

16784 Underactuated Project

November 2018

derivations of state equations

$$\begin{aligned} g_1(\mathbf{x}_n, \mathbf{u}_n, n) &= 0 \\ &\approx g_1(\mathbf{x}_n^{nom}, \mathbf{u}_n^{nom}, n) + \frac{\partial g_1}{\partial \mathbf{x}} \Big|_{\mathbf{x}_n^{nom}} (\mathbf{x} - \mathbf{x}_n^{nom}) + \frac{\partial g_1}{\partial \mathbf{u}} \Big|_{\mathbf{u}_n^{nom}} (\mathbf{u} - \mathbf{u}_n^{nom}) \\ &\approx -\mathbf{e}_n + \mathbf{D}_n \delta \mathbf{x}_n + \mathbf{E}_n \delta \mathbf{u}_n = 0 \\ \mathbf{e}_n &= \mathbf{D}_n \delta \mathbf{x}_n + \mathbf{E}_n \delta \mathbf{u}_n \end{aligned}$$

$$\begin{aligned} g_2(\mathbf{x}_n, n) &= 0 \\ &\approx g_2(\mathbf{x}_n^{nom}, n) + \frac{\partial g_2}{\partial \mathbf{x}} \Big|_{\mathbf{x}_n^{nom}} (\mathbf{x} - \mathbf{x}_n^{nom}) \\ &\approx -\mathbf{d}_n + \mathbf{C}_n \delta \mathbf{x}_n \\ \mathbf{d}_n &= \mathbf{C}_n \delta \mathbf{x}_n \end{aligned}$$

$$\begin{aligned} g_3(\mathbf{x}_N, N) &= 0 \\ &\approx g_3(\mathbf{x}_N^{nom}, N) + \frac{\partial g_3}{\partial \mathbf{x}} \Big|_{\mathbf{x}_N^{nom}} (\mathbf{x} - \mathbf{x}_N^{nom}) \\ &\approx -\mathbf{d}_N + \mathbf{C}_N \delta \mathbf{x}_N \\ \mathbf{d}_N &= \mathbf{C}_N \delta \mathbf{x}_N \end{aligned}$$