Multidimensional Knapsack Problem

Using a Genetic Algorithm

Introduzione

Problema

$$\max \sum_{j=1}^{n} p_{j} x_{j}$$

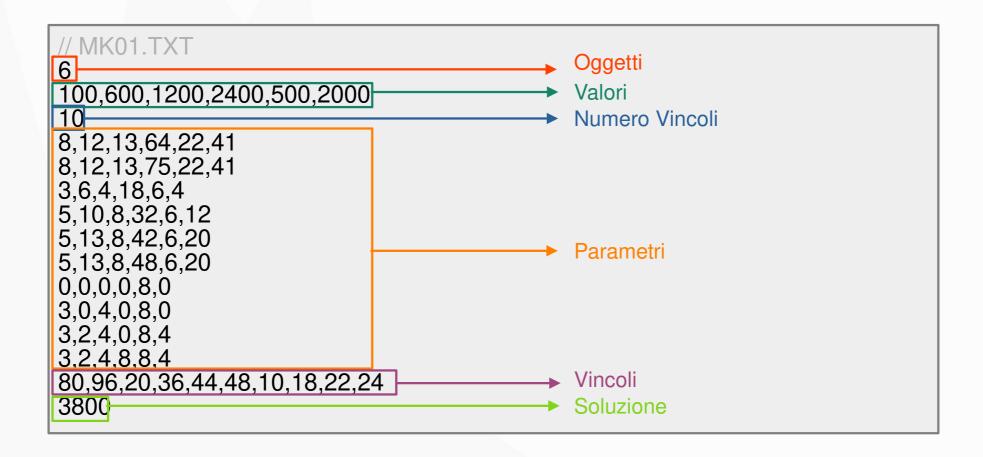
subject to:
$$\sum_{j=1}^{n} r_{i,j} x_{j} \le b_{i}$$
, $i=1,2,...,m$

Soluzione

$$items = [0, 0, 1, 1, 1, 0, 1, 0]$$

 $fitness = 3980.21$

Istanze del Problema



Istanze del Problema

ID	f0	f1	f2	f3	f4	f5	f6	f7	f8	f9	Value
0	8.0	8.0	3.0	5.0	5.0	5.0	0.0	3.0	3.0	3.0	100.0
1	12.0	12.0	6.0	10.0	13.0	13.0	0.0	0.0	2.0	2.0	600.0
2	12.0	13.0	4.0	8.0	8.0	8.0	0.0	4.0	4.0	4.0	1200.0
3	64.0	75.0	18.0	32.0	42.0	48.0	0.0	0.0	0.0	8.0	2400.0
4	22.0	22.0	6.0	6.0	6.0	6.0	8.0	8.0	8.0	8.0	500.0
5	41	41.0	4.0	12.0	20.0	20.0	0.0	0.0	4.0	4.0	2000.0

Implementazione

Initial Population

```
def init_population(self):
        self.population: List[Solution] = []
        self.f_obj: List[float] = list(np.zeros(self.num_elem))
        self.best: Solution = None
        self.best_f: float = float('-inf') # tiny number
        for i in range(self.num_elem):
            tmp_sol: Solution = np.zeros(self.num_items)
            # list of indexes (e.g. 1 means df[1])
            T: List[int] = list(range(self.num_items))
12
            # temporary actual constrints sum
            R = np.zeros(len(self.problem.W))
            # randomly extract an item
            j = T.pop(random.randint(0, len(T) - 1))
            item = self.problem.df.loc[:, self.problem.df.columns !=
                                           'Value'].loc[j].to_numpy()
21
            while all(R + item <= self.problem.W):</pre>
                tmp_sol[j] = 1
                R = R + item
                # no more items left, continue to new solution
                if len(T) \ll 0:
                    break
                j = T.pop(random.randrange(len(T)))
                item = self.problem.df.loc[:, self.problem.df.columns !=
                                               'Value'].loc[j].to_numpy()
        self.population.append(tmp_sol)
        self.f_obj[i] = self.problem.objective_function(tmp_sol)
        self.update_best(tmp_sol, self.f_obj[i], 0)
```

Mating Pool Selection

```
def select_mating_pool(self) → List[Tuple[Solution, Solution]]:
        def tournament(k: int = 5) \rightarrow Solution:
            random_select_solutions = [
                    random.randint(0,
                           len(self.population) - 1) for _ in range(k)
            # generate a dictioray {solution index : solution fitness}
            # e.g. solution 1/16 has fitness vale of 287
            selected_objectivefunctions = {
12
                i: self.f_obj[i]
                     for i in random_select_solutions
            # find solution index with max fitless value
            # e.g. solution 3/16 has the max fintess value
            max_index = max(selected_objectivefunctions,
                             key=selected_objectivefunctions.get)
21
            return self.population[max_index]
        mating_pool = []
        for i in range(len(self.population) // 2):
            c1 = tournament()
            c2 = tournament()
            mating_pool.append((
                     c1,
                     c2,
            ))
        return mating_pool
```

Crossover Operator

```
def do_crossover(self, mating_pool: List[Tuple[Solution,Solution]])
                                                           → List[Solution]:
        def uniform_crossover_operator(s1: Solution, s2: Solution)
                                                           → Solution:
            From parents (s1 and s2) generate only 1 child (c) using
            a random probability to choose a chromosome from s1 or s2
            c = np.zeros(len(s1))
12
            for i in range(len(s1)):
                # random True or False.
                c[i] = s1[i] if bool(random.getrandbits(1)) else s2[i]
            return c
        children = []
21
        for s1, s2 in mating_pool:
            if random.random() < self.pcross:</pre>
22
                c = uniform_crossover_operator(s1, s2)
                children.append(c)
                continue
            children.append(s1)
            children.append(s2)
        return children
```

Mutation Operator

```
do_mutation(self, children: List[Solution]):
         Randomly flip bits according to pmut probability
         for child in children:
             for i in range(len(child)):
                 if random.random() < self.pmut:</pre>
                          child[i] = int(not child[i])
11
12
13
21
22
```

Repair Operator

```
def repair_operator(self, children: List[Solution]) → Solution:
        for child in children:
            child_parameters = self.problem.df.loc[:,
                               self.problem.df.columns != 'Value'].
                                           loc[child ==1].sum().to_numpy()
            if all(child_parameters <= self.problem.W):</pre>
                continue
            old_child = child.copy()
12
            # DROP PHASE
            i = 0
            while any(child_parameters > self.problem.W):
                # delete item from solution
                child[self.problem.sorted_value_objects_indexes[i]] = 0
                # update parameters
                child_parameters = self.problem.df.loc[:,
                                  self.problem.df.columns != 'Value'].loc[
21
                                               child == 1].sum().to_numpy()
                i = i + 1
            # ADD PAHSE
            for i in reversed(range(len(child))):
                # temporary edited child
                tmp_child = child.copy()
29
                # add item to solution
                tmp_child[self.problem.sorted_value_objects_indexes[i]] = 1
                # update parameters
                tmp_child_parameters = self.problem.df.loc[:,
                                    self.problem.df.columns !='Value'].loc[
                                            tmp_child == 1].sum().to_numpy()
                # update child with tmp mods
                # if is feasible solution
                if all(tmp_child_parameters <= self.problem.W):</pre>
                    child = tmp_child.copy()
                    child_parameters = tmp_child_parameters
```

Select New Population

```
def select_new_population(self, children: List[Solution], gen: int):
        def select_best():
            total_solutions: List[Solution] = self.population + children
            total_fintesses: List[float] = self.f_obj + [
                self.problem.objective_function(c) for c in children
            assert len(total_solutions) == len(total_fintesses)
            total_indexes: List[int] = list(range(len(total_solutions)))
12
            total_indexes.sort(key=lambda i: total_fintesses[i],
                                                    reverse=True)
            best_indexes: List[int] = total_indexes[:self.num_elem]
            self.population = [total_solutions[i] for i in best_indexes]
            self.f_obj = [total_fintesses[i] for i in best_indexes]
            self.update_best(self.population[0], self.f_obj[0], gen)
21
        select_best()
22
```

Tuning Phase

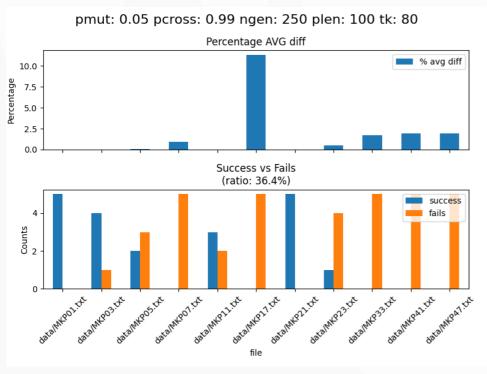
Tuning Dataset

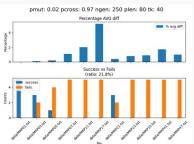
File	Oggetti	Vincoli
MKP01.txt	6	10
MKP03.txt	15	10
MKP05.txt	28	10
MKP07.txt	50	5
MKP11.txt	28	2
MKP17.txt	105	2
MKP21.txt	30	5
MKP23.txt	40	5
MKP33.txt	60	5
MKP41.txt	80	5
MKP47.txt	90	5

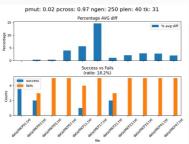
Output

```
,file,gen,found,target,success,diff
0,data/MKP01.txt,52,3800.0,3800.0,True,0.0
1,data/MKP01.txt,1,3800.0,3800.0,True,0.0
2,data/MKP01.txt,0,3800.0,3800.0,True,0.0
3,data/MKP01.txt,48,3800.0,3800.0,True,0.0
4, data/MKP01.txt,87,3800.0,3800.0,True,0.0
5, data/MKP03.txt,20,3915.0,4015.0,False,100.0
6, data/MKP03.txt,76,3525.0,4015.0, False,490.0
7, data/MKP03.txt,81,3850.0,4015.0, False,165.0
8, data/MKP03.txt,44,3965.0,4015.0, False,50.0
9,data/MKP03.txt,0,3820.0,4015.0,False,195.0
10, data/MKP05.txt,16,11880.0,12400.0,False,520.0
11, data/MKP05.txt,90,11940.0,12400.0,False,460.0
```

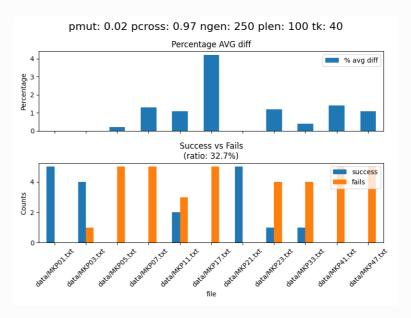
Risultati

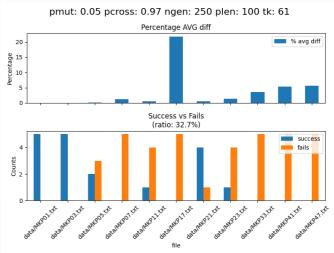












Top 3

pmut	pcross	ngen	plen	tk	Success Ratio (%)	Max AVG Diff (%)
0.05	0.99	250	100	80	36.4	12.0
0.02	0.97	250	100	41	32.7	5.0
0.05	0.97	250	100	61	32.7	21.0

Testing Phase

Testing Dataset

File	Oggetti	Vincoli
MKP02.txt	10	10
MKP04.txt	20	10
MKP06.txt	39	5
MKP08.txt	60	30
MKP10.txt	28	2
MKP12.txt	28	2
MKP20.txt	30	5
MKP22.txt	30	5
MKP24.txt	40	5
MKP30.txt	50	5
MKP36.txt	70	5
MKP40.txt	80	5
MKP46.txt	90	5
MKP48.txt	27	4
MKP50.txt	29	2
MKP54.txt	28	4

Risultati

