

Machine Learning - Sheet 1

Deadline: 26.04.2018 - 12:00

Task 1: Boolean Functions

(5 Points)

Give decision trees to represent the following Boolean functions:

- (a) $A \wedge \neg B$
- (b) $A \vee (B \wedge C)$
- (c) $A \times B$
- (d) $(A \wedge B) \vee (C \wedge D)$
- (e) M of N: a function that depends on variables X_1, \ldots, X_N , and returns true if and only if exactly M of the N variables are true.

Task 2: Literature (0 Points)

Read pages 55-60 of the book Machine Learning [1].

Task 3: Entropy (6 Points)

An information source emits four symbols A, B, C, D, which occur with probabilities $p(A), \ldots, p(D)$.

- 1. Suppose that p(A) = 0.5, p(B) = 0.3, p(C) = 0.1, p(D) = 0.1. Compute the entropy H(p).
- 2. For which probabilities is the entropy H maximal? For which is it minimal?
- 3. Explain in your own words what the entropy is.
- 4. How is the entropy used for the decision tree construction?

Task 4: ARFF Files (0 Points)

Make yourself familiar with ARFF files (see http://www.cs.waikato.ac.nz/ml/weka/arff.html).

Task 5: Information Gain

(9 Points)

Implement the following methods in Java or Python:

1. Implement the method entropyOnSubset that takes three arguments: a dataset $D = [inst_0, ..., inst_{N-1}]$, a list of indices $I = [i_0, i_1, ..., i_{m-1}]$ that describe a subset of the dataset, and a class attribute C. The subset of the dataset is then defined as

$$S := \{ inst_{i_j} | 0 \le j < m \}.$$



The entropy of S relative to the C-wise classification is then

$$H(S) := -\sum_{v \in values(C)} p_v \cdot log_2(p_v),$$

where p_v is the proportion of S belonging to class v. The value H(S) is what the entropyOnSubsetmethod should return.

2. Let D, I, S and C be as above. Implement the method informationGain that takes D, I, C and an additional attribute A as arguments, and returns

$$InformationGain(S,A) := H(S) - \sum_{v \in values(A)} \frac{|S_v|}{|S|} \cdot H(S_v),$$

where S_v are those instances that take value v at attribute A.

3. Implement an ARFF file parser and test your codes from previous steps on the Weather dataset (weather.nominal.arff).

References

[1] Tom M. Mitchell. Machine learning. McGraw Hill series in computer science. McGraw-Hill, 1997.