You are using countermodel generation for classical predicate logic.

Tableau for

 $\forall x \exists y R(x,y)$

 $\not\vDash \exists y \forall x R(x,y)$:

$$\underbrace{\frac{4. \ \, \neg R(a,a)}{\exists y R(a,y)} \ \, (\neg \forall, 3, [x/a])}_{ \ \, \underline{3}\underline{x} \ \, (\neg \forall x R(x,a) \ \, (\neg \exists, 1, [y/a]*)}$$

 $\neg \exists y \forall x R(x,y)$

 $\forall x \exists y R(x,y)$

(A)

(A)

The tableau is open:

The inference is refutable.

Countermodels:

Structure $S_{31} = \langle \mathcal{D}, \mathcal{I} \rangle$ with

 $\mathcal{D} = \{a, b\}$

 $\mathcal{I}: R \mapsto \{\langle a, b \rangle, \langle b, a \rangle\}$

Structure
$$S_{18} = \langle \mathcal{D}, \mathcal{I} \rangle$$
 with $\mathcal{D} = \{a, b\}$
 $\mathcal{I}: R \mapsto \{\langle a, a \rangle, \langle b, b \rangle\}$

This computation took 0.144 seconds.