R Notebook

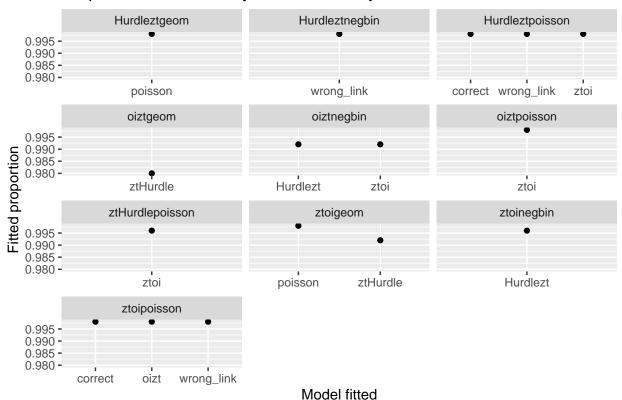
General results:

```
summarised_df <- results_data_frame |>
  group_by(data_generation, data_fitted) |>
  summarise(mean_point
                                    = mean(point, na.rm = TRUE),
            mean_ci_length_norm
                                    = mean(conf_int_normal_upper - conf_int_normal_lower, na.rm = TRUE)
            coverage_ci_norm
                                    = mean((conf_int_normal_lower < 1000) & (1000 < conf_int_normal_upp
            mean_ci_length_log_norm = mean(conf_int_log_normal_upper - conf_int_log_normal_lower, na.rm
                                    = mean((conf_int_log_normal_lower < 1000) & (1000 < conf_int_log_normal_lower)
            coverage_ci_log_norm
                                    = mean(!is.na(point)))
            succesful_fits
## 'summarise()' has grouped output by 'data_generation'. You can override using
## the '.groups' argument.
print(summarised_df, n=20)
## # A tibble: 80 x 8
## # Groups:
               data_generation [12]
      data_generation data_fitted mean_point mean_ci_length_norm coverage_ci_norm
##
      <chr>
                      <chr>
                                       <dbl>
                                                            <dbl>
                                                                             <dbl>
## 1 Hurdleztgeom
                      correct
                                     1.01e 3
                                                          1.67e 2
                                                                             0.93
## 2 Hurdleztgeom
                      negbin
                                     3.77e 6
                                                          1.84e 6
                                                                             0.896
## 3 Hurdleztgeom
                      oizt
                                     8.72e 2
                                                          6.96e 1
                                                                             0
                                     6.99e 2
                                                          2.40e 1
                                                                             0
## 4 Hurdleztgeom
                      poisson
## 5 Hurdleztgeom
                                     1.01e 3
                                                          1.67e 2
                                                                             0.932
                      wrong_link
## 6 Hurdleztgeom
                      ztHurdle
                                     1.09e 3
                                                          2.25e 2
                                                                             0.734
## 7 Hurdleztgeom
                      ztoi
                                     8.73e 2
                                                          7.89e 1
                                                                             0
                                                          7.15e14
## 8 Hurdleztnegbin correct
                                     1.19e15
                                                                             0.886
                      geom
                                                          1.80e 2
## 9 Hurdleztnegbin
                                     1.19e 3
                                                                             0
                                                          1.83e 2
## 10 Hurdleztnegbin
                                     9.95e 2
                                                                             0.84
                      oizt
## 11 Hurdleztnegbin
                      poisson
                                     8.16e 2
                                                          2.23e 1
                                                                             0
                                                          3.95e14
## 12 Hurdleztnegbin
                      wrong_link
                                     9.15e13
                                                                             0.840
## 13 Hurdleztnegbin
                      ztHurdle
                                     3.02e 6
                                                          1.09e 7
                                                                             0.896
                                     3.02e 6
## 14 Hurdleztnegbin
                                                          1.09e 7
                                                                             0.896
## 15 Hurdleztpoisson correct
                                     1.00e 3
                                                          1.04e 2
                                                                             0.956
                                                          8.24e 2
## 16 Hurdleztpoisson geometric
                                     2.28e 3
                                                                             0
## 17 Hurdleztpoisson oizt
                                     9.07e 2
                                                          4.23e 1
                                                                             0
                                                          1.04e 2
## 18 Hurdleztpoisson wrong_link
                                     1.00e 3
                                                                             0.958
## 19 Hurdleztpoisson ztHurdle
                                     1.07e 3
                                                          1.44e 2
                                                                             0.704
## 20 Hurdleztpoisson ztoi
                                     9.08e 2
                                                          4.24e 1
## # i 60 more rows
## # i 3 more variables: mean_ci_length_log_norm <dbl>,
       coverage_ci_log_norm <dbl>, succesful_fits <dbl>
```

```
pp <- summarised_df |>
    subset(succesful_fits < 1) |>
    as.data.frame() |>
    mutate(data_generation = ordered(data_generation)) |>
    ggplot(aes(y = succesful_fits, x = data_fitted)) +
    geom_point() +
    facet_wrap(~data_generation, scales = c("free_x"), ncol = 3) +
    ylab("Fitted proportion") +
    xlab("Model fitted") +
    ggtitle("Proportion of succesfully fitted models by true distribution of counts")

pp
```

Proportion of succesfully fitted models by true distribution of counts

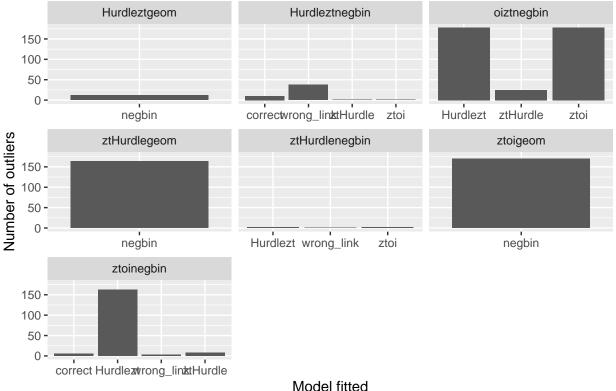


Visualising outliers (i.e. when estimated regression parameters tend to boundary):

```
results_data_frame |>
    subset(!is.na(point)) |>
    subset(point > 10000) |>
    group_by(data_generation, data_fitted) |>
    summarise(n = n()) |>
    ggplot(aes(x = data_fitted, weight = n)) +
    geom_bar() +
    facet_wrap(~ data_generation, scales = c("free_x")) +
    ylab("Number of outliers") +
    xlab("Model fitted") +
    ggtitle("Exreme outliers (estimate > 10 * true size) by true distribution of counts")
```

'summarise()' has grouped output by 'data_generation'. You can override using ## the '.groups' argument.

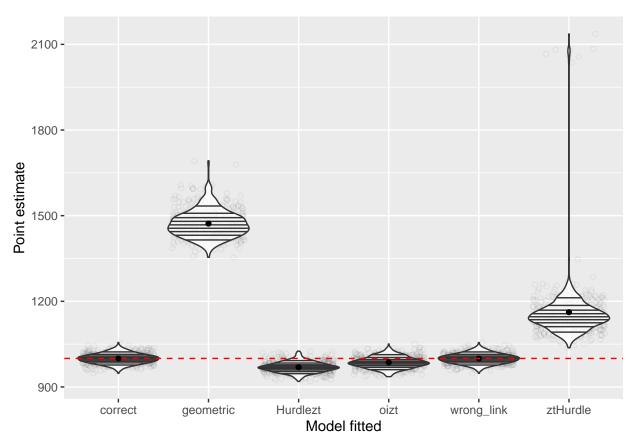
Exreme outliers (estimate > 10 * true size) by true distribution of counts



Point estimates

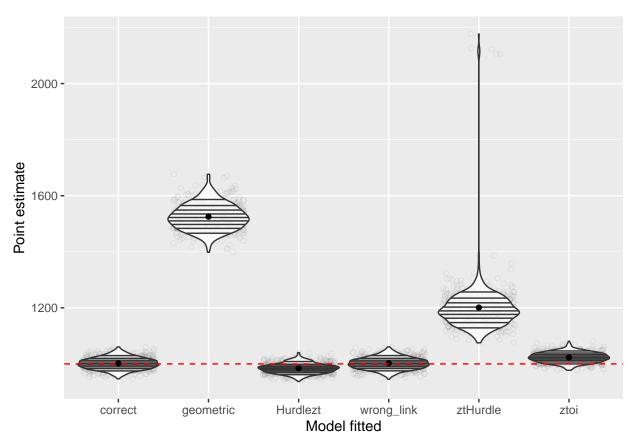
Results for counts generated by ztoipoisson:

```
p1 <- results_data_frame |>
  subset(!is.na(point) & (data_generation == "ztoipoisson")) |>
  subset(point < 25000) |>
  ggplot(aes(x = data_fitted, y = point)) +
  geom jitter(alpha = 0.05, shape = 1) +
  geom_violin(alpha = 0.8, draw_quantiles = 1:9 / 10, scale = "width") +
  stat_summary(fun = function(x) mean(x, na.rm = TRUE), geom = "point") +
  geom_hline(yintercept = 1000, linetype="dashed", color = "red") +
  ylab("Point estimate") +
  xlab("Model fitted")
p1
```



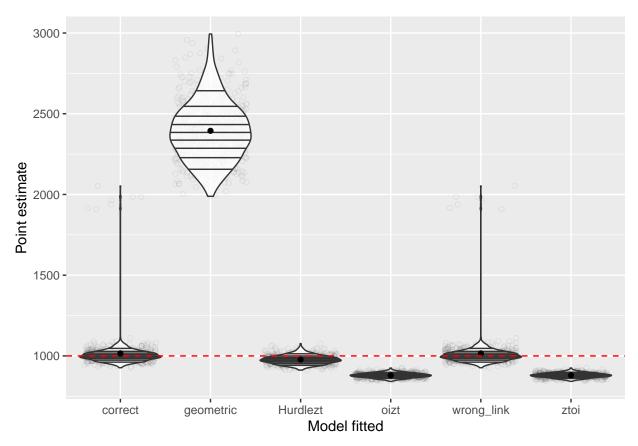
Results for counts generated by oiztpoisson:

```
p2 <- results_data_frame |>
    subset(!is.na(point) & (data_generation == "oiztpoisson")) |>
    subset(point < 25000) |>
    ggplot(aes(x = data_fitted, y = point)) +
    geom_jitter(alpha = 0.05, shape = 1) +
    geom_violin(alpha = 0.8, draw_quantiles = 1:9 / 10, scale = "width") +
    stat_summary(fun = function(x) mean(x, na.rm = TRUE), geom = "point") +
    geom_hline(yintercept = 1000, linetype="dashed", color = "red") +
    ylab("Point estimate") +
    xlab("Model fitted")
```



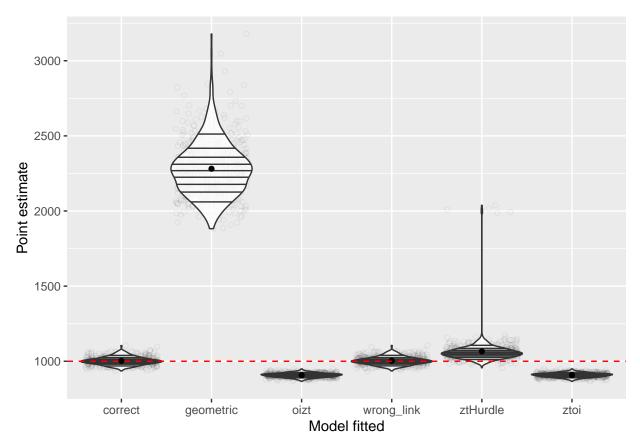
Results for counts generated by ztHurdlepoisson:

```
p3 <- results_data_frame |>
    subset(!is.na(point) & (data_generation == "ztHurdlepoisson")) |>
    subset(point < 25000) |>
    ggplot(aes(x = data_fitted, y = point)) +
    geom_jitter(alpha = 0.05, shape = 1) +
    geom_violin(alpha = 0.8, draw_quantiles = 1:9 / 10, scale = "width") +
    stat_summary(fun = function(x) mean(x, na.rm = TRUE), geom = "point") +
    geom_hline(yintercept = 1000, linetype="dashed", color = "red") +
    ylab("Point estimate") +
    xlab("Model fitted")
```



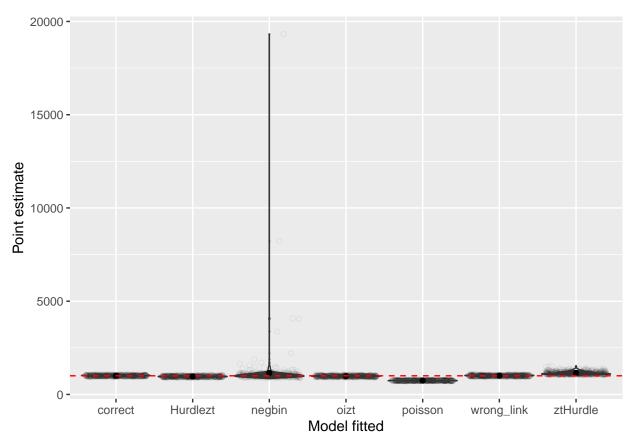
Results for counts generated by hurdleztpoisson:

```
p4 <- results_data_frame |>
    subset(!is.na(point) & (data_generation == "Hurdleztpoisson")) |>
    subset(point < 25000) |>
    ggplot(aes(x = data_fitted, y = point)) +
    geom_jitter(alpha = 0.05, shape = 1) +
    geom_violin(alpha = 0.8, draw_quantiles = 1:9 / 10, scale = "width") +
    stat_summary(fun = function(x) mean(x, na.rm = TRUE), geom = "point") +
    geom_hline(yintercept = 1000, linetype="dashed", color = "red") +
    ylab("Point estimate") +
    xlab("Model fitted")
```



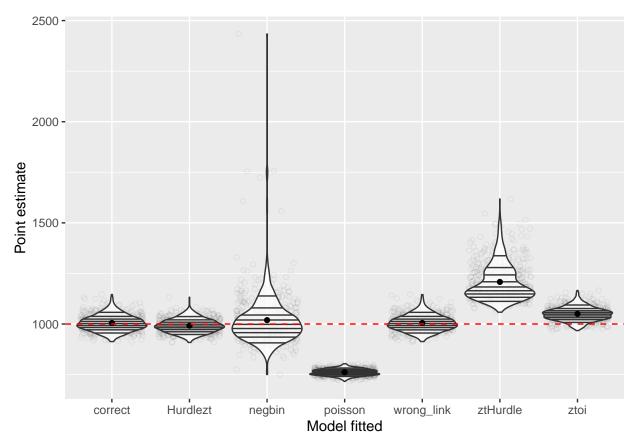
Results for counts generated by ztoigeom:

```
p5 <- results_data_frame |>
    subset(!is.na(point) & (data_generation == "ztoigeom")) |>
    subset(point < 25000) |>
    ggplot(aes(x = data_fitted, y = point)) +
    geom_jitter(alpha = 0.05, shape = 1) +
    geom_violin(alpha = 0.8, draw_quantiles = 1:9 / 10, scale = "width") +
    stat_summary(fun = function(x) mean(x, na.rm = TRUE), geom = "point") +
    geom_hline(yintercept = 1000, linetype="dashed", color = "red") +
    ylab("Point estimate") +
    xlab("Model fitted")
```



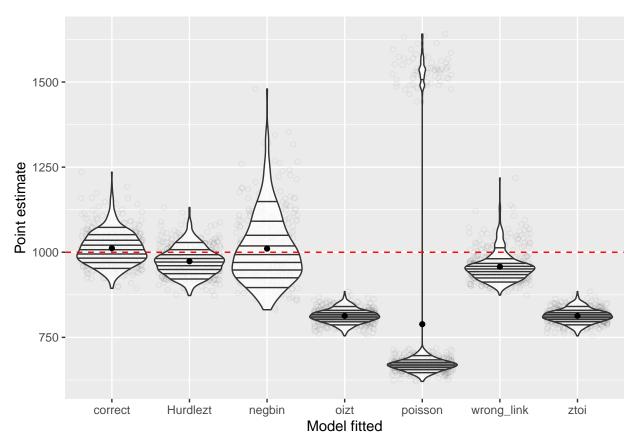
Results for counts generated by oiztgeom:

```
p6 <- results_data_frame |>
    subset(!is.na(point) & (data_generation == "oiztgeom")) |>
    subset(point < 25000) |>
    ggplot(aes(x = data_fitted, y = point)) +
    geom_jitter(alpha = 0.05, shape = 1) +
    geom_violin(alpha = 0.8, draw_quantiles = 1:9 / 10, scale = "width") +
    stat_summary(fun = function(x) mean(x, na.rm = TRUE), geom = "point") +
    geom_hline(yintercept = 1000, linetype="dashed", color = "red") +
    ylab("Point estimate") +
    xlab("Model fitted")
```



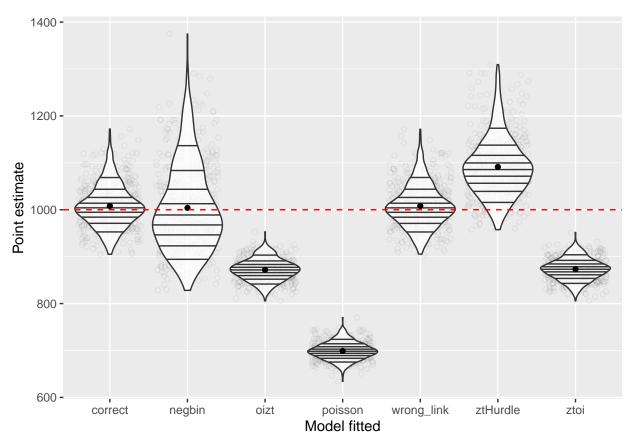
Results for counts generated by ztHurdlegeom:

```
p7 <- results_data_frame |>
    subset(!is.na(point) & (data_generation == "ztHurdlegeom")) |>
    subset(point < 25000) |>
    ggplot(aes(x = data_fitted, y = point)) +
    geom_jitter(alpha = 0.05, shape = 1) +
    geom_violin(alpha = 0.8, draw_quantiles = 1:9 / 10, scale = "width") +
    stat_summary(fun = function(x) mean(x, na.rm = TRUE), geom = "point") +
    geom_hline(yintercept = 1000, linetype="dashed", color = "red") +
    ylab("Point estimate") +
    xlab("Model fitted")
```



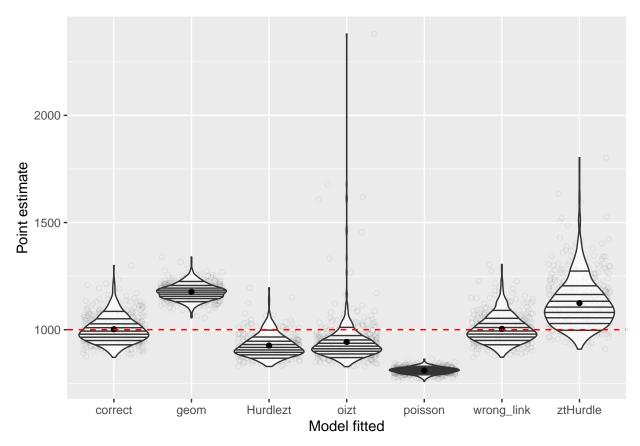
Results for counts generated by hurdleztgeom:

```
p8 <- results_data_frame |>
    subset(!is.na(point) & (data_generation == "Hurdleztgeom")) |>
    subset(point < 25000) |>
    ggplot(aes(x = data_fitted, y = point)) +
    geom_jitter(alpha = 0.05, shape = 1) +
    geom_violin(alpha = 0.8, draw_quantiles = 1:9 / 10, scale = "width") +
    stat_summary(fun = function(x) mean(x, na.rm = TRUE), geom = "point") +
    geom_hline(yintercept = 1000, linetype="dashed", color = "red") +
    ylab("Point estimate") +
    xlab("Model fitted")
```



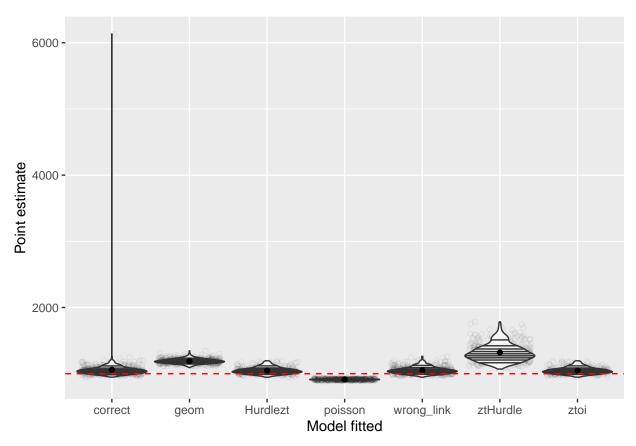
Results for counts generated by ztoinegbin:

```
p9 <- results_data_frame |>
    subset(!is.na(point) & (data_generation == "ztoinegbin")) |>
    subset(point < 10000) |>
    ggplot(aes(x = data_fitted, y = point)) +
    geom_jitter(alpha = 0.05, shape = 1) +
    geom_violin(alpha = 0.8, draw_quantiles = 1:9 / 10, scale = "width") +
    stat_summary(fun = function(x) mean(x, na.rm = TRUE), geom = "point") +
    geom_hline(yintercept = 1000, linetype="dashed", color = "red") +
    ylab("Point estimate") +
    xlab("Model fitted")
```



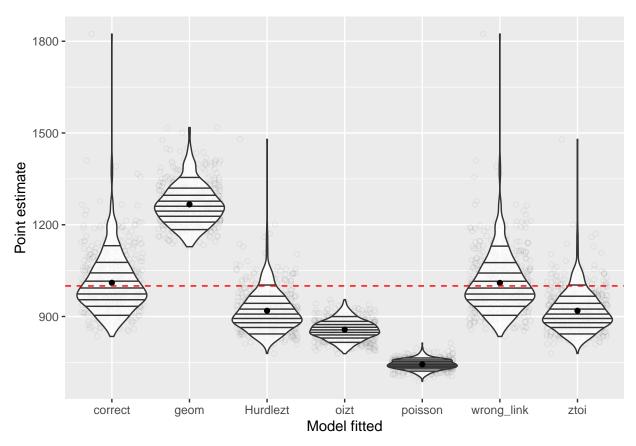
Results for counts generated by oiztnegbin:

```
p10 <- results_data_frame |>
    subset(!is.na(point) & (data_generation == "oiztnegbin")) |>
    subset(point < 10000) |>
    ggplot(aes(x = data_fitted, y = point)) +
    geom_jitter(alpha = 0.05, shape = 1) +
    geom_violin(alpha = 0.8, draw_quantiles = 1:9 / 10, scale = "width") +
    stat_summary(fun = function(x) mean(x, na.rm = TRUE), geom = "point") +
    geom_hline(yintercept = 1000, linetype="dashed", color = "red") +
    ylab("Point estimate") +
    xlab("Model fitted")
```



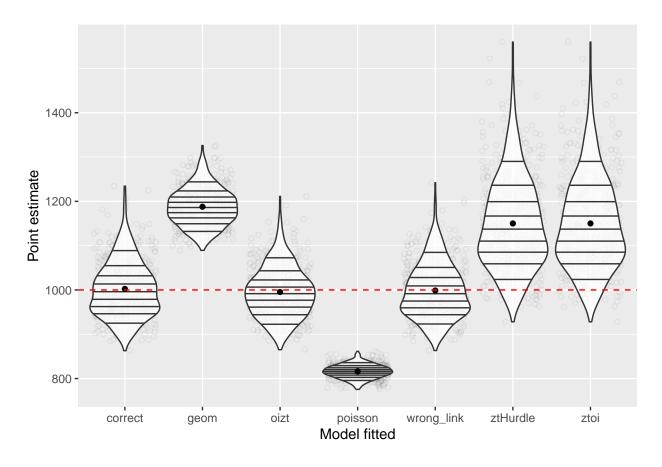
Results for counts generated by ztHurdlenegbin:

```
p11 <- results_data_frame |>
    subset(!is.na(point) & (data_generation == "ztHurdlenegbin")) |>
    subset(point < 25000) |>
    ggplot(aes(x = data_fitted, y = point)) +
    geom_jitter(alpha = 0.05, shape = 1) +
    geom_violin(alpha = 0.8, draw_quantiles = 1:9 / 10, scale = "width") +
    stat_summary(fun = function(x) mean(x, na.rm = TRUE), geom = "point") +
    geom_hline(yintercept = 1000, linetype="dashed", color = "red") +
    ylab("Point estimate") +
    xlab("Model fitted")
```



Results for counts generated by hurdleztnegbin:

```
p12 <- results_data_frame |>
    subset(!is.na(point) & (data_generation == "Hurdleztnegbin")) |>
    subset(point < 25000) |>
    ggplot(aes(x = data_fitted, y = point)) +
    geom_jitter(alpha = 0.05, shape = 1) +
    geom_violin(alpha = 0.8, draw_quantiles = 1:9 / 10, scale = "width") +
    stat_summary(fun = function(x) mean(x, na.rm = TRUE), geom = "point") +
    geom_hline(yintercept = 1000, linetype="dashed", color = "red") +
    ylab("Point estimate") +
    xlab("Model fitted")
```



Confidence intervals

Normal

Exact binomial tests for coverage of lognormal confindence intervals with $H_0: p = 0.95, H_1 = \neg H_1$:

```
dd <- results_data_frame |>
  subset(!is.na(point)) |>
  subset(point < 25000) |>
  mutate(covr_norm = (conf_int_normal_lower < 1000) & (conf_int_normal_upper > 1000),
         covr_log = (conf_int_log_normal_lower < 1000) & (conf_int_log_normal_upper > 1000)) |>
  group_by(data_generation, data_fitted) |>
  summarise(n = n(),
            mean = mean(covr_norm, na.rm = TRUE))
## 'summarise()' has grouped output by 'data_generation'. You can override using
## the '.groups' argument.
dd <- cbind(dd, p_value = NA, lower = NA, upper = NA)
for (x in 1:NROW(dd)) {
  jj \leftarrow binom.test(x = as.numeric(dd[x, 4]) * as.integer(dd[x, 3]), n = as.integer(dd[x, 3]), p = .95)
  \# this jj object has some very weird interactions with the rest of R ecosystem
  dd[x, 5] <- jj$p.value |> as.numeric()
  dd[x, 6] <- jj[[4]][1]
```

```
dd[x, 7] \leftarrow jj[[4]][2]
}
print(dd[, c(1:2, 4, 5)] |> mutate(p_value = round(p_value, digits = 4)),
      n = NROW(dd)
## # A tibble: 80 x 4
## # Groups:
               data_generation [12]
##
      data_generation data_fitted
                                     mean p_value
##
      <chr>
                       <chr>
                                    <dbl>
                                             <dbl>
##
                                   0.93
                                            0.0501
   1 Hurdleztgeom
                       correct
##
    2 Hurdleztgeom
                      negbin
                                   0.918
                                            0.0024
                                   0
                                            0
  3 Hurdleztgeom
                       oizt
## 4 Hurdleztgeom
                                   0
                                            0
                      poisson
## 5 Hurdleztgeom
                      wrong_link
                                   0.932
                                            0.0797
## 6 Hurdleztgeom
                       ztHurdle
                                   0.734
                                            0
## 7 Hurdleztgeom
                       ztoi
                                   0
                                            0
## 8 Hurdleztnegbin
                                   0.904
                                            0
                      correct
## 9 Hurdleztnegbin
                       geom
                                   0
                                            0
## 10 Hurdleztnegbin
                       oizt
                                   0.84
                                            0
## 11 Hurdleztnegbin
                      poisson
                                   0
                                            0
## 12 Hurdleztnegbin
                                            0
                      wrong_link
                                   0.896
## 13 Hurdleztnegbin
                      ztHurdle
                                   0.896
                                            0
                                   0.896
## 14 Hurdleztnegbin
                      ztoi
                                            0
## 15 Hurdleztpoisson correct
                                   0.956
                                            0.608
## 16 Hurdleztpoisson geometric
                                            0
                                   0
## 17 Hurdleztpoisson oizt
                                   0
                                            0
## 18 Hurdleztpoisson wrong_link
                                   0.958
                                            0.473
## 19 Hurdleztpoisson ztHurdle
                                   0.704
                                            0
## 20 Hurdleztpoisson ztoi
                                   0
                                            0
## 21 oiztgeom
                      Hurdlezt
                                   0.924
                                            0.0132
## 22 oiztgeom
                                   0.906
                       correct
                                            0
## 23 oiztgeom
                                   0.834
                                            0
                      negbin
## 24 oiztgeom
                      poisson
                                   0
                                            0
                      wrong_link 0.9
                                            0
## 25 oiztgeom
## 26 oiztgeom
                       ztHurdle
                                   0.0592
## 27 oiztgeom
                                   0.71
                                            0
                       ztoi
## 28 oiztnegbin
                      Hurdlezt
                                   0.997
                                            0
                                   0.992
                                            0
## 29 oiztnegbin
                       correct
## 30 oiztnegbin
                                   0
                                            0
                       geom
## 31 oiztnegbin
                       poisson
                                   0
                                            0
                       wrong_link 0.996
## 32 oiztnegbin
                                            0
                                   0.0505
                                           0
## 33 oiztnegbin
                       ztHurdle
                                   0.997
## 34 oiztnegbin
                       ztoi
                                   0.776
## 35 oiztpoisson
                                            0
                      Hurdlezt
                                   0.918
## 36 oiztpoisson
                       correct
                                            0.002
## 37 oiztpoisson
                                   0
                                            0
                       geometric
## 38 oiztpoisson
                       wrong_link 0.916
                                            0.0013
## 39 oiztpoisson
                       ztHurdle
                                   0
                                            0
## 40 oiztpoisson
                       ztoi
                                   0.772
                                            0
                                   0.864
## 41 ztHurdlegeom
                      Hurdlezt
## 42 ztHurdlegeom
                       correct
                                   0.972
                                            0.0232
```

negbin

43 ztHurdlegeom

0.382

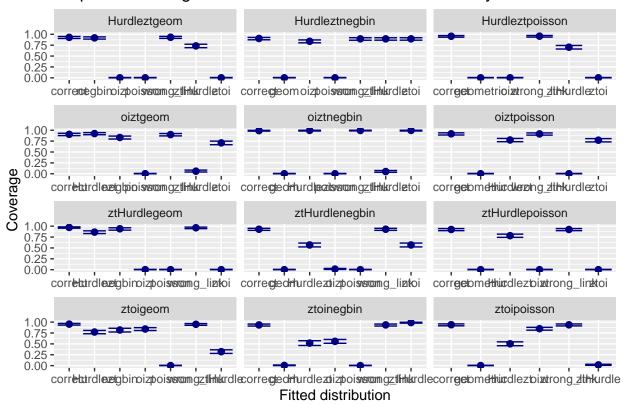
0.940

```
## 44 ztHurdlegeom
                      oizt
                                   0
## 45 ztHurdlegeom
                      poisson
                                           0
## 46 ztHurdlegeom
                      wrong link 0.964
                                           0.181
## 47 ztHurdlegeom
                                   0
                                           0
                      ztoi
## 48 ztHurdlenegbin
                      Hurdlezt
                                   0.568
## 49 ztHurdlenegbin
                                   0.93
                                           0.0501
                      correct
## 50 ztHurdlenegbin
                      geom
                                   0
                                           0
## 51 ztHurdlenegbin
                      oizt
                                   0.014
                                           0
                      poisson
## 52 ztHurdlenegbin
                                   0
                                           0
                                           0.0498
## 53 ztHurdlenegbin
                      wrong_link
                                   0.930
## 54 ztHurdlenegbin
                      ztoi
                                   0.568
## 55 ztHurdlepoisson Hurdlezt
                                   0.782
## 56 ztHurdlepoisson correct
                                   0.924
                                           0.0132
## 57 ztHurdlepoisson geometric
                                           0
## 58 ztHurdlepoisson oizt
                                   0
                                           0
## 59 ztHurdlepoisson wrong_link
                                   0.924
                                           0.0132
## 60 ztHurdlepoisson ztoi
                                           0
                                   0
## 61 ztoigeom
                      Hurdlezt
                                   0.772
                                           0
                                   0.954
## 62 ztoigeom
                      correct
                                           0.758
## 63 ztoigeom
                      negbin
                                   0.819
## 64 ztoigeom
                      oizt
                                   0.842
                                           0
## 65 ztoigeom
                                   0
                      poisson
## 66 ztoigeom
                      wrong_link 0.95
                                           1
                      ztHurdle
                                   0.321
## 67 ztoigeom
## 68 ztoinegbin
                      Hurdlezt
                                   0.518
                                           0
## 69 ztoinegbin
                      correct
                                   0.935
                                           0.147
## 70 ztoinegbin
                                   0.004
                       geom
                                           0
                                   0.558
## 71 ztoinegbin
                      oizt
                                           0
## 72 ztoinegbin
                                           0
                      poisson
                                   0
## 73 ztoinegbin
                      wrong_link 0.936
                                           0.148
## 74 ztoinegbin
                      ztHurdle
                                   0.990
                                           0
## 75 ztoipoisson
                      Hurdlezt
                                   0.502
                                           0
## 76 ztoipoisson
                       correct
                                   0.940
                                           0.303
## 77 ztoipoisson
                                   0
                                           0
                       geometric
## 78 ztoipoisson
                                   0.850
                       oizt
## 79 ztoipoisson
                      wrong_link 0.938
                                           0.217
## 80 ztoipoisson
                       ztHurdle
                                   0.016
                                           0
```

Visual results with confidence intervals:

```
qq1 <- dd |>
    ggplot(aes(x = data_fitted)) +
    facet_wrap(~ data_generation, scales = c("free_x"), ncol = 3) +
    geom_point(aes(y = mean), colour = "navy", cex = 2) +
    geom_errorbar(aes(ymin = lower, ymax = upper), colour = "navy") +
    ggtitle("Empirical coverage of studentized confidence intervals by true distribution of counts") +
    xlab("Fitted distribution") +
    ylab("Coverage")
```

Empirical coverage of studentized confidence intervals by true distribution

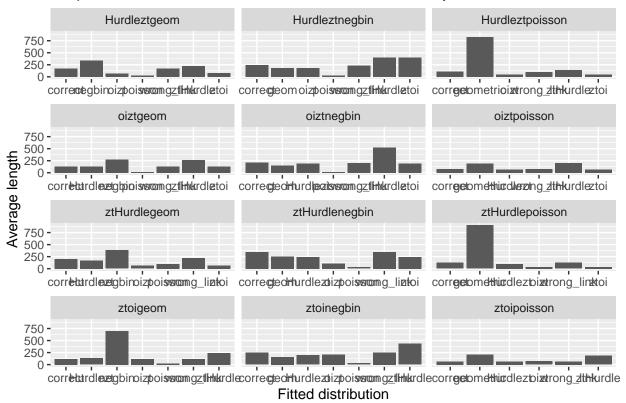


Average sizes of confidence intervals:

```
qq2 <- results_data_frame |>
    subset(!is.na(point)) |>
    subset(point < 25000) |>
    group_by(data_generation, data_fitted) |>
    summarise(len = mean(conf_int_normal_upper - conf_int_normal_lower, na.rm = TRUE)) |>
    ggplot(aes(x = data_fitted, weight = len)) +
    geom_bar() +
    facet_wrap(~ data_generation, scales = c("free_x"), ncol = 3) +
    ylab("Average length") +
    xlab("Fitted distribution") +
    ggtitle("Empirical size of studentized confidence intervals by true distribution of counts")

## 'summarise()' has grouped output by 'data_generation'. You can override using
## the '.groups' argument.
```

Empirical size of studentized confidence intervals by true distribution of cou



Logormal

Exact binomial tests for coverage of normal confindence intervals with $H_0: p = 0.95, H_1 = \neg H_1$:

```
dd <- results_data_frame |>
  subset(!is.na(point)) |>
  subset(point < 25000) |>
  mutate(covr_norm = (conf_int_normal_lower < 1000) & (conf_int_normal_upper > 1000),
         covr_log = (conf_int_log_normal_lower < 1000) & (conf_int_log_normal_upper > 1000)) |>
  group_by(data_generation, data_fitted) |>
  summarise(n = n(),
            mean = mean(covr_log, na.rm = TRUE))
## 'summarise()' has grouped output by 'data_generation'. You can override using
## the '.groups' argument.
dd <- cbind(dd, p_value = NA, lower = NA, upper = NA)
for (x in 1:NROW(dd)) {
  jj \leftarrow binom.test(x = as.numeric(dd[x, 4]) * as.integer(dd[x, 3]), n = as.integer(dd[x, 3]), p = .95)
  # this jj object has some very weird interactions with the rest of R ecosystem
  dd[x, 5] <- jj$p.value |> as.numeric()
  dd[x, 6] \leftarrow jj[[4]][1]
  dd[x, 7] \leftarrow jj[[4]][2]
}
```

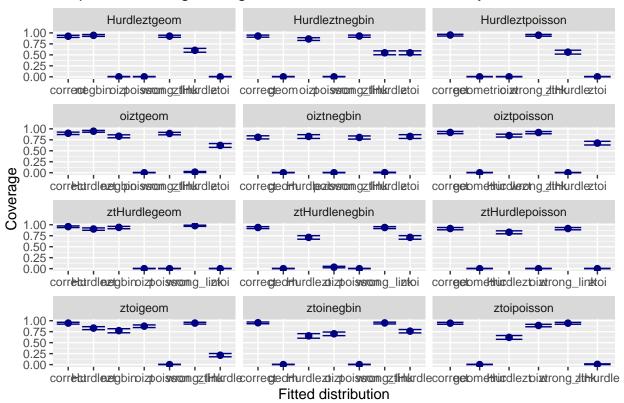
```
## # A tibble: 80 x 4
## # Groups:
               data_generation [12]
##
      data generation data fitted
                                      mean p value
      <chr>
                      <chr>
                                      <dbl>
                                              <dbl>
##
   1 Hurdleztgeom
                       correct
                                   0.924
                                             0.0132
##
    2 Hurdleztgeom
                      negbin
                                   0.945
                                             0.602
    3 Hurdleztgeom
                                             0
                       oizt
##
                                   0
                                             0
  4 Hurdleztgeom
                       poisson
                       wrong_link
                                   0.926
                                             0.0179
    5 Hurdleztgeom
##
   6 Hurdleztgeom
                       ztHurdle
                                   0.604
                                             0
  7 Hurdleztgeom
                       ztoi
## 8 Hurdleztnegbin
                                   0.929
                                             0.0373
                      correct
  9 Hurdleztnegbin
                                             0
                       geom
                                   0
                                   0.862
                                             0
## 10 Hurdleztnegbin
                       oizt
                                             0
## 11 Hurdleztnegbin
                      poisson
                                   0
## 12 Hurdleztnegbin
                      wrong_link
                                   0.928
                                             0.0414
## 13 Hurdleztnegbin
                      ztHurdle
                                   0.547
                                             0
## 14 Hurdleztnegbin
                                   0.547
                                             0
## 15 Hurdleztpoisson correct
                                   0.952
                                             1
## 16 Hurdleztpoisson geometric
                                             0
## 17 Hurdleztpoisson oizt
                                   0
                                             0
                                             0.837
## 18 Hurdleztpoisson wrong_link
                                   0.948
## 19 Hurdleztpoisson ztHurdle
                                   0.562
                                             0
## 20 Hurdleztpoisson ztoi
                                   0
                                             0
## 21 oiztgeom
                                   0.946
                                             0.681
                      Hurdlezt
## 22 oiztgeom
                       correct
                                   0.9
                                             0
## 23 oiztgeom
                                   0.832
                                             0
                      negbin
                                             0
## 24 oiztgeom
                       poisson
## 25 oiztgeom
                       wrong_link 0.894
                                             0
                       ztHurdle
                                   0.0143
                                             0
## 26 oiztgeom
                                   0.622
                                             0
## 27 oiztgeom
                       ztoi
## 28 oiztnegbin
                      Hurdlezt
                                   0.827
                                             0
## 29 oiztnegbin
                                   0.808
                                             0
                       correct
## 30 oiztnegbin
                       geom
                                   0
                                             0
                                             0
## 31 oiztnegbin
                       poisson
                                   0
## 32 oiztnegbin
                       wrong_link 0.804
                                             0
## 33 oiztnegbin
                       ztHurdle
                                   0.00211
                                             0
                                   0.827
                                             0
## 34 oiztnegbin
                       ztoi
                                   0.848
## 35 oiztpoisson
                      Hurdlezt
                                             0
                                             0.002
                                   0.918
## 36 oiztpoisson
                       correct
## 37 oiztpoisson
                       geometric
                                   0
                                             0
                                             0.0013
## 38 oiztpoisson
                       wrong_link
                                   0.916
                       ztHurdle
                                             0
## 39 oiztpoisson
                                   0.675
                                             0
## 40 oiztpoisson
                       ztoi
                       Hurdlezt
                                   0.904
## 41 ztHurdlegeom
                                   0.958
                                             0.473
## 42 ztHurdlegeom
                       correct
## 43 ztHurdlegeom
                      negbin
                                   0.940
                                             0.382
## 44 ztHurdlegeom
                       oizt
                                   0
                                             0
## 45 ztHurdlegeom
                       poisson
## 46 ztHurdlegeom
                       wrong_link 0.98
                                             0.0009
```

```
## 47 ztHurdlegeom
## 48 ztHurdlenegbin Hurdlezt
                                   0.713
                                            0
## 49 ztHurdlenegbin
                      correct
                                   0.938
                                            0.217
## 50 ztHurdlenegbin
                                            0
                      geom
                                   0
## 51 ztHurdlenegbin
                                   0.034
                                            0
## 52 ztHurdlenegbin poisson
                                            0
                                   0
## 53 ztHurdlenegbin wrong link
                                  0.938
                                            0.217
## 54 ztHurdlenegbin ztoi
                                   0.713
                                            0
## 55 ztHurdlepoisson Hurdlezt
                                   0.83
                                            0
## 56 ztHurdlepoisson correct
                                            0.0006
                                   0.914
## 57 ztHurdlepoisson geometric
## 58 ztHurdlepoisson oizt
                                   0
                                            0.0006
## 59 ztHurdlepoisson wrong_link
                                   0.914
## 60 ztHurdlepoisson ztoi
                                            0
## 61 ztoigeom
                                   0.832
                                            0
                      Hurdlezt
## 62 ztoigeom
                      correct
                                   0.946
                                            0.681
                                   0.773
## 63 ztoigeom
                                            0
                      negbin
## 64 ztoigeom
                      oizt
                                   0.876
                                            0
## 65 ztoigeom
                      poisson
                                   0
                                            0
## 66 ztoigeom
                      wrong_link 0.946
                                            0.681
## 67 ztoigeom
                      ztHurdle
                                   0.214
                                            0
## 68 ztoinegbin
                      Hurdlezt
                                   0.655
                                            0
## 69 ztoinegbin
                                   0.953
                                            0.836
                      correct
## 70 ztoinegbin
                      geom
                                   0
                                            0
                                            0
## 71 ztoinegbin
                      oizt
                                   0.702
## 72 ztoinegbin
                      poisson
                                   0
                                            0
## 73 ztoinegbin
                      wrong_link 0.950
                                            0.918
                                   0.762
## 74 ztoinegbin
                      ztHurdle
                                            0
## 75 ztoipoisson
                      Hurdlezt
                                   0.62
                                            0
## 76 ztoipoisson
                      correct
                                   0.944
                                            0.537
## 77 ztoipoisson
                      geometric
                                   0
                                            0
## 78 ztoipoisson
                      oizt
                                   0.892
                                            0
## 79 ztoipoisson
                      wrong_link
                                   0.944
                                            0.537
                                   0.006
## 80 ztoipoisson
                      ztHurdle
```

Visual results with confidence intervals:

```
qq3 <- dd |>
    ggplot(aes(x = data_fitted)) +
    facet_wrap(~ data_generation, scales = c("free_x"), ncol = 3) +
    geom_point(aes(y = mean), colour = "navy", cex = 2) +
    geom_errorbar(aes(ymin = lower, ymax = upper), colour = "navy") +
    ggtitle("Empirical coverage of log normal confidence intervals by true distribution of counts") +
    xlab("Fitted distribution") +
    ylab("Coverage")
```

Empirical coverage of log normal confidence intervals by true distribution o



Average sizes of confidence intervals:

```
qq4 <- results_data_frame |>
    subset(!is.na(point)) |>
    subset(point < 25000) |>
    group_by(data_generation, data_fitted) |>
    summarise(len = mean(conf_int_log_normal_upper - conf_int_log_normal_lower, na.rm = TRUE)) |>
    ggplot(aes(x = data_fitted, weight = len)) +
    geom_bar() +
    facet_wrap(~ data_generation, scales = "free", ncol = 3) +
    ylab("Average length") +
    xlab("Fitted distribution") +
    ggtitle("Empirical size of log normal confidence intervals by true distribution of counts")

## 'summarise()' has grouped output by 'data_generation'. You can override using
## the '.groups' argument.
```

Empirical size of log normal confidence intervals by true distribution of cou

