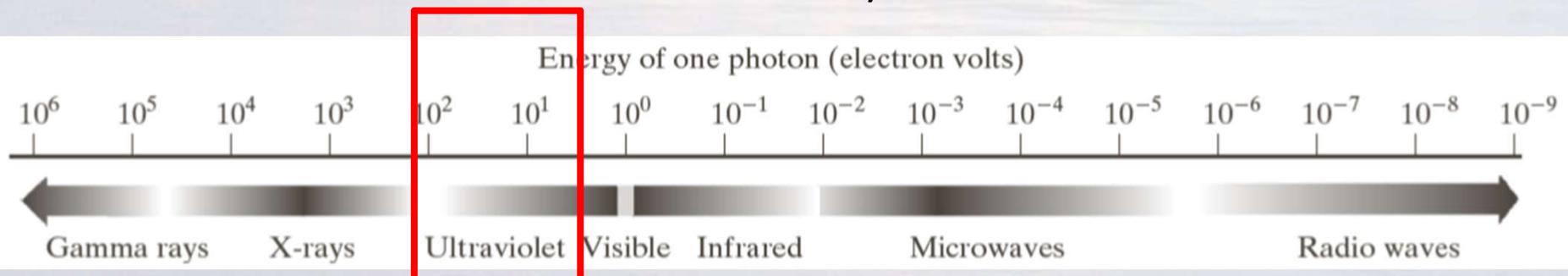
cells



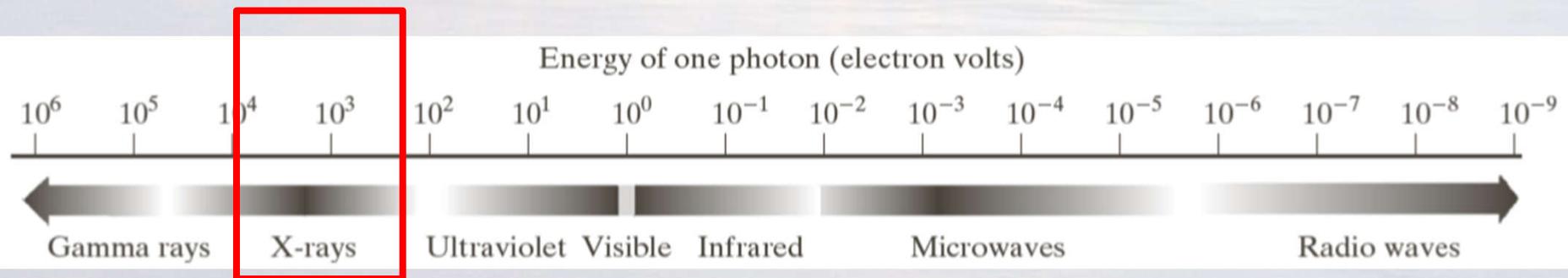
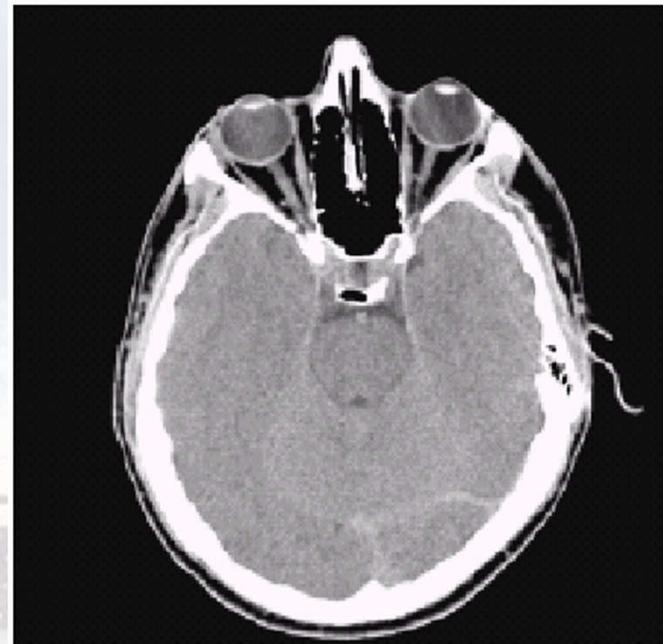
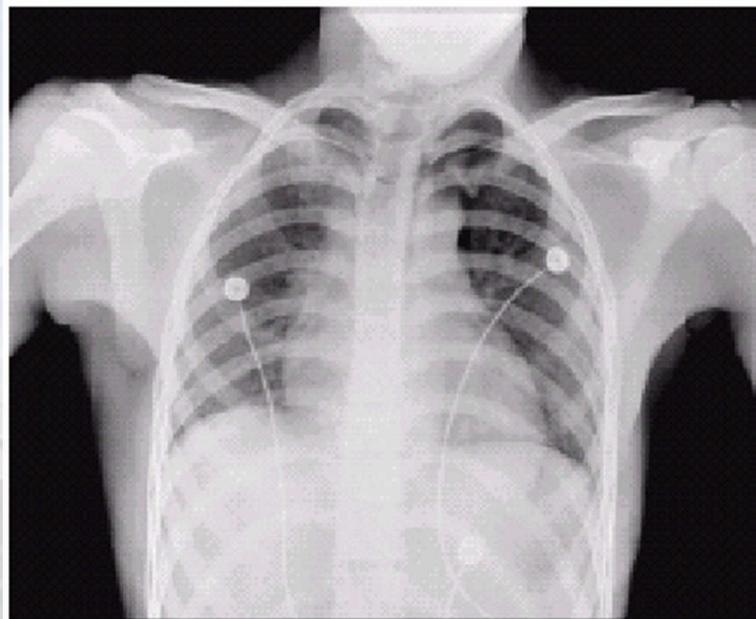
healthy corn



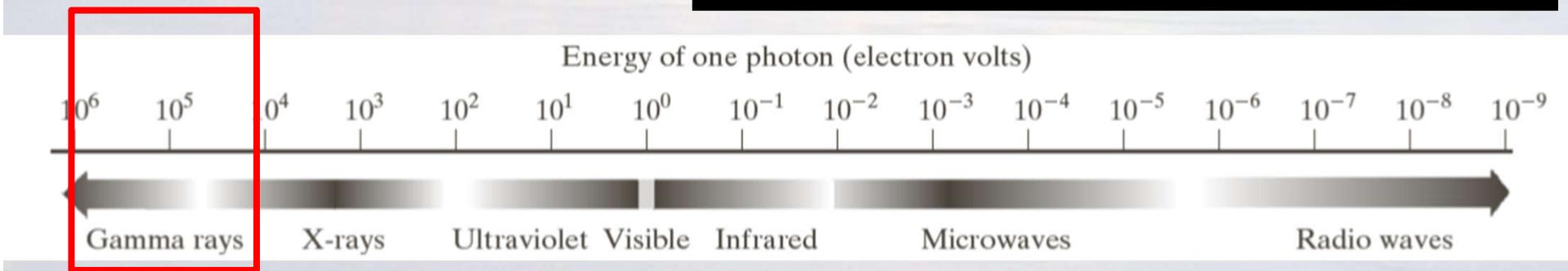
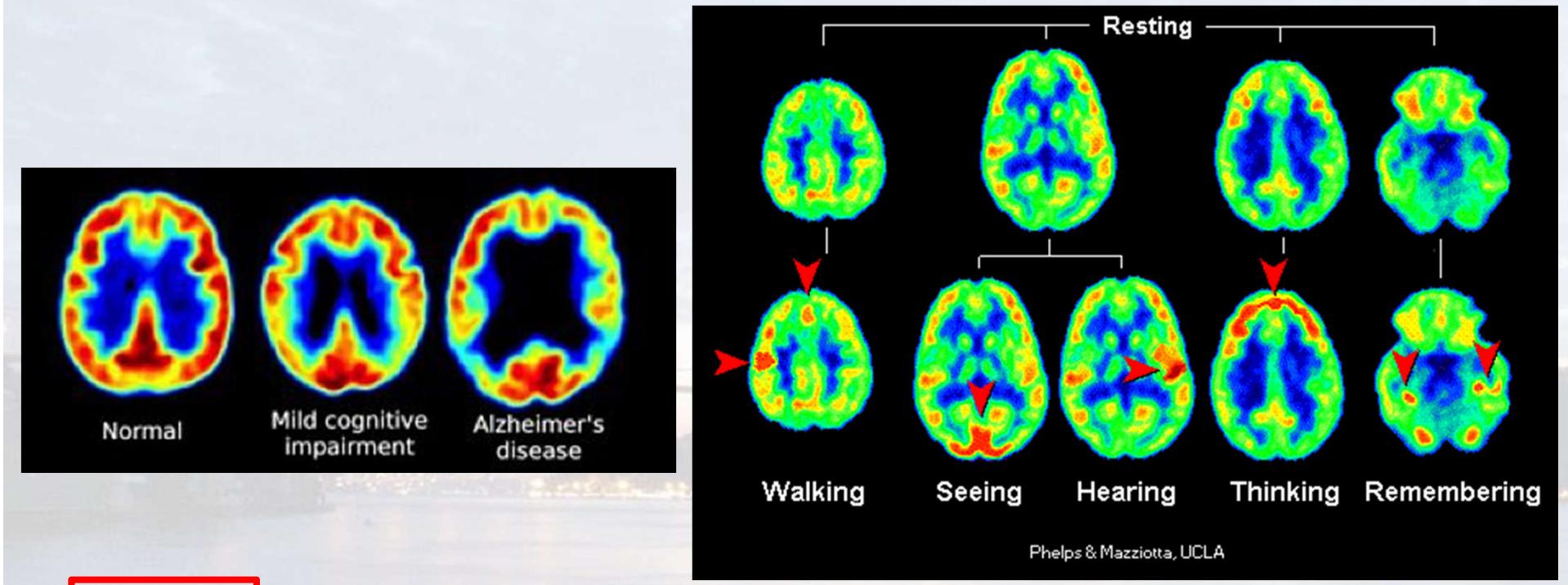
smut corn



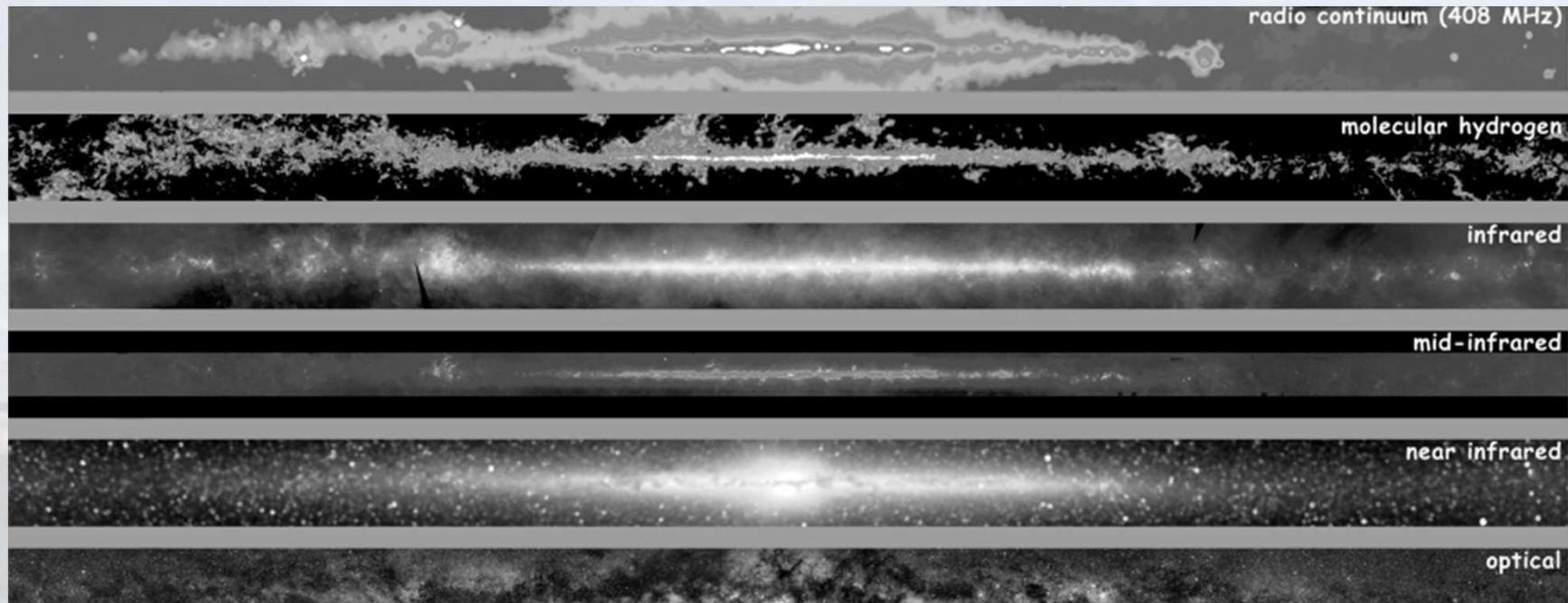
## X-ray imaging;



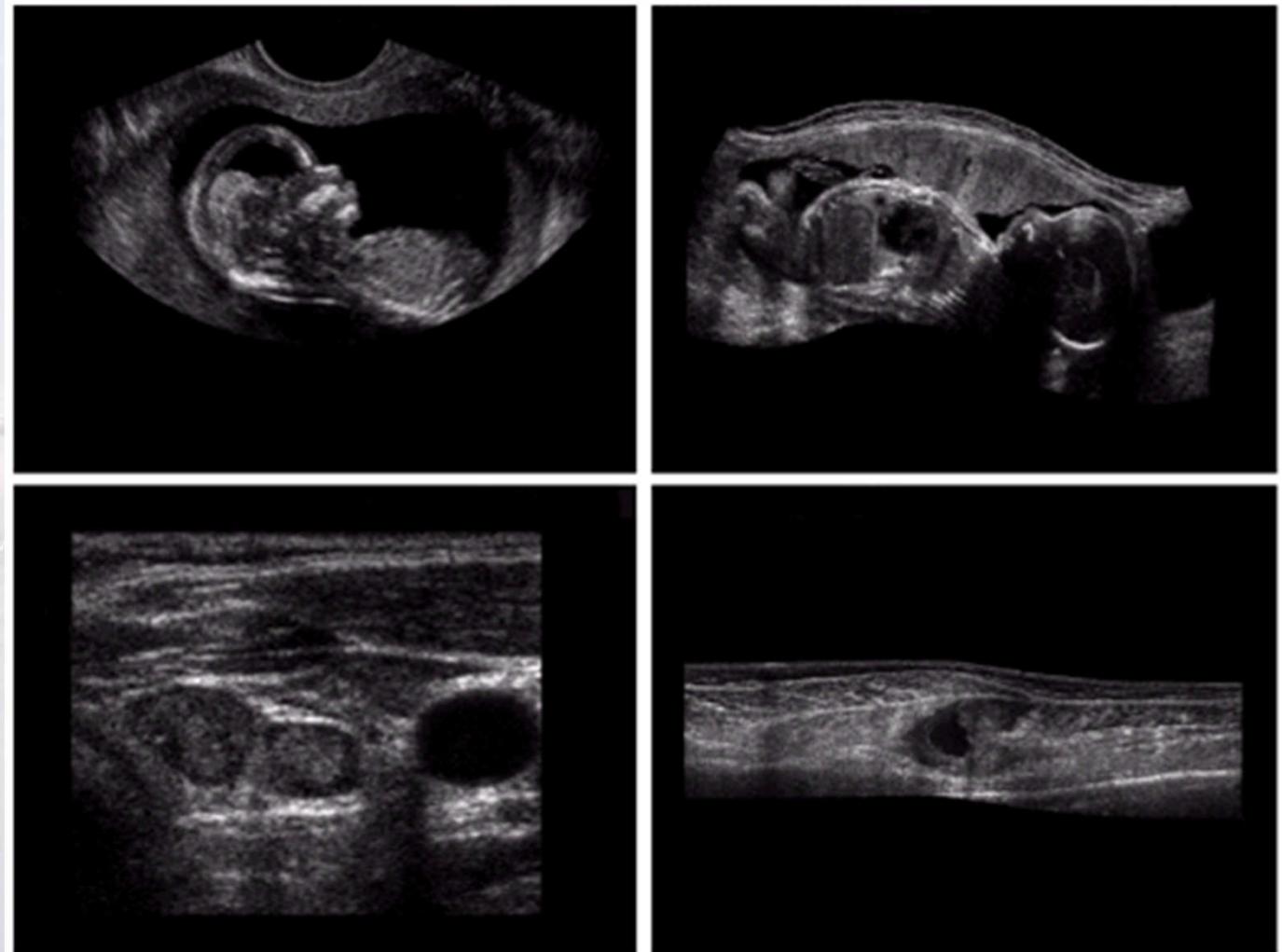
## Positron Emission Tomography (PET);



The wavelengths provide much more...

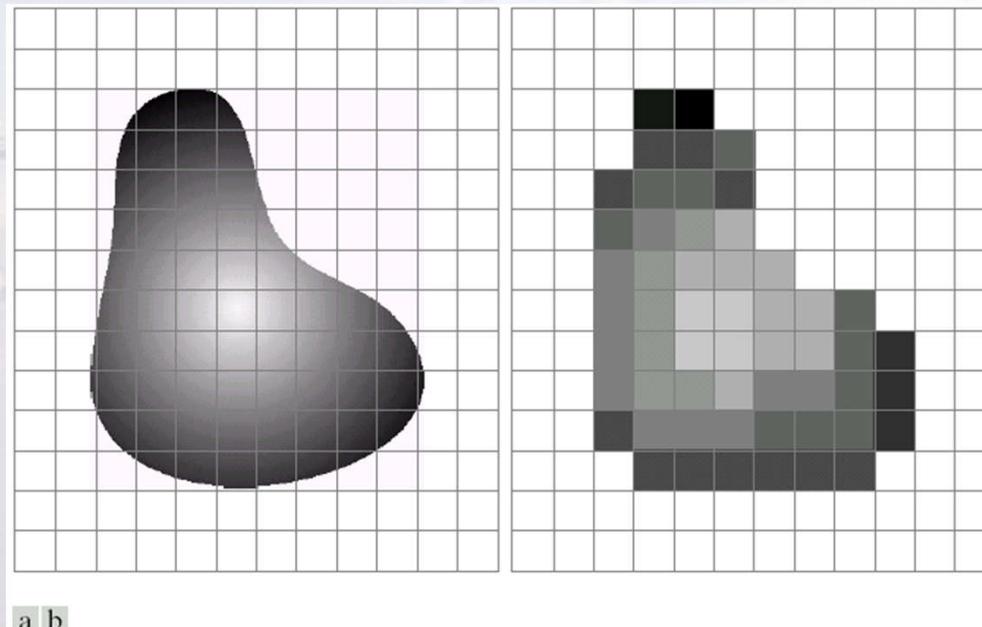


We are not limited with electromagnetic waves; sound waves can also be used to produce **ultrasound** images.



Digital image acquisition is basically about transforming the view of a continuous object  $f(x, y)$  into a discrete one  $f[x, y]$ , so that we can store it on a digital medium, and process it.

It involves two stages: **sampling** and **quantization**, that correspond respectively to the discretization of **space** and **amplitude** of the original continuous function.



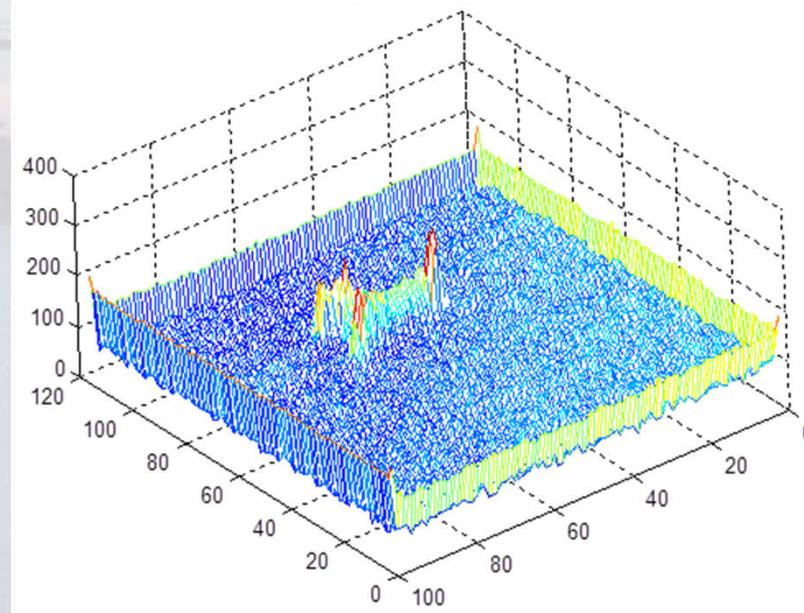
**FIGURE 2.17** (a) Continuos image projected onto a sensor array. (b) Result of image sampling and quantization.

In signal processing, **sampling** is the conversion of a continuous function in space (or time) into a discrete one.

**Problem 1: how to determine the sampling frequency?** If too high, the data becomes too large, if too low, we lose information ☹

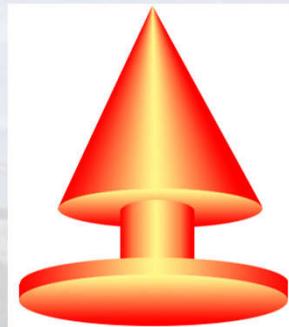
**Problem 2: how to determine the value of each sample?**

For problem 2; we use the “rain gauge” principle, and measure the amount of “photon rain” that falls into every sample.



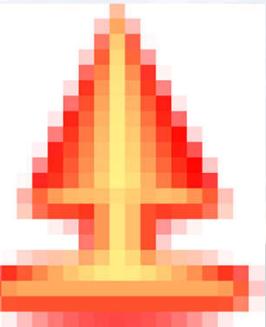
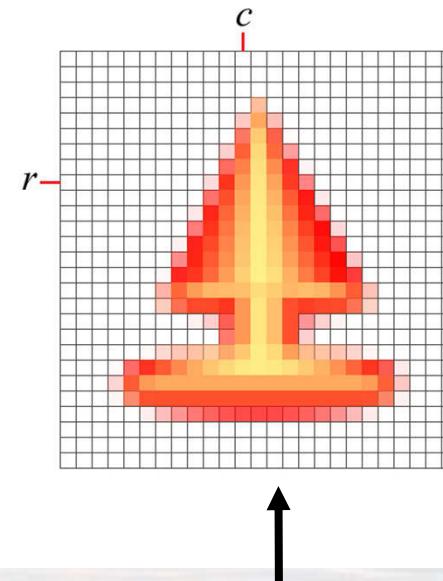
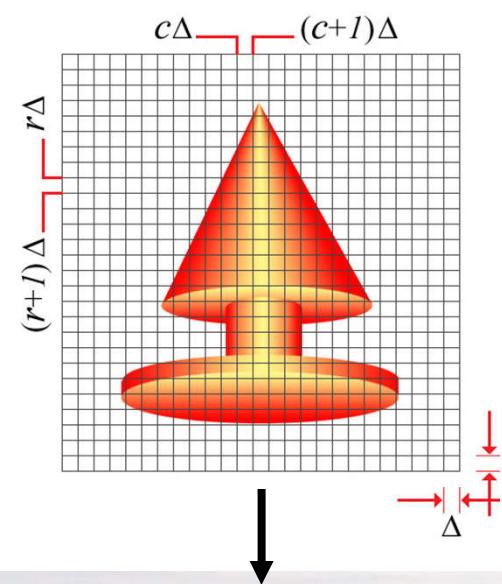
Amount of “photon rain”, i.e. the integral of photons in every grid square

Take the average  
within each square.



$$I_C(\rho, \chi)$$

continuous image



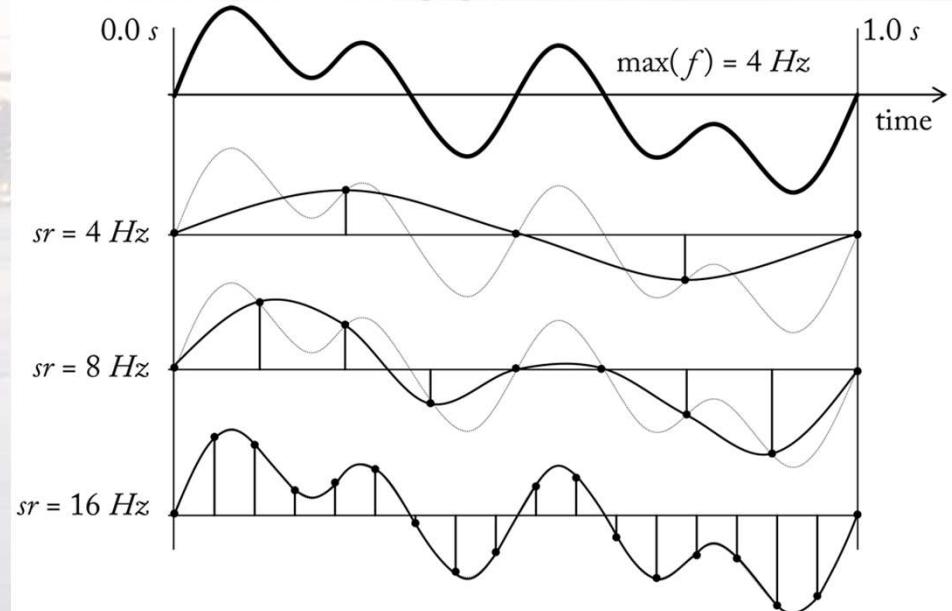
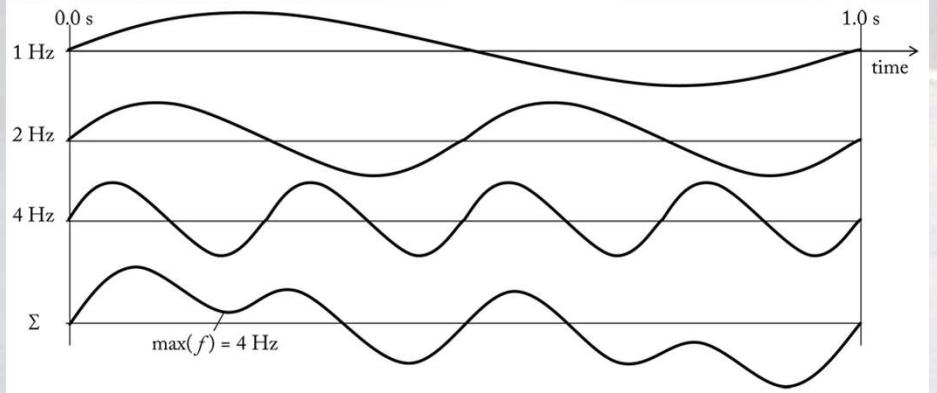
$$I_S(r, c)$$

sampled image

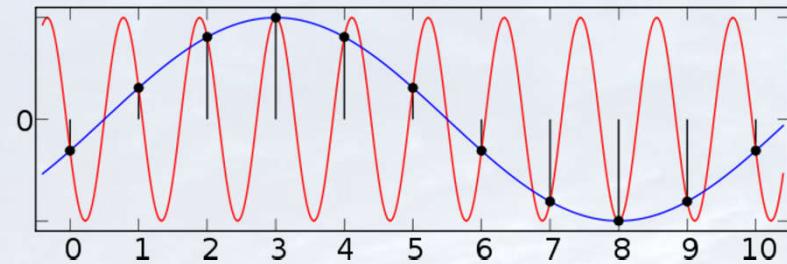
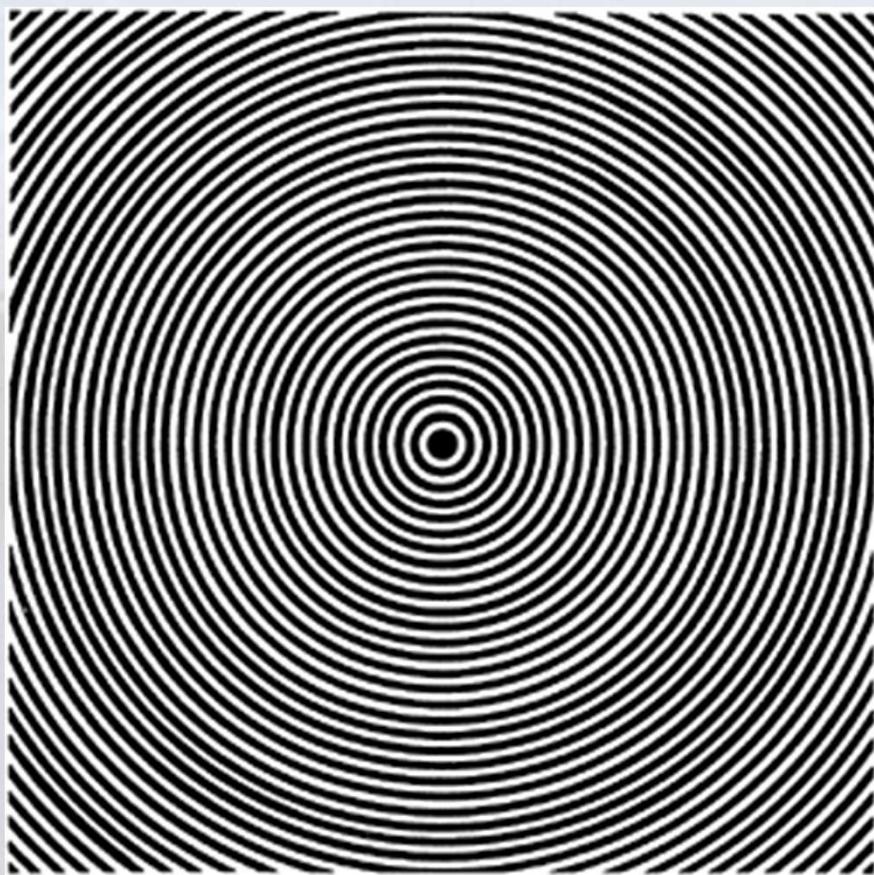
$$I_S(r, c) = \frac{1}{\Delta^2} \int_{r\Delta}^{(r+1)\Delta} \int_{c\Delta}^{(c+1)\Delta} I_C(\rho, \chi) \delta\rho \delta\chi$$

As to problem 1, the solution has been provided by the ***Nyquist-Shannon Sampling Theorem***, which provides a sufficient condition for a sampling frequency that permits a discrete sequence to capture all the information from a continuous function of finite bandwidth.

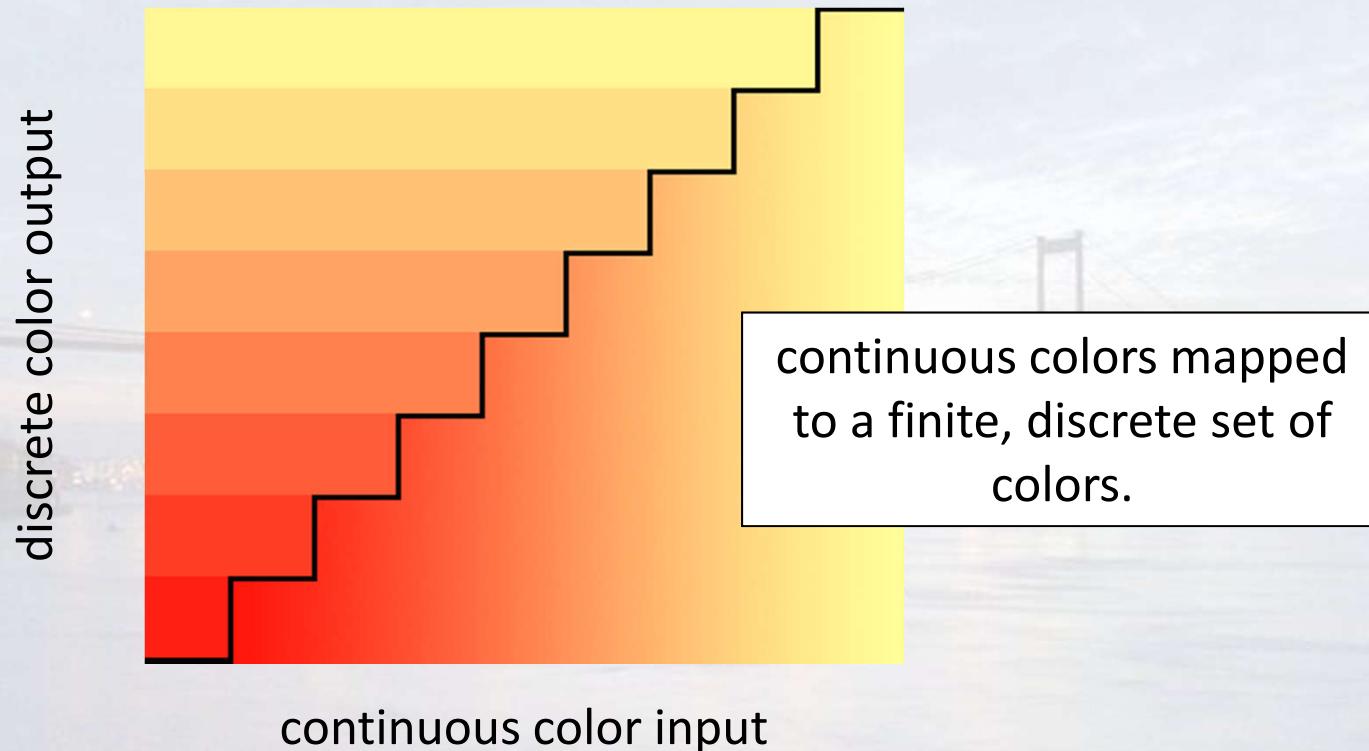
In short, the theorem states that if a continuous function has no higher frequency than  $B$  Hz, then it can be completely determined with a sampling frequency above  $2B$  Hz.

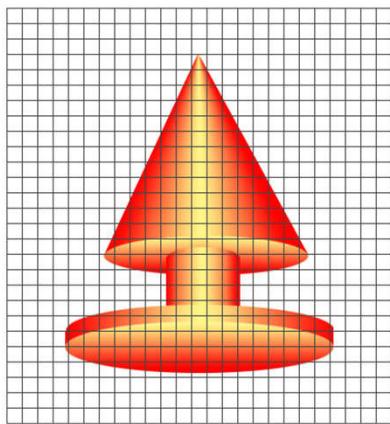


Failing to satisfy the Nyquist-Shannon Sampling Theorem, leads to *aliasing* or *Moiré patterns* in images.

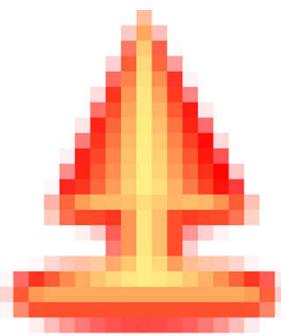


Quantization refers to the discretization of amplitude. There is an infinite number of possible pixel intensities, we can only store (and process) a finite amount!

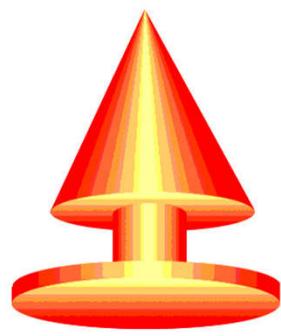




real image



sampled



quantized



sampled &  
quantized

**Spatial resolution** is a measure of the smallest discernible detail in an image.  
It is stated as line pairs per unit distance, e.g. 640x480, dots per inch (dpi), etc.

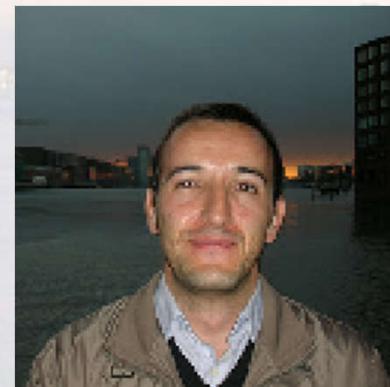
**Intensity resolution** is the smallest discernible change in intensity level.

It is stated in a bit number:  $k$  bits =  $2^k$  colors.

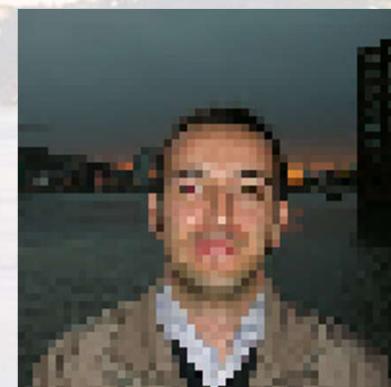
So an 8-bit gray-level image can contain up to  $2^8 = 256$  distinct levels.



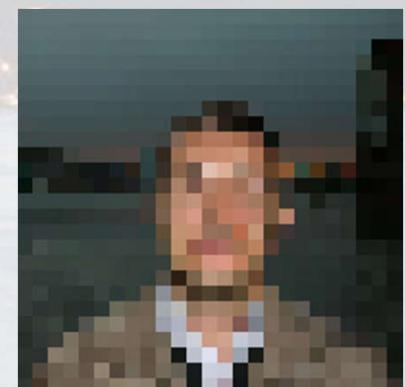
256x256



128x128



64x64

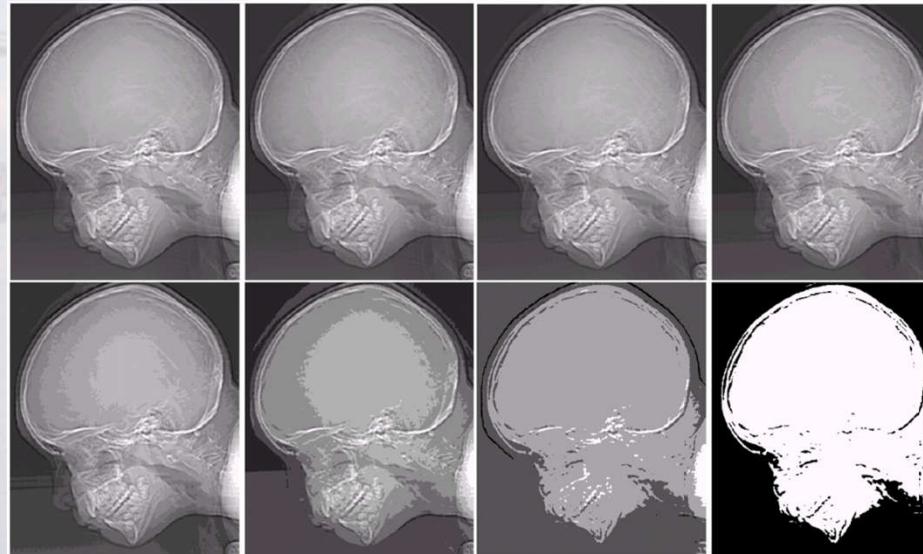


32x32

Images often have a size that is a power of 2; e.g. 512x512, 1024x1024, 2048x1024. This is because it simplifies calculations (e.g. Mip-mapping, Fourier Transform).

How many bits do we need to store an image? Well, if the image is of size  $W \times H$ , and it has an intensity resolution of  $n$  bits, that means every pixel can possess  $2^n$  distinct values; thus we need  $n \times W \times H$  bits for storing this image.

256 (8 bits), 128, 64, 32 gray levels



16 (4 bits), 8, 4, 2 gray levels

Image file formats ([https://en.wikipedia.org/wiki/Image\\_file\\_formats](https://en.wikipedia.org/wiki/Image_file_formats))

**Raster formats:** JPEG, TIFF, BMP, PNG, PPM, etc

**Vector formats:** SVG, etc.

With various properties in terms of image quality, file size, and intended context of use.

Read chapters 1 and 2 (2.1, 2.2, 2.3, 2.4) from DIP.