

Lecture 4 - Curved Boundaries

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schedule

- 27 Jan - Curved Boundaries, HW 1 Due
- 1 Feb - Plastic Zone
- 3 Feb - Plastic Zone, HW 2 Due, HW 1 Self-grade due
- 8 Feb - Fracture Toughness

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- curved boundaries
- stress concentration factors

errata and supplemental charts

- on p. 64 there is a + missing between two terms, see Lecture 2 for the fix
- Also on p. 64, in equation 29 it is not clear, but use the f_w from a previous equation, on p. 56
- Some of the black and white figures can be difficult to use, we have scanned and re-created the plots online
- Interactive versions of compounding figures from p. 50, 71-73 can be found at here¹

¹<http://ndaman.github.io/damagetolerance/examples/Compounding%20Figures.html>

finite height - p. 50

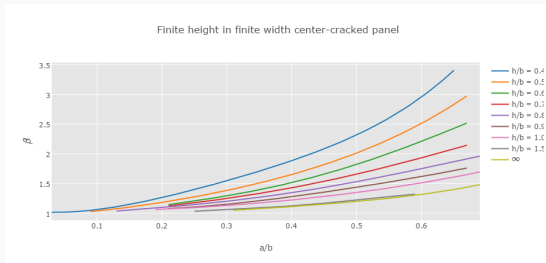


Figure 1: beta for finite height effects, see text p. 50 or interactive chart linked in previous slide

offset crack - p. 71

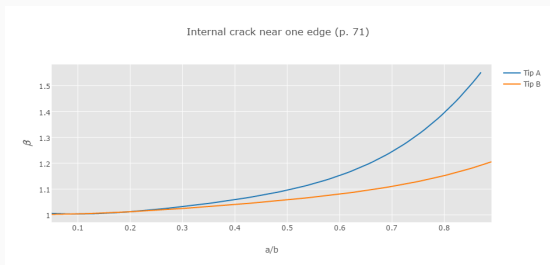


Figure 2: beta for offset internal crack, see text p. 71 or interactive chart linked previously

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crack near hole - p. 72

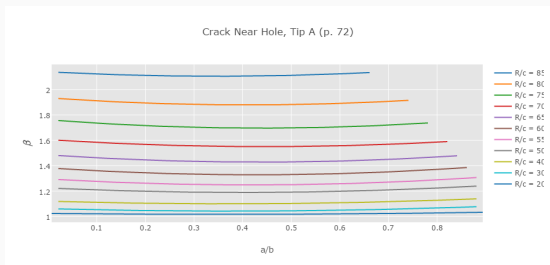


Figure 3: beta for the crack tip farther away from a hole, see text p. 72 or interactive chart linked previously

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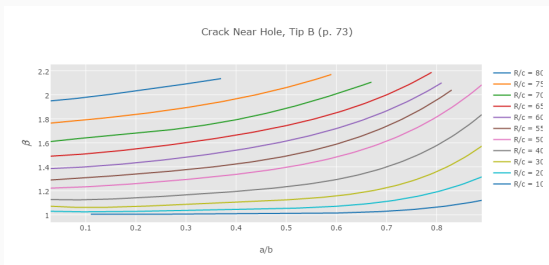


Figure 4: beta for the crack tip closer to a hole, see text p. 73 or interactive chart linked previously

curved boundaries

short cracks on curved boundaries

- For short cracks, we can use the *stress concentration factor* on a curved boundary to determine the stress intensity factor
- The stress concentration factor only gives the maximum stress at the curved boundary, thus the longer the crack is, the farther away from the curved boundary (and maximum stress) it is.
- Stress concentration factors can be found: pp. 82-85 in the text
- Also see supplemental text on Blackboard or here²

²http://ndaman.github.io/damagetolerance/classdocs/stress_concentrations.pdf

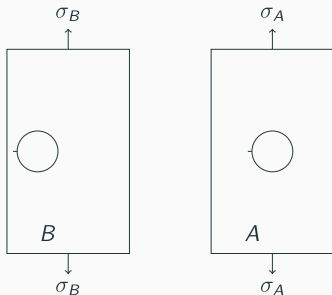
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short cracks on curved boundaries

- Suppose we want to determine the stress intensity on a panel, panel B
- We find a similar panel with a known stress intensity factor, panel A
- We adjust the applied load on panel A such that $K_{I,A} = K_{I,B}$
- The magnitude of this load adjustment is determined using the *stress concentration factors* in panels B and A Note: the notation: K_t for stress concentration factor, K_I for stress intensity factor

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short cracks on curved boundaries



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short cracks on curved boundaries

- Since A is a fictional panel, we set the applied stress, σ_A such that

$$\sigma_{max,B} = \sigma_{max,A}$$

- Substituting stress concentration factors

$$K_{t,B}\sigma_B = K_{t,A}\sigma_A$$

- Solving for σ_A

$$\sigma_A = \frac{K_{t,B}}{K_{t,A}}\sigma_B$$

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- Since the crack is short and $\sigma_{max,A} = \sigma_{max,B}$ we can say

$$\begin{aligned} K_{I,B} &= K_{I,A} \\ &= \sigma_A \sqrt{\pi C} \beta_A \\ &= \frac{K_{t,B}}{K_{t,A}} \sigma_B \sqrt{\pi C} \beta_A \end{aligned}$$

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example 6 (p. 86)

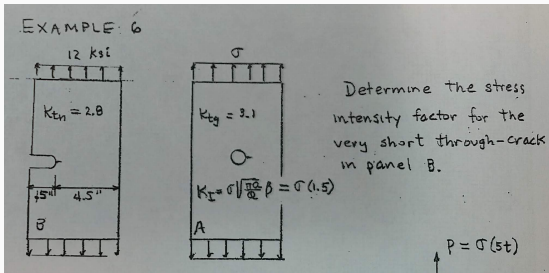


Figure 5: See p. 86, there is a short through crack on the edge of a 0.5" deep notch on a 5 inch wide panel with a remote 12 ksi stress applied. The net section stress concentration factor is 2.8, while the global stress concentration factor for a similar panel with a hole is

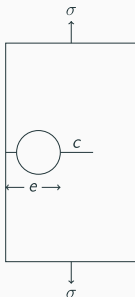
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long cracks on curved boundaries

- As a crack becomes very large, the effect of the curved boundary diminishes
- We find expressions for β_L (long crack) and β_S (short crack)
- We connect β_S to β_L using a straight line from β_S to a tangent intersection with β_L

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long cracks on curved boundaries



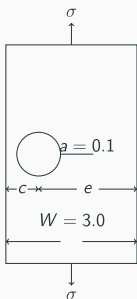
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- Example here³

³<https://colab.research.google.com/drive/1bq0pXDgYL-xTPwUAQ0tffKBcMoS8sgry?usp=sharing>

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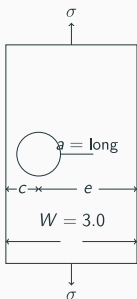
group one



- $c = 0.75$, $e = 2.25$, $r = 0.5$
- assume a is short and calculate β for this case
- calculate in terms of β for known state

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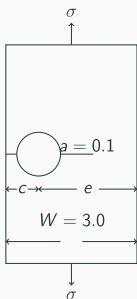
group two



- $c = 0.75$, $e = 2.25$, $r = 0.5$
- assume a is long and calculate β for this case
- calculate in terms of β for known state

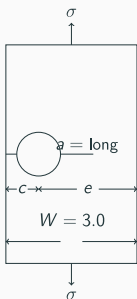
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group three



- $c = 0.75$, $e = 2.25$, $r = 0.5$
- assume a is short and calculate β for this case
- calculate in terms of β for known state

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- $c = 0.75$, $e = 2.25$, $r = 0.5$
- assume a is long and calculate β for this case
- calculate in terms of β for known state

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discussion

Draw a sketch to show how we could use this method to find cracks of intermediate length near a curved boundary

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stress concentration factors

centered hole tension - p. 82

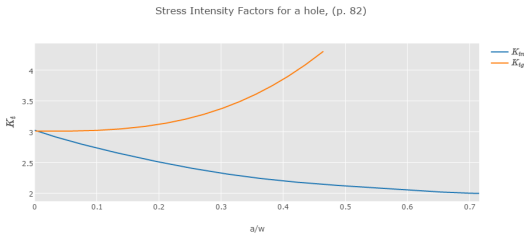
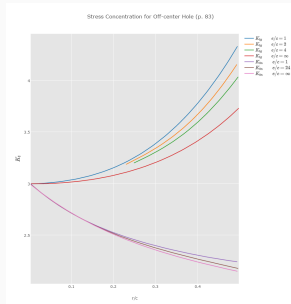


Figure 6: A plot of stress concentration factors near a hole, see text p. 82 or the interactive plots linked in the last slide.

K_{tg} uses stress for the cross-sectional area if no hole was present, K_{tn} uses stress at the net section (subtracting hole

off-center hole tension - p. 83



K_{tg} uses stress for the cross-sectional area if no hole was present, K_{tn} uses stress at the net section (subtracting hole area). c is the distance from the closest edge to the center of

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bending of a bar with u-shaped notch - p. 84

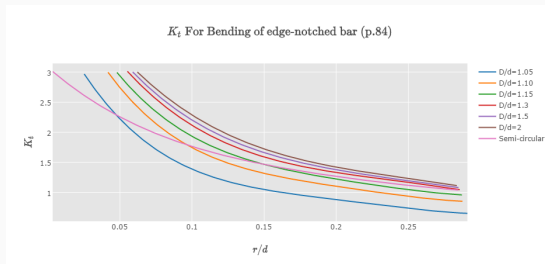
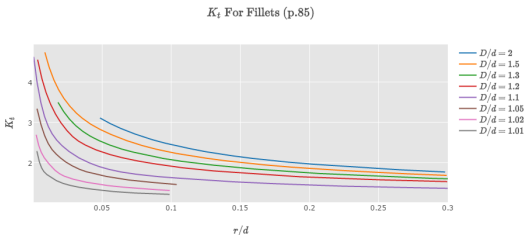


Figure 7: A plot of stress concentration factors in a bar with a u-shaped notch, see text p. 84 or the interactive plots linked in the last slide.

Nominal stress used for K_t is given by $\sigma_{nom} = 6M/hd^2$ where

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D is the larger width (before the step), d is the width after the step. Nominal stress is $\sigma_{nom} = P/hd$, where h is specimen thickness. r is the fillet radius.

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interactive page

- An interactive page with these plots can be accessed here⁴

⁴<http://ndaman.github.io/damagetolerance/examples/Stress%20Concentration%20Factors.html>

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