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Recursive

```
public int gcd(int x, int y) {  
  
    1 if (y == 0) {  
    1     return x;  
    }  
    1 if (x >= y && x != 0) {  
    1     return gcd(y, x % y) ;  
    }  
    1     return 0;  
}
```

1(1)+1(1)+1

1+1+1

3

O(1) Constant

```
public int ack(int x, int y) {  
  
    1     if (x == 0) {  
    1         y = y + 1;  
    1         return y;  
    }  
    1     if (y == 0) {  
    1         return ack(x - 1, 1);  
    }  
    1     if (x != 0 && y != 0) {  
    1         return ack(x - 1, ack(x, y - 1));  
    }  
  
    1     return 0;  
}
```

1(1+1)+1(1)+1(1)+1

1(2)+1+1+1

4

O(1) Constant

Iteratively

```
public int gcd(int x, int y) {  
    logN    while(y != 0 && x >= y && x != 0) {  
        1        y = x%y;  
        1        return y;  
    }  
    1    return x;  
}
```

$\log N(1+1)+1$

$\log N(2)+1$

$2\log N+1$

$2\log N+0$

$2\log N$

$1\log N$

$O(\log N)$ LOGARITHMIC

```
public int ack(int x, int y) {  
    N    while (x == 0) {  
        1        y = y + 1;  
        1        return y;  
    }  
    N    while (y == 0) {  
        1        x = x - 1;  
        1        return x, 1;  
    }  
    N    while (y != 0 && x >= y && x != 0){  
        1        x = x - 1;  
        1        y = x, y-1;  
    }  
    1    return x;  
}
```

$N(1+1)+N(1+1)+N(1+1)+1$

$N(2)+N(2)+N(2)+1$

$$2N+2N+2N+1$$

$$6N+1$$

$$6N+0$$

$$6N$$

$$1N$$

$$\underline{O(N) \text{ LINEAR}}$$