

Decision Trees and Random Forests



Prof. Ankur Sinha

Indian Institute of Management Ahmedabad

Gujarat India

Decision Trees

- Used for classification
 - Legitimate or fraudulent credit card transactions
 - Grant a loan or not
 - Tumor is benign or not
 - News item is on Finance, Politics, Sports, or Arts
 - The stocks next day would move up or down

Example

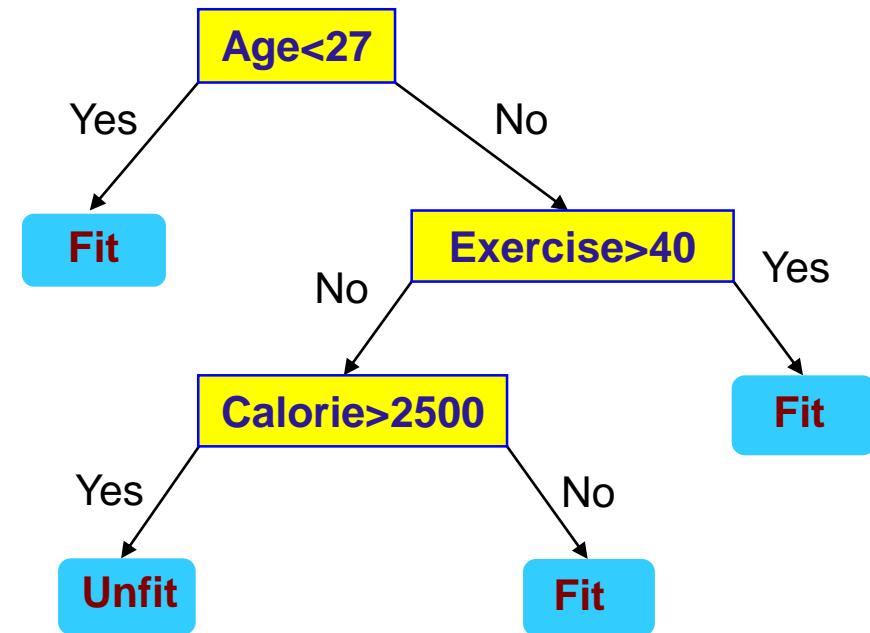
Person	Calorie Intake	Exercise Duration	Age	Fit (Yes/No)
Person 1	2089	20	47	0
Person 2	2569	54	23	1
Person 3	2790	58	28	1
Person 4	1882	20	41	1
Person 5	2160	55	20	1
Person 6	2408	22	29	1
Person 7	2740	44	25	1
Person 8	2700	8	29	0
Person 9	2635	52	33	1
Person 10	1918	22	40	1

Example

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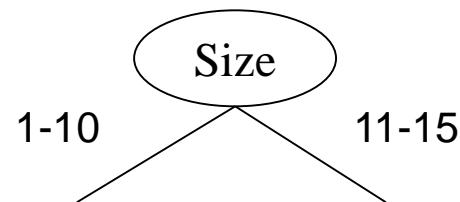
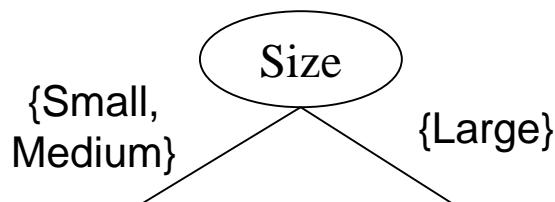
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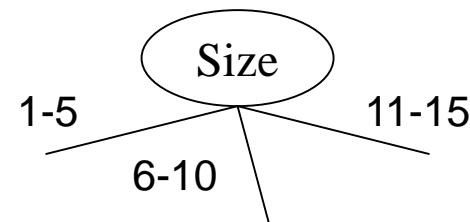
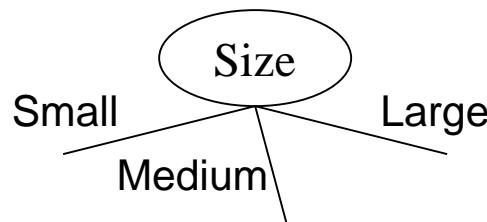
Which attribute to choose at each node?
 How to split the attribute?
 What is the depth of the tree?

Decision Trees

- Binary Split



- Multiway Split



Gini Index

- Gini index measures impurity
- Used in Classification and Regression Tree (CART) algorithm

$$Gini(t) = 1 - \sum_j p_j^2$$

At node t

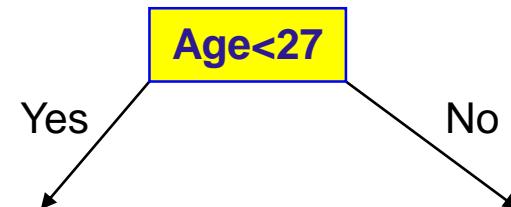
$$GINI_{split} = \sum_{i=1}^k \frac{n_i}{n} GINI(i)$$

Parent node is split into k partitions
Number of objects in partition i is n_i

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Person 11	2218	41	59	1
Person 12	2461	36	48	0
Person 13	2057	49	26	1
Person 14	2394	19	39	0
Person 15	2319	53	38	1
Person 16	2190	23	43	0
Person 17	2589	11	18	0
Person 18	2640	29	57	0
Person 19	2508	59	55	1
Person 20	2419	38	28	1
Person 21	2998	10	57	0
Person 22	2155	50	36	1
Person 23	1959	16	26	1
Person 24	1904	24	45	1
Person 25	1980	42	37	1
Person 26	1937	55	30	1
Person 27	2433	4	32	0
Person 28	2773	1	27	0
Person 29	1914	58	25	1
Person 30	1913	30	37	1

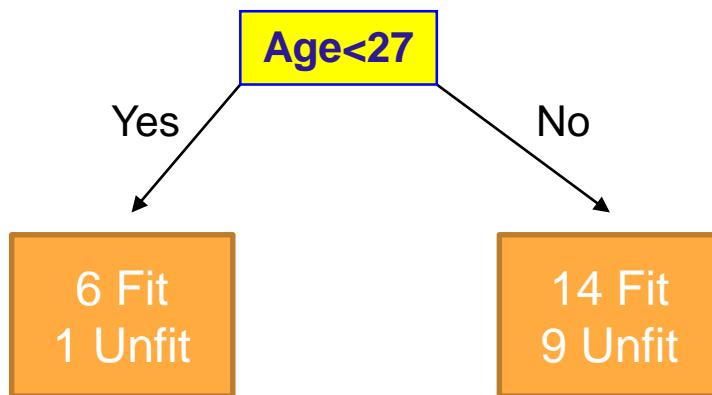
Find the Gini Index for the data
 $=1-(10/30)^2-(20/30)^2 = 0.4422$



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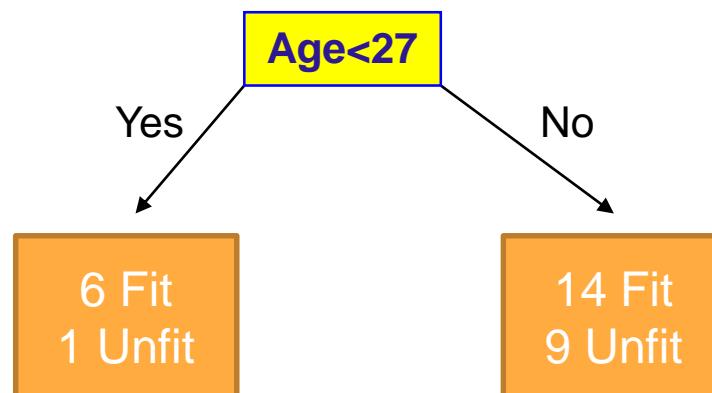
$$\text{Gini} = 1 - (1/7)^2 - (6/7)^2 = 0.2449$$

$$\text{Gini} = 1 - (9/23)^2 - (14/23)^2 = 0.4764$$

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Find the Gini Index for the data
 $=1-(10/30)^2-(20/30)^2 = 0.4422$



$$\text{Gini} = 1 - (1/7)^2 - (6/7)^2 = 0.2449$$

$$\text{Gini} = 1 - (9/23)^2 - (14/23)^2 = 0.4764$$

Weighted Gini=0.4223 (Impurity reduced)

$$=0.2449 \times 7/30 + 0.4764 \times 23/30$$

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Find out the best criterion to split on such that the purity increases

Entropy

- Entropy measures impurity
- Information gain, Used in ID3 (Iterative Dichotomiser) algorithm, refers to difference between entropy before the split and average entropy after the split

$$Entropy(t) = - \sum_j p_j \log_2 p_j$$

At node t

$$GAIN_{split} = Entropy(p) - \left(\sum_{i=1}^k \frac{n_i}{n} Entropy(i) \right)$$

Parent node p is split into k partitions
Number of objects in partition i is n_i

Entropy

- Gain ratio, which is adjusted information gain is used by C4.5, an improvement of ID3

$$GainRATIO_{split} = \frac{GAIN_{Split}}{SplitINFO}$$

$$SplitINFO = -\sum_{i=1}^k \frac{n_i}{n} \log \frac{n_i}{n}$$

$$Entropy(t) = - \sum_j p_j \log_2 p_j$$

At node t

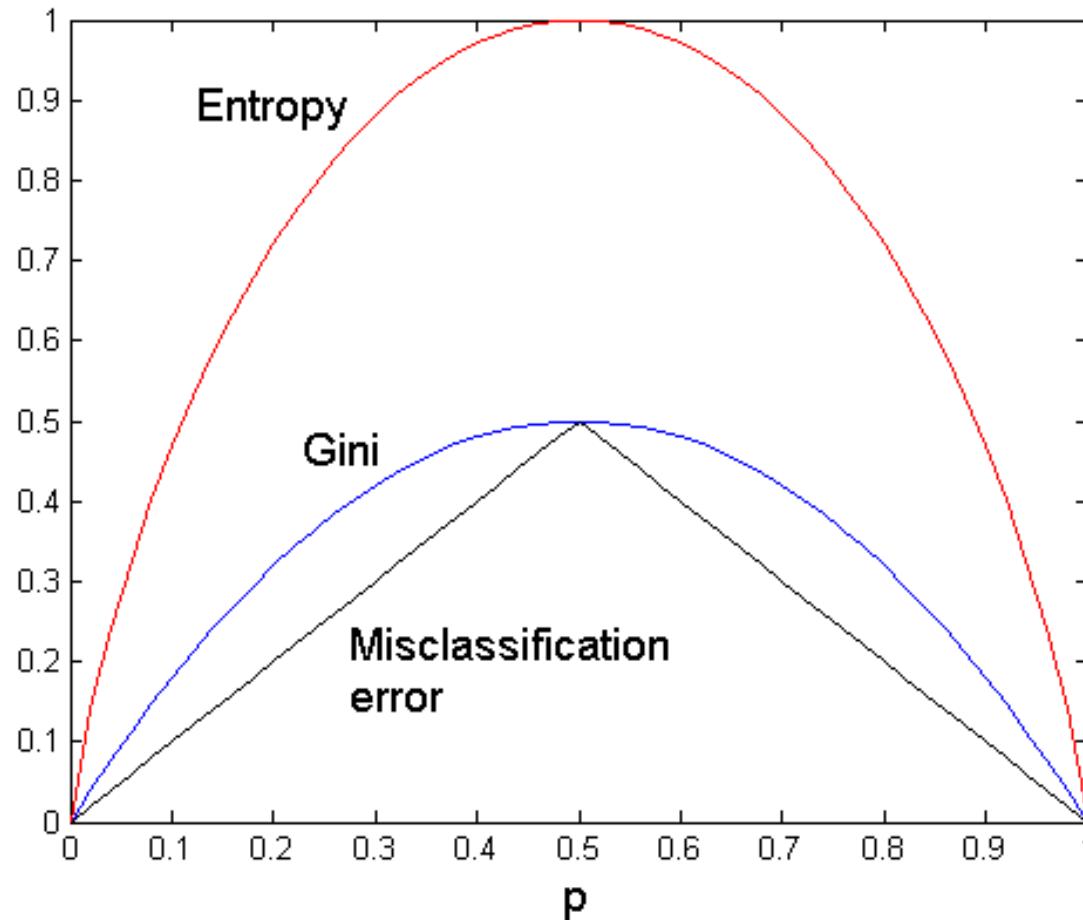
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Classification Error

- Classification error measure impurity

$$Error(t) = 1 - \max_j p_j \quad \text{At node t}$$

Comparing Different Criteria



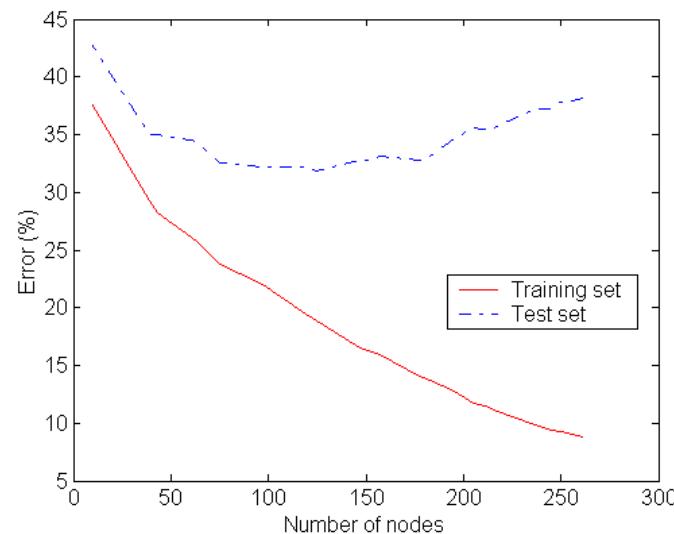
A two class problem with $p_1=p$ and $p_2=1-p$

Occam's Razor

- A deep decision tree can fit almost any data
- Occam's razor says that between two models of similar generalization errors, one should prefer the model which is simple

Addressing Overfitting

- Pre-pruning
 - Stop the algorithm when the tree becomes large
- Post-pruning
 - Trim the nodes in the bottom-up manner

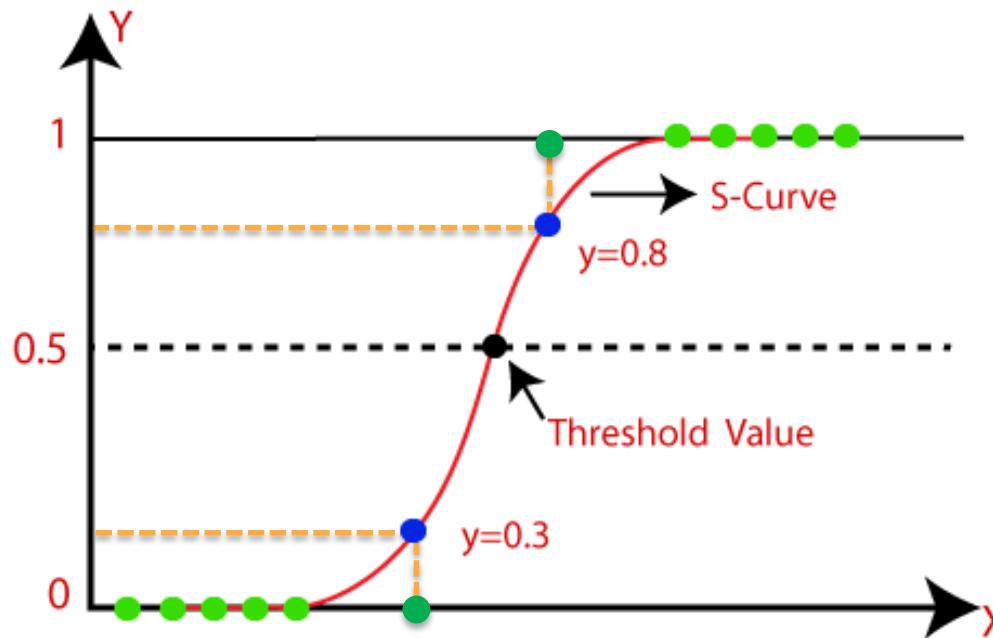


Random forests

- Creates an ensemble of trees and performs voting for the most popular class
- Random trees are generated by sampling small datasets (with replacement) from the original dataset and selecting only a subset of features at each node from the original set of features for investigation and choosing the best from the subset for creating the split
- Random forests lead to better generalized performance as compared to decision trees

Logistic Regression

- In finance logistic regression is commonly used to model the credit risk of individuals or enterprises
- It returns probability which may be more desired instead of strict classification



Feature Selection

- Correlation Coefficient
- Fisher's score
- Forward feature selection
- Backward feature selection
- Best subset feature selection
- Lasso (L1) regularization

Regressors or classifiers implemented in Python often provide an efficient feature selection approach: For a model created with Sklearn, try the following:

```
>>model.feature_importances_
```

Thank you