

$$(1) \sum F_x = 0 = 80 \Delta A \cos 30^\circ - 25 \Delta A \sin 30^\circ + \cos 30^\circ \sigma_{x'} \Delta A + \sin 30^\circ \tau_{x'y'} \Delta A = 0$$

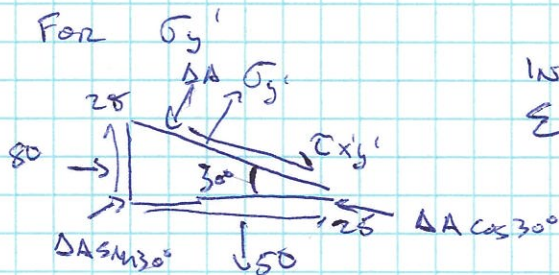
$$(2) \sum F_y = 0 = 25 \Delta A \cos 30^\circ + 80 \Delta A \sin 30^\circ + \sin 30^\circ \sigma_{x'} \Delta A + \cos 30^\circ \tau_{x'y'} \Delta A = 0$$

$$\begin{aligned} (1) &\Rightarrow (\tau_{x'y'} \sin 30^\circ + \sigma_{x'} \cos 30^\circ = -80 \cos 30^\circ + 25 \sin 30^\circ) / \cos 30^\circ \\ + (2) &\Rightarrow (\tau_{x'y'} \cos 30^\circ - \sigma_{x'} \sin 30^\circ = -25 \cos 30^\circ + 80 \sin 30^\circ) / \sin 30^\circ \end{aligned}$$

$$\tau_{x'y'} (\tan 30^\circ + \cot 30^\circ) = -80 + 25 \tan 30^\circ - 25 \cot 30^\circ - 80$$

$$\tau_{x'y'} = -68.8 \text{ MPa}$$

$$\sigma_{x'} = -25.8 \text{ MPa}$$



IN THIS CASE, WE SAVE SOME TIME BY CONSIDERING $\sum \vec{F}_{y'}$ ← SUM OF FORCES IN y'

$$\sum F_{y'} = 0 \Rightarrow \sigma_{y'} \Delta A + 25 \Delta A \sin 30^\circ \cos 30^\circ + 80 \Delta A \sin 30^\circ \sin 30^\circ + 25 \Delta A \cos 30^\circ \sin 30^\circ - 50 \Delta A \cos 30^\circ \cos 30^\circ$$

$$\Rightarrow \sigma_{y'} = -25 \sin 30^\circ \cos 30^\circ - 80 \sin 30^\circ \sin 30^\circ - 25 \sin 30^\circ \cos 30^\circ + 50 \cos^2 30^\circ = -4.15 \text{ MPa}$$