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CORSO DI LAUREA IN INFORMATICA

A Deep Learning approach for Time
Series Imputation on Photovoltaic data

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Contents

1	Background	1
1.1	Problem Definition	1
1.2	Photovoltaic Implant	2
1.2.1	Solar Module	2
1.2.2	Solar Array	2
1.2.3	Junction Box	3
1.2.4	Inverter	3
1.2.5	System Metering	4
1.3	Open-Meteo	4
1.4	Multi Layer Perceptron	5
1.5	Recurrent Neural Network	7
1.5.1	Gated Recurrent Unit	7
1.6	Transformer	8
1.7	Dataset	11
1.7.1	Inverter	12
1.7.2	Junction Box	14
1.7.3	Solargis	15
1.7.4	Meteorology	17
1.7.5	Meter	18
1.7.6	Other	19
2	Data Preprocessing	20
2.1	Dataset Realization	20
2.1.1	Timestamp cyclical encoding	22
2.1.2	Historical weather	23
2.1.3	Dealing with gaps	27
2.1.4	Target Feature	28
2.1.5	Re-Sampling	30
2.2	Feature Selection	31
2.3	Dataset Splitting	34

3 Deep Learning Models	35
3.1 MLP	36
3.1.1 Architecture	36
3.1.2 Training	38
3.2 RNN	40
3.2.1 Architecture	40
3.2.2 Training	43
3.3 Transformers	45
3.3.1 Architecture	46
3.3.2 Training	48
4 Experimental Results	51
4.1 MLP based model Evaluation	52
4.2 RNN based model Evaluation	55
4.3 Transformer based model Evaluation	59
4.4 Model Comparisons	64
4.5 Final Conclusions	68

Abstract

The growing need for the adoption of tools capable of generating clean energy from renewable and sustainable sources has led to extensive generation and collection of energy production data, especially from photovoltaic panels installed worldwide. However, these data often have gaps and deficiencies due to various factors such as temporary failures, adverse weather conditions, or malfunctions of sensors and data collection instruments. Accurate imputation of these gaps is crucial to ensure the reliability of analyses and predictions based on this data. This thesis aims to address the problem of imputing time series data from photovoltaic panels using advanced deep learning techniques. In particular, a deep learning model based on Fully Connected Neural Networks (FCNN) and Recurrent Neural Networks (RNN) are proposed to capture the complex temporal relationships between the total energy produced (target feature) and various components of the system. The models were trained on a dataset consisting of real data from a photovoltaic system with a power capacity of approximately $1MW$.

Chapter 1

Background

1.1 Problem Definition

This thesis aims to address the problem of imputing time series data from photovoltaic systems. Specifically, it often happens that data acquisition instruments in a system temporarily fail, causing a period of time, more or less extended, where the curve of the total energy produced is missing. (***VP* la frase seguente non va bene èer una tesi, non è scientifica, cosa sarebbe una simple formula?** Direi semplicemente quali sono le cose da considerare e la variabilità dettata anche dai diversi momenti della giornata e/o dell'anno) To try to fill this “gap” a simple formula is not sufficient, as various factors such as solar irradiance, ambient temperature, presence of clouds, rainfall, etc., need to be taken into account.

Formally, we can define the problem as follows. (***VP* nella def l'attenzione è puntata sui given invece che sull'oggetto della formula.)**

Definition 1.1.1 (Imputation problem). Given:

- A set of time series data representing a photovoltaic system, $S = S_1, S_2, \dots, S_N$, where N represents the number of available time series,
- A target time series $t \in S$ that represent the Total Generated Energy,

where each time series S_i is composed of ordered pairs (t_i, v_i) , where t_i is a timestamp representing the moment when the value v_i was recorded, the objective of the imputation problem is to estimate the missing or damaged values in the time series t .

1.2 Photovoltaic Implant

Solar photovoltaic (PV) energy systems are made up of different components. Each component has a specific role. The type of component in the system depends on the type of system and the purpose. For example, a simple PV-direct system is composed of a solar module or array (two or more modules wired together) and the load (energy-using device) it powers. A solar energy system produces direct current (DC)[21]. This is electricity which travels in one direction. The loads in a simple PV system also operate on direct current (DC). A stand-alone system with energy storage (a battery) will have more components than a PV- direct system. (*VP* Frasi corte d'accordo... ma quelle di questo paragrafo troppo. Rendilo più fluido. Inoltre non ho capito che c'entra la DC qui visto che ne parli anche dopo.)

1.2.1 Solar Module

The majority of solar modules available on the market and used for residential and commercial solar systems are silicon- crystalline. These modules consist of multiple strings of solar cells, wired in series (positive to negative), and are mounted in an aluminum frame. The size or area of the cell determines the amount of amperage; the larger the cell, the higher the amperage [21].

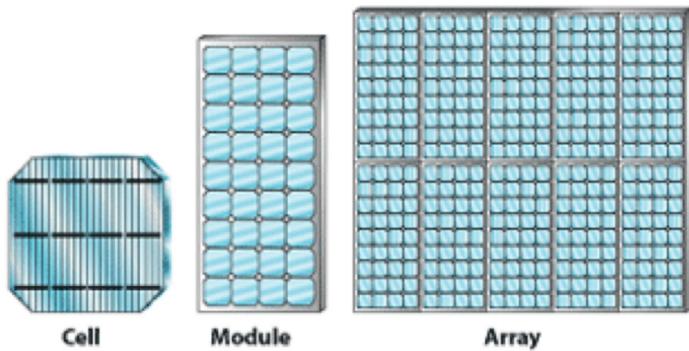


Figure 1.1: The solar cell is the basic component. Cells wired together and mounted in a frame compose a solar module. Several modules wired together form an array[21].

1.2.2 Solar Array

The solar array is made up of multiple PV modules wired together. Connecting the negative wire of one module to the positive wire of a second module is the

beginning of a series string. Wiring modules in series results in the voltage of each of the two modules is added together. A series string represents the summed voltages of each individual module. The negative cable of one module is connected to the positive cable of the next module. In a large system, multiple strings are assembled and the non-connected ends are connected to homerun leads which are landed at the terminals of an enclosure located near the array. The goal is to wire modules in series to build voltage.

1.2.3 Junction Box

A PV system array with multiple strings of modules will have a positive lead and a negative lead on the end of each string. The positive leads will be connected to individual fuses and the negative leads will be connected to a negative busbar in an enclosure. This is called the source circuit[21]. The junction box serves to “combine” multiple series strings into one parallel circuit. For example, an array with three strings of 10 modules wired in series would produce 300 volts (10 modules x 30 volts) per string and 4 amps per string. When the leads are landed in the combiner box, the circuit would produce 300 volts at 12 amps (3 strings x 4 amps/string). Once the circuits are combined, leaving the box it is referred to as the output circuit.

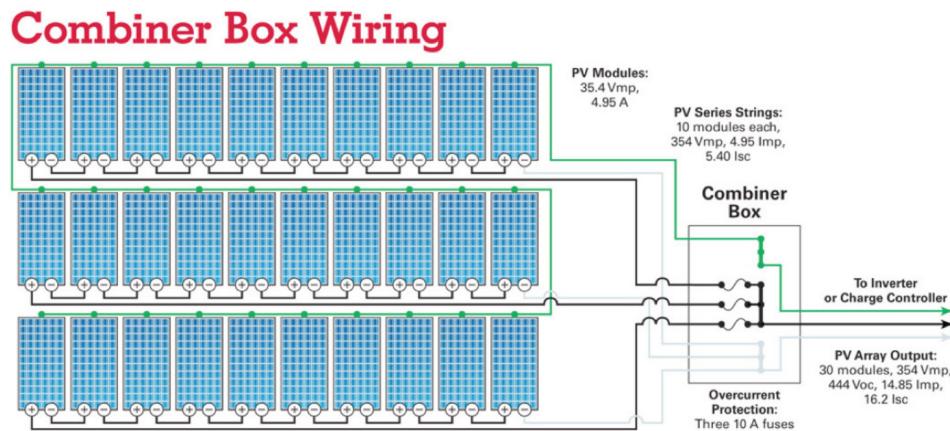


Figure 1.2: This figure represent an output circuit made of 3 string, each one hosts 10 solar modules[21].

1.2.4 Inverter

Energy from an array or a battery bank is direct current. This will provide for DC loads such a lights, fans, pumps, motors, and some specialty equipment. However,

if the energy is to be used to power loads that operate on alternating current (AC), as what is found in a residence, the current needs to be converted. The inverter changes DC energy to AC energy. Inverters are available in many different sizes for various-sized loads. A string inverter is used to convert DC power from a solar array to AC power and can be connected to an AC distribution power panel (service panel) in a residence or facility[21].

1.2.5 System Metering

Several tools are available to help the solar user to monitor their system. On stand-alone or off-grid PV systems, the battery meter is used to measure the energy coming in and going out of the battery bank. Charging and discharging of batteries, and proper functioning of the charging system is important to alert the user to incomplete charging, battery decline, or possible system shutdown[21]. System monitoring with web-based tools and apps allow the solar user to see system activity using a cell phone or tablet from a location away from their system.

1.3 Open-Meteo

Open-Meteo is an open-source weather data platform and community-driven weather forecasting project. It aims to provide access to weather data and forecasts that are openly accessible to the public and can be used for a variety of applications, including research, development, and personal use. It offers a diverse range of APIs that go beyond traditional weather forecasting such as past weather data, ocean data, air quality, ensemble forecasts, climate forecasts based on IPCC predictions, and even floods [24]. Open-Meteo offers over 80 years of hourly weather data, covering any location on earth, all at a 10 kilometer resolution. This extensive dataset is very useful to delve into the past and analyze historical weather patterns.

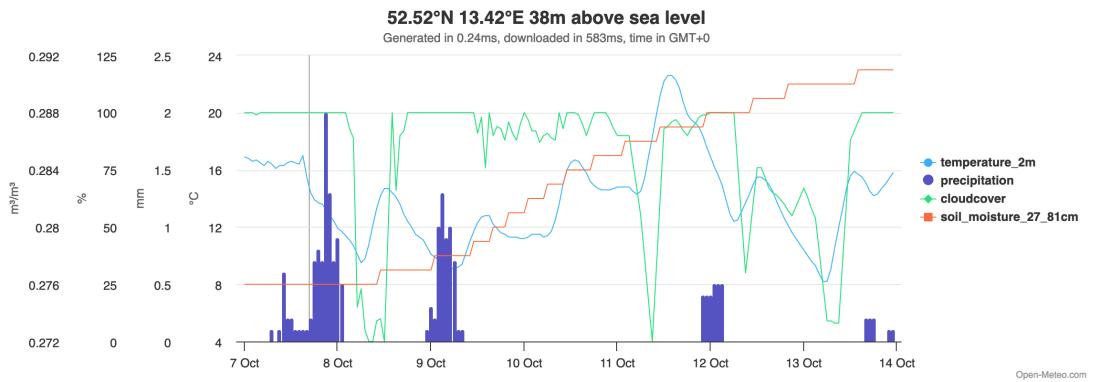


Figure 1.3: A plot about some Open-Meteo data.

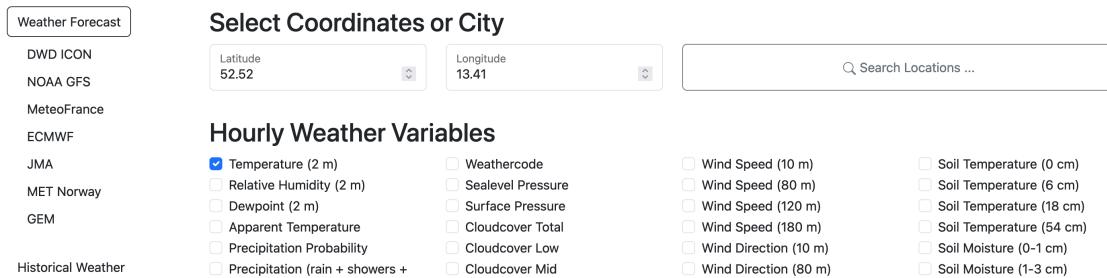


Figure 1.4: Open-Meteo forecast features.

1.4 Multi Layer Perceptron

The Multi Layer Perceptron model is the most known and most frequently used type of neural network. The signals are transmitted within the network in one direction, from input to output: there is no loop, the output of each neuron does not affect the neuron itself. Layers which are not directly connected to the environment are called hidden.

There are also feed-back networks, which can transmit impulses in both directions, due to reaction connections in the network. These types of networks are very powerful and can be extremely complicated. Introduction of several layers was determined by the need to increase the complexity of decision regions.

A perceptron with a single layer and one input generates decision regions under the form of semi planes. By adding another layer, each neuron acts as a standard perceptron for the outputs of the neurons in the anterior layer, thus the output of the network can estimate convex decision regions, resulting from the intersection of the semi planes generated by the neurons.

The power of the multilayer perceptron comes precisely from non-linear activation functions. Almost any non-linear function can be used for this purpose, except for polynomial functions. Currently, the functions most commonly used today are the single-pole (or logistic) sigmoid [17].

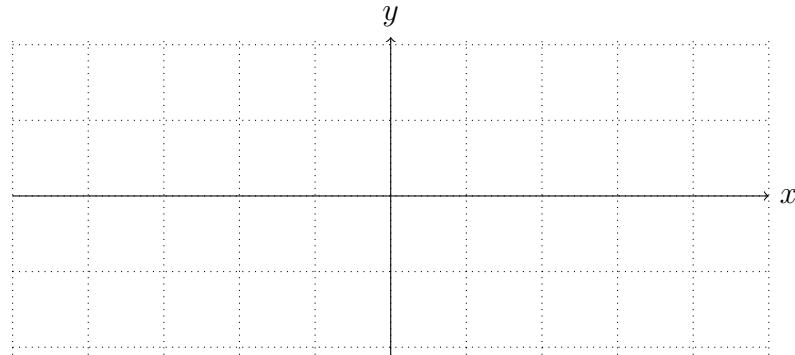


Figure 1.5: Sigmoid function $\sigma(x) = \frac{1}{1+e^{-x}}$

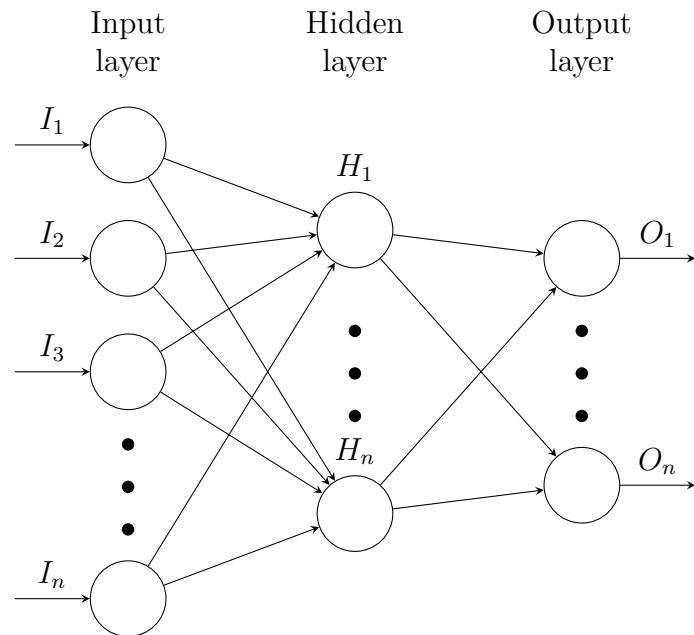
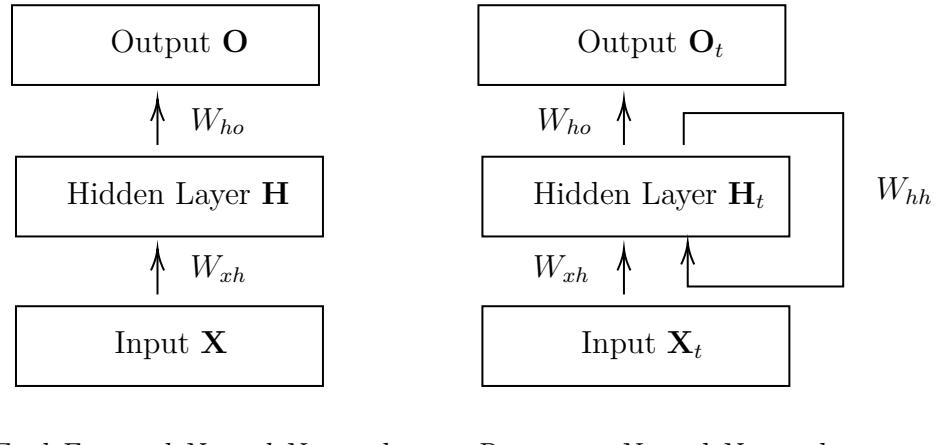


Figure 1.6: Multi Layer Perceptron architecture.

1.5 Recurrent Neural Network

Recurrent Neural Networks (RNNs) are a type of neural network architecture which is mainly used to detect patterns in sequences of data. Such data can be handwriting, genomes, text or numerical time series which are often produced in industry settings (e.g. stock markets or sensors). However, they are also applicable to images if these get respectively decomposed into a series of patches and treated as a sequence. On a higher level, RNNs find applications in Language Modelling and Generating Text, Speech Recognition, Generating Image Descriptions or Video Tagging.

What differentiates Recurrent Neural Networks from Multi-Layer Perceptrons (MLPs) and in general Feedforward Neural Networks is how information gets passed through the network. While Feedforward Networks pass information through the network without cycles, the RNN has cycles and transmits information back into itself [18]. This enables them to extend the functionality of Feedforward Networks to also take into account previous inputs $X_{0:t-1}$ and not only the current input X_t . This difference is visualised on a high level in Figure 1.7. Note, that here the option of having multiple hidden layers is aggregated to one Hidden Layer block H . This block can obviously be extended to multiple hidden layers.



Feed Forward Neural Network *Recurrent Neural Network*

Figure 1.7: Visualization of difference between MLPs and RNN.

1.5.1 Gated Recurrent Unit

Gated Recurrent Units (GRU) are an advanced variation of RNNs (Recurrent Neural Network) [1]. GRUs use update gate and reset gate for solving a standard RNNs vanishing gradient issue. These are essentially 2 vectors that decide the type of information to be passed towards the output. What makes these vectors

special is that programmers can train them to store information, especially from long ago [3].

They do all of this by utilizing its gated units which help solve vanishing/exploding gradient problems often found in traditional recurrent neural networks. These gates are helpful for controlling any information to be maintained or discarded for each step. It is also worth keeping in mind that gated recurrent units make use of reset and update gates.

- **Update Gates Function:** The main function of the update gate is to determine the ideal amount of earlier info that is important for the future. One of the main reasons why this function is so important is that the model can copy every single past detail to eliminate fading gradient issue.
- **Reset Gate's Function:** A major reason why reset gate is vital because it determines how much information should be ignored. It would be fair to compare reset gate to LSTMs forget gate because it tends to classify unrelated data, followed by getting the model to ignore and proceed without it.

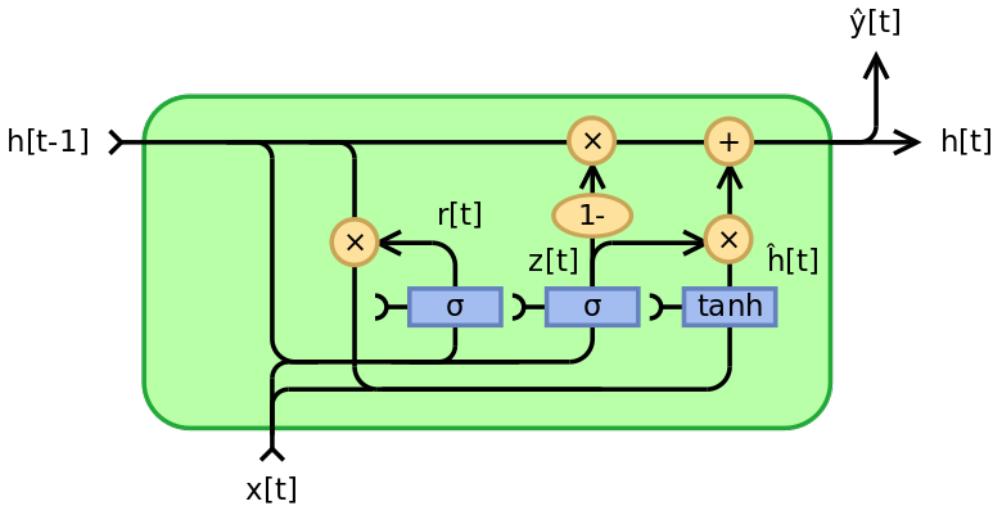


Figure 1.8: Gated Recurrent Unit (GRU) architecture.

1.6 Transformer

Recurrent neural networks, long short-term memory and gated recurrent neural networks in particular, have been firmly established as state of the art approaches in sequence modeling and transduction problems such as language modeling and

machine translation [22]. Recurrent models typically factor computation along the symbol positions of the input and output sequences. Aligning the positions to steps in computation time, they generate a sequence of hidden states h_t , as a function of the previous hidden state h_{t-1} and the input for position t . This inherently sequential nature precludes parallelization within training examples, which becomes critical at longer sequence lengths, as memory constraints limit batching across examples. Attention mechanisms [23] have become an integral part of compelling sequence modeling and transduction models in various tasks, allowing modeling of dependencies without regard to their distance in the input or output sequences. The Transformer allows for significantly more parallelization [4].

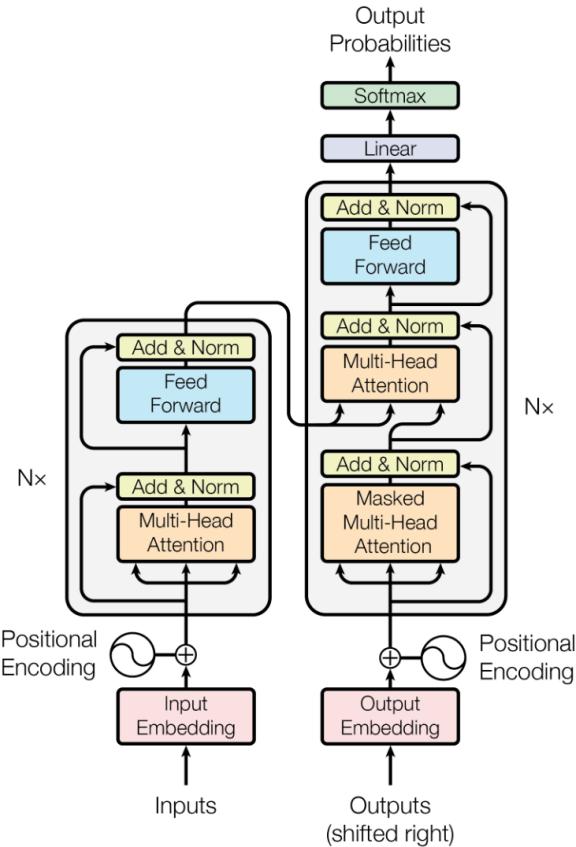


Figure 1.9: This figure shows the Transformers model architecture [23].

Most competitive neural sequence transduction models have an encoder-decoder structure [22]. Here, the encoder maps an input sequence of symbol representa-

tions (x_1, \dots, x_n) to a sequence of continuous representations $z = (z_1, \dots, z_n)$. Given z , the decoder then generates an output sequence (y_1, \dots, y_m) of symbols, one element at a time. At each step the model is auto-regressive, consuming the previously generated symbols as additional input when generating the next.

The Transformer follows this overall architecture using stacked self-attention and point-wise, fully connected layers for both the encoder and decoder, shown in the left and right halves of Figure 1.9, respectively.

- *Encoder:* The encoder is composed of a stack of $N = 6$ identical layers. Each layer has two sub-layers. The first is a multi-head self-attention mechanism[23], and the second is a simple, position- wise fully connected feed-forward network. Residual connection are employed around each of the two sub-layers, followed by layer normalization. That is, the output of each sub-layer is $\text{LayerNorm}(x + \text{Sublayer}(x))$, where $\text{Sublayer}(x)$ is the function implemented by the sub-layer itself. To facilitate these residual connections, all sub-layers in the model, as well as the embedding layers, produce outputs of dimension $d_{\text{model}} = 512$.
- *Decoder:* The decoder is also composed of a stack of $N = 6$ identical layers. In addition to the two sub-layers in each encoder layer, the decoder inserts a third sub-layer, which performs multi-head attention over the output of the encoder stack. Similar to the encoder, there are residual connections around each of the sub-layers, followed by layer normalization. The self-attention sub-layer is modified in the decoder stack to prevent positions from attending to subsequent positions. This masking[23], combined with fact that the output embeddings are offset by one position, ensures that the predictions for position i can depend only on the known outputs at positions less than i .
- *Attention:* An attention[23] function can be described as mapping a query and a set of key-value pairs to an output, where the query, keys, values, and output are all vectors[4]. The output is computed as a weighted sum of the values, where the weight assigned to each value is computed by a compatibility function of the query with the corresponding key[23].

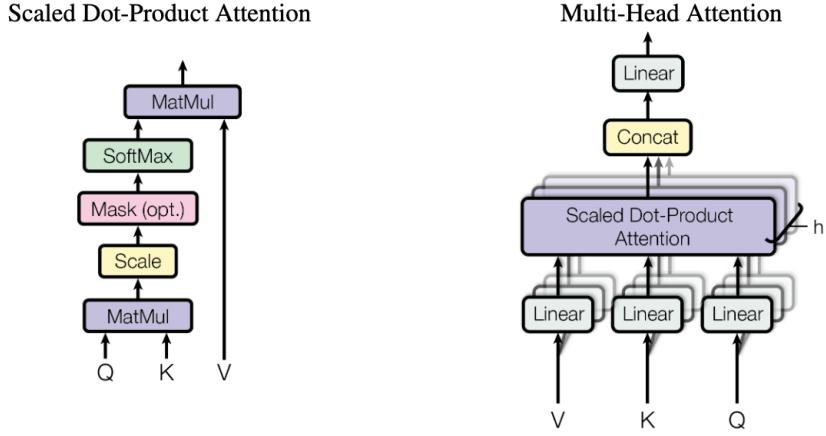


Figure 1.10: Scaled Dot-Product Attention[23] (left). Multi-Head Attention[23] consists of several attention layers running in parallel (right).

1.7 Dataset

(*VP* Sposterei questa sezione nel prossimo cap, che potresti intitolare **Dataset and Data Preprocessing**.) The dataset at our disposal describes a period of almost two years (from 02-02-2022 to 16-06-2023) and comes from a 978 kW photovoltaic plant located in the province of Bari. It consists of 3 inverters, 27 field panels, 1 meter, 1 solarimeter, 2 interface protections and 1 “system” device in which data from Solargis are stored. The dataset is organized into files, one for each type of device, representing each individual day, and the data is aggregated every 5 minutes. Each row contains a reference to the device it belongs to (`deviceName` and `deviceId`).

File Name
2022_02_02_Rofilo_NP00003174_inverter.csv
2022_02_02_Rofilo_NP00003174_meteorology.csv
2022_02_02_Rofilo_NP00003174_meter.csv
2022_02_02_Rofilo_NP00003174_other.csv
2022_02_02_Rofilo_NP00003174_plantDevice.csv
2022_02_02_Rofilo_NP00003174_stringbox.csv
2022_02_03_Rofilo_NP00003174_inverter.csv
2022_02_03_Rofilo_NP00003174_meteorology.csv
2022_02_03_Rofilo_NP00003174_meter.csv
2022_02_03_Rofilo_NP00003174_other.csv
2022_02_03_Rofilo_NP00003174_plantDevice.csv
2022_02_03_Rofilo_NP00003174_stringbox.csv
...

Table 1.1: Some files from our dataset.

timestamp	serial	...	TotalEnergy(kWh)	Frequency(Hz)	deviceid
2022-10-23 04:30:00	INV01	...	357196.88	50.06	83204
2022-10-23 04:35:00	INV01	...	357196.88	50.06	83204
...
2022-10-23 13:00:00	INV01	...	357921.16	49.95	83204
2022-10-23 13:05:00	INV01	...	357935.24	49.95	83204
...
01/02/2023 23:45	INV01	...	431324.36	49.88	83204
01/02/2023 23:50	INV01	...	431324.36	49.88	83204

Table 1.2: Some lines from an Inverter file.

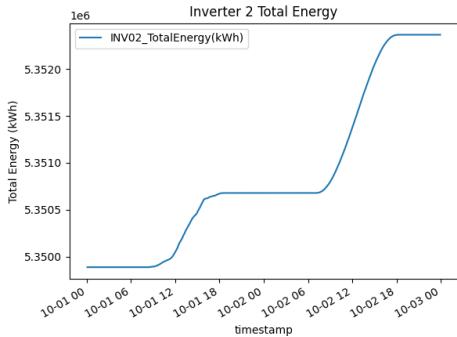
1.7.1 Inverter

Inside the files related to the inverters, we can find data such as the processor's operating temperature (`InternalTemperature`), various Alternating and Direct currents produced (`CurrentAC` and `CurrentDC`), Delivered Power, total energy produced by the individual inverter and other status and control bits that indicate various stages of the inverter's life (boot, reset, ready, etc.).

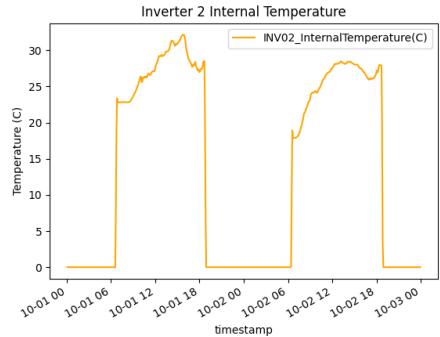
Down below a table with all the available features:

Name	Unit Symbol	Description
CommunicationCode	-	Communication Code
Failure 3	-	Active Alarm
Failure 4	-	Isolation Alarm
CurrentDC	A	Photovoltaic field Current
CurrentAC	A	Network Current
CurrentAC Phase1	A	Line RMS Current Phase R
CurrentAC Phase2	A	Line RMS Current Phase S
CurrentAC Phase3	A	Line RMS Current Phase T
TotalEnergy	kWh	Active Energy Delivered
Frequency	Hz	Network Frequency
PowerAC Phase1	kW	Line PA Phase R
PowerAC Phase2	kW	Line PA Phase S
PowerAC Phase3	kW	Line PA Phase T
PowerAC	kW	Delivered PA
PowerDC	kW	Photovoltaic field Power
Status	-	Inverter State
Failure	-	Network docking PLL State
Failure 2	-	Network State 1
Failure 1	-	Network State 2
InternalTemperature	C	CPU Temp.
HeatSinkTemperature	C	IGBT Temp.
VoltageDC	V	Photovoltaic field Voltage
VoltageAC	V	Network Voltage
VoltageAC Phase1	V	Line RMS Voltage Phase R
VoltageAC Phase2	V	Line RMS Voltage Phase S
VoltageAC Phase3	V	Line RMS Voltage Phase T

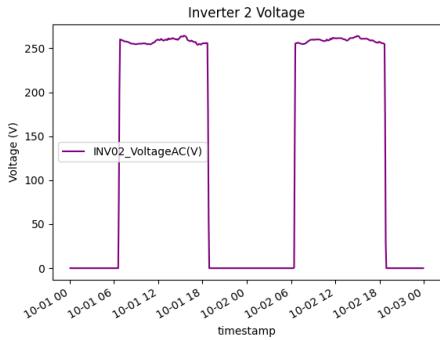
Table 1.3: All available features from an `inverter` file.



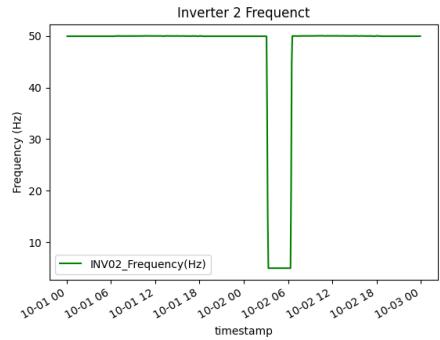
(a) Inverter 2 Total Energy plot.



(b) Inverter 2 CPU Temperature plot.



(c) Inverter 2 Voltage AC plot.



(d) Inverter 2 Frequency plot.

1.7.2 Junction Box

In the files related to the Junction Box or Combiner Box, we find data that describes the current production of the various strings they are connected to (CurrentString1–7, in general, each Junction Box manages 7 strings), some temperatures (such as ModuleTemperature), and some control bits to check proper operation.

Name	Unit Symbol	Description
CommunicationCode	-	Communication Code
Failure	-	Strings Alarm
CurrentString1	A	Current I1
CurrentString2	A	Current I2
CurrentString3	A	Current I3
CurrentString4	A	Current I4
CurrentString5	A	Current I5
CurrentString6	A	Current I6
CurrentString7	A	Current I7
AverageStringCurrent	A	Average Current
Irradiance	W/m ²	Modules Irradiation
Failure 1	-	Open Strings
Failure 2	-	Not Perform. Strings
EnvironmentTemperature	C	Environment Temperature
ModuleTemperature	C	Modules Temperature
InternalTemperature	C	Board Temperature

Table 1.4: All available features form a `stringbox` file.

1.7.3 Solargis

Solargis is a company specialized in providing solar data and forecasting services for photovoltaic installations and solar energy-related projects[19]. Their main goal is to provide precise and reliable information on solar irradiation and solar weather conditions anywhere in the world. This data is essential for the design, optimization, and management of photovoltaic systems. Solargis collects and provides detailed data on global, direct, and diffuse solar irradiation at every geographical location[19]. This data allows photovoltaic system developers to assess the amount of available solar energy in a given area, which is crucial for properly sizing the system and calculating production forecasts.

timestamp	...	SolargisGHI(W/m2)	SolargisGTI(W/m2)
2022-08-01 11:40:00	...	896	978
2022-08-01 11:45:00	...	896	978
2022-08-01 11:50:00	...	896	978
2022-08-01 11:55:00	...	914	1001
2022-08-01 12:00:00	...	914	1001
2022-08-01 12:05:00	...	914	1001
2022-08-01 12:10:00	...	928	1019
2022-08-01 12:15:00	...	928	1019
2022-08-01 12:20:00	...	928	1019

Table 1.5: Some Solargis data from 2022_08_01_Rofilo_NP00003174_plantDevice.csv file

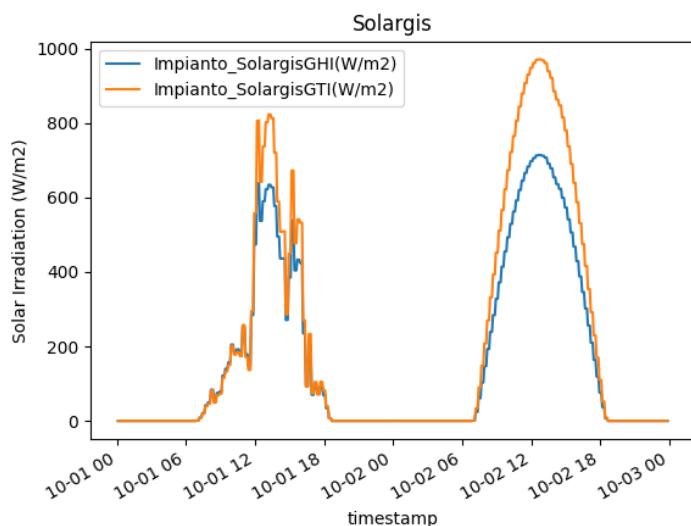


Figure 1.12: Solargis GHI & GTI plot.

Solar radiation takes a long journey until it reaches Earth's surface. So when modelling solar radiation, various interactions of extra-terrestrial solar radiation with the Earth's atmosphere, surface and objects are to be taken into account[19]. The component that is neither reflected nor scattered, and which directly reaches the surface, is called direct radiation; this is the component that produces shadows. The component that is scattered by the atmosphere, and which reaches the ground is called diffuse radiation. The small part of the radiation reflected by the

surface and reaching an inclined plane is called the reflected radiation. These three components together create global radiation.

In solar energy applications, the following parameters are commonly used in practice:

- Direct Normal Irradiation/Irradiance (DNI) is the component that is involved in thermal (concentrating solar power, CSP) and photovoltaic concentration technology (concentrated photovoltaic, CPV)[19].
- Global Horizontal Irradiation/Irradiance (GHI) is the sum of direct and diffuse radiation received on a horizontal plane. GHI is a reference radiation for the comparison of climatic zones; it is also essential parameter for calculation of radiation on a tilted plane[19].
- Global Tilted Irradiation/Irradiance (GTI), or total radiation received on a surface with defined tilt and azimuth, fixed or sun-tracking. This is the sum of the scattered radiation, direct and reflected. It is a reference for photovoltaic (PV) applications, and can be occasionally affected by shadow[19].

Name	Unit Symbol	Description
SolargisGHI	W/m ²	Solargis Global Horizontal Irradiation
SolargisGTI	W/m ²	Solargis Global Tilted Irradiation

Table 1.6: All available features from a `plantDevice` file.

1.7.4 Meteorology

In the Meteo files, we can find some environment temperature and solar irradiance data. Is important to mention that these features are not as powerful as weather forecast or Solargis data for the Imputation task.

Name	Unit Symbol	Description
COMMUNICATION_CODE SOL	-	Communication Code
Irradiance SOL	W/m ²	Irradiance
Module Temperature HEX SOL	-	All Registers
Module Temperature SOL	C	Module Temperature

Table 1.7: All available features from a `meteo` file.

1.7.5 Meter

The Meter files contain information about the current injected into and drawn from the network. It is from here that we get the values of our target feature `Cont_TotalEnergy(kWh)`.

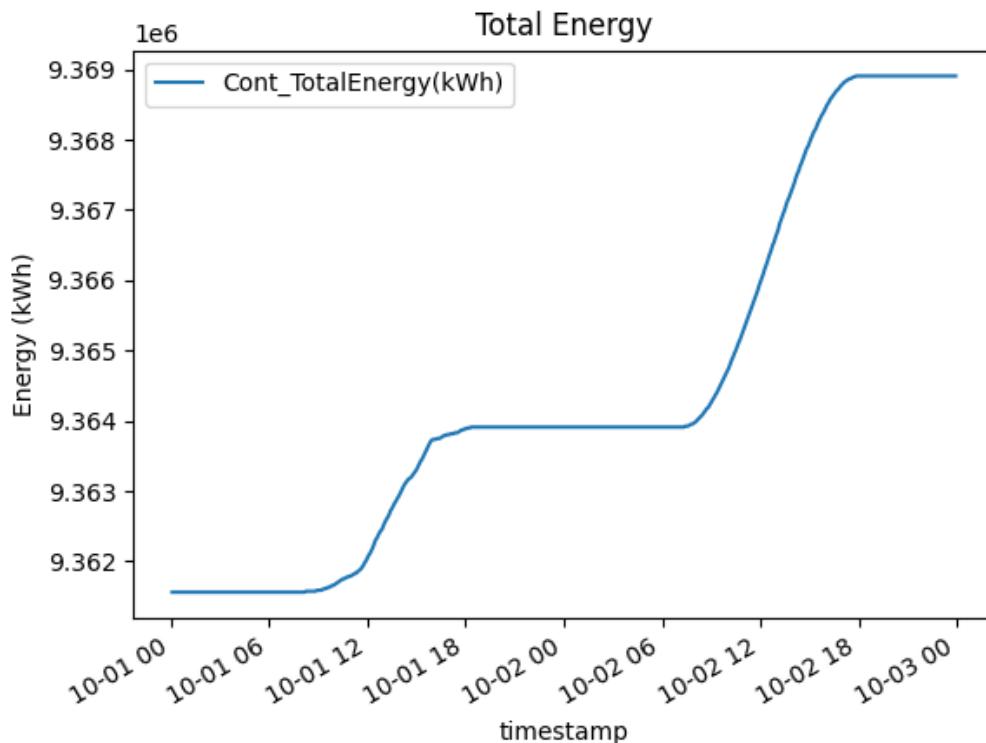


Figure 1.13: Total Energy plot, our target feature.

Name	Unit Symbol	Description
COMMUNICATION_CODE Cont	-	Communication Code
Status Cont	-	Status
Totale Energia Immessa Cont	kWh	Total Energy
Totale Energia Prelevata Cont	kWh	Total Energy Imported

Table 1.8: All available features from a `meter` file.

1.7.6 Other

In the Other type files, we can find the remaining, less relevant, features that describe the behavior and functioning of the leftover elements that make up the photovoltaic plant system.

Name	Unit Symbol	Description
COMMUNICATION_CODE NV10P	-	Communication Code
CB-State NV10P	-	CB State
Frequency NV10P	Hz	Frequency
IN1 NV10P	-	Digital IN 1
IN2 NV10P	-	Digital IN 2
Last Trip Cause NV10P	-	Last Trip Cause
NV10P - Trip BF	-	Digital IN 25
NV10P - Trip f<	-	Digital IN 24
NV10P - Trip f>	-	Digital IN 23
NV10P - Trip U<	-	Digital IN 21
NV10P - Trip U>	-	Digital IN 22
UE NV10P	V	UE
UL1 NV10P	V	Voltage AC Phase 1
UL2 NV10P	V	Voltage AC Phase 2
UL3 NV10P	V	Voltage AC Phase 3
Un NV10P	V	Un
Unp NV10P	V	Unp
COMMUNICATION_CODE NA16	-	Communication Code
CB-State NA16	-	CB State
IE NA16	A	IE
IL1 NA16	A	Current AC Phase 1
IL2 NA16	A	Current AC Phase 2
IL3 NA16	A	Current AC Phase 3
IN1 NA16	-	Digital IN 1
IN2 NA16	-	Digital IN 2
NA16 - Protection Trip	-	Digital IN 25

Table 1.9: All available features from an `other` file.

Chapter 2

Data Preprocessing

Having the dataset divided into different files, one for each day and device (see Section 1.7), with the presence of some periods, ranging from a few minutes to several days, of missing data (likely due to a data collection tool failure), results in many issues during the training phase and makes it almost impossible (***VP* non ho capito che vuoi dire, e non funziona grammaticalmente**). In this chapter, we will see how we have addressed these problems by opting for a monolithic tabular structure for the dataset and discussing the approaches we have used for handling missing data.

2.1 Dataset Realization

(***VP*** se sposti la sez 1.7, devi distinguere fra il dataset dei dati originali e quello ottenuto dalla loro lavorazione. Il primo potrebbe essere "Original Dataset"

For the creation of a dataset that can be passed directly to our imputation models, we devised a procedure that allowed us to merge all the original files into a single file, where for each timestamp, we have all the data for the entire system at that exact moment. Below is the final structure of the dataset and the algorithm for generating it.

timestamp	DEV.NAME ₁ _FEAT ₁	...	DEV.NAME _n _FEAT _n
01/10/2022 10:00
01/10/2022 10:05
01/10/2022 10:10

Table 2.1: Final dataset feature structure.

Algorithm 1 Dataset aggregation algorithm

Require: `data_folder`**Ensure:** `data_folder` exists

```
dev_types ← find all file types inside data_folder (e.g. meter, inverter, ...)  
dev_content ← a dictionary with dev_types types as keys and empty values  
for each key in dev_content.keys do  
    files ← find all file matching type key inside data_folder  
    sort files by date (asc.)  
    temp_type_aggregate ← an empty csv table  
    for each file in files do  
        append all file lines to temp_type_aggregate table  
    end for  
    dev_content[key] ← temp_type_aggregate  
end for  
    ▷ At this time we have a dictionary mapping a file type with all its available  
    data  
  
dataset ← an empty csv table  
for each type, data in dev_content do           ▷ type is key, data is value  
    rename all data columns to data.deviceID_column.name  
    except for 'timestamp' column  
    dataset ← dataset and data tables using 'timestamp' column  
end for  
save dataset table to file
```

timestamp	INV01_PowerAC	...	Cont_TotalEnergy
2022-02-02 00:05:00	NaN	...	NaN
2022-02-02 00:10:00	NaN	...	NaN
...
2022-06-22 10:20:00	175.66	...	8900941.5
2022-06-22 10:25:00	178.29	...	8900995.5
2022-06-22 10:30:00	180.82	...	8901036.0
...
2023-06-16 18:00:00	NaN	...	NaN
2023-06-16 18:05:00	NaN	...	NaN

Table 2.2: Some data from dataset after running Algorithm 1

2.1.1 Timestamp cyclical encoding

To enable the models to learn the alternation of minutes, days, and months as effectively as possible during the training phase, we applied a procedure to transform each individual timestamp into a pair of sine and cosine values, thus performing a cyclic encoding of various seasonalities.

Algorithm 2 Cyclical Encoding Algorithm

Require: dataset table

Ensure: dataset is not empty

```

dataset['minute_sin'] ← sin(2π( $\frac{\text{dataset.timestamp.minute}}{60}$ ))
dataset['minute_cos'] ← cos(2π( $\frac{\text{dataset.timestamp.minute}}{60}$ ))
dataset['hour_sin'] ← sin(2π( $\frac{\text{dataset.timestamp.hour}}{24}$ ))
dataset['hour_cos'] ← cos(2π( $\frac{\text{dataset.timestamp.hour}}{24}$ ))
dataset['day_sin'] ← sin(2π( $\frac{\text{dataset.timestamp.day}}{31}$ ))
dataset['day_cos'] ← cos(2π( $\frac{\text{dataset.timestamp.day}}{31}$ ))
dataset['month_sin'] ← sin(2π( $\frac{\text{dataset.timestamp.month}}{12}$ ))
dataset['month_cos'] ← cos(2π( $\frac{\text{dataset.timestamp.month}}{12}$ ))

```

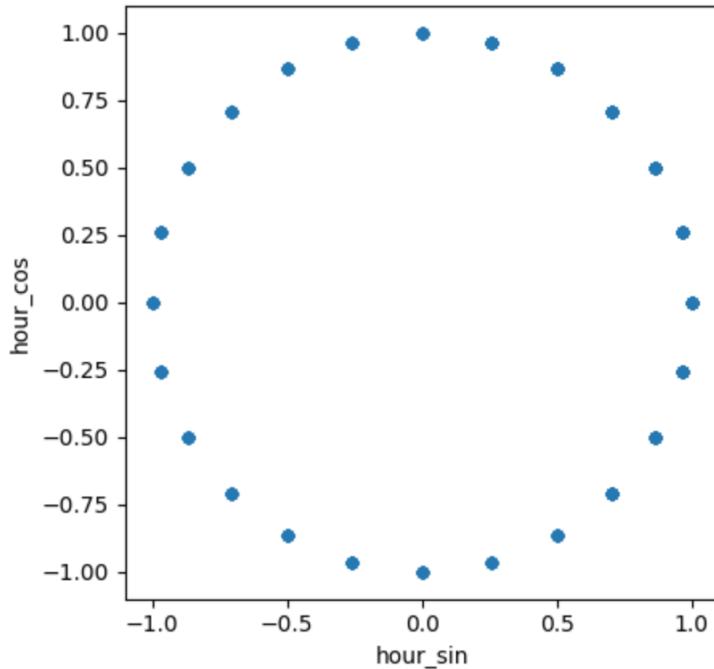


Figure 2.1: Hour cyclical encoding plot.

2.1.2 Historical weather

In addition to the information from Solargis (see Section 1.7.3), the models may require other weather data, such as cloud cover, rainfall, etc. Therefore, we made an API call to Open-Meteo servers (see Section 1.3), using the “Historical Weather” functionality, to obtain the accurate past forecasts for the time period covered by our dataset (from 02-02-2022 to 18-06-2023).

Algorithm 3 Open-Meteo data request Algorithm

Require: dataset table

Ensure: dataset is not empty

```
meteo_data ← require meteo feature from Open-Meteo public API  
dataset ← merge dataset and meteo_data tables using timestamp column  
  
/* At this time we have dataset timestamps as 5 minute frequency and  
meteo_data as 1 hour frequency. */  
  
use a forward fill method to fill gaps inside dataset table only for meteo_data  
columns.
```

We have obtained most of the information made available by Open-Meteo since the API request is free [24] and computationally and storage-wise inexpensive. These will be filtered at a later time (see Section 2.2). Among these, we find `sunrise` and `sunset`, which indicate the exact time (down to the minute) of when dawn and sunset occurred, respectively. These two features will be used to create a new column in our dataset called `is_day`, which will allow the model to understand whether it is analyzing a period of time during the day or night. This is to ensure that it does not make energy production predictions during the night.

Feature	Unit	Note
temperature_2m	°C	Air temperature at 2 meters above ground.
relativehumidity_2m	%	Relative humidity at 2 meters above ground.
dewpoint_2m	°C	Dew point temperature at 2 meters above ground. The dew point of a given body of air is the temperature to which it must be cooled to become saturated with water vapor. This temperature depends on the pressure and water content of the air.
apparent_temperature	°C	Apparent temperature is the perceived feels-like temperature combining wind chill factor, relative humidity and solar radiation.
precipitation	mm	Total precipitation (rain, showers, snow) sum of the preceding hour. Data is stored with a 0.1 mm precision. If precipitation data is summed up to monthly sums, there might be small inconsistencies with the total precipitation amount.
weathercode	wmo	Weather condition as a numeric code. Follow WMO weather interpretation codes. Weather code is calculated from cloud cover analysis, precipitation and snowfall. As barely no information about atmospheric stability is available, estimation about thunderstorms is not possible.
pressure_msl surface_pressure	hPa	Atmospheric air pressure reduced to mean sea level (msl) or pressure at surface. Typically pressure on mean sea level is used in meteorology. Surface pressure gets lower with increasing elevation.
cloudcover	Instant	Total cloud cover as an area fraction.
et0_fao_	mm	ET_0 Reference Evapotranspiration of a well watered grass field. Based on FAO-56 Penman-Monteith equations ET_0 is calculated from temperature, wind speed, humidity and solar radiation. Unlimited soil water is assumed. ET_0 is commonly used to estimate the required irrigation for plants.
evapotranspiration		

vapor_pressure_deficit	kPa	Vapor Pressure Deficit (VPD) in kilopascal (kPa). For high VPD (>1.6), water transpiration of plants increases. For low VPD (<0.4), transpiration decreases.
windspeed_10m windspeed_100m	km/h	Wind speed at 10 or 100 meters above ground. Wind speed on 10 meters is the standard level.
winddirection_10m winddirection_100m	̄	Wind direction at 10 or 100 meters above ground.
windgusts_10m	km/h	Gusts at 10 meters above ground of the indicated hour. Wind gusts in CERRA are defined as the maximum wind gusts of the preceding hour.
soil_temperature_0_to_7cm soil_temperature_7_to_28cm soil_temperature_28_to_100cm soil_temperature_100_to_255cm	̄C	Average temperature of different soil levels below ground.
soil_moisture_0_to_7cm soil_moisture_7_to_28cm soil_moisture_28_to_100cm soil_moisture_100_to_255cm	m ³ /m ³	Average soil water content as volumetric mixing ratio at 0-7, 7-28, 28-100 and 100-255 cm depths.

Table 2.3: All feature selected from Open-Meteo with description[24].

The new feature `is_day` contains two values: 0 and 1, representing *Night* and *Day*, respectively. To create this feature, we add 0 with a frequency of 5 minutes until sunrise, then add 1 until sunset, and finally add more 0s until the end of the day. We repeat this process for each day in the dataset to create a new column that, for each timestamp, will indicate whether it is day or night.

Algorithm 4 is_day feature generation Algorithm

Require: dataset table, sunrise and sunset table
Ensure: dataset is not empty, sunrise and sunset tables match dataset days
is_day \leftarrow empty table column
for each day **in** dataset.days **do**
 temp_is_day \leftarrow empty table column
 day_start \leftarrow sunrise[day] \triangleright get sunrise timestamp for that day
 day_start \leftarrow find the nearest dataset.timestamp to day_start
 day_end \leftarrow sunset[day]
 day_end \leftarrow find the nearest dataset.timestamp to day_end
 /* if sunrise[day] = 7:04 then day_start = 7:05 */

 /* 0 means Night, 1 mean Day */
 temp_is_day \leftarrow add 0s starting from 00:00 to day_start
 as 5 minute frequency
 temp_is_day \leftarrow add 1s starting from day_start to day_end
 as 5 minute frequency
 temp_is_day \leftarrow add 0s starting from day_end day end
 as 5 minute frequency
 append to is_day column temp_is_day values
end for
merge is_day column to dataset table

2.1.3 Dealing with gaps

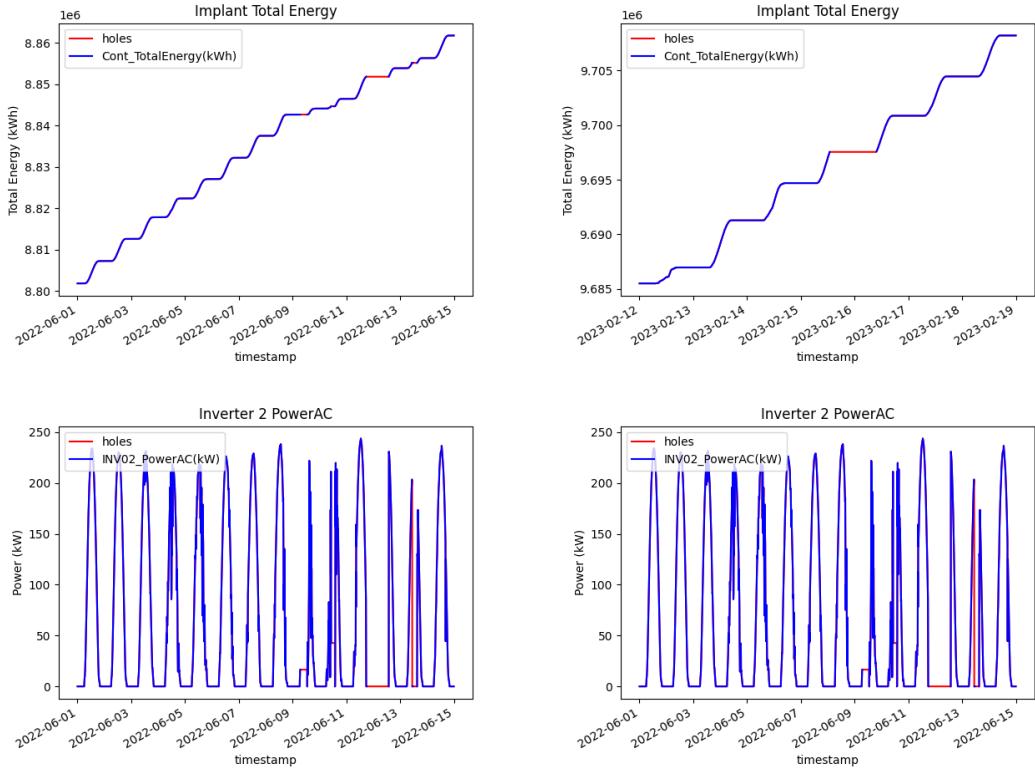


Figure 2.2: Some dataset ‘holes’. The charts at the top refer to the Implant’s Total Energy, while those at the bottom refer to the Inverter 2’s Power. The charts on the left range from 01-06-2022 to 15-06-2022, while those on the right range from 12-02-2023 to 19-02-2023.

As we can see from Figure 2.2, there are certain periods within the dataset (highlighted in red) where data is missing, which we refer to as ‘holes’. These data gaps can cause problems during model training (hindering the correct calculation of the loss function), and therefore, they need to be removed.

One possible approach for holes removal is to perform a *fill* operation: filling the gap with the first available non-null value. This tactic may be considered acceptable only if the time span involves just a few timestamps. However, if we are talking about several hours or even days, it significantly distorts the overall production and instantaneous power trends, resulting, especially in very unfortunate cases, with extremely abnormal production curves.

The solution we have adopted to address this problem is the removal of the entire day when a hole occurs. For example, if we have a data gap from 12-02-2023

23:00 to 13-02-2023 10:40, the days 12-02-2023 and 13-02-2023 will be completely removed. With this method, we lose some data, but as we will see later, the number of gaps is not extremely high, and this data loss is not debilitating. The following algorithm summarizes what has just been described.

Algorithm 5 Holes Removal Algorithm.

Require: dataset table

Ensure: dataset is not empty

```

holes ← find all timestamp from dataset
table, where there are some Nans inside the
columns
for each row in dataset.rows do
    if row.timestamp is in holes then
        drop row from dataset table
    end if
end for
```

Timestamp
2022-06-09
2022-06-10
2022-06-11
2022-06-12
2022-06-13
2022-06-28
2022-06-29
2022-06-30
2022-08-26
2022-09-23
2022-10-06
2023-02-03
2023-02-15
2023-02-16
2023-03-26

Table 2.4: Timestamps deleted after running the Algorithm 5

2.1.4 Target Feature

For the deep learning models that we will introduce later, it could be very difficult learning how to predict the Total Missing Energy, as it is a curve that grows constantly, potentially to infinity. These models need to have features that vary within a limited range of values. To achieve this, we transformed the variable `Cont_TotalEnergy(kWh)` from cumulative to instantaneous values of produced energy, thereby limiting its values within a finite range. This new feature was added to the dataset with the name `target`.

Algorithm 6 Cumulative Energy to Instant Energy Algorithm.

Require: dataset table

Ensure: dataset is not empty

```
target ← empty column
for each (prev_val, val) in dataset["Cont_TotalEnergy(kWh)"] do
    diff ← val – prev_val
    append diff value to target column
end for
/* Now we have target column with first value missing */
/* We can add a 0 as fist value because its night time */
append (in head) 0 to target column
merge target and dataset
```

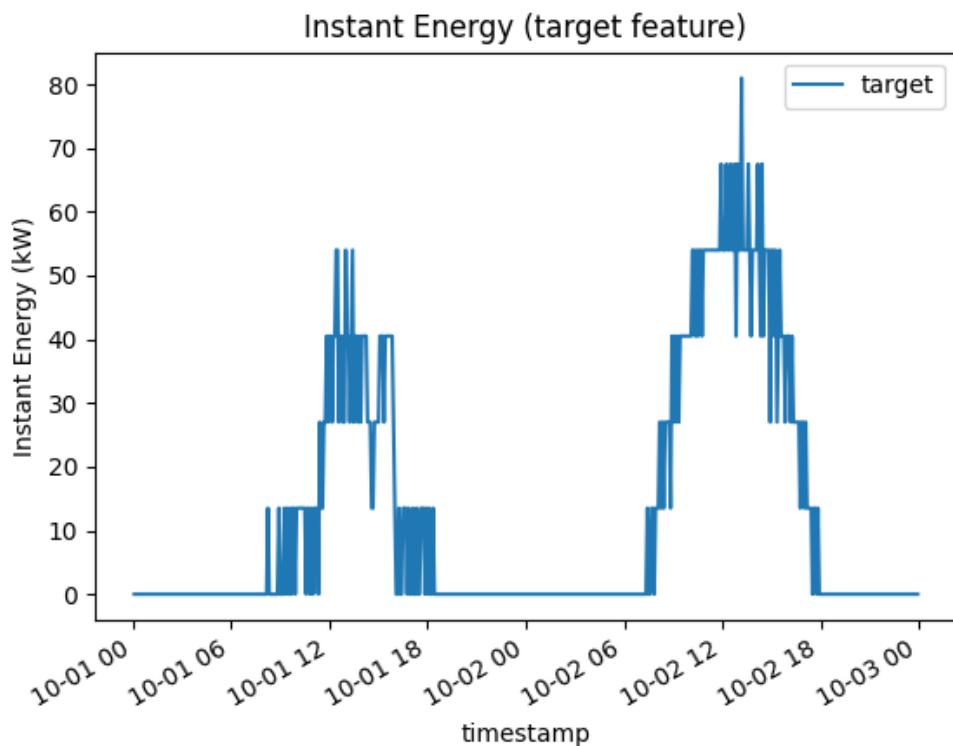


Figure 2.3: Instant Energy (target feature) 2 days plot.

2.1.5 Re-Sampling

Finally, after all the operations described above, we obtain a dataset with samples taken at 5-minute intervals. As we can see from Figure 2.3, this data appears to be quite noisy, which could pose challenges during the training phase. Moreover, most of the reports provided by photovoltaic plant operators are at a 15-minute frequency. To prevent potential issues and align with this standard, we have written and applied a re-sampling procedure.

Algorithm 7 15 minute Re-Sampling Algorithm.

Require: dataset table

Ensure: dataset is not empty

```
for each feature in dataset.features do
    if feature is Cumulative then
        feature ← sample feature column using 15 min. sampling rate
    else
        feature ← aggregate values every 15 minutes and sum them to form a
single value
    end if
end for
```

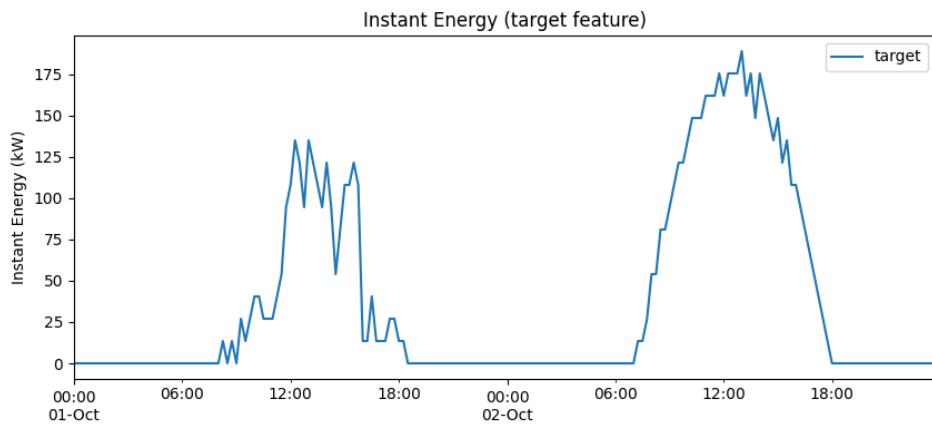


Figure 2.4: Instant Energy feature on 15 minute re-sampled dataset.

2.2 Feature Selection

After applying all the procedures described in the previous section, we find ourselves with a dataset composed of 764 columns. This high number of features would make it nearly impossible to train various models, both from a purely hardware perspective and due to the excessive information redundancy. In an attempt to minimize the number of features as much as possible, we applied and combined the results of two essential tools for feature selection: the *Correlation Matrix*[14] and the *Power Predictive Score*[6].

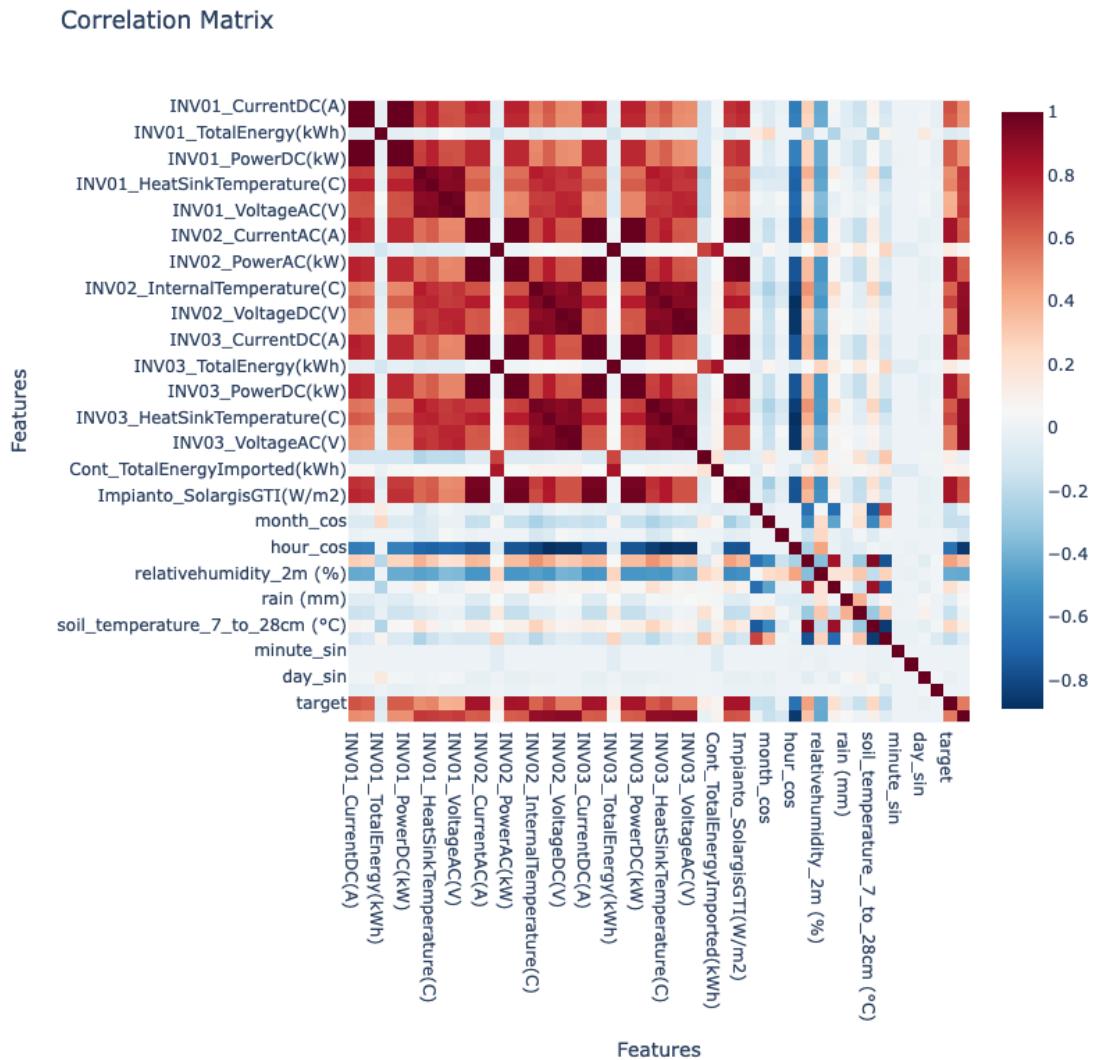


Figure 2.5: Correlation Matrix

As we can infer, even with a naive approach, all the information from the various String Boxes and Junction Boxes is perfectly summarized by the data provided by the various Inverters (see Section 1.2); a similar reasoning can be applied to the features coming from *Other* (those starting with `other_`), as they do not provide any useful information for energy estimation. Consulting the Correlation Matrix (Figure 2.5), we can see that this naive reasoning is confirmed because the features of the junction boxes have a high level of correlation with those of the Inverters. In general, we want to retain features that are minimally correlated with each other and aim to discard highly correlated ones, keeping only those that are more representative.

Applying this approach straightforwardly, however, is not the best choice because it could lead to the loss of important information. Let's consider an example: let's take into account the features `INV01_Power(kW)`, `INV02_Power(kW)`, and `INV03_Power(kW)`; by examining the correlation matrix, these three features are highly correlated, and, therefore, we should retain only one of them. However, all three are important for predicting our target. For instance, if Inverter 1 experiences any issues and is not operating at 100%, this will impact the total energy production, making all three of these features indispensable. Therefore, in conjunction with the correlation matrix, we have utilized the *Power Predictive Score* (PPS): an asymmetric, data-type-agnostic score that can detect linear or non-linear relationships between two or more columns[6]. The score ranges from 0 (no predictive power) to 1 (perfect predictive power)[6].

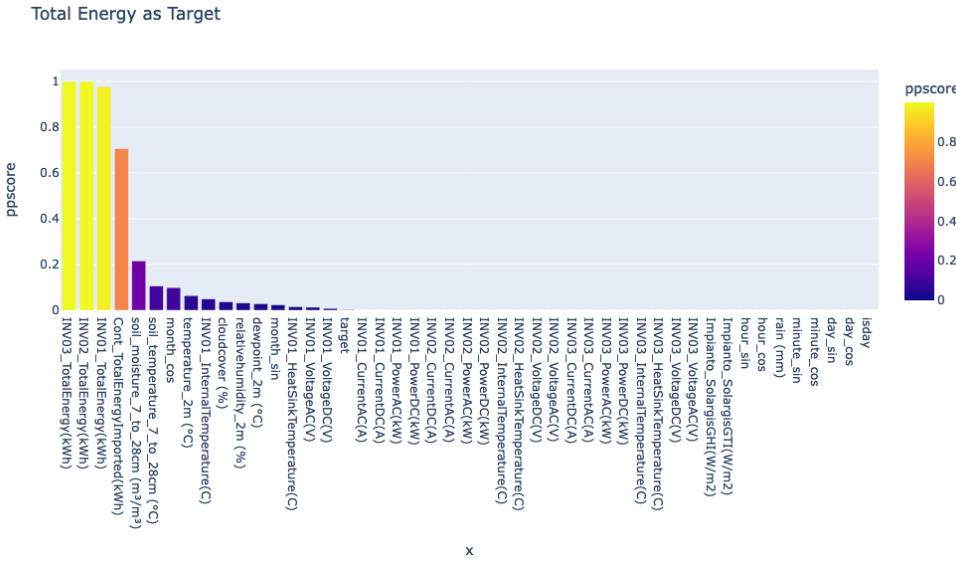


Figure 2.6: All features PPS using `Cont_TotalEnergy(kWh)` as target.

Instant Energy as Target

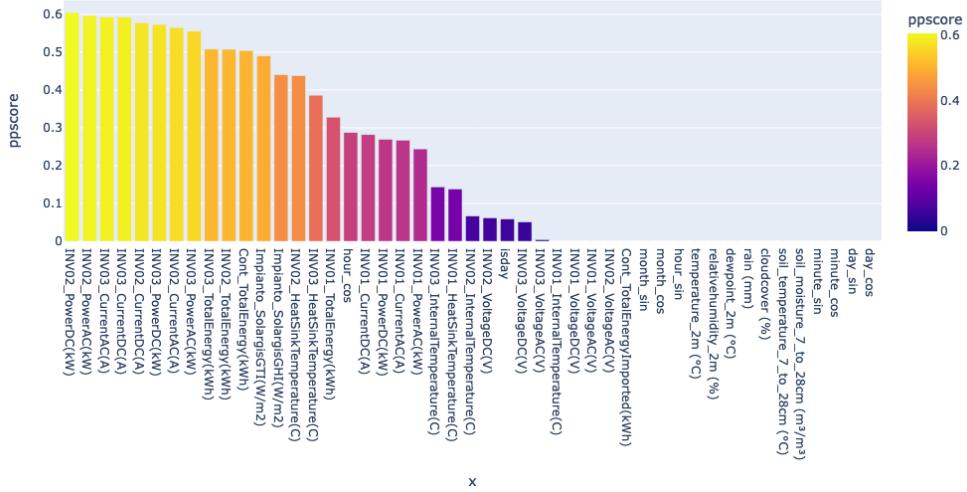


Figure 2.7: All feature PPS using Instant Energy (target) as Target.

As we can see in Figures 2.6 and 2.7, the features that perform better in predicting the instantaneous energy production trend are indeed those of the Inverters, confirming the reasoning described earlier. Finally, by combining the results obtained from the Correlation Matrix and the Power Predictive Score, we obtain a final set of 32 features.

INV01_PowerAC(kW)	INV03_TotalEnergy(kWh)	min_sin
INV01_PowerDC(kW)	INV01_HeatSinkTemperature(C)	min_cos
INV02_PowerAC(kW)	INV02_HeatSinkTemperature(C)	target
INV02_PowerDC(kW)	INV03_HeatSinkTemperature(C)	
INV03_PowerAC(kW)	Impianto_SolargisGHI(W/m2)	
INV03_PowerDC(kW)	Impianto_SolargisGTI(W/m2)	
INV01_CurrentAC(A)	rain (mm)	
INV01_CurrentDC(A)	cloudcover (%)	
INV02_CurrentAC(A)	hour_sin	
INV02_CurrentDC(A)	hour_cos	
INV03_CurrentAC(A)	day_sin	
INV03_CurrentDC(A)	day_cos	
INV02_PowerAC(kW)	month_sin	
INV02_PowerDC(kW)	month_cos	

Table 2.5: All feature selected after this phase.

2.3 Dataset Splitting

After completing the Feature Selection phase (Section 2.2), we decided to divide the obtained dataset into three different sets:

- *Training*: It covers the period from 01-06-2022 to 28-02-2023. This set will be used during the training phase to allow the model to learn the plant's performance and how to predict energy trends during various gaps. It starts in June because there are some issues with the Inverter 1's features before that.
- *Validation*: It spans from 01-03-2023 to 31-03-2023. It will be used in the training phase to assess the presence of overfitting or if this phase might have failed.
- *Testing*: It starts on 01-04-2023 and continues until 30-04-2023. This set will be used in the Evaluation phase to estimate the model's performance on a data period it has never seen before.

	Start	End	Rows
Training	01-06-2022	28-02-2023	24864
Validation	01-03-2023	31-03-2023	2880
Testing	01-04-2023	30-04-2023	2880

Table 2.6: Summary table of how the dataset was divided.

Chapter 3

Deep Learning Models

In this chapter, we will present three models based on different architectures: the first, our baseline, is based on a Multi-Layer Perceptron, which will be the most basic one. The second model is based on a Recurrent Neural Network, and finally, the last one utilizes the newer and more powerful Transformer layers. We will describe in detail their architecture, the various training phases, and any associated issues along with their strengths and weaknesses for each model.

It's important to note that these models were implemented using only the PyTorch[16] library. Each run was preceded by setting a seed (the same for all runs of each model) to allow for comparisons and ensure the repeatability of the various operations. For training phase, the dataset created in the previous Chapter (2) was used and divided into training, validation, and testing sets as described in Section 2.3. All of these phases were executed on a machine with 64 GB (2x32GB) DDR5 5600MT/s of RAM, an AMD Ryzen 9 7950X3D processor, and an Nvidia 4090 GPU.

3.1 MLP

In this section, we will introduce the first model, which we will refer to as the baseline model, based on a Multi-Layer Perceptron. We will analyze its architecture, the training phase, and its final performance.

3.1.1 Architecture

This neural network is designed to predict the instantaneous energy output over a period of exactly 2 days. To do this, it requires input data that includes the performance of the system (features selected during the Preprocessing phase, see Chapter 2) for exactly one day before and one day after the period in question. This enables it to understand how the system is performing and, consequently, provide the energy output trend. The model consists of 6 main layers:

- **Input layer:** This is the first layer of the network. It takes two input tensors: *before* and *after*. These tensors represent the day before and the day after the specific period we want to predict. They have the shape [BATCH_SIZE, 96, 33], where 96 is the number of timestamps in our dataset that make up one day, and 33 represents the features obtained from the Data Preprocessing phase. These tensors are then flattened and concatenated to be passed to the subsequent layer. The output of this layer goes through a Batch Normalization[10] layer, and the Rectified Linear Unit (ReLU)[5] activation function is used.
- **Hidden layers:** In total, there are 4 layers, each of which takes the output of the previous layer as input and reduces the number of neurons by half. Batch Normalization[10] is applied to the result, and the Rectified Linear Unit (ReLU)[5] is used as the activation function.
- **Output layer:** The final layer of our network, it takes the result from the previous layer and outputs the value of the Instantaneous Energy Produced during the specific period. It produces a tensor with a shape of [BATCH_SIZE, 192, 1]. The SoftPlus[5] function is used as the final activation function.

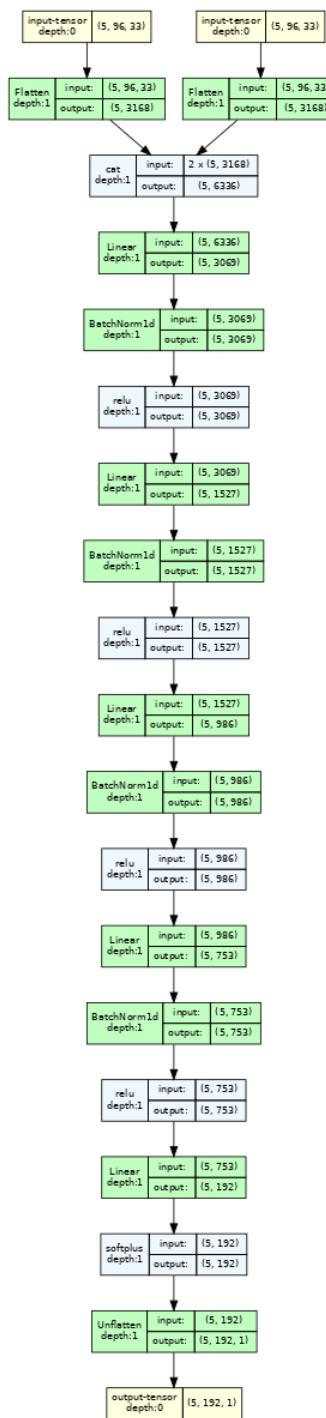


Figure 3.1: Beseline Model architecture visualization.

3.1.2 Training

The model was trained by artificially creating gaps of two days in length within the training dataset. These gaps were passed to the network in the format described earlier, and the output result was compared to the actual instantaneous energy produced during the gap. An *Early Stopping*[8] procedure was implemented to prevent training from continuing if the model was not improving its performance. A procedure, called *Save Best*, has also been integrated, which saves the model to a file whenever the Validation Loss improves. The validation dataset was applied in this phase to assess the learning progress at the end of each epoch. A normalization procedure of the area was applied to the model's output in relation to that of the gap to ensure that the output starts exactly from the last value of the instantaneous energy produced *before* and ends exactly with the first value of the energy produced *after*. Adam[11] was used as the optimizer, and L1Loss[2] (Equation 3.1) served as the loss function. We chose to set the batch size parameter to 10, the learning rate λ to 0.01, a maximum of 100 epochs, and a patience value of 20 for Early Stopping.

$$L = \{l_1, \dots, l_N\}^\top, \quad l_n = |x_n - y_n|, \quad (3.1)$$

$$\ell(x, y) = \text{mean}(L) \quad (3.2)$$

Total Parameters (#)	26543400
Trainable Parameters (#)	26543400
Training Duration (s)	24.0
Model Size (MB)	101.3

Table 3.1: Baseline Model specification.

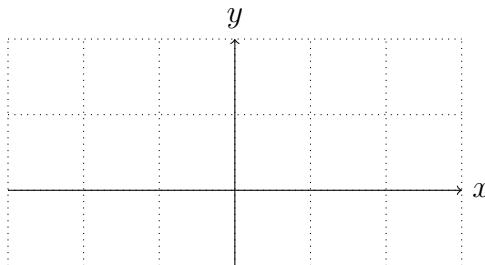


Figure 3.2: Rectified Linear Unit function. $\text{ReLU}(x) = \max(0, x)$

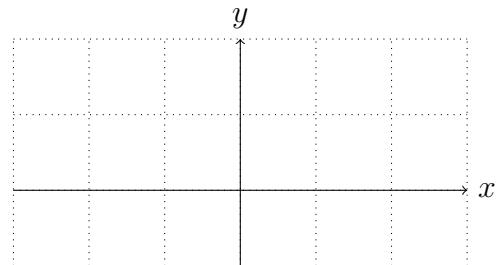


Figure 3.3: SoftPlus function. $\text{SoftPlus}(x) = \frac{1}{\beta} \log(1 + e^{\beta x})$

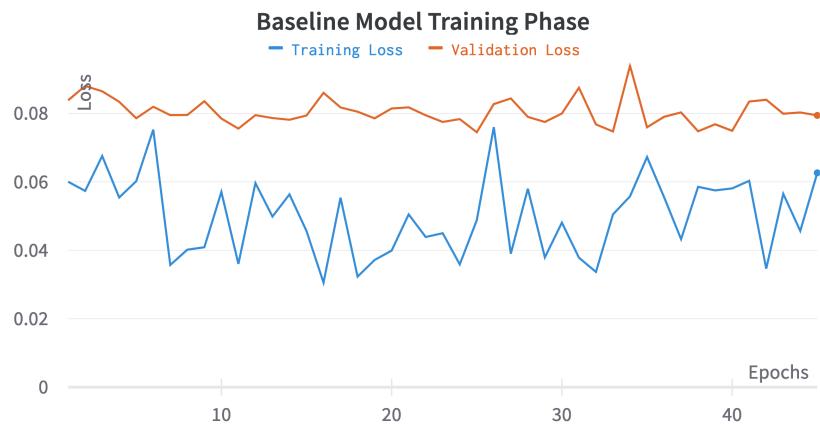


Figure 3.4: The chart displays the loss progression during the training phase. The blue line represents the Training Loss, while the orange line represents the Validation Loss.

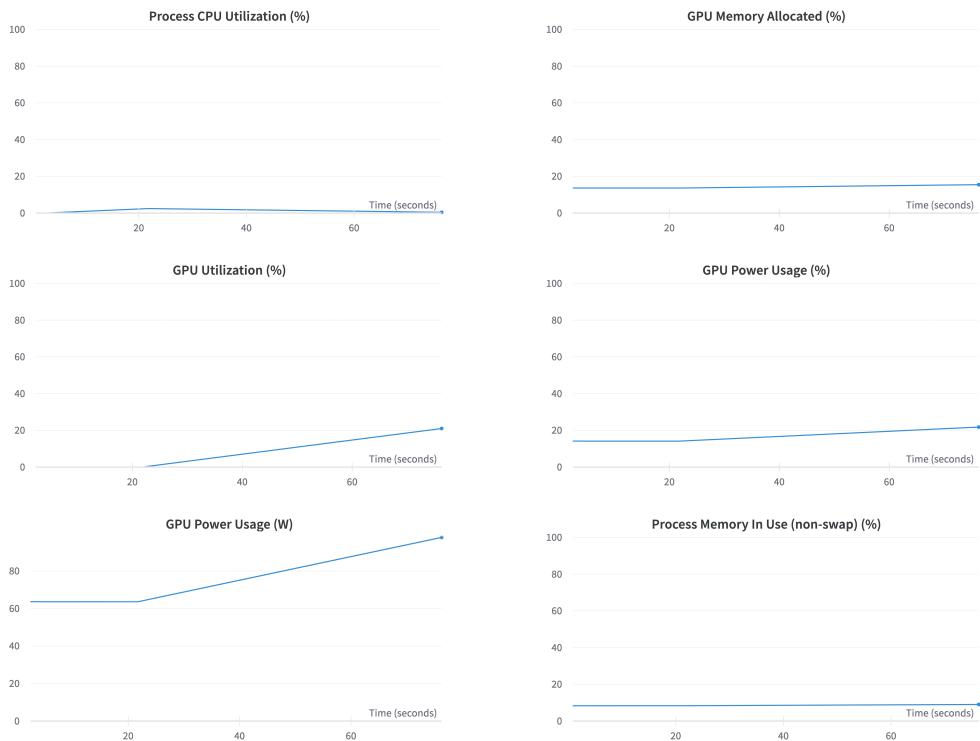


Figure 3.5: System resources utilized during the Training phase.

Algorithm 8 MLP model Training Algorithm

Require: train/validation datasets; Baseline Neural Network Model

Batch Size $\leftarrow 10$

Learning Rate $\lambda \leftarrow 0.01$

Epochs $\leftarrow 100$

Patience $\leftarrow 20$

loss $\leftarrow \text{L1Loss}()$

Optimizer \leftarrow Adam Optimizer

for each epoch **in** epochs **do**

for each (batch_id, before, after, target) **in** train.next_batch() **do**

 train_prediction $\leftarrow \text{model}(\text{before}, \text{after})$ ▷ Model inference

 train_prediction $\leftarrow \frac{\text{train_prediction} \cdot \sum \text{train_prediction}}{\sum \text{target}}$ ▷ Area normalization

 train_loss $\leftarrow \text{loss}(\text{train_prediction}, \text{target})$

 Optimizer step

 Back Propagation

end for

 stop computing gradient

for each (batch_id, vbefore, vafter, vttarget) **in** validation.next_batch() **do**

 val_prediction $\leftarrow \text{model}(\text{vbefore}, \text{vafter})$ ▷ Model inference

 val_prediction $\leftarrow \frac{\text{val_prediction} \cdot \sum \text{val_prediction}}{\sum \text{vttarget}}$ ▷ Area normalization

 val_loss $\leftarrow \text{loss}(\text{val_prediction}, \text{vttarget})$

end for

 check for Early Stopping

 check for Save Best Result

 start computing gradient

end for

3.2 RNN

We will now introduce a second model based on Recurrent Neural Networks. We will examine its structure, analyze the training phase, and finally evaluate its performance, demonstrating how it manages to outperform the previous architecture, the Baseline model introduced in Section 3.1.

3.2.1 Architecture

This model is designed to make the most of the capabilities of Recurrent Neural Networks to predict the behavior of instant energy production during a variable-

length gap period.

The required input format is quite similar to the previous one: a tensor named *before* containing the plant's status for a period before the gap, a tensor named *after* with information about the plant for a period after the gap, and an additional tensor named *future* containing features that are *always* available even during blackout periods. These features specifically include `Solargis`, `isday`, and information obtained from OpenMeteo. This last tensor should assist the model in prediction by helping it better understand the state of meteorological conditions and adapt instant production accordingly.

Now, let's display the main elements that compose it.

- **Input:** As described earlier, the model requires 3 input tensors: *before*, *after*, and *future*. The first two should contain plant's information from some period of time before and after the gap, while the last one will have weather features to support predictions, which can vary in length. An example of input could be `[BATCH_SIZE, 23, 33]` for *before*, `[BATCH_SIZE, 120, 33]` for *after*, and `[BATCH_SIZE, 79, 13]` for *future*.
- **Encoder:** This component's role is to identify the most important features described by the *before* and *after* tensors to understand how the plant is operating. These two tensors are passed to two different GRU[1] layers, which will analyze these time series and extract key information. The final output of each GRU will then be extracted and concatenated together to form the Hidden State for the *Decoder*.
- **Middle layer:** This layer consists of 2 Fully Connected Layers. It takes as input the result of the Encoding phase and reshapes it to the necessary format for input to the *Decoder*. For both layers, the ReLU[5] function is used as the activation function.
- **Decoder:** Its role is to reprocess the information obtained from the Encoder and predict the instant energy produced during the blackout. It consists of a GRU layer that takes the *future* tensor as input and uses the result of the Middle Layer as the hidden state.
- **Output Layer:** This is the final layer of this architecture, and its task is to transform the output from the Decoder into a tensor of shape `[Batch_Size, Gap_Len, 1]`, representing the instant energy produced by the plant during the gap. It consists of a Fully Connected Layer. Its output is then multiplied by the feature `isday` to ensure that the model's prediction is always zero during the night.

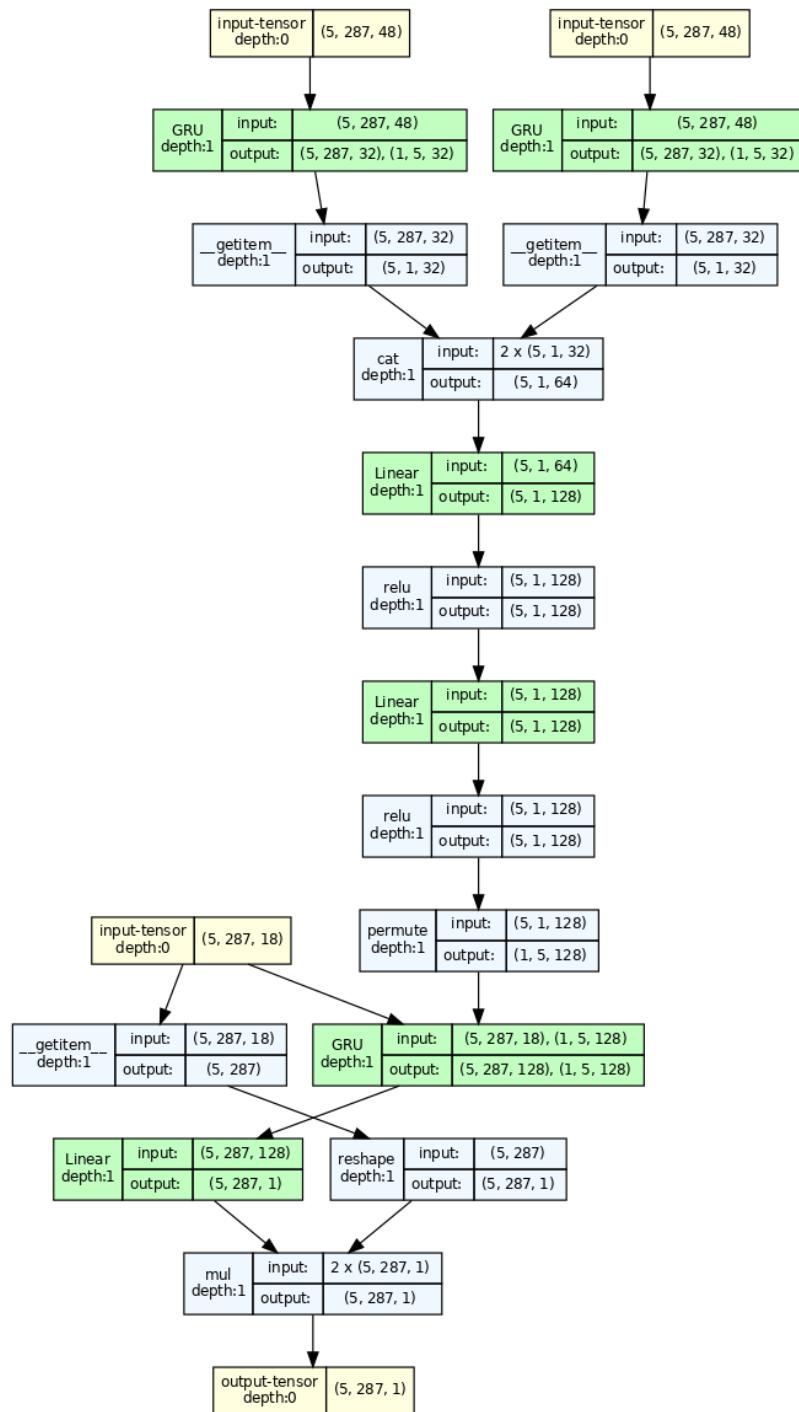


Figure 3.6: Recurrent Neural Network Based Model architecture visualization.

3.2.2 Training

The model was trained to learn the trend of the instant energy production curve of the plant during gaps of variable lengths, ranging from a minimum of 60 timestamp to a maximum of 4 days, using variable dimensions for both *before* and *after*, ranging from 2 timestamps up to a maximum of 1 day. These gaps were artificially generated in the training dataset and provided to the model as described earlier, with attention to grouping gaps of the same length in batches to avoid complications during training.

In this case, an *Early Stopping*[8] and *Save Best* procedure were implemented as well to ensure that the model always saves the best-performing model and to prevent resource waste.

The validation dataset was applied in this phase to conduct an initial and preliminary evaluation of the training process and highlight potential issues. A normalization procedure was also applied to scale the prediction area with respect to the ground truth area. This allows the model to learn the shape of the curve and not exceed the limits of energy production during the gap.

The Adam[11] optimizer was used, and the L1Loss[2] was applied as the loss function. The batch size was set to 10, the learning rate (λ) was set to 0.0001, a maximum of 100 epochs was set, and the patience was set to 20.

Total Parameters (#)	92737
Trainable Parameters (#)	92737
Training Duration (s)	49.0
Model Size (KB)	366.6

Table 3.2: RNN based model specification.

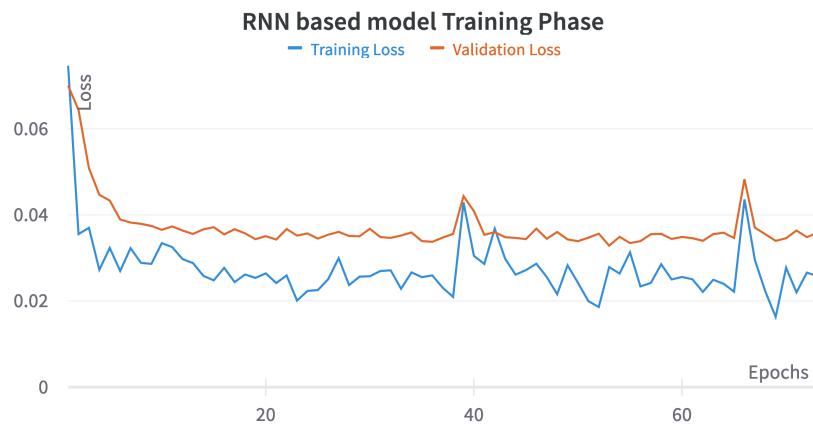


Figure 3.7: The chart displays the loss progression during the training phase. The blue line represents the Training Loss, while the orange line represents the Validation Loss.

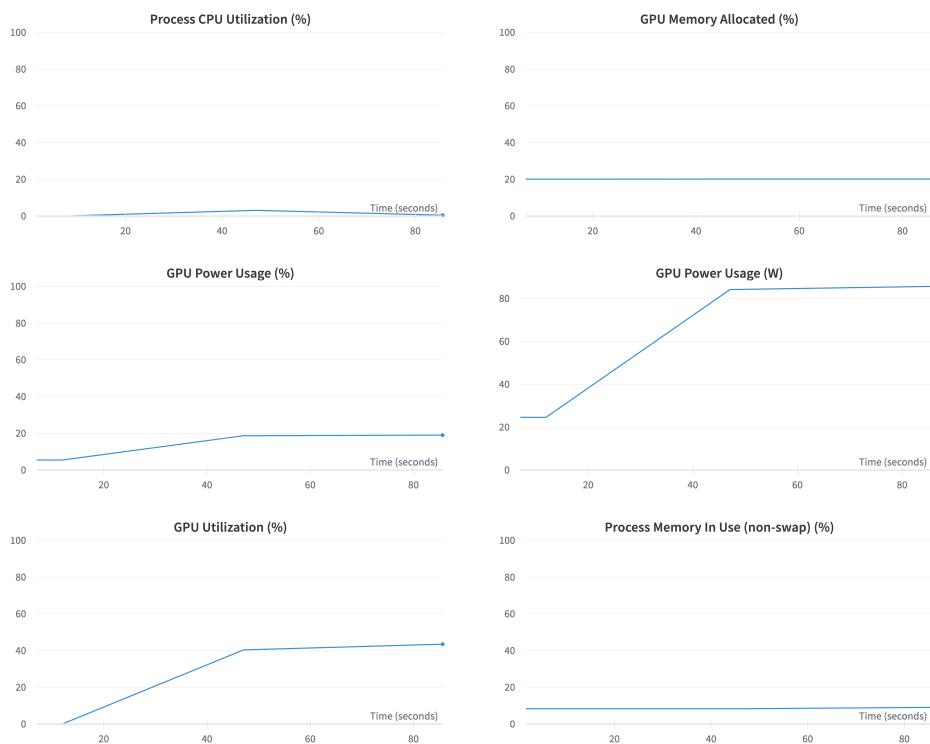


Figure 3.8: System resources utilized during the Training phase.

Algorithm 9 RNN model Training Algorithm

Require: train/validation datasets; Baseline Neural Network Model

Batch Size $\leftarrow 10$

Learning Rate $\lambda \leftarrow 0.01$

Epochs $\leftarrow 100$

Patience $\leftarrow 20$

loss $\leftarrow \text{L1Loss}()$

Optimizer \leftarrow Adam Optimizer

Min Gap size $\leftarrow 1$ day

Max Gap size $\leftarrow 4$ days

for each epoch **in** epochs **do**

for each (batch_id, before, after, future, target) **in** train.next_batch() **do**

 train_prediction \leftarrow model(before, after, future) \triangleright Model inference

 train_prediction $\leftarrow \frac{\text{train_prediction} \cdot \sum \text{train_prediction}}{\sum \text{target}}$ \triangleright Area normalization

 train_loss \leftarrow loss(train_prediction, target)

 Optimizer step

 Back Propagation

end for

 stop computing gradient

for each (batch_id, vb, va, vf, vt) **in** validation.next_batch() **do**

 val_prediction \leftarrow model(vb, va, vf) \triangleright Model inference

 val_prediction $\leftarrow \frac{\text{val_prediction} \cdot \sum \text{val_prediction}}{\sum \text{vt}}$ \triangleright Area normalization

 val_loss \leftarrow loss(val_prediction, vt)

end for

 check for Early Stopping

 check for Save Best Result

 start computing gradient

end for

3.3 Transformers

Now, we will introduce a third model with an architecture based on Transformers[23]. We will analyze its layers, the training phase, highlighting the differences compared to the previous ones, especially in the construction of the input. We will see how this model will prove to be the best among the three models presented in this thesis.

3.3.1 Architecture

The input and operation of this model are slightly different from what we have seen previously. This model requires an entire week as input, with a gap represented by a sequence of special characters, specifically “-1”. This gap can have an extremely variable length, ranging from a minimum of 2 timestamps to the equivalent of one-third of a week, and it can be positioned anywhere within the week.

The model’s objective is to learn to predict the entire week, including the gap. Through a masking system, we can then extract only the values of interest. Let’s now delve into the specific elements that characterize and make up this model:

- **Input:** As described earlier, the input is a tensor containing one week of data with the target feature that includes a period of -1 (representing the gap).
- **Convolution:** The input goes through two convolutional layers to extract and understand the most important and representative features of the time series. Each layer undergoes batch normalization, and the Gaussian Error Linear Units (GELU)[9] function is used as the activation function.
- **Positional Encoder:** To help the model understand the temporal sequence and the order of the different time series, a positional encoder called Time Absolute Position Encoding (tAPE)[7] is implemented. It incorporates the series length and input embedding dimension for absolute position encoding[7].
- **Transformer Encoder:** After performing positional encoding on the output of the convolutional layers, it is passed to the transformer. This transformer[23] consists of 2 transformer layers, each of which contains 8 heads for multi-head attention[23], 64 layers for the feed-forward part, a dropout rate of 0.1, and GELU as the activation function.
- **Output:** This is the final layer of the network, responsible for reshaping the transformer’s output to the required dimension for use. It is a feed-forward layer with an output dimension of 1, and it applies the Softplus[5] function as the activation function.

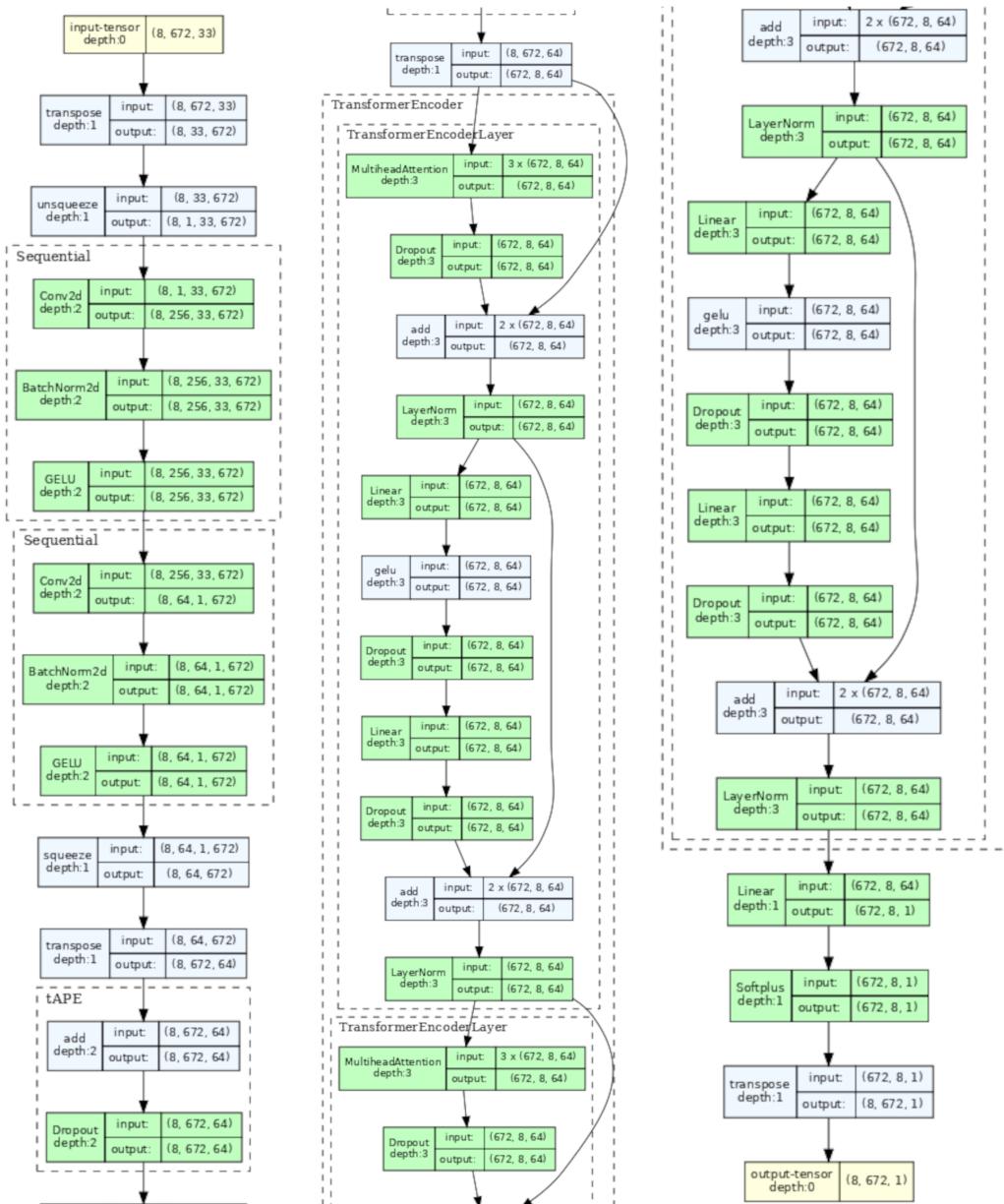


Figure 3.9: Transformer Based Model architecture visualization.

3.3.2 Training

The model was trained using the input format discussed earlier, generating gaps artificially in the training dataset, while also ensuring the creation of a gap mask. This mask is an array of the same length as the input time series, composed of two elements: 1 to indicate the gap timestamps and 0 for regular timestamps. This allows obtaining only the predicted values within the gap, which are used for evaluating the loss function.

In this case, a procedure for normalizing the area was applied to ensure that the model learns the gap curve's behavior. The L1Loss[2] function was employed as the loss function, and AdamW[12] was used as the optimizer with a learning rate (λ) set to 0.00001. The learning rate is then adjusted during training using a cosine annealing scheduler[15][13] to provide optimal conditions for the model during this phase.

Additionally, a validation dataset was used to assess the model's performance during training and to enable the *Early Stopping*[8] and *Save Best* procedures, which were also implemented in this case.

Total Parameters (#)	594177
Trainable Parameters (#)	594177
Training Duration (s)	900.0
Model Size (MB)	2.4

Table 3.3: Transformer based model specification.

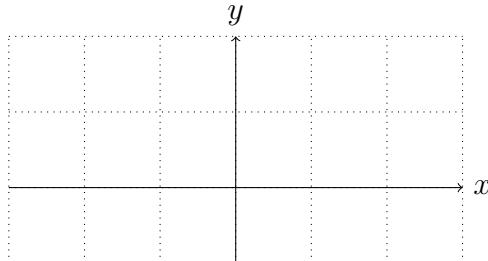


Figure 3.10: Gaussian Error Linear Units (GELU). $GELU(x) = x * \Phi(x)$

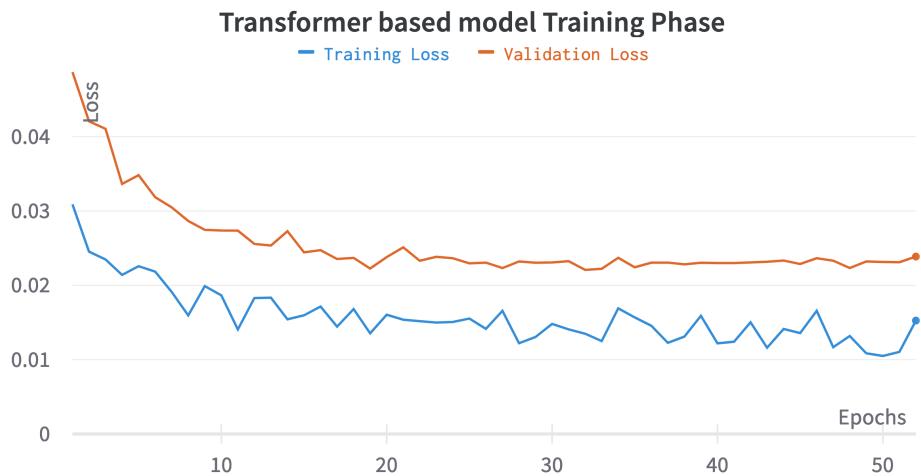


Figure 3.11: The chart displays the loss progression during the training phase. The blue line represents the Training Loss, while the orange line represents the Validation Loss.

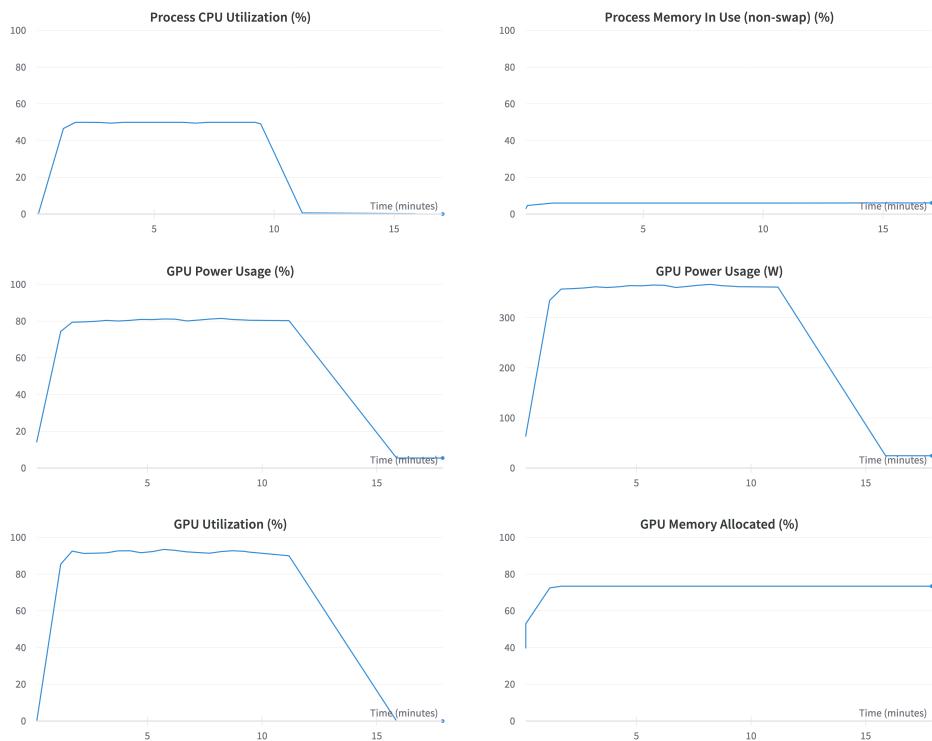


Figure 3.12: System resources utilized during the Training phase.

Algorithm 10 Transformer based model Training Algorithm

Require: train/validation datasets; Transformer based Neural Network Model

```
Batch Size ← 8
Learning Rate  $\lambda$  ← 0.00001
Epochs ← 100
Patience ← 20
loss ← L1Loss()
Optimizer ← AdamW Optimizer
Scheduler ← CosineAnnealingScheduler
Min Gap size ← 2 timestamps
Max Gap size ←  $\frac{\text{week length}}{3}$  timestamps

for each epoch in epochs do
    for each (batch_id, src_data, tgt_data, mask) in train.next_batch() do
        train_prediction ← model(src_data)                                ▷ Model inference
        train_prediction ← train_prediction · mask
        train_prediction ←  $\frac{\text{train\_prediction} \cdot \sum \text{train\_prediction}}{\sum \text{tgt\_data}}$       ▷ Area normalization
        train_loss ← loss(train_prediction[mask = 1], tgt_data[mask = 1])
        Optimizer step
        Back Propagation
    end for
    Scheduler step
    stop computing gradient
    for each (batch_id, vs, vt, vm) in validation.next_batch() do
        val_prediction ← model(vs)                                     ▷ Model inference
        val_prediction ← val_prediction · vm
        val_prediction ←  $\frac{\text{val\_prediction} \cdot \sum \text{val\_prediction}}{\sum \text{vt}}$           ▷ Area normalization
        val_loss ← loss(val_prediction[vm = 1], vt[vm = 1])
    end for
    check for Early Stopping
    check for Save Best Result
    start computing gradient
end for
```

Chapter 4

Experimental Results

In this final chapter, we will analyze the results of the models previously described by comparing their respective training phases, highlighting any issues and strengths of the model. We will test their performance using the Testing dataset, as described in Section 2.3, and evaluate them using various metrics. Among these metrics, we will employ the MAE (Mean Absolute Error)[20] to highlight the difference between the model’s predictions and the ground truth and the R^2 (R-squared)[20] index to understand how well the model-predicted curve approximates the real one. Here’s a brief introduction to the indices we will use:

- **Mean Absolute Error (MAE)**: This metric represents the average point-wise error that the model makes compared to the ground truth. It is expressed in kW.
- **R^2 (R-squared)**: This index quantifies how well the prediction curve approximates the ground truth. It helps us understand how well the model approximates the trend of the reference instant prediction.
- **Mean Absolute Percentage Error (MAPE)**[20]: It indicates the error of the model relative to the ground truth, measured in percentage. The calculation of this metric in our case can be quite problematic due to the presence of many values close to zero or exactly zero. Therefore, the calculation is performed by only considering positive values.

4.1 MLP based model Evaluation

From the training phase graph shown in Figure 3.4, we can see that it has concluded successfully because the two curves (training loss and validation loss) do not diverge but remain at a relatively constant distance from each other. This also suggests that there is no overfitting. However, the values of the two loss functions do not appear to decrease significantly as the epochs progress, indicating that the model may not have generalized well.

From the graphs in Figure 3.5, it is apparent that the machine on which this model was trained was relatively underutilized. In particular, it's worth noting that GPU utilization did not exceed 30%, and GPU memory was barely utilized, staying at around 20%. This suggests that the model can be trained on less powerful machines as well. The model is also relatively lightweight in terms of memory, with just 100 MB (see Table 3.1), and the training time did not exceed 30 seconds. Inference time is extremely fast, taking less than a second.

Gap period	MAE (kW)	MAPE (%)	R ²
02-04 to 03-04	18.63	128.47	0.64
03-04 to 04-04	06.90	64.97	0.52
05-04 to 06-04	17.99	109.78	0.42
06-04 to 07-04	20.07	113.99	0.62
11-04 to 12-04	10.66	33.84	0.92

Table 4.1: The table displays the values of MAE (Mean Absolute Error)[20], MAPE (Mean Absolute Percentage Error)[20] and the R² (R-squared)[20] index applied to the model predictions shown in Figures 4.1 and 4.2.

	MAE (kW)	MAPE (%)	R ²
AVG	14.11	70.98	0.69
STD. DEV	3.81	27.99	0.17

Table 4.2: MLP based model Global metrics.

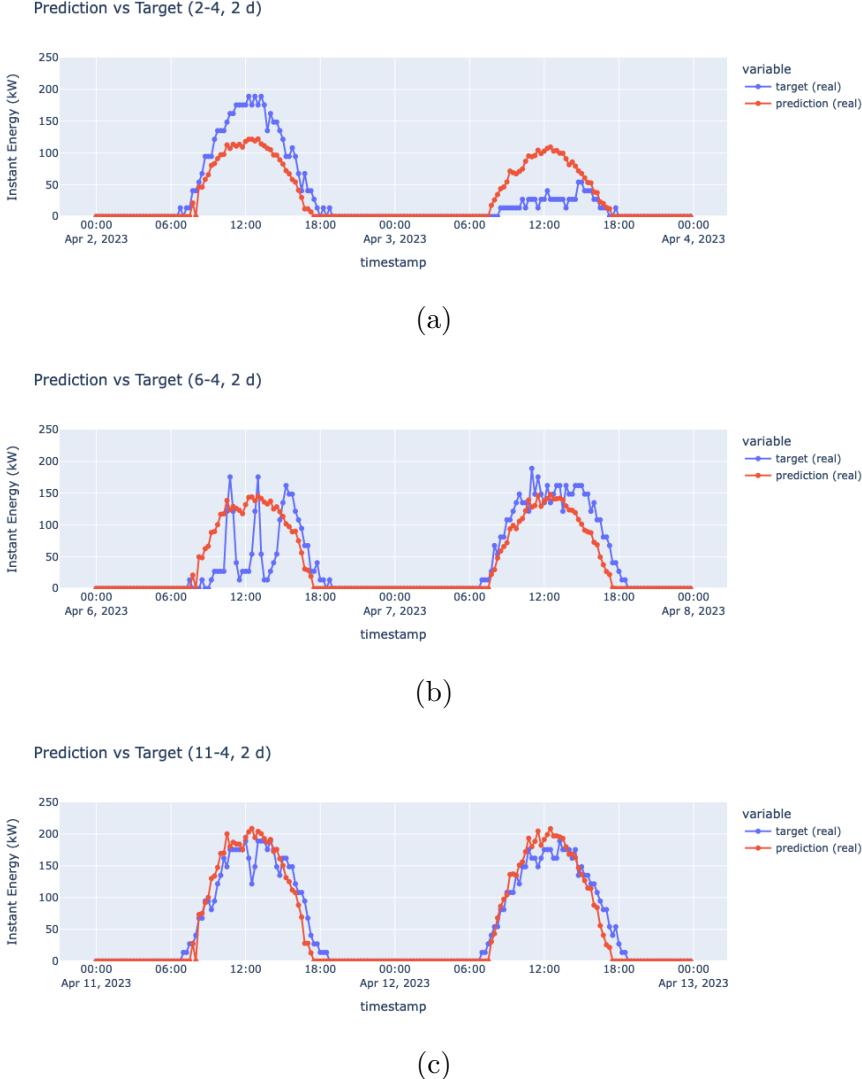


Figure 4.1: The figure displays three predictions made by the model, where you can observe the network’s output (in red) and the ground truth (in blue). The model was tested on two gaps, each covering a period of 2 days. The first gap (a) spans from 02-04-2023 to 04-04-2023, the second gap (b) spans from 06-04-2023 to 06-08-2023 and the third starts from 11-04-2023 to 12-04-2023.

Analyzing the graphs presented in Figure 4.1, we can confirm the previous suspicion that the model did not learn well how to predict the trend of instant energy production from the plant. Plot (a) clearly illustrates how the model’s prediction is very timid and fails to grasp the possibility that some days may be more productive than others. In graph (b), we can see how the model almost

approximates the second day but makes a significant mistake on the first, failing to understand the potential for production spikes during the day. In (c), on the other hand, we can see how the model’s output manages to understand the ground truth’s behavior quite well. In fact, we have an R^2 index value of 0.96 and low values for MAE and MAPE. These claims are supported by the data shown in Table 4.1.

It’s also evident that the model struggles to handle the day/night cycle, often ending production much earlier than it should. However, it consistently predicts zero energy production during the night, which is a positive aspect.

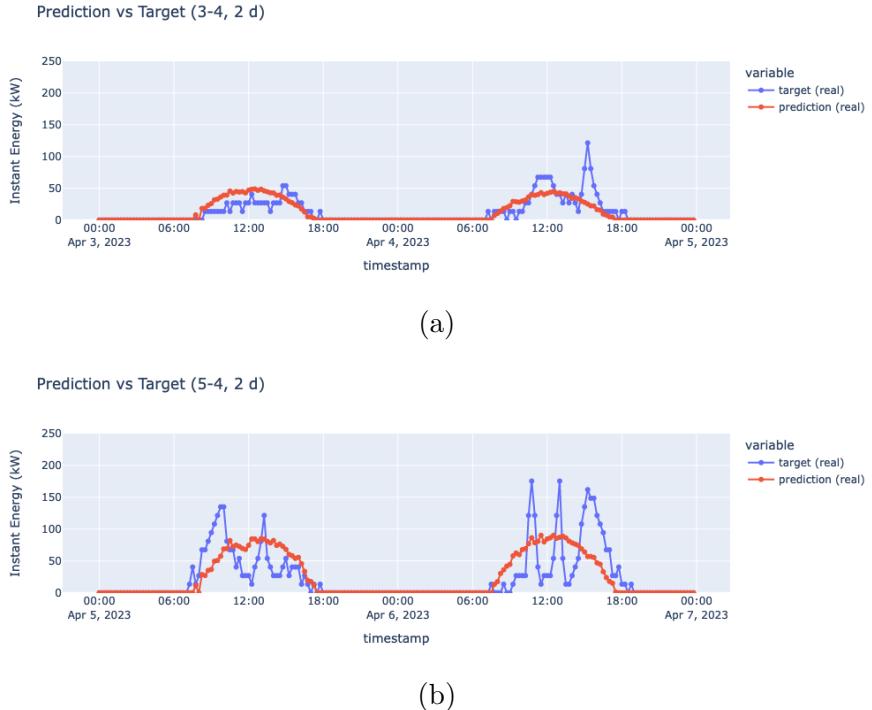


Figure 4.2: The figure displays two model predictions (in red) for two-day gaps and their respective ground truth (in blue). (a) corresponds to a gap from 03-04-2023 to 04-04-2023, while (b) covers the period from 05-04-2023 to 06-04-2023.

Figure 4.2 highlights the significant limitations of the model, demonstrating how it fails to identify potential peak values in production and how the predicted day curves are consistently similar to each other. It’s also important to note that the model can only work with gaps of a fixed size, and if a gap of a larger size is encountered, it would be necessary to retrain the model.

Analyzing the data presented in Tables 4.1 and 4.2, it can be confirmed that the performance of this model is quite limited. The R^2 index hovers around 0.60,

with an average of 0.69 and a standard deviation of 0.17. This indicates that the target curve is not well approximated by the model's output. While the *MAE* appears to be relatively low (it's important to consider that the nighttime period significantly lowers the average, as the difference between target and prediction is zero during that time) the values of *MAPE* are quite high, at times even reaching 100% error, with an average value of 71% and a standard deviation of 28%.

In conclusion, despite the presented model being relatively straightforward to implement and train, it is not suitable for effectively addressing the problem of imputation.

4.2 RNN based model Evaluation

From the graphs shown in Figure 3.7, we can see that the training phase was successful, and after an initial descent, the loss values remained relatively constant without displaying any abnormal trends. The statistics presented in Figure 3.8 reveal that the machine at our disposal was not fully utilized, suggesting that this architecture can be trained and used on less powerful computers than the one we have. Additionally, the model appears to be very lightweight, both in terms of the relatively small number of parameters and its weight, which doesn't exceed 400 KB. The inference time does not even approach one second, making it extremely fast in execution.

Gap Period	MAE (kW)	MAPE (%)	R ²
02-04 to 05-04	4.72	28.12	0.96
03-04 to 06-04	5.11	33.01	0.91
04-04 to 04-04	3.60	27.15	0.93
07-03 to 10-4	7.52	34.22	0.90
12-04 to 14-04	6.61	20.68	0.96

Table 4.3: The table displays the MAE, MAPE, and R² values applied to some model predictions during the testing phase, some of which are shown in Figure 4.3.

	MAE (kW)	MAPE (%)	R ²
AVG	6.92	30.32	0.92
STD. DEV	1.74	9.30	0.05

Table 4.4: Global metrics for the RNN-based model calculated on gaps of varying sizes.

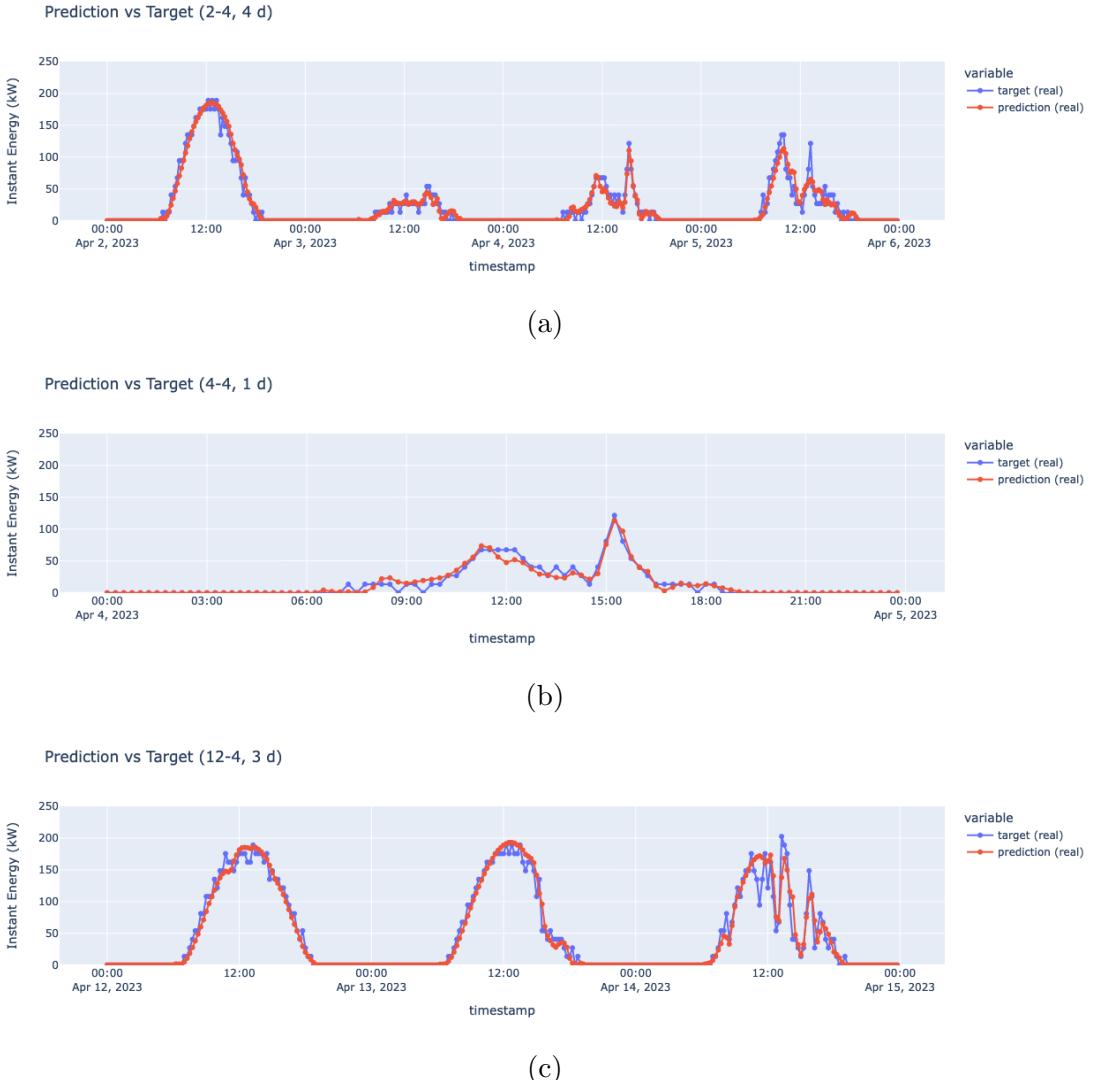


Figure 4.3: In the figure, three model predictions (in red) are shown alongside the ground truth (in blue) for gaps of varying sizes. These predictions were made using data from the testing dataset. The tensors *before*, *after*, and *future* have variable dimensions, as described earlier.

Analyzing some model predictions as shown in Figure 4.3, we can observe how the real instant energy production curves (displayed in blue) are closely approximated by the model (red curves). The model effectively understands the plant's behavior, even managing to predict production spikes. We can also see that energy production is consistently zero during the night, and it adeptly captures the day/night cycle by gradually reducing production as sunset approaches.

In graph (a), we can see a 4-day gap from 02-04-2023 to 06-04-2023. The first two days are predicted very well, while in the last part, we can see that a production spike was not detected. For this period we have a quite high R^2 index of 0.96, 4.72 kW as MAE and 28.12 % for the MAPE, which are quite good values. In graph (b), we can observe a 1-day gap on 04-04-2023. We notice that the overall trend is almost entirely approximated correctly, except for some time intervals around 12:00, indeed, we have slightly better results with an MAE of 3.60 kW and a MAPE of 27.15%. The last graph (c) is related to a 3-day gap, and we can see that the first two days are approximated well, while in the last day, the production spikes are identified but with values not entirely similar to those of the ground truth. All the results presented so far are consistent with the average values shown in Table 4.4 demonstrating that the model returns fairly consistent outputs among them.

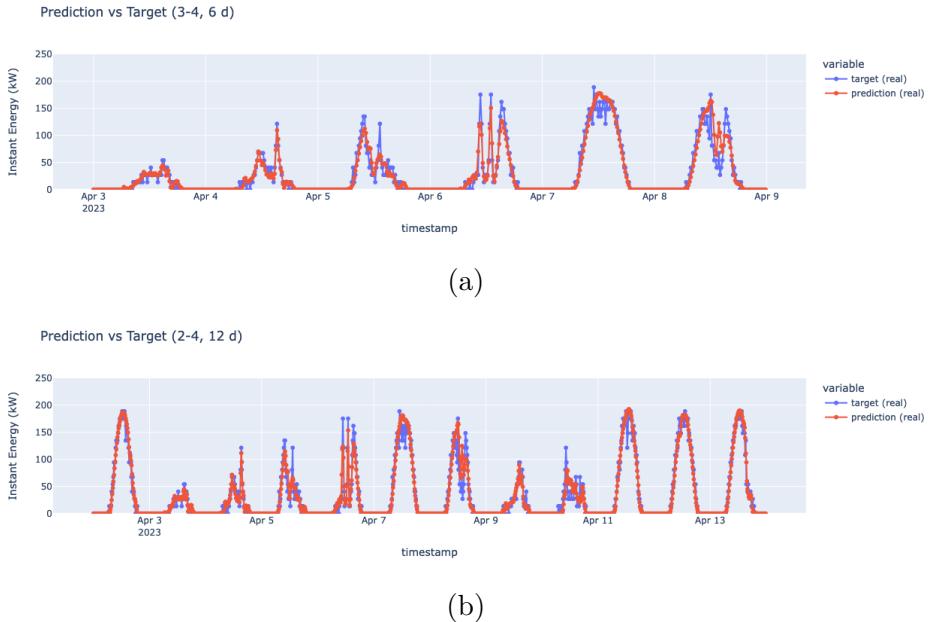


Figure 4.4: The graphs depict two model predictions for gaps that exceed the maximum limit of days set during the training phase. The first one (a) shows a 6-day gap, while the second one (b) presents a 12-day gap.

It is interesting to note how the model still performs well even when presented with gaps that exceed the maximum length set during training. In Figure 4.4, two graphs are shown: (a) represents a 6-day gap (two days longer than the training length), and (b) a 12-day gap (eight days longer than the training length).

Gap Period	MAE (kW)	MAPE (%)	R ²
03-04 to 08-04	6.56	30.94	0.92
02-04 to 13-04	5.99	27.50	0.95

Table 4.5: The table displays the MAE, MAPE, and R² values applied to the model predictions shown in Figure 4.4.

Gap Size	AVG MAE (kW)	AVG MAPE (%)	AVG R ²
12 days	6.64 ± 0.79	25.66 ± 5.90	0.95 ± 0.02
6 days	6.85 ± 0.93	27.44 ± 6.78	0.94 ± 0.02
2 days	6.86 ± 1.87	28.83 ± 10.02	0.92 ± 0.06
< 60 ts	8.93 ± 2.22	36.14 ± 4.40	0.86 ± 0.07

Table 4.6: Global results for the RNN-based model with fixed gap size. The table provides the average values along with their respective standard deviations.

Taking into account the data in Tables 4.3, 4.4, 4.5 and 4.6, it can be confirmed that this Recurrent Neural Network-based model is highly performant. The average MAE value is $6.92 \text{ kW} \pm 1.74$, which is relatively low, while the average R^2 index is 0.92 ± 0.05 , and it almost always approaches the ideal value of 1.0[20]. Furthermore, the average MAPE value is 30.32 ± 9.30 , which is a significant improvement compared to the previous model.

Equally positive results are obtained for gaps that exceed the maximum training phase length of 4 days. From Table 4.6, we can see that for the 12, 6 and 2-day gaps, the average MAE, MAPE and R^2 index are quite similar compared to the values shown in Table 4.4, some are slightly better, while others are slightly worse, but they remain stable and confirm the values shown earlier. Clearly, we see a drop in performance with gap sizes shorter than 60 timestamps, as evident from the increase in MAE and MAPE and the decrease in the R^2 index.

In conclusion, it can be affirmed that this model effectively harnesses the potential offered by Recurrent Neural Networks and excels in predicting the trend of instant energy production during data gaps, even for gaps spanning multiple days.

4.3 Transformer based model Evaluation

From the graph shown in Figure 3.11, we can observe that the training and validation loss curves, after an initial descent, remain relatively constant, and most importantly, they do not seem to diverge from each other. This indicates that the training phase has concluded successfully, with the validation loss value being lower by 0.01 compared to the RNN-based model.

From the graphs in Figure 3.12, which show the machine's usage during the training phase, and from Table 3.3, it can be inferred that the model utilizes almost all of the available hardware resources, suggesting that it is computationally intensive and might be challenging to train on less powerful machines. However, it's essential to note that the inference time is extremely fast, not exceeding one second, and the model file size is very compact, with a dimension of approximately 2 MB.

Gap Period	MAE (kW)	MAPE (%)	R ²
05-04 10:15 to 07-04 17:45	5.02	22.38	0.98
01-04 10:00 to 01-04 19:45	7.24	11.72	0.96
02-04 09:30 to 04-04 08:15	3.14	25.11	0.99
05-04 03:00 to 06-04 01:30	4.02	24.40	0.96

Table 4.7: The table displays the values of MAE (Mean Absolute Error), MAPE (Mean Absolute Percentage Error) and the R² (R-squared) index applied to some model predictions made during testing phase shown in Figures 4.6.

variable gap size		2 days gap size	
	AVG		AVG
AVG MAE (kW)	3.83 ± 1.40	AVG MAE (kW)	3.76 ± 0.39
AVG MAPE (%)	18.49 ± 7.99	AVG MAPE (%)	18.14 ± 6.76
AVG R ²	0.97 ± 0.05	AVG R ²	0.98 ± 0.02

(a)

(b)

Table 4.8: Table (a) displays the global metrics calculated on the model's output with variable gap sizes, while (b) refers to the global metrics with a fixed two-day gap size. Both tables include the mean value and the standard deviation.

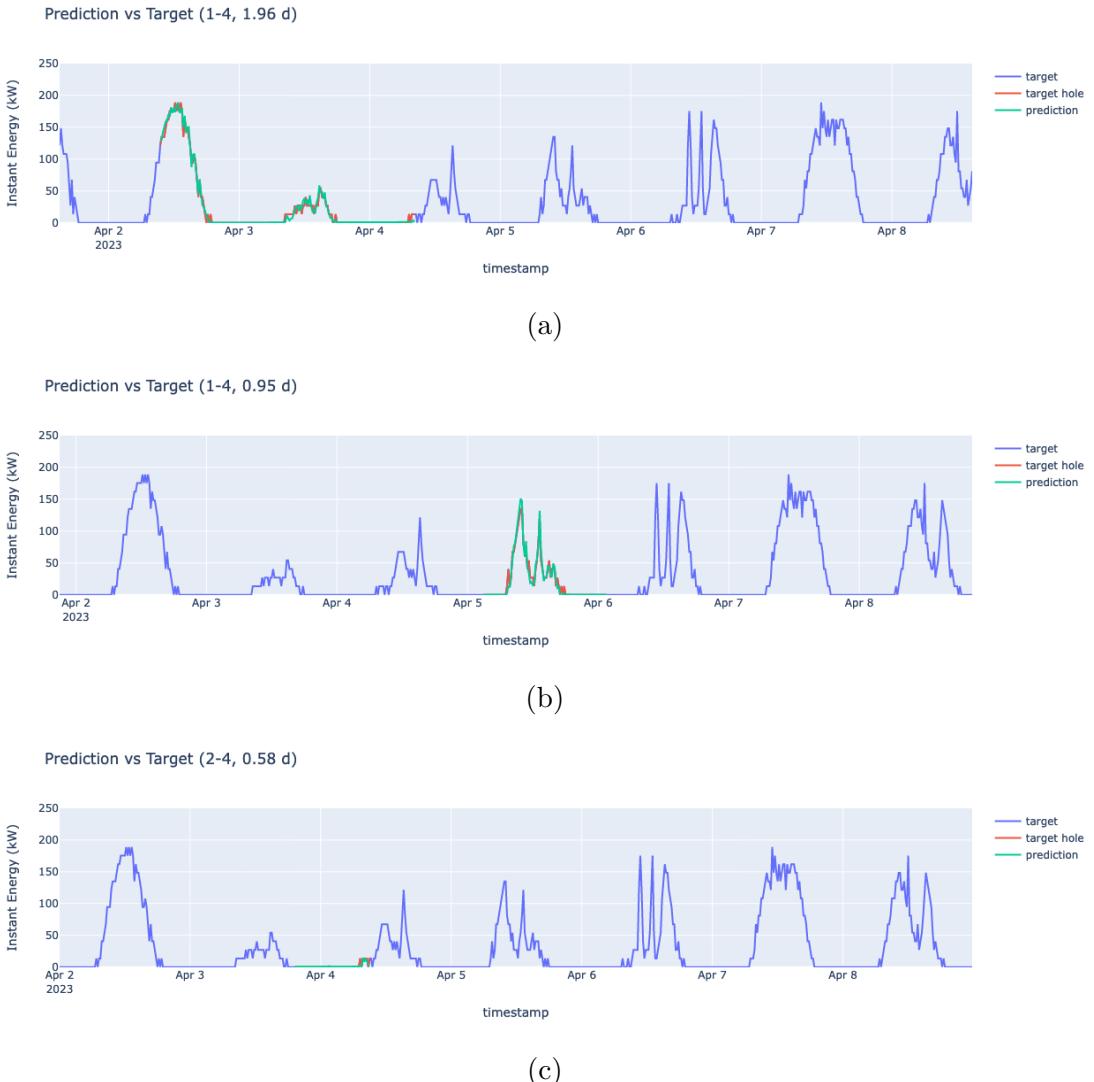
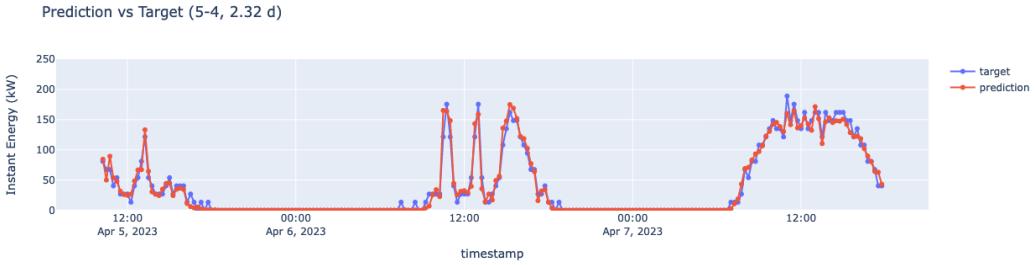
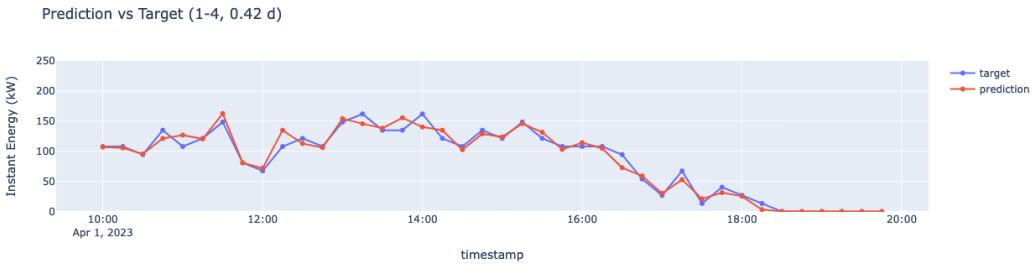


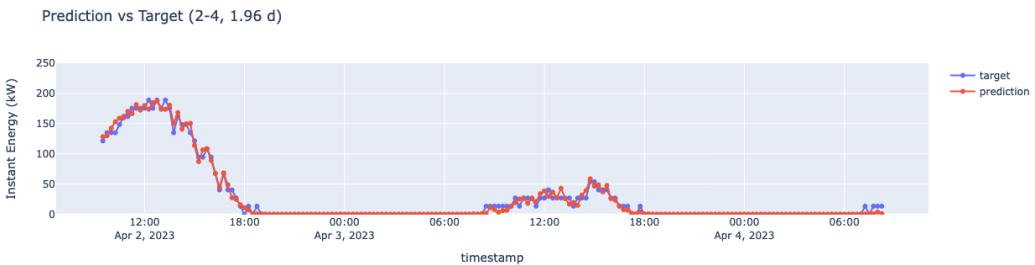
Figure 4.5: This figure shows some of the input time series provided to the model during the testing phase. We can see the entire series (in blue), the ground truth only for the gap period (in red), and the model’s output only in the relevant gap period (in green). In graph (a), we have a gap size of almost two days, in (b) almost one day, and in (c) just over half a day.



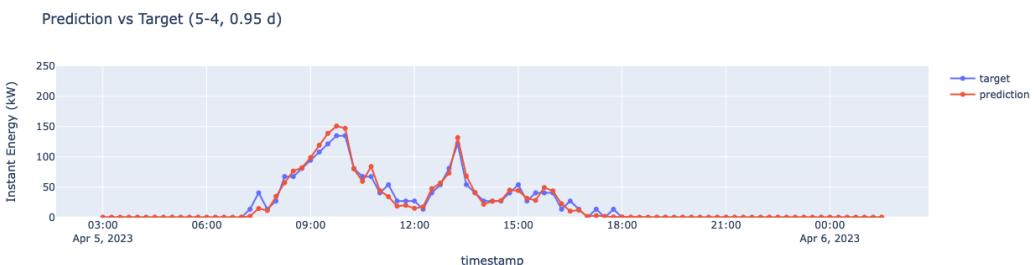
(a)



(b)



(c)



(d)

Figure 4.6: This figure displays some results of the model obtained during the testing phase, using gaps of varying lengths. You can see the model's outputs (in red) compared to their respective ground truths (in blue).

Analyzing the results of the evaluation phase presented partly in Table 4.7 and in the graphs in Figure 4.6, we can see that this model is very effective in predicting instantaneous energy during gaps of varying sizes. It excels in this task, whether for gaps of nearly a day or up to three days. We can observe that the R^2 index in these cases is consistently high, almost always hovering around the value of 0.97, with relatively low MAE and MAPE values.

Examining the global metrics reported in Table 4.8 (a), we can confirm these findings. It shows an extremely low average MAE of 3.83 kW with a standard deviation of 1.40 kW, an average MAPE of 18.49% with a standard deviation of 7.99%, and an average R^2 value of 0.97 ± 0.05 . This demonstrates how the model effectively approximates the ground truth with very low errors.

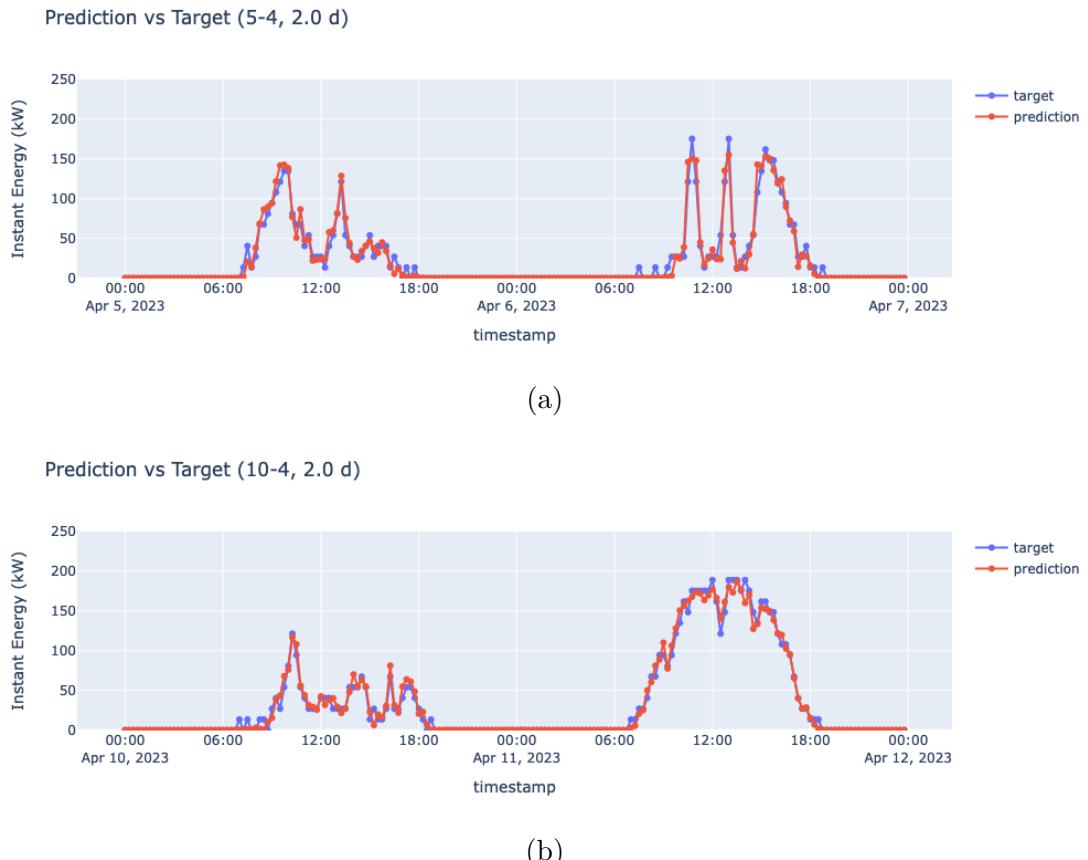


Figure 4.7: In this figure, some outputs from the testing phase of the model with a fixed 2-day gap size are presented. The model's predictions are shown in red, while the ground truth is in blue.

By repeating the evaluation phase with fixed gap sizes of two days to allow for a comparison with the other models, we can notice a slight improvement in the model's performance. Analyzing the data presented in Table 4.8 (b), we have an average MAE of 3.76 ± 0.39 kW (2% improvement with a 72% better standard deviation), an average MAPE of $18.14 \pm 6.76\%$ (2% improvement with a 15% better standard deviation), and an average R^2 value of 0.98 ± 0.02 (1% improvement). In general, there is a 2% overall increase in performance with a significant reduction in the standard deviation values.

Gap Period	MAE (kW)	MAPE (%)	R^2
04-04 to 05-04	3.72	30.48	0.96
05-04 to 06-04	4.25	26.99	0.96
06-04 to 07-04	4.59	20.39	0.98
07-04 to 08-04	4.33	15.29	0.98
08-04 to 09-04	3.72	22.86	0.97
09-04 to 10-04	3.52	29.76	0.94
10-04 to 11-04	3.88	20.91	0.99

Table 4.9: The table displays the values of MAE (Mean Absolute Error), MAPE (Mean Absolute Percentage Error), and the R^2 (R-squared) index applied to some model predictions made during the testing phase with a fixed gap size of 2 days. Some of these predictions are shown in Figures 4.7.

In conclusion, we can affirm that, despite the more demanding training phase, this model excels in the task of estimating instant energy production during periods of significantly variable gap sizes, achieving significantly better MAE, MAPE, and R^2 index values compared to those of the previous architectures.

4.4 Model Comparisons

In this final section, we will compare the three models discussed in this thesis, analyzing their training phases, performance during testing phase, and identifying their strengths and weaknesses through the previous evaluation phase. We will determine which of these models is more suitable for solving the problem of time series imputation of photovoltaic data. It's essential to specify that to perform these comparisons, we reran the evaluation phase, fixing the gap size at 2 days and recalculating the various metrics used.

	Model Size (KB)	Train Time (s)	GPU Usage (%)	CPU Usage (%)
MLP	101.30	24.00	20	10
RNN	366.60	49.00	20	27
TRN	2400.0	900.00	96	56

Table 4.10: The table presents some data obtained during the training phase of each model.

Analyzing the data shown in Table 4.10, we can see that the fastest and lightest model to train is the MLP-based one, followed by the RNN-based architecture, and finally, the Transformer. As seen in the previous sections, the first two models can certainly be trained on less powerful hardware compared to the available one, while it might be challenging for the last model. However, it's important to note that the inference time for each model is less than a second.

For all three models, the training phase was successfully completed without encountering significant issues. Comparing the graphs showing the training and validation loss curves, as shown in Figure 3.4, 3.7, and 3.11, we can see that the best one is the Transformer-based model with a final validation loss value of 0.02, which is 0.01 lower than that of the RNN-based model.

	MLP	RNN	TRN	Incr. Gain (%)	
				RNN	TRN
MAE (kW)	14.11 ± 3.81	6.86 ± 1.87	3.76 ± 0.39	51.38	45.18
MAPE (%)	70.98 ± 27.99	28.83 ± 10.02	18.14 ± 6.76	59.38	30.07
R²	0.69 ± 0.17	0.92 ± 0.06	0.98 ± 0.02	25.00	6.12

Table 4.11: In the table, you can find the average values of MAE, MAPE, and the R^2 index for the three models, along with their respective standard deviations. Additionally, the Incremental Gain is provided, showing the percentage increase of the RNN model compared to MLP and the Transformer compared to RNN.

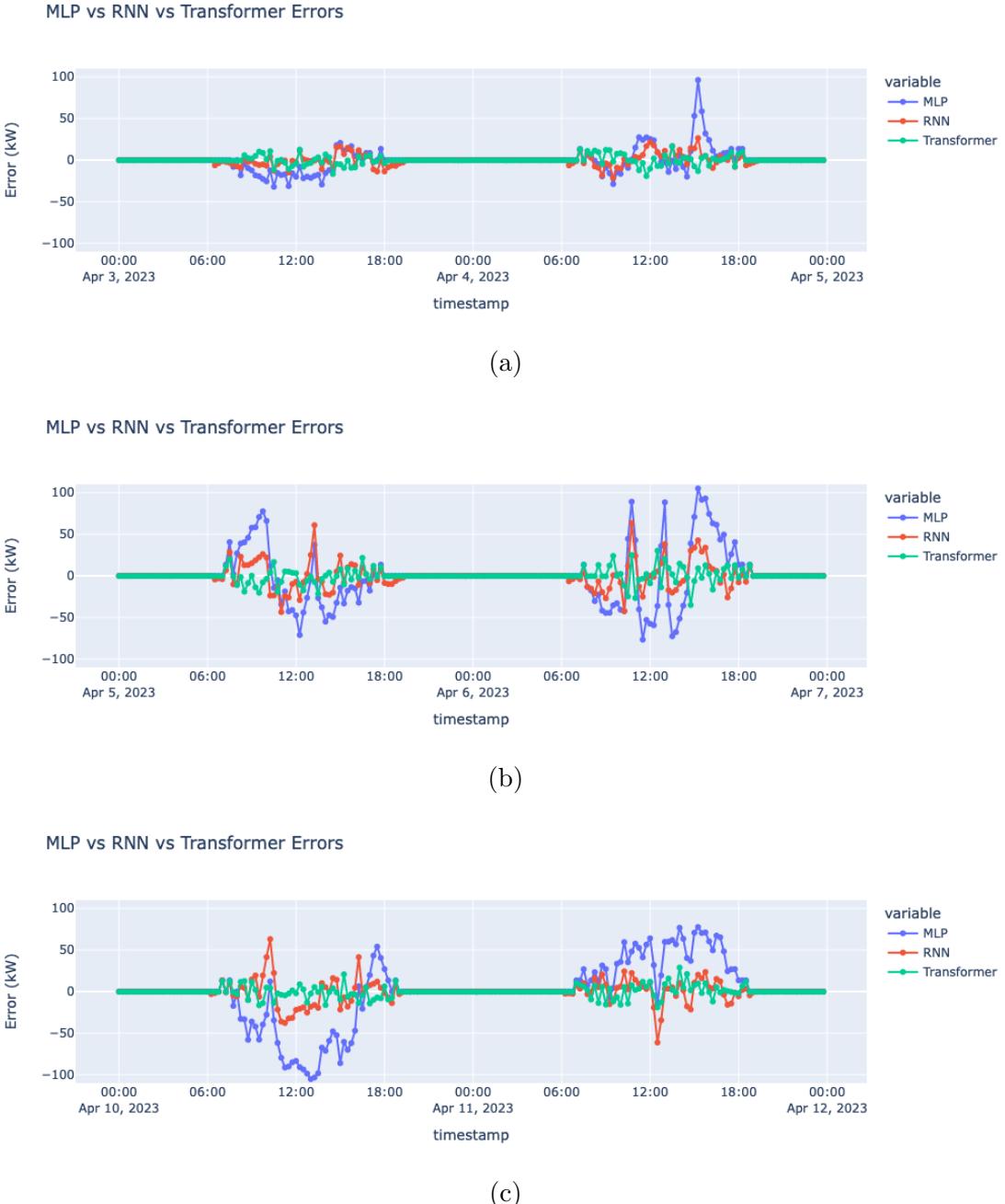


Figure 4.8: The figure compares the errors made by the three models in predicting gaps with a two-day gap size. The blue curve represents the errors of the MLP-based model, the red curve represents the errors of the RNN-based model, and the green curve represents the errors of the Transformer-based model.

Examining Table 4.11, which shows the average values of MAE, MAPE, and the R^2 index for the various models, we can observe that the one based on the Transformer is significantly better. The RNN-based model is undoubtedly better than the MLP-based one, with the MAE value being 51% lower and the MAPE showing an improvement of almost 60%. The R^2 index has also improved by 25%, indicating that the output of this model much better approximates the instantaneous energy values produced by the plant during 2-day gap periods.

However, the Transformer-based architecture excels in this task, with a 45% improvement in MAE compared to the RNN-based model, a 30% improvement in MAPE, and a 6% improvement in the R^2 index. This model performs significantly better in predicting the plant's instantaneous energy compared to the RNN-based model, with the added capability of better detecting and understanding the presence of production peaks even over significantly variable time intervals.

	AVG MAE (kW)	AVG Min Err (kW)	AVG Max Err (kW)
MLP	13.91	0.35	96.81
RNN	7.14	0.20	65.56
TRN	3.76	0.12	26.39

Table 4.12: The table displays the average values of the metrics presented in Table 4.13.

These statements are supported by the graphs presented in Figure 4.8 and the corresponding data in Tables 4.13 and 4.12. The graphs illustrate the differences in point errors made by the various models. From these, we can see that the Transformer's errors (green line) are extremely compact and often close to the ideal value of 0, with an average value of 3.76 kW. The model based on RNN also has a similar curve (red line) but with values slightly farther from the ideal value and occasional error peaks, with an average value of 7.14 kW. The model based on MLP shows the worst error curve, often significantly deviating from the value of 0, featuring high error peaks, and having an average value of 13.91 kW.

We can also observe that the model based on the Transformer has a much lower average maximum point error, at 26.40 kW, compared to the RNN at 65.55 kW and the MLP at 98.81 kW. Similarly, for the average minimum point error, the Transformer-based architecture consistently performs the best, with an average value of 0.12 compared to 0.20 for RNN and 0.35 for MLP.

Gap	MAE (kW)			Incr. Gain (%)	
	MLP	RNN	TRN	RNN	TRN
03-04 to 04-04	6.90	3.65	2.73	47.10	25.21
04-04 to 05-04	10.41	5.87	3.72	43.61	36.63
05-04 to 06-04	17.99	7.83	4.25	56.48	45.72
10-04 to 11-04	22.14	6.90	3.88	68.83	43.76

(a)

Gap	Min. Err. (kW)			Incr. Gain (%)	
	MLP	RNN	TRN	RNN	TRN
03-04 to 04-04	0.10	0.05	0.04	50.00	20.00
04-04 to 05-04	0.20	0.14	0.05	30.00	64.28
05-04 to 06-04	0.07	0.03	0.02	57.14	33.33
10-04 to 11-04	0.19	0.13	0.10	31.57	23.07

(b)

Gap	Max. Err. (kW)			Incr. Gain (%)	
	MLP	RNN	TRN	RNN	TRN
03-04 to 04-04	96.28	26.38	19.22	72.60	27.14
04-04 to 04-05	89.01	60.44	20.69	32.10	65.77
05-04 to 06-04	105.01	63.29	35.10	39.73	44.54
10-04 to 11-04	105.20	63.05	28.85	40.06	54.24

(c)

Table 4.13: In the table, the values of MAE (a), Minimum Error (b), and Maximum Error (c) are reported for each model in their respective testing periods. Additionally, the Incremental Gain in percentage is also shown for the RNN compared to the MLP and the Transformer compared to the RNN. These data correspond to the graphs in Figure 4.8.

Finally, after the analysis presented in this chapter of the various models, we can conclude that the best model for solving the imputation problem with data from time series of photovoltaic plants, despite the somewhat resource-intensive training phase, is undoubtedly the one based on the Transformer. This is due to its low MAE and MAPE values, and its near-perfect R^2 index. Moreover, the RNN-based model performs reasonably well in this task and could be a good alternative if one is willing to accept a slightly higher overall error in exchange for a significantly faster and lighter training phase compared to the Transformer.

4.5 Final Conclusions

In conclusion, the models described and evaluated in this work have shown varying degrees of success in predicting the instant energy production curve of the plant during gaps. The Multi-Layer Neural Network-based model, despite being computational lightweight and efficient, demonstrated limited ability to generalize and predict production variations effectively. It struggled to capture the possibility of production spikes and had difficulty managing the day/night cycle.

The Recurrent Neural Network-based model exhibited promise, particularly in capturing diverse energy production variations and handling more complex and variable patterns, it outshone the MLP-based model in various ways. This model can effectively handle gaps of various sizes, ranging from just a few timestamps to a large number of days. Furthermore, it demonstrates the ability to distinguish the day/night cycle and adjust production output accordingly. Its training phase is extremely fast and lightweight, making it very suitable for practical applications in addressing this problem, despite slightly higher errors.

Lastly, the absolute best model is the one based on the Transformer architecture. Its low error compared to the others and excellent ability to handle time series of highly variable lengths make it ideal for this task. It excels in approximating the energy produced by the plant during data gaps, comprehending the day/night alternation well and predicting potential energy spikes. Unfortunately, the training phase is quite resource-intensive, but once this hurdle is overcome, the inference time is extremely low.

Overall, the models provide valuable insights into energy production trends, and their predictability can be useful in real photovoltaic implants contexts. However, further model refinement and optimization, along with the introduction of techniques that can handle variable gap sizes and more complex patterns, may be necessary to achieve more accurate and reliable predictions. Additionally, expanding the dataset and applying advanced techniques for time series prediction could contribute to more successful models in the future.

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