Computational Mathematics

Module description

This module gives you the mathematical foundations you need to learn how to think abstractly and introduces you to many of the standard mathematical tools and models necessary to understand and design computational systems and algorithms. By taking this module you will learn a wide range of the mathematical concepts and techniques that underpin Computer Science. In particular, you will study number systems, special functions, graphing, linear algebra and basic concept of combinatorics and probability theory.

Learners get to practice all of the above in multiple, weekly exercises and their knowledge is tested through engaging assignments and quizzes.

Module goals and objectives

Upon successful completion of this module, you will be able to:

- 1. Transform numbers between number bases and perform arithmetic in number bases
- 2. Use trigonometric definitions and identities to solve triangles and trigonometric equations, and to compute with vectors
- 3. Describe, represent, analyse and discover relationships between quantities by using functions, graphs, limits and differentiation, with functions including trigonometric, exponential and logarithmic
- 4. Translate between geometric and algebraic representations of shapes and spaces, including points, lines, vectors, matrices and linear transformations
- Use combinatorial techniques to describe, represent and count sample spaces and events, and calculate probabilities)

Textbook and Readings

Specific essential readings for each topic from the following list are included in the Readings page for each topic:

- -Croft, A. and R. Davison Foundation maths (Pearson) PDF available in Coursera https://www.dawsonera.com/abstract/9781292095196
- -Song Y. Yan- Number theory for computing (Springer)
- -Larson, R. Precalculus with limits (Cengage) https://www.dawsonera.com/abstract/9781337516853
- -Bone, G., G. Chadha, N. Saunders- A Level physics A for OCR Year 1 and AS Student Book (OUP) PDF available via Coursera
- -Vince- Mathematics for computer graphics (Springer) -

https://www.dawsonera.com/abstract/9781846282836

Kuldeep Singh, Linear Algebra: Step by Step Oxford Press (2013

Module outline

The module consists of ten topics that focus on key areas of the fundamentals of computational mathematics.

	Key concepts:
Topic 1.	Number bases, conversion and operations
	Learning outcomes:
	Represent numbers in different bases
	Convert from one number base to another
	Perform basic operations with binary numbers.

	Key concepts:		
Topic 2.	Sequences and series, recursion, arithmetic and geometric sequences		
	Learning outcomes:		
	Explain the notion of a number sequence and of convergence/divergence of a sequence		
	Use the recursion and the induction principle to define the elements of a sequence with application to arithmetic and geometric sequences		
	Introduce the notion of series and perform summation of geometric and arithmetic series		
	Key concepts:		
Topic 3.	modular arithmetic, congruent integers		
	Learning outcomes:		
	Define congruence modulo an integer		
	Classify two integers as congruent		
	Perform operations with congruent numbers		
Topic 4.	Key concepts: Angles, triangles and trigonometric relations		

	Learning outcomes:
	Work with angles and angle units, convert between degrees and radians.
	Derive and apply basic properties and trigonometric relations in triangles
	Solve basic problems with triangle elements using sine and cosine rule.
Topic 5.	Key concepts: Functions, Cartesian coordinates, graphs, kinematics.
	Learning outcomes:
	Define a function, its domain, codomain and type.
	Locate points on the plane using Cartesian coordinates.
	Plot a function in Cartesian coordinates.
	Derive and plot speed and distance travelled for uniform and uniformly accelerated motion
Topic 6.	Key concepts: Trigonometric functions
	Learning outcomes:
	Extend definition of Sin, Cos and Tan to any

	angle and derive their properties using the unit circumference in Cartesian coordinates. Define and use inverse of trigonometric functions (Arcfunctions) Plot trigonometric functions in Cartesian Coordinates
Topic 7.	Key concepts: Exponential and logarithmic functions
	Learning outcomes:
	Define exponential function from extension of integer powers to powers of any real number and derive its basic properties.
	Define logarithm as inverse of exponential function and derive its basic properties.
	Plot exponential and logarithmic functions in the Cartesian plane.
Topic 8.	Key concepts: Limits and differentiation
	Learning outcomes:
	Define and calculate the limit of a function at a point
	Use limits to identify asymptotic behavior of a function

	Formulate and calculate the derivative of a function from first principles Use differentiation to characterize the behavior of a function, to individuate local minima and maxima and turning points in its plot.
Topic 9.	Key concepts: Algebra, vector and matrices Learning outcomes: Define vector spaces and linear transformations Represent linear transformations as matrices and define composition of transformations as product of matrices. Solve a matrix equation of the form Mv=w where M is a square matrix and v and w two column vectors
Topic 10.	Key concepts: Combinatorics and Probability Learning outcomes:

Define combinations and permutations and learn how to apply them to counting problems
Thow to apply them to counting problems
Describe the sample space of a given
experiment and compute the probability P(x) of an outcome x of the experiment
Compute the joint probability of two events and determine if they are dependent or independent
determine it triey are dependent of independent

Activities of this module

The module is comprised of the following elements:

- Lecture videos. In each week the concepts you need to know will be presented through a collection of short video lectures. You may stream these videos for playback within the browser by clicking on their titles or download the videos.
- Practice Quizzes. Topics include practice quizzes, intended for you to assess your
 understanding of the content. You will be allowed unlimited attempts at each practice
 quiz. There is no time limit on how long you take to complete each attempt at the quiz.
 These quizzes do not contribute toward your final score in the class.
- Graded Assignments. There are two graded assignments, each is worth 50% of the final module grade. Each of these assignments is comprised of multiple parts which learners work on during earlier weeks. All assignments will be graded by the project tutors.
- Discussion Prompt. Topics also include discussion prompts. You will see the
 discussion prompt alongside other items in the lesson. Each prompt provides a space
 for you to respond. After responding, you can see and comment on your peers'
 responses. All prompts and responses are also accessible from the general discussion
 forum and the topic discussion forum.
- Readings. Topics may include several suggested readings. They are good supplementary materials for you to further understand the course topics.

How to pass this module

The module has two major assessments each worth 50% of your grade:

- Coursework. The coursework consists of several activities. They are detailed in the table below.
- Written examination. Details about the written examination are in the table below. Past papers will be available.

Activity	Required?	Deadline week	Estimated time per module	% of final grade
End of topic quizzes Topics 1-5	Yes	1-10	1-2 hours per quiz	0%
Written, staff graded coursework	Yes	11	Approximately 20 hours	50%
Written examination	Yes	22	2 hours 15 minutes	50%