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# GraphNAS: Graph Neural Architecture Search with Reinforcement Learning

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## Abstract

Graph Neural Networks (GNNs) have been popularly used for analyzing non-Euclidean data such as social network data and biological data. Despite their success, the design of graph neural networks requires a lot of manual work and domain knowledge. In this paper, we propose a Graph Neural Architecture Search method (*GraphNAS* for short) that enables automatic search of the best graph neural architecture based on reinforcement learning. Specifically, GraphNAS first uses a recurrent network to generate variable-length strings that describe the architectures of graph neural networks, and then trains the recurrent network with reinforcement learning to maximize the expected accuracy of the generated architectures on a validation data set. Extensive experimental results on node classification tasks in both transductive and inductive learning settings demonstrate that GraphNAS can achieve consistently better performance on the Cora, Citeseer, Pubmed citation network, and protein-protein interaction network. On node classification tasks, GraphNAS can design a novel network architecture that rivals the best human-invented architecture in terms of test set accuracy.

## 1 Introduction

Graph Neural Networks (GNNs) have been popularly used for analyzing graph data such as social network data and biological data. The basic idea of GNNs such as GraphSAGE [Hamilton *et al.*, 2017] is to propagate feature information between neighboring nodes so that nodes can learn feature representations by using locally connected graph structure information.

Although GNNs have achieved great success, one shorting is to tune many parameters of the graph neural architectures. Similar to CNNs that contain many manually setting parameters such as the **sizes of filters**, the **types of pooling layers and residual connections**, tuning the parameters of GNNs generally takes heavy manual work which requires domain knowledge as well.

Recently we observe that reinforcement learning has been successfully used to generate accurate neural architectures for

CNNs and RNNs. The seminar work NAS [Zoph and Le, 2016] uses a recurrent network as controller to generate CNN and RNN network descriptions (which are referred to as child networks), and then uses the validation results of the child networks as feedback of the controller to maximize the expected accuracy of the generated architectures of the CNNs and RNNs. According to the experimental reports, the NAS search algorithm can improve CNNs and RNNs on benchmark data by percentage of 0.09 on the CIFAR-10 data and 3.6 perplexity on the Penn Treebank data. **Inspired by NAS, a large body of advanced neural architecture search algorithms based on reinforcement learning have been proposed to improve its efficient and accuracy**, such as the Efficient neural architecture search algorithm (ENAS [Pham *et al.*, 2018]) and Stochastic Neural Architecture Search algorithm (SNAS [Xie *et al.*, 2018]).

The promising results of using NAS to search neural architectures for CNNs and RNNs motivate us to use reinforcement learning to search graph neural architectures in this work. **Our idea** is similar to NAS for CNNs and RNNs that first uses a **recurrent network as controller** to generate the descriptions of GNNs and then **compute the rewards** of the GNNs **as feedback of the controller** to **maximize the expected accuracy** of the generated architectures of the GNNs. However, when using NAS for graph neural architecture search, the following new challenges need to be addressed:

- **Challenge 1. How to design the search space of GNNs.** Different from CNNs for processing regular grid-structural inputs, GNNs for processing graph data that are non-Euclidean and irregularly distributed in a feature space generally contain both spatial and convolutional descriptions [Hamilton *et al.*, 2017] and GCN [Kipf and Welling, 2017].
- **Challenge 2. How to design an efficient reinforcement learning search algorithm.** The search space of GNNs are generally **very large**. When generating the descriptions for GNNs by the controller, the training of reinforcement learning converges slowly.
- **Challenge 3. How to evaluate the performance of the algorithm in both transductive and inductive learning settings is the third challenge.**

In this paper, we present an efficient *Graph Neural Architecture Search* algorithm GraphNAS that can automatically

generate neural architecture for GNNs by using reinforcement learning. To solve *Challenge 1*, GraphNAS designs a search space covering **sampling functions**, **aggregation functions** and **gated functions**. To solve *Challenge 2*, GraphNAS uses a **new parameters sharing and architecture search algorithm** that is more efficient than NAS for CNNs and RNNs. To solve *Challenge 3*, we **validate the performance of GraphNAS on node classification tasks in both transductive and inductive learning settings**. The results demonstrate that GraphNAS can achieve consistently better performance on the Cora, Citeseer, Pubmed citation network, and protein-protein network. The **contribution** of the paper is fourfold:

- We first study the problem of using reinforcement learning to search graph neural architectures, which has the potential to save a lot of manual work for designing graph neural architectures.
- We present a new **GraphNAS algorithm** that can efficiently search the graph neural architectures in a large search space.
- We validate the performance of GraphNAS on real-world data sets. The results show that GraphNAS can design a graph neural architecture that rivals **the best human-invented architecture in terms of accuracy and F1 score on test sets**.
- We publish the Python codes based on Pytorch for future comparisons at: <https://github.com/GraphNAS/GraphNAS-simple>

## 2 Related work

**Graph Neural Networks.** The notation of graph neural networks was firstly outlined in the work [Gori *et al.*, 2005]. Inspired by the convolutional networks in computer vision, a large number of methods that re-define the notation of convolution filter for graph data have been proposed recently. convolution filters for graph data fall into two categories, spectral-based and spatial-based.

**As spectral methods usually handle the whole graph simultaneously and are difficult to parallel or scale to large graphs,** spatial-based graph convolutional networks have rapidly developed recently [Hamilton *et al.*, 2017; Monti *et al.*, 2017; Niepert *et al.*, 2016; Gao *et al.*, 2018; Velickovic *et al.*, 2017]. These methods directly perform the convolution in the graph domain by aggregating the neighbor nodes’ information. Together with **sampling strategies, the computation can be performed in a batch of nodes instead of the whole graph** [Hamilton *et al.*, 2017; Gao *et al.*, 2018].

Recent graph neural architectures follow the **neighborhood aggregation scheme** that consists of three types of functions, i.e., **neighbor sampling**, **correlation measurement**, and **information aggregation**. Each layer of GNNs includes the combination of the three types of functions. For example, each layer of semi-GCN [Kipf and Welling, 2017] consists of the first-order neighbor sampling, correlation measured by node’s degree and the aggregate function. ? ? ?

In this paper, we use reinforcement learning to search the **best combination of these types of functions on each layer of GNNs**, instead of manual settings in the previous work.

**Neural architecture search.** Neural architecture search (NAS) has been popularly used to design convolutional architectures for classification tasks with image and text streaming as input [Zoph and Le, 2016; Pham *et al.*, 2018; Xie *et al.*, 2018; Zoph *et al.*, 2018; Bello *et al.*, 2017].

The seminal work of using reinforcement learning for neural architecture search aims to automatically design deep neural architecture by using a **recurrent network to generate structure description of CNNs and RNNs**. Following the NAS, Evolution-based NAS such as work in [Real *et al.*, 2017; Real *et al.*, 2018] employs **evolution algorithm** to simultaneously optimize topology alongside with parameters. However, evolution-based methods take enormous computational time and could not leverage the efficient gradient back-propagation. To achieve the state-of-the-art performance as human-designed architectures, the work [Real *et al.*, 2018] takes 3150 GPU days for the whole evolution.

In comparison, the work ENAS [Pham *et al.*, 2018] is end-to-end for gradient back-propagation. To get rid of the architecture sampling process, DARTS [Liu *et al.*, 2018a] replace the feedback triggered by constant rewards in reinforcement learning with more efficient gradient feedback from generic loss.

## 3 Methods

In this section, we first introduce the problem of searching graph neural architectures with reinforcement learning. Then, we establish the search space and we discuss an efficient search algorithm based on **policy gradient descent** and the **parameter sharing** method **during training**.

### 3.1 Problem formulation

Given the search space of a graph neural architecture  $\mathcal{M}$ , we aim to find the best architecture  $m^* \in \mathcal{M}$  that maximizes the accuracy  $\mathcal{R}$  of the network on a validation set  $D$ . Here we use reinforcement learning to obtain  $m^*$  by sampling from feasible architectures in the space  $\mathcal{M}$  based on the rewards  $\mathcal{R}$  observed on  $D$ .

**Figure 1** shows the entire reinforcement learning framework. First, **the recurrent network generates network descriptions of GNNs**. Then, the generated GNNs are tested on the given validate set  $D$  and the **test results** are used as feedback of the recurrent network. The iteration maximizes the expected accuracy of the generated GNNs on the set  $D$ .

Formally, during the learning process, the recurrent network as the controller maximizes the expected accuracy  $\mathcal{E}_{P(m;\theta)}[\mathcal{R}(m(w^*, \mathcal{G}))]$  on the validation set  $D$ , where  $P(m;\theta)$  is the distribution of  $m$  parameterized by the choice of controller  $\theta$ , **and the shared weights  $w^*$  describing the architecture**. The learning is to minimize the training loss  $\mathcal{L}_{train}(m(w, \mathcal{G}))$  which can be represented as a bi-level optimization problem listed below,

$$\begin{aligned} \max_w \quad & \mathcal{E}[\mathcal{R}(m(w^*, \mathcal{G}))] \\ \text{s.t.} : \quad & w^* = \operatorname{argmin}_w \mathcal{L}_{train}(m(w, \mathcal{G})). \end{aligned} \quad (1)$$

优化目标：在测试集上GNN的准确率最高=在此参数下，GNN的损失值最小

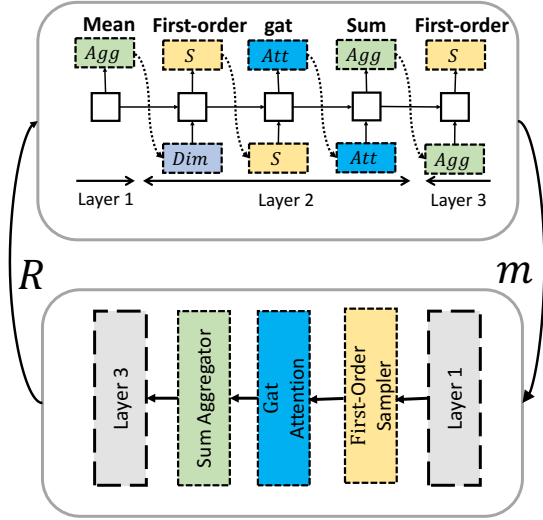


Figure 1: A simple illustration of GraphNAS. A recurrent network (the upper part) generates descriptions of graph neural architectures (the lower part), and then the validation results of the generated GNNs are used as **feedback** of the recurrent network (the upper part) to maximize the expected accuracy of the generated graph neural architecture (the lower part). The actions showed in current picture is not complete. All actions are described in Section 3.2

Table 1: Attention functions

Attention	Formula
const	$e_{ij}^{con} = 1$
gcn	$e_{ij}^{gcn} = 1/\sqrt{d_i d_j}$
gat	$e_{ij}^{gat} = leaky\_relu((W_l * h_i + W_r * h_j))$
sym-gat	$e_{ij}^{sym} = e_{ji}^{gat} + e_{ij}^{gat}$
cos	$e_{ij}^{cos} = \langle W_l * h_i, W_r * h_j \rangle$
linear	$e_{ij}^{lin} = tanh(sum(W_l * h_j))$
gene-linear	$e_{ij}^{gat} = W_a * tanh(W_l * h_i + W_r * h_j)$

The training process of Eq.(1) will be discussed in the remaining parts of this section. The goal of GraphNAS is to find  $m^*$  that maximizes the expected validation accuracy  $\mathcal{E}[\mathcal{R}(m(\mathcal{G}))]$ .

### 3.2 Search Space

In GraphNAS, we use a controller network to generate the descriptions of GNNs. The controller network used in GraphNAS is implemented as a recurrent neural network which requires a **state space**. In order to define the search space, we introduce a generalized framework of GNNs, where **each layer can be described as follows**,

1. **Feature transform functions.** The hidden embedding  $H^{i-1}$  ( $H^0$  represents the initial input) is multiplied by a weight matrix  $W_T$ , which is used to extract features and reduce feature dimensions. **For each layer of GNNs, the output dimension  $DLM$  is required.**
2. **Sampling functions.** Select the receptive field  $N(v)$  for a given target node. Many GNNs samples the first-

order neighbors iteratively and collect messages globally. GraphSAGE and PinSAGE sample a fixed size neighbor to speed up for large graphs. FastGCN uses importance sampling while maintaining the performance of the algorithm. LGCN sorts the first-order neighbors' features and selects top- $k$  features. For each layer, one of the sampling methods **SAM** is required.

3. **Correlation measure functions.** Calculate the correlation of node  $v$  with its neighbors  $N(v)$ . GAT assigns neighborhood importance by using attention layers. Semi-GCN assigns neighborhood importance according to the **degree of nodes**. More choices are listed in Table 1. For each layer, we choose one correlation measurement method **ATT** and repeat times  $\mathcal{K}$ .
4. **Aggregation functions.** Aggregate data from neighbors to generate an embedding for each node  $v$ . Most GNNs use the **sum aggregator**, **Mean aggregator**, **LSTM aggregator** and **pooling aggregator**. **MLP aggregator** are described in the work [Xu *et al.*, 2018]. For each layer, one of the aggregation functions **AGG** is required.
5. **Residual functions.** Merge historical hidden representation  $H^{his}$  as a part of the current embedding after a transform function. The merge function includes concatenation and adding. For each layer of GNNs, a previous **layer's index  $\mathcal{I}$**  and the activation function **ACT** of the current layer are required to build a residual layer.
6. **Gated functions.** As in GeniePath [Liu *et al.*, 2018b], the attention procedure learns the importance of neighbors with different sizes. Gated procedure extracts and filters signals aggregated from neighbors of distant hops.

To sum up, we define the search space of GNNs  $\mathcal{M}$  as follows: the **sampling dimension SAM**, the **correlation measure dimension ATT**, the **aggregation dimension AGG**, the numbers of multi-heads  $\mathcal{K}$ , the **output hidden embedding DLM**, the **previous layers' index  $\mathcal{I}$**  and the **activation function ACT**. As a result, GraphNAS can generate the architecture descriptions as a sequence of tokens. Each token represents one of the functions in the architecture space  $\mathcal{M}$ .

Note that we do not predict training parameters such as the **learning rates** of GNNs and we also assume that the architectures without **gated procedures** bring large computation and improvement during the initial stage of training. It is possible to add those actions as one of the predictions. **In our experiments, the process of generating an architecture stops if the number of layers exceeds a preset value.**

### 3.3 Search Algorithm

**Training the controller parameters  $\theta$ .** In order to maximize the objective function given in Eq.(1), we describe a **policy gradient method** to update parameters  $\theta$  so that the controller network generates better architectures over time.

The architecture descriptions (hyperparameters) of GNNs that **the controller predicts can be viewed as a list of actions  $m_{1:T}$** . GNNs will achieve an accuracy of  $m(w, \mathcal{G})$  on a held-out dataset at convergence. We use the accuracy  $\mathcal{R}$  as reward signal and use **reinforcement learning to train the controller**. Since the reward signal  $\mathcal{R}$  is non-differentiable, we use a policy gradient method to iteratively update  $\theta$  with a moving av-





graph on average. Each node has 50 features including positional, motif genes and signatures. Each node has multiple labels from 121 classes.

## 4.2 Baseline Methods

In order to evaluate the GNNs searched by GraphNAS, we choose the state-of-the-art GNNs for comparisons,

- Chebyshev [Defferrard *et al.*, 2016]. The method approximates the graph spectral convolutions by a truncated expansion in terms of Chebyshev polynomials up to T-th order. This method needs the graph Laplacian in advance, so that it only works in the transductive setting.
- Semi-GCN [Kipf and Welling, 2017] is the same as Chebyshev, **it works only in the transductive setting.**
- GraphSAGE [Hamilton *et al.*, 2017] consists of a group of inductive graph representations with different aggregation functions. The GCN-mean with residual connections is equivalent to GraphSAGE using mean pooling.
- GAT [Velickovic *et al.*, 2017] introduces attention into GNN. Therefore, GAT archives good results in both transductive and inductive learning.
- LGCN [Gao *et al.*, 2018] enables regular convolutional operations on generic graphs which archives good results in both transductive and inductive learning.

All the tasks in transductive learning are **single-label classification**. We use **accuracy as the measure for comparison**. On the other hand, tasks in transductive learning are **multi-label classification**, and we use **F1 score as the measure**.

## 4.3 Architecture on Transductive learning

**Search space.** Our search space consists of the functions listed in Section 3.2. For each layer of GNNs, the controller has to sample actions  $m \in DIM, SAM, ATT, K, AGG, ACT$  which do not contain previous layer index  $\mathcal{I}$  for skip connection. **In experiments on the citation dataset, there are usually two layers for GNNs**

**Training details.** The controller is a one-layer LSTM with **100 hidden units**. It is trained with the **ADAM optimizer** [Kingma and Ba, 2015] with a **learning rate of 0.0035**. The weights of the controller are initialized uniformly between -0.1 and 0.1. To prevent **premature convergence**, we also use a tanh of 2.5 and a temperature of 5.0 for the sampling logits [Bello *et al.*, 2017; Bello *et al.*, 2016], and add the controller’s sample entropy to the reward, weighted by 0.0001.

Once the controller samples an architecture, a child model is constructed and trained for 200 epochs **without parameter sharing**. During training, we apply **L2 regularization** with  $\lambda = 0.0005$  for Cora and Citeseer. Furthermore, dropout with  $p = 0.6$  is applied to **both layers’ inputs**, as well as to the normalized attention coefficients. For Pubmed, we set L2 regularization to  $\lambda = 0.001$ .

In all experiments, child models are initialized using the **Glorot initialization** [Glorot and Bengio, 2010] and trained to minimize **cross-entropy loss** on the training nodes using the **Adam SGD optimizer** [Kingma and Ba, 2015] with an initial learning rate of 0.01 for Pubmed, and 0.005 for all the

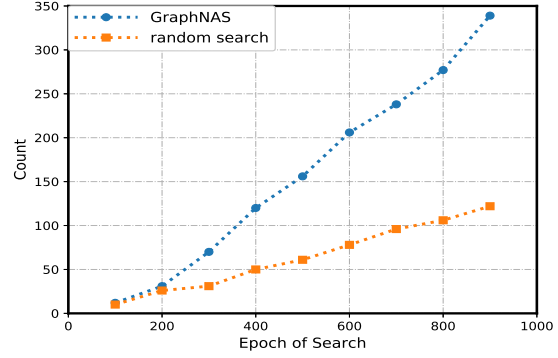


Figure 3: The number of GNNs whose accuracy over 0.81 on the validation set during search. Red line stands for GraphNAS, blue line stands for random search. GraphNAS outperforms random search.

Table 3: Performance of GraphNAS and the state-of-the-art on Cora.

Models	Depth	Params	Time(s)	Accuracy
Chebyshev	2	92K	0.49	81.2%
GCN	2	23K	0.08	81.5%
GAT	2	237K	0.62	83.0±0.7%
LGCN	2	56K	0.14	83.3±0.5%
random	2	364K	1.29	82.0±0.6%
GraphNAS	2	188K	0.13	84.2±1.0%

other datasets. In both cases we use an **early stopping strategy** according to the cross-entropy loss and accuracy on the validation nodes, with a patience of 100 epochs.

During training the controller, we fix the number of child network layers to be **two**, because many GNNs obtain the best performance on these dataset with **two layers**. Besides, we do not force GNNs sharing parameters, because training GNNs to convergence are fast on these datasets and models are easy to over-fitting in a semi-supervision task.

**Results.** After the controller trains 1,000 architectures, we collect **the top 5 architectures that achieve the best validation accuracy**. Then, we compute the test accuracy and time for each epoch of such models and summarize their results in Table 3. **The time reported here is the training time for running one epoch using a single 1080Ti GPU**. As can be seen from the table, GraphNAS can design several promising architectures that perform as well as some of the best models on this dataset. Other experiments results on citation network are listed in Table 4.

**Random Search.** Besides reinforcement learning, one can use random search to find the network. Although this baseline seems simple, it is often very hard to surpass. We report the number of GNNs model which has accuracy over 0.81 on validation set during search in Figure 3. And we list the best structure found by random search in Table3. The results show that GraphNAS trends to find better GNNs.

## 4.4 Architecture on Inductive Learning

**Search space.** We use the full search space defined in Section 3.2. For skip-connection, we perform two sets of experi-

Table 4: Performance of GraphNAS and the state-of-the-art models on Citeseer and Pubmed in term of accuracy.

Models	Citeseer	Pubmed
Chebyshev	69.8%	74.4%
GCN	70.3%	79.0%
GAT	72.5 $\pm$ 0.7%	79.0 $\pm$ 0.3%
LGCN	73.0 $\pm$ 0.6%	79.5 $\pm$ 0.2%
GraphNAS	73.1 $\pm$ 0.9%	79.6 $\pm$ 0.4%

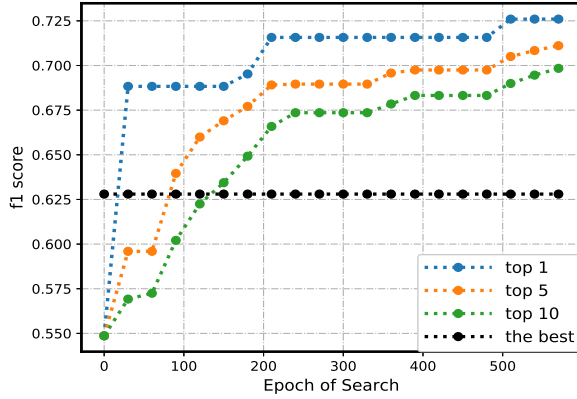


Figure 4: F1 score of the best GNNs on the ppi validation set during GraphNAS search. Blue is the best, Green is the average of top 5, Red is the average of top 10, Black is the best search in 600 structures which appears at the search 500<sup>th</sup>.

ments, where one fixes the input of residual layer with output of the last hidden layer and the other allows the controller to predict previous layer index to build skip-connection.

**Training details.** The setting of training and the controller are the same as in transductive learning. We use **parameter sharing** to solve the huge computational resource requirements. The shared parameters of the child models are trained using the **Adam SGD optimizer** with a learning rate of 0.005. Before training the controller, **the exploration process is executed at the first 20 epochs**. After that the controller is trained for 50 epochs. During training of the child model, we apply no L2 regularization and dropout. During the process, each GNN model sampled by the controller is trained for five epochs with shared parameters.

During the training of the controller, we fix the number of child networks **layers at three**, because most GNNs obtain the best performance on this dataset are with three layers.

**Results.** After the controller trained for 1,000 time, we let the controller to output the best model from 200 sampled GNNs. And we then compute the micro-f1 score and the time for each epoch of the model and summarize the results in Table 5. The time reported here is the training time for running one epoch using a single 1080Ti GPU. As can be seen from the table, GraphNAS can design several promising architectures that perform as well as the best models on this dataset.

**Effectiveness of parameters sharing.** To evaluate the effectiveness of parameter sharing strategy during search, we

Table 5: Performance of GraphNAS and the state-of-the-art on PPI.

Models	Depth	Params	micro-F1(%)
GraphSAGE(lstm)	2	0.26M	61.2
GeniePath	3	1.81M	97.9
GAT	3	3.64M	97.3 $\pm$ 0.2
LGCN	-	-	77.2 $\pm$ 0.2
GraphNAS( no sc)	3	3.95M	98.6 $\pm$ 0.1
GraphNAS with sc	3	2.11M	97.7 $\pm$ 0.2
NAS-like search	3	0.95M	95.7 $\pm$ 0.2
ENAS-like search	3	1.38M	96.5 $\pm$ 0.2

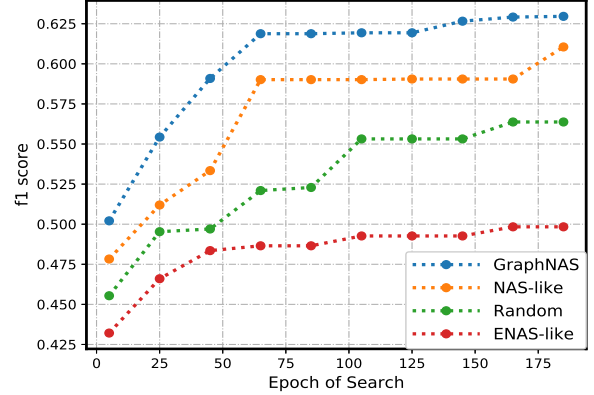


Figure 5: GraphNAS compares with *random search*, *NAS-like GraphNAS*, and *ENAS-like GraphNAS* on ppi dataset. GrpahNAS has the best F1 score.

compare the F1 score of the best structure designed by GraphNAS with parameters sharing and trained from scratch in Figure 4. **Both of them are trained for five epochs.**

**Comparison against Search strategy.** We compare GraphNAS with other search strategies including random search, reinforcement learning without parameter sharing (NAS-like), and GraphNAS without iterations of GNNs during training the controller (ENAS-like). Each sampled GNN is trained for two epochs. We show the model’s validation F1-score during training in Figure 5. The performance of the found best model are listed in Table5. The results show that GraphNAS trends to find a better GNN model.

## 5 Conclusions

In this paper, we study a new problem of graph neural architecture search with reinforcement learning. We present a GraphNAS algorithm that can design accurate graph neural network architectures that rival the best human-invented architectures in terms of test set accuracy. **Experiments on node classification tasks in both transductive and inductive learning settings** demonstrate that GraphNAS can achieve consistently better performance on citation networks, and protein-protein interaction network. Comparisons with existing search strategies show that the new parameters sharing and search strategy used in GraphNAS are effective.

## References

- [Bello *et al.*, 2016] Irwan Bello, Hieu Pham, Quoc V. Le, Mohammad Norouzi, and Samy Bengio. Neural combinatorial optimization with reinforcement learning. *CoRR*, abs/1611.09940, 2016.
- [Bello *et al.*, 2017] Irwan Bello, Barret Zoph, Vijay Vasudevan, and Quoc V. Le. Neural optimizer search with reinforcement learning. In *ICML*, 2017.
- [Defferrard *et al.*, 2016] Michaël Defferrard, Xavier Bresson, and Pierre Vandergheynst. Convolutional neural networks on graphs with fast localized spectral filtering. In *NIPS*, 2016.
- [Gao *et al.*, 2018] Hongyang Gao, Zhengyang Wang, and Shuiwang Ji. Large-scale learnable graph convolutional networks. In *KDD*, 2018.
- [Glorot and Bengio, 2010] Xavier Glorot and Yoshua Bengio. Understanding the difficulty of training deep feed-forward neural networks. In *AISTATS*, 2010.
- [Gori *et al.*, 2005] M. Gori, G. Monfardini, and F. Scarselli. A new model for learning in graph domains. In *IEEE International Joint Conference on Neural Networks*, 2005.
- [Hamilton *et al.*, 2017] William L. Hamilton, Zhitaoying, and Jure Leskovec. Inductive representation learning on large graphs. In *NIPS*, 2017.
- [Kingma and Ba, 2015] Diederik P. Kingma and Jimmy Ba. Adam: A method for stochastic optimization. *CoRR*, abs/1412.6980, 2015.
- [Kipf and Welling, 2017] Thomas N. Kipf and Max Welling. **Semi-supervised classification with graph convolutional networks**. In *International Conference on Learning Representations (ICLR)*, 2017.
- [Liu *et al.*, 2018a] Hanxiao Liu, Karen Simonyan, and Yiming Yang. Darts: Differentiable architecture search. *CoRR*, abs/1806.09055, 2018.
- [Liu *et al.*, 2018b] Ziqi Liu, Chaochao Chen, Longfei Li, Jun Zhou, Xiaolong Li, and Le Song. Geniepath: Graph neural networks with adaptive receptive paths. *CoRR*, abs/1802.00910, 2018.
- [Monti *et al.*, 2017] Federico Monti, Davide Boscaini, Jonathan Masci, Emanuele Rodolà, Jan Svoboda, and Michael M. Bronstein. Geometric deep learning on graphs and manifolds using mixture model cnns. *2017 IEEE Conference on Computer Vision and Pattern Recognition (CVPR)*, pages 5425–5434, 2017.
- [Niepert *et al.*, 2016] Mathias Niepert, Mohamed Ahmed, and Konstantin Kutzkov. Learning convolutional neural networks for graphs. In *ICML*, 2016.
- [Pham *et al.*, 2018] Hieu Pham, Melody Y. Guan, Barret Zoph, Quoc V. Le, and Jeff Dean. Efficient neural architecture search via parameter sharing. In *ICML*, 2018.
- [Real *et al.*, 2017] Esteban Real, Sherry Moore, Andrew Selle, Saurabh Saxena, Yutaka Leon Suematsu, Quoc V. Le, and Alexey Kurakin. Large-scale evolution of image classifiers. In *ICML*, 2017.
- [Real *et al.*, 2018] Esteban Real, Alok Aggarwal, Yanping Huang, and Quoc V. Le. Regularized evolution for image classifier architecture search. *CoRR*, abs/1802.01548, 2018.
- [Velickovic *et al.*, 2017] Petar Velickovic, Guillem Cucurull, Arantxa Casanova, Adriana Romero, Pietro Liò, and Yoshua Bengio. Graph attention networks. *CoRR*, abs/1710.10903, 2017.
- [Williams, 1992] Ronald J. Williams. Simple statistical gradient-following algorithms for connectionist reinforcement learning. *Machine Learning*, 8(3-4):229–256, 1992.
- [Xie *et al.*, 2018] Sirui Xie, H P Zheng, Chunxiao Liu, and Liang Lin. Snas: Stochastic neural architecture search. *CoRR*, abs/1812.09926, 2018.
- [Xu *et al.*, 2018] Keyulu Xu, Weihua Hu, Jure Leskovec, and Stefanie Jegelka. How powerful are graph neural networks? *CoRR*, abs/1810.00826, 2018.
- [Zoph and Le, 2016] Barret Zoph and Quoc V. Le. Neural architecture search with reinforcement learning. *CoRR*, abs/1611.01578, 2016.
- [Zoph *et al.*, 2018] Barret Zoph, Vijay Vasudevan, Jonathon Shlens, and Quoc V. Le. Learning transferable architectures for scalable image recognition. *2018 IEEE/CVF Conference on Computer Vision and Pattern Recognition*, pages 8697–8710, 2018.