AE 737: Mechanics of Damage Tolerance

Lecture 14 - Stress based fatigue

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schedule

- 10 Mar Stress-based fatigue
- 12 Mar Stress-based fatigue
- 17 Mar Strain-based fatigue
- 19 Mar Crack growth, HW6 Due

outline

- fatigue
- nominal and local stress
- fatigue tests
- fatigue life analysis

fatigue

fatigue

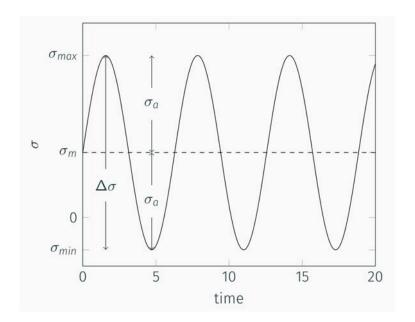
- We refer to damage from repeated, or cyclic loads as fatigue damage
- Some of the earliest work on fatigue began in the 1800's
- Chains, railway axles, etc.
- \bullet An estimated 80% of failure expenses are due to fatigue

fatigue

- There are three main approaches to fatigue analysis
 - Stress based fatigue analysis
 - Strain based fatigue analysis
 - Fracture mechanics fatigue analysis

stress based fatigue

- One of the simplest assumptions we can make is that a load cycles between a constant maximum and minimum stress value
- This is a good approximation for many cases (axles, for example) and can also be easily replicated experimentally
- This is referred to as constant amplitude stressing



- $\bullet \ \Delta \sigma$ is known as the stress range, and is the difference between max and min stress
- ullet σ_m is the mean stress, and can sometimes be zero, but this is not always the case
- ullet σ_a is the stress amplitude, and is the variation about the mean

• We can express all of these in terms of the maximum and minimum stress

$$egin{aligned} \Delta\sigma &= \sigma_{max} - \sigma_{min} \ \sigma_m &= rac{\sigma_{max} + \sigma_{min}}{2} \ \sigma_a &= rac{\sigma_{max} - \sigma_{min}}{2} \end{aligned}$$

- It is also common to describe some ratios
- The stress ratio, R is defined as

$$R = rac{\sigma_{min}}{\sigma_{max}}$$

• And the amplitude ratio, A is defined as

$$A=rac{\sigma_a}{\sigma_m}$$

useful relations

• There are some useful relationships between the above equations

$$egin{aligned} \Delta\sigma &= 2\sigma_a = \sigma_{max}(1-R) \ \sigma_m &= rac{\sigma_{max}}{2}(1+R) \ R &= rac{1-A}{1+A} \ A &= rac{1-R}{1+R} \end{aligned}$$

nominal and local stress

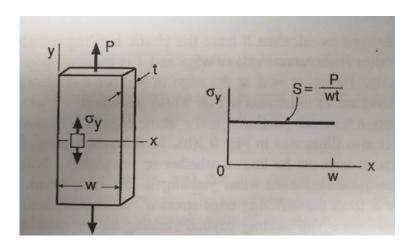
definition and notation

- It is important to distinguish between the nominal (global) stress and the local stress at some point of interest
- ullet We use σ for the stress at a point (local stress)
- ullet We use S as the nominal (global) stress
- $\bullet \ \ \text{In simple tension, } \sigma = S$

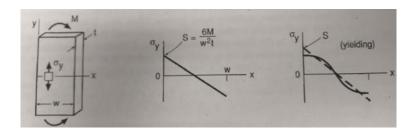
notation

- \bullet For many cases (bending, notches), $\sigma \neq S$ in general
- ullet We must also be careful to note σ_y , in some cases $S<\sigma_y$ but at some locations $\sigma>\sigma_y$

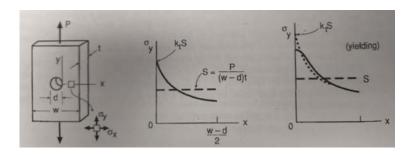
simple tension



bending



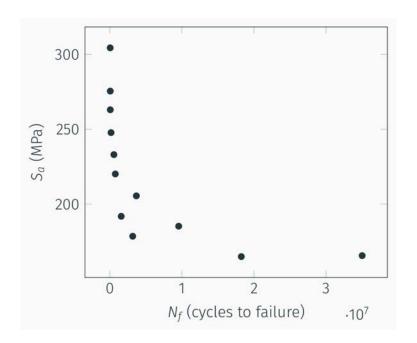
notches



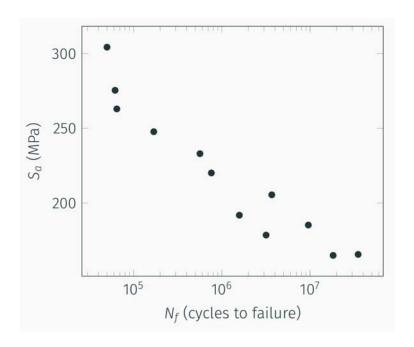
fatigue life analysis

- Stress-life curves, or S-N curves, are generated from test data to predict the number of cycles to failure
- ullet In general, one set (or family) of S-N curves is generated using the same σ_m
- Usually S_a (the nominal stress equivalent of σ_a) is plotted versus N (the number of cycles)

- Each individual point on an S-N curve represents one fatigue experiment
- To find enough data to form statistical significance, as well as to fit a curve across all levels of fatigue is very time-consuming
- In the following plot, if only one test was performed for each point, the total number of cycles tested would be about $7.3x10^7$
- For a 100 Hz machine, this represents over 200 hours of consecutive testing



- On a linear scale, the data appear not to agree well with any standard fit
- It is also very difficult to differentiate between low-cycle fatigue failure stresses
- Instead S-N curves are often plotted on a semi-log or log-log scale, so pay attention to the axes



curve fits

• If the curve is nearly linear on a log-linear plot, we use the following form to fit the data

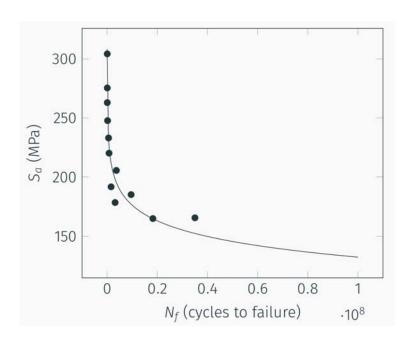
$$\sigma_a = C + D \log N_f$$

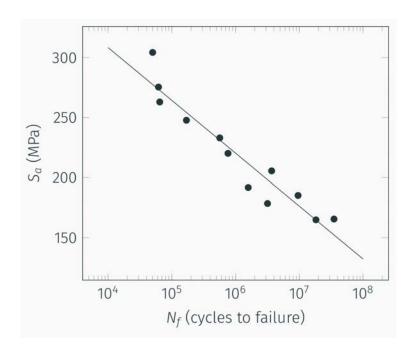
• When the data are instead linear on a log-log scale, the following form is generally used

$$\sigma_a = \sigma_f'(2N_f)^b$$

 • σ_f' and b are often considered material properties and can often be looked up on a table (p. 235)

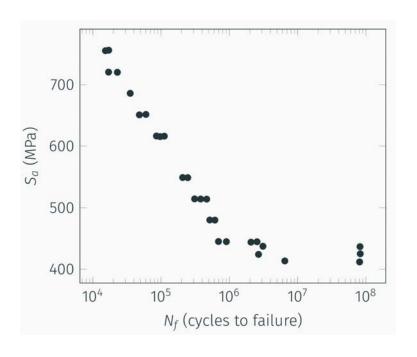
curve fit





- The fatigue limit, or endurance limit, is a feature of some materials where below a certain stress, no fatigue failure is observed
- Below the fatigue limit, this material is considered to have infinite life
- This most notably occurs in plain-carbon and low-alloy steels
- ullet In these materials, σ_e is considered to be a material property

- This phenomenon is not typical of aluminum or copper alloys
- ullet It is sometimes arbitrarily assigned using whatever the failure stress is at some large number of cycles (10⁷ or 10⁸)



high and low cycle fatigue

- Some other important terms are high cycle fatigue and low cycle fatigue
- $\bullet\,$ "High cycle fatigue" generally is considered anything above 10^3 cycles, but varies somewhat by material

high and low cycle fatigue

- High cycle fatigue occurs when the stress is sufficiently low that yielding effects do not dominate behavior
- When yielding effects do dominate behavior, the strain-based approach is more appropriate