**Extra Practice for Midterm**

**Heuristic/State Space Problems:**

There exists a game (called The Initiative\*) where you are searching for a specific piece of treasure on an n x n board. Each grid location has up to two places where you can search for treasure, and you have tokens that start in the top-left corner. The actions you can take each turn are: move up to 2 spaces on the grid, reveal all treasure in your current space, and reveal 1 of the treasures on any square in the board. You win the game once you find the treasure, navigate to the square containing it, and then travel to the bottom right square on the board.  
\*This description is slightly modified from the original game.  
  
(a) What variables would you use to represent the game state for this problem? Remember that the game state should be represented by a minimal set of variables.

(b) Using your state representation from a, how would the below state be represented/encoded? (? Represents a potential unrevealed treasure, N represents no treasure, and T represents a treasure. \* represents the player, and the contents of each || represent a grid cell. A 3x3 grid is being represented here.)  
  
|\*?? | N? | ?? |   
| ?? | ? | N? |   
| ?? | NN | ?? |

(c) What are the possible actions at each game state? What is the maximum number of actions you could take on a turn?  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
(d) What would the goal state look like, given your answer from a?   
  
  
  
  
  
  
  
  
  
(e) What heuristic might you use to solve this problem using A\* (assuming that the cost of each action is 1)? Is the heuristic admissible? Consistent?

**ML/MAP Problem:**

Suppose there is a bowl of chocolate candies at a party. Each candy is filled either with marshmallow filling or peanut-butter filling, but from the outside, the two types of candy are indistinguishable. Suppose you know that the friend of yours who prepared the bowl of candy made the bowl in one of three ways: the bowl either has:

25% marshmallow candy and 75% peanut butter (Option A), or

50% each kind (Option B), or

75% marshmallow and 25% peanut butter (Option C)

Suppose you reach into the bowl and draw out three pieces of candy, one at a time. Assume the type of candy you get when you choose each piece is conditionally independent of all the other candy choices, given you know the proportions of the candy in the bowl (this is not true in general, because each time you take a piece of candy it changes the proportions in the bowl, but let's just make the math easier and assume they don't change.)   
  
The first piece you choose is peanut butter, and the next two are each marshmallow.

Suppose your goal for this problem is to figure out of the three different possible proportions of candy in the bowl, which one your friend used.

1. What is the ML hypothesis after you choose the first piece of candy? After the second piece? After the third piece?
2. Suppose that you know your friend really likes peanut butter candy, so you estimate that there is a 2/3 chance the bowl is actually from Option A, and a 1/6 chance (each) from Option B and Option C. What is the MAP hypothesis after the first, second, and third pieces of candy are chosen from the bowl?

A picture containing text, tool, scissors

Description automatically generated

You should be prepared for problems relating to:

* Bayes nets and probabilistic reasoning
* Djikstra’s algorithm, A\* algorithm, greedy best-first search
* Minimax (with both alpha/beta pruning and with heuristics)
* Which approach that we’ve talked about so far is best for a specific context and why
* Heuristic design (including consistent/admissible), problem setup, and discussion about the state space.