

Name:

Exam 2

1. (30 pts.) Consider the problem of an infinite plate with a hole under biaxial tension as shown in Figure 1.

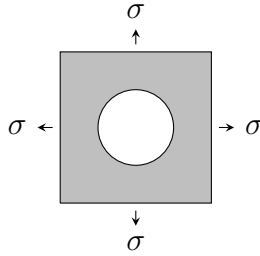


Figure 1: Infinite plate with a hole under biaxial tension

- (a) Formulate boundary conditions for the problem
- (b) Develop the Airy stress function in polar coordinates to satisfy the remote boundary conditions
- (c) How would you proceed to finish the problem?

2. (30 pts.) You are tasked with testing a material which is assumed to be monoclinic under a unique biaxial test ($\sigma_{11} = \sigma$, $\sigma_{22} = 2\sigma$, all other $\sigma_{ij} = 0$).
- (a) Find the strain in terms of the applied stress, σ
 - (b) What, if anything, could you measure from this experiment to confirm whether or not the material is, in fact, monoclinic?

3. (40 pts.) You are attempting to characterize a large deformation material using a new potential function you found in a paper. This potential function is expressed in terms of the invariants of stretch, which are given below for an incompressible material.

$$I_1 = \lambda_1^2 + \lambda_2^2 + \lambda_3^2 \quad (1)$$

$$I_2 = \frac{1}{\lambda_1^2} + \frac{1}{\lambda_2^2} + \frac{1}{\lambda_3^2} \quad (2)$$

$$I_3 = J^2 = \lambda_1^2 \lambda_2^2 \lambda_3^2 \quad (3)$$

Recall that the Cauchy stress can be found in terms of W as

$$\sigma_i = \lambda_i \frac{\partial W}{\partial \lambda_i} \quad (4)$$

. The potential function to be implemented is given as

$$W = C_{11}(I_1 - 3)(I_2 - 3) + C_{22}(I_1 - 3)^2(I_2 - 3)^2 + D(J - 1)^2 \quad (5)$$

. Find σ_1 as a function of the applied stretch, λ , for the following loading conditions:

$$\text{uniaxial} \quad \lambda_1 = \lambda \quad \lambda_2 = \lambda_3 \quad (6)$$

$$\text{biaxial} \quad \lambda_1 = \lambda \quad \lambda_2 = \lambda \quad (7)$$

$$\text{plane strain shear} \quad \lambda_1 = \lambda \quad \lambda_2 = 1 \quad (8)$$

