

- - Check if any features have perfect correlation with target
- - Review each feature: "Can I get this before the sale?"
- 
- **\*\*Prevention\*\***:
- - Careful data pipeline auditing
- - Separate feature engineering from model training
- - Use time-based validation (harder to leak future into past)
- 
- **#### Pitfall 2: Not Modeling in Log-Space**
- 
- **\*\*Problem\*\***: Price distributions are heavily right-skewed
- ...
- Price distribution:
- Mean: \$18
- Median: \$12
- 90th percentile: \$35
- 99th percentile: \$150

Max: \$2,500

### Consequence:

- Models optimize average error → focus on common prices
- Large errors on expensive books don't matter much to MAE
- Predicting \$50 for a \$200 book is a \$150 error, but predicting \$12 for a \$10 book is only \$2 error

### Solution: Log-transform target

python

- *# Train on log prices*
- `y_train_log = np.log1p(y_train)`
- `model.fit(X_train, y_train_log)`
- 
- *# Predict and transform back*
- `y_pred_log = model.predict(X_test)`

`y_pred = np.expm1(y_pred_log) #  $\exp(x) - 1$ , inverse of  $\log1p$`

### Benefits:

- Treats percentage errors equally across price ranges
- More Gaussian distribution → better for linear models
- RMSLE natively optimized

**Caveat:** Back-transformation introduces **bias** (Jensen's inequality)

```
python
    ○ # Correction for bias

predictions_corrected = np.exp(predictions_log + 0.5 * residual_variance)
```

For tree models this matters less, but for neural networks it's important.

### **Pitfall 3: Overfitting to Text Features**

**Example:** 190 bag-of-words features caused linear regression to overfit badly

- In-sample  $R^2 = 0.95$  (great!)
- Out-of-sample  $R^2 = 0.18$  (terrible!)

**Why:** With many sparse text features (1000s of words), linear models can memorize training examples

**Solutions:**

#### **1. Dimensionality Reduction:**

```
python
    ○ from sklearn.decomposition import TruncatedSVD
    ○ svd = TruncatedSVD(n_components=50) # Reduce 5000 terms to 50 components

X_text_reduced = svd.fit_transform(X_text_tfidf)
```

#### **2. Feature Selection:**

```
python
    ○ from sklearn.feature_selection import SelectKBest, f_regression
    ○ selector = SelectKBest(f_regression, k=100) # Keep top 100 features

X_selected = selector.fit_transform(X_text, y)
```

#### **3. Regularization:**

```
python
    ○ from sklearn.linear_model import Ridge
```

```
model = Ridge(alpha=10.0) # Strong L2 penalty
```

#### 4. Use Tree Models:

- Random Forests and boosting handle high-dimensional sparse features much better
- They implicitly select relevant features through splitting

**Finding:** On same dataset, Random Forest achieved  $R^2 = 0.42$  with full text features (no overfitting), while linear regression peaked at 0.19.

#### Pitfall 4: Ignoring Temporal Drift

**Scenario:** Train on 2020-2023 data, deploy in 2025

- 2020-2021: Pandemic reading boom, high demand, higher prices
- 2023: Return to normal, prices stabilize
- 2025: New market conditions (streaming services offer audio, affecting book demand)

**Model trained on old data may:**

- Overestimate prices (baked in pandemic premium)
- Miss new trends (AI-generated books flooding market)
- Not account for platform changes (Amazon fee increases)

**Solutions:**

##### 1. Time-decayed Training Weights:

python

- *# Give more weight to recent data*
- `time_weights = np.exp(-0.5 * (current_date - df['sale_date']).dt.days / 365)`

```
model.fit(X, y, sample_weight=time_weights)
```

##### 2. Rolling Window Training:

python

- *# Only use last 2 years of data*
- `recent_data = df[df['sale_date'] >= '2023-01-01']`

```
model.fit(recent_data[features], recent_data['price'])
```

##### 3. Scheduled Retraining:

- Retrain model monthly/quarterly with fresh data

- Monitor performance degradation over time
- Set up alerts if accuracy drops below threshold

#### 4. Online Learning:

python

- *# Incrementally update model with new data*
- `from sklearn.linear_model import SGDRegressor`
- `model = SGDRegressor()`
- `for batch in new_data_stream:`

`model.partial_fit(batch[features], batch['price'])`

#### Pitfall 5: Ignoring Market Dynamics

**Problem:** Treating each listing as independent, ignoring competitive environment

**Reality:**

- On Amazon, if you're the 15th seller offering "Good" condition, your price must be competitive
- On eBay, if there are 5 active auctions for the same book, supply glut depresses prices

**Example:** Model predicts \$25 for a book based on historical average

- But currently 8 sellers list it at \$18-20
- Listing at \$25 → won't sell (overpriced relative to competition)

**Solutions:**

##### 1. Competitive Features:

python

- `df['num_competing_offers'] = get_current_offer_count(isbn)`
- `df['lowest_competing_price'] = get_lowest_price(isbn)`

`df['your_rank_if_priced_at_X'] = compute_rank(your_price, competing_prices)`

##### 2. Dynamic Adjustment:

python

- `base_prediction = model.predict(features)`
- `competitive_adjustment = compute_competitive_factor(isbn, base_prediction)`
- `final_prediction = base_prediction * competitive_adjustment`

- o ```
- o
- o **\*\*3. Reinforcement Learning\*\*** (advanced):
- o - Model the market **as** a Markov Decision Process
- o - State: Your inventory, competing listings, historical sales velocity
- o - Action: Set price at \$X
- o - Reward: Profit **if** sold, small penalty **if** inventory sits
- o - Learn optimal pricing policy through simulation
- o
- o **#### Pitfall 6: Poor Uncertainty Quantification**
- o
- o **\*\*Bad practice\*\***: Showing users a single point estimate
- o ```
- o Suggested price: \$23.47
- o ```
- o
- o **\*\*Problems\*\***:
- o - **False** precision (why .47 cents?)
- o - No indication of confidence
- o - User doesn't know **if** this **is** rock-solid (common textbook) **or** wild guess (rare collectible)
- o
- o **\*\*Better practice\*\***: Show ranges **and** confidence
- o ```
- o Suggested price: \$22 - \$26
- o Confidence: High (similar books sold recently)
- o
- o Comparable sales:
- o - \$24 (3 days ago, Very Good condition)
- o - \$21 (1 week ago, Good condition)
- o
- o - \$25 (2 weeks ago, Like New condition)

## How to generate ranges:

### 1. Quantile Regression (predict multiple percentiles):

python

- o **from** sklearn.ensemble **import** GradientBoostingRegressor
- o
- o **# Train three models**
- o model\_10th = GradientBoostingRegressor(loss='quantile', alpha=0.10)
- o model\_50th = GradientBoostingRegressor(loss='quantile', alpha=0.50) **# Median**
- o model\_90th = GradientBoostingRegressor(loss='quantile', alpha=0.90)

- 
- *# Predictions give 80% prediction interval*
- `lower = model_10th.predict(X)`
- `median = model_50th.predict(X)`

`upper = model_90th.predict(X)`

## 2. Quantile Regression Forests:

python

- `from sklearn.ensemble import RandomForestRegressor`
- 
- `rf = RandomForestRegressor(n_estimators=100)`
- `rf.fit(X_train, y_train)`
- 
- *# Each tree gives a prediction; distribution of predictions = uncertainty*
- `predictions_per_tree = [tree.predict(X_test) for tree in rf.estimators_]`
- `lower = np.percentile(predictions_per_tree, 10, axis=0)`

`upper = np.percentile(predictions_per_tree, 90, axis=0)`

## 3. Conformal Prediction (model-agnostic):

python

- `from sklearn.model_selection import train_test_split`
- 
- *# Split calibration set*
- `X_train, X_cal, y_train, y_cal = train_test_split(X, y, test_size=0.2)`
- 
- *# Train model on training set*
- `model.fit(X_train, y_train)`
- 
- *# Compute nonconformity scores on calibration set*
- `cal_predictions = model.predict(X_cal)`
- `nonconformity_scores = np.abs(y_cal - cal_predictions)`
- 
- *# For new prediction, interval is:*
- `prediction = model.predict(X_new)`
- `quantile = np.quantile(nonconformity_scores, 0.90) # 90% coverage`

`interval = (prediction - quantile, prediction + quantile)`

**Benefits:** Guaranteed coverage rate (90% of true prices will fall in these intervals) regardless of model type.

#### 4. Bayesian Approaches:

python

```
○ import pymc3 as pm
○
○ with pm.Model() as model:
○     # Priors
○     alpha = pm.Normal('alpha', mu=0, sd=10)
○     beta = pm.Normal('beta', mu=0, sd=10, shape=n_features)
○     sigma = pm.HalfNormal('sigma', sd=5)
○
○     # Likelihood
○     mu = alpha + pm.math.dot(X, beta)
○     y_obs = pm.Normal('y_obs', mu=mu, sd=sigma, observed=y)
○
○     # Inference
○     trace = pm.sample(2000)
○
○     # Posterior predictive distribution = uncertainty
○     ppc = pm.sample_posterior_predictive(trace, samples=1000)
○     predictions_distribution = ppc['y_obs']
○
○     # 90% credible interval
○     lower = np.percentile(predictions_distribution, 5, axis=0)
○     upper = np.percentile(predictions_distribution, 95, axis=0)
○     '''
○
○     **User-facing design**:
○     '''
○
○     |
○     | Suggested Listing Price |
○     | |
○     | $24 (typical sale price) |
○     | |
○     | Range: $21 - $27 |
○     | Based on 12 recent sales |
○     | |
○     | [Quick Sale] $21 |
○     | [Maximum Value] $27 |
○     | |
○     | Confidence: ●●●○ High |
```

---

## 4.4 Model Interpretation and Explainability

For user trust and debugging, understanding *why* the model predicts a certain price is crucial.

### Feature Importance

**Tree-based models** (built-in):

```
python

○ import matplotlib.pyplot as plt
○
○ # After training XGBoost/LightGBM/Random Forest
○ importances = model.feature_importances_
○ features = X.columns
○
○ # Sort and plot
○ indices = np.argsort(importances)[::-1][:20] # Top 20
○ plt.barh(range(20), importances[indices])
○ plt.yticks(range(20), features[indices])
○ plt.xlabel('Feature Importance')

plt.title('Top 20 Predictive Features')
```

**Typical findings:**

1. **Condition** (35% importance) - dominates everything
2. **Edition\_year** (12%)
3. **Text\_feature: "signed"** (8%)
4. **Avg\_rating** (7%)
5. **Format\_hardcover** (6%) ...

**Insight:** Condition is 3× more important than any other feature → ensure accurate condition data.

### SHAP Values (SHapley Additive exPlanations)

**Why SHAP?**

- Works for any model (trees, neural networks, linear)
- Shows contribution of each feature to a specific prediction
- Theoretically grounded (game theory)

```
python
```



```

○ import shap
○
○ # Create explainer
○ explainer = shap.TreeExplainer(model) # For tree models
○ shap_values = explainer.shap_values(X_test)
○
○ # Explain a single prediction
○ shap.initjs()
○ shap.force_plot(explainer.expected_value, shap_values[0], X_test.iloc[0])
○ '''
○
○ **Example explanation**:
○ '''
○ Base prediction: $18.50 (average across all books)
○
○ Condition = "Like New"      → +$8.00
○ Format = "Hardcover"        → +$3.50
○ Has_signature = True        → +$12.00
○ Book_age = 5 years          → -$2.00
○ Num_competing_offers = 23   → -$4.00
○
○      _____
○ Final prediction:          $36.00
○ '''
○
○ **User-facing explanation**:
○ '''
○ Why $36?
○
○ ✓ Like New condition adds $8
○ ✓ Hardcover format adds $3.50
○ ✓ Author signed adds $12
○ ✗ Multiple sellers competing reduces by $4
○ ✗ 5 years old reduces by $2
○
○

```

Similar books without signature typically sell for \$24

### Benefits:

- Builds user trust (transparency)
- Helps users understand what drives value
- Catches model errors (if SHAP says "blue cover adds \$50", something's wrong)

### Partial Dependence Plots

**Shows:** How predictions change as one feature varies (holding others constant)

```
python

○ from sklearn.inspection import partial_dependence, plot_partial_dependence
○
○ fig, ax = plt.subplots(figsize=(12, 4))
○ plot_partial_dependence(
○     model, X_train,
○     features=['book_age', 'avg_rating', 'num_pages'],
○     ax=ax
○
○ )
```

**Example insights:**

- **Book age:** Prices drop linearly for first 10 years, then flatten (classics hold value)
- **Avg rating:** Sharp increase above 4.5 stars (quality premium)
- **Num pages:** Weak positive relationship (thicker books slightly more expensive, but noisy)

**Use case:** Validate model learns sensible relationships (catches if model learned spurious correlations)

## 4.5 Deployment Considerations

### Latency Requirements

**Mobile app scanning barcode:**

- User expects near-instant feedback (< 2 seconds)
- **Challenges:**
  - API call to get ISBN metadata: ~200ms
  - Fetch competitive data (Amazon/eBay): ~500ms
  - Model inference: ?
  - Display result: ~100ms

**Inference time comparison:**

- **Linear regression:** < 1ms (thousands of predictions/sec)
- **Random Forest (100 trees):** ~10ms
- **XGBoost (500 rounds):** ~20ms
- **LSTM (small network):** ~50ms on CPU
- **BERT-based:** ~200ms on CPU, ~10ms on GPU

**Solutions for speed:**

## 1. Model Optimization:

```
python

○ # Reduce tree count
○ model = lgb.LGBMRegressor(n_estimators=100) # vs. 1000
○
○ # Quantize model (reduce precision)
○ import onnx
○ onnx_model = convert_to_onnx(model)

quantized = quantize_dynamic(onnx_model) # INT8 instead of FP32
```

## 2. Caching:

```
python

○ from functools import lru_cache
○
○ @lru_cache(maxsize=10000)
○ def predict_price(isbn, condition, format):
○     # Cache predictions for common ISBN+condition combos
○     features = get_features(isbn, condition, format)

return model.predict(features)
```

## 3. Async Processing:

```
python

○ # Return fast initial estimate, then refine
○ initial_estimate = simple_lookup(isbn) # Database of recent averages
○ send_to_user(initial_estimate)
○
○ # Meanwhile, run full model
○ detailed_prediction = run_full_model(isbn, features)

send_update_to_user(detailed_prediction)
```

## 4. Edge Deployment:

- Deploy lightweight model (50MB) directly in mobile app
- No API latency
- Works offline
- Update model monthly via app update

**Trade-off:** Smaller model (faster) vs. Larger model (more accurate)

**Practical approach:**

- Use simple lookup for common books (e.g., top 10,000 ISBNs account for 50% of queries)
- Run full model for rare books where accuracy matters more

### **Handling Cold Starts (Rare Books)**

**Problem:** 40% of ISBNs in your query stream have **zero historical sales** in training data

- Self-published books
- Very old out-of-print titles
- Foreign editions
- New releases

**Model trained on popular books will struggle**

**Solutions:**

**1. Content-Based Features** (don't require historical sales):

python

- *# These features work even for new books*
- - Publication year (determines age)
- - Format (hardcover vs paperback)
- - Genre (from categorization)
- - Synopsis text (using pre-trained BERT)
- - Author's other books' average prices

- Publisher's typical price range

**2. Transfer Learning from Similar Books:**

python

- *# Find similar books using embeddings*
- `synopsis_embedding = bert_model.encode(new_book_synopsis)`
- `similar_books = find_nearest_neighbors(synopsis_embedding, known_books_embeddings, k=10)`
- 
- *# Use weighted average of similar books' prices*
- `predicted_price = np.average([book.avg_price for book in similar_books],`

- weights=[book.similarity\_score for book in similar\_books]

)

### 3. Fallback to Publisher's List Price:

python

- if isbn not in training\_data:
- list\_price = get\_list\_price(isbn)
- if list\_price:
- *# Use rule-based depreciation*
- condition\_multipliers = {
- 'New': 0.85,
- 'Like New': 0.70,
- 'Very Good': 0.55,
- 'Good': 0.40,
- 'Acceptable': 0.25
- }
- predicted\_price = list\_price \* condition\_multipliers[condition]
- '''
- 
- *\*\*4. Wide Prediction Intervals\*\*:*
- '''
- Sorry, this book is rare in our database.
- 
- Estimated price: \$15 - \$45
- Confidence: Low
- 
- Suggestion: Check current Amazon listings for this ISBN
- '''
- 
- *\*\*Honest communication\*\* beats overconfident wrong predictions.*
- 
- *##### Continuous Learning Pipeline*
- 
- *\*\*Production ML system needs ongoing improvement\*\*:*
- '''
- User lists book → Suggested price → User adjusts? → Lists at final price →

Sells or not? → Feedback loop → Retrain model

### Feedback mechanisms:

#### 1. Implicit Feedback:

python

- *# Track user behavior*
- `if user_adjusted_price_down:`
- *# Model may have overpriced*
- `log_event('overpricing_signal', isbn=isbn, suggested=suggested, actual=actual)`
- 
- `if sold_within_24_hours:`
- *# Model priced well (or underpriced)*
- `log_event('quick_sale', isbn=isbn, price=price)`
- 
- `if no_sale_after_30_days:`
- *# Model may have overpriced, or item damaged*

`log_event('stale_listing', isbn=isbn, price=price)`

## 2. Explicit Feedback:

python

- *# Ask users after sale*
- `"Did this book sell at the suggested price?"`
- ☐ Yes, sold at \$24 (suggested)
- ☐ Sold, but I adjusted to \$20
- ☐ Haven't sold yet
- 
- *# Collect actual outcomes*
- `feedback_db.store({`
- `'isbn': isbn,`
- `'suggested_price': 24,`
- `'actual_listing_price': 20,`
- `'sale_price': 20,`
- `'days_to_sale': 7,`
- `'user_satisfaction': 4/5`

`})`

## 3. A/B Testing:

python

- *# Randomly assign users to model variants*
- `if user_id % 2 == 0:`
- `prediction = model_v1.predict(features) # Current model`

```

    ○ else:
    ○     prediction = model_v2.predict(features) # New model
    ○
    ○ # Compare performance
    ○ analyze_ab_test(
    ○     metric='conversion_rate', # % of listings that sold
    ○     variant_a='model_v1',
    ○     variant_b='model_v2'
    ○
    ○
    ○ )

```

#### 4. Automated Retraining:

```

python

    ○ # Weekly retraining pipeline
    ○ def retrain_pipeline():
    ○     # Fetch new sales data from last week
    ○     new_data = fetch_sales_data(since='7_days_ago')
    ○
    ○     # Append to training set
    ○     training_data = load_training_data()
    ○     updated_data = pd.concat([training_data, new_data])
    ○
    ○     # Keep only recent 2 years (prevent dataset bloat)
    ○     updated_data = updated_data[updated_data['date'] >= '2023-01-01']
    ○
    ○     # Retrain
    ○     new_model = train_model(updated_data)
    ○
    ○     # Validate performance hasn't degraded
    ○     validation_metrics = evaluate_model(new_model, validation_set)
    ○     if validation_metrics['rmse'] < current_model_rmse * 1.1: # Within 10%
    ○         deploy_model(new_model)
    ○     else:
    ○
    ○
    ○ alert_team("Model degradation detected")

```

#### 5. Drift Detection:

```

python

    ○ from scipy import stats
    ○
    ○ # Monitor prediction distribution over time

```

- week1\_predictions = predictions['2025-01-01':'2025-01-07']
- week2\_predictions = predictions['2025-01-08':'2025-01-14']
- 
- *# Statistical test for distribution shift*
- ks\_statistic, p\_value = stats.ks\_2samp(week1\_predictions, week2\_predictions)
- 
- if p\_value < 0.01:
- alert\_team(f"Prediction distribution shifted significantly (p={p\_value})")

*# May need retraining or investigation*

## 6. Feature Drift Monitoring:

python

- *# Track feature distributions*
- current\_avg\_rating = recent\_data['avg\_rating'].mean()
- baseline\_avg\_rating = 4.2 *# Historical average*
- 
- if abs(current\_avg\_rating - baseline\_avg\_rating) > 0.3:
- *# Data quality issue or market shift*

investigate\_feature\_drift('avg\_rating')

## Model Versioning and Rollback

Production requires safety nets:

python

- *# Model registry*
- models = {
- 'v1.0': {
- 'path': 's3://models/xgboost\_v1.0.pkl',
- 'deployed': '2024-06-01',
- 'metrics': {'rmse': 5.2, 'mae': 3.8},
- 'status': 'retired'
- },
- 'v1.1': {
- 'path': 's3://models/xgboost\_v1.1.pkl',
- 'deployed': '2024-09-01',
- 'metrics': {'rmse': 4.8, 'mae': 3.5},
- 'status': 'production'
- },
- 'v2.0': {



```

○     'path': 's3://models/lightgbm_v2.0.pkl',
○     'deployed': '2025-01-15',
○     'metrics': {'rmse': 4.5, 'mae': 3.2},
○     'status': 'canary' # 5% of traffic
○ }
○ }
○
○ # Canary deployment
○ def get_prediction(features, user_id):
○     if hash(user_id) % 100 < 5: # 5% of users
○         return models['v2.0'].predict(features)
○     else:
○         return models['v1.1'].predict(features)
○
○ # Monitor canary performance
○ canary_errors = monitor_errors(model='v2.0', window='24h')
○ if canary_errors > baseline_errors * 1.5:

```

```
rollback_to('v1.1')
```

### Rollback procedures:

python

```

○ def emergency_rollback():
○     # Instantly switch all traffic back to previous version
○     update_load_balancer(target_model='v1.1')
○
○     # Alert team
○     send_alert("Emergency rollback to v1.1 completed")
○
○     # Investigate new model offline

```

```
diagnose_model_issues('v2.0')
```

---

## 5. Market Dynamics and Decision Optimization

Statistical accuracy is necessary but not sufficient. Real-world pricing exists in a **competitive, dynamic market** where strategic considerations matter.

### 5.1 Prediction vs. Prescription

**Predictive question:** "What price will this book likely sell for?"

- Answers: "Based on historical data, similar books sold for \$22-26"
- Optimizes: Statistical accuracy (RMSE, MAE)

**Prescriptive question:** "What price should I list to maximize my objective?"

- Answers: "List at \$24 to sell quickly, or \$28 if you can wait for the right buyer"
- Optimizes: User utility (revenue, time-to-sale, convenience)

**Why they differ:**

**Example:** Used textbook, Good condition

- **Predicted average sale price:** \$32
- **Observed price distribution:**
  - 25% sold at \$25-28 (underpriced, sold in <3 days)
  - 50% sold at \$30-34 (well-priced, sold in 1-2 weeks)
  - 25% sold at \$35-40 (optimistic pricing, sold in 4-8 weeks)

**User's objective matters:**

- **Student needing quick cash:** List at \$27 (below average, sells in 2 days)
- **Casual seller, patient:** List at \$36 (above average, wait 6 weeks)
- **Professional reseller:** List at \$32 (median, balances time and revenue)

**Causal vs. Correlational:**

- Predictive model learns: "Books priced at \$40 typically sell for... \$40"
- But this is **selection bias**: Only well-priced \$40 books actually sell at \$40
- Overpriced \$40 listings don't sell (not in training data as "sales")
- **Causal question:** "If I price at \$40, what's the probability it sells within 30 days?"

## 5.2 Modeling Sale Probability

**Two-stage approach:**

**Stage 1: Will it sell?** (Classification)

python

- `from sklearn.ensemble import RandomForestClassifier`
- 
- *# Target: 1 if sold within 30 days, 0 if not*
- `X_features = ['listing_price', 'condition', 'num_competing_offers',`
- `'price_relative_to_market', ...]`

- `y_sold = df['sold_within_30_days']`
- 
- `classifier = RandomForestClassifier()`
- `classifier.fit(X_train, y_sold)`
- 
- *# Predict sale probability at different price points*
- `prices_to_test = [20, 25, 30, 35, 40]`
- `for price in prices_to_test:`
- `features_at_price = construct_features(isbn, condition, price)`
- `prob_sale = classifier.predict_proba(features_at_price)[0, 1]`
- `print(f"Price ${price}: {prob_sale:.1%} chance of sale in 30 days")`
- `...`
- 
- 
- *\*\*Output\*\*:*
- `...`
- Price \$20: 95% chance of sale in 30 days
- Price \$25: 85% chance
- Price \$30: 65% chance
- Price \$35: 40% chance

Price \$40: 20% chance

## Stage 2: If it sells, at what price? (Regression on sold items only)

python

- *# Train only on items that sold*
- `sold_items = df[df['sold'] == True]`

`price_model.fit(sold_items[features], sold_items['sale_price'])`

## Combined recommendation:

python

- `def recommend_price(isbn, condition, user_objective='balanced'):`
- *# Test price points*
- `price_range = np.arange(10, 50, 2)`
- `expected_values = []`
- 
- `for price in price_range:`
- `prob_sale = sale_probability_model.predict(price)`
- 
- `if user_objective == 'quick_sale':`
- *# Optimize for high probability of sale*

```

    utility = prob_sale
    elif user_objective == 'max_revenue':
        # Optimize expected revenue
        utility = prob_sale * price
    elif user_objective == 'balanced':
        # Balance revenue and time
        expected_days = 30 / prob_sale # Rough estimate
        utility = (prob_sale * price) / (1 + 0.1 * expected_days)
    expected_values.append(utility)

    optimal_idx = np.argmax(expected_values)
    return price_range[optimal_idx]
'''
'''Example output''':
'''
Quick sale strategy: List at $22 (90% chance of sale, avg 3 days)
Balanced strategy: List at $28 (70% chance of sale, avg 12 days)

```

Max revenue strategy: List at \$34 (45% chance of sale, avg 25 days)

### 5.3 Competitive Dynamics

**Game theory perspective:** Your pricing decision affects and is affected by competitors.

**Nash equilibrium concept:**

- If all sellers use the same ML model → prices converge to similar values
- This can lead to **price wars** (everyone undercuts by \$0.50)
- Or **implicit collusion** (everyone prices high because model says to)

**Amazon Buy Box dynamics:**

**Buy Box algorithm** (simplified):

python

```

def buy_box_probability(your_price, your_rating, your_fulfillment):
    # Fetch competing offers
    competitors = get_competing_offers(isbn)

    # Calculate competitiveness
    price_rank = rank(your_price, [c.price for c in competitors])

```