

# **AE 737 - MECHANICS OF DAMAGE TOLERANCE**

## LECTURE 23

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# SCHEDULE

- 19 Apr - Damage Tolerance, Homework 8 Due
- 21 Apr - Exam 2
- 26 Apr - Exam Solutions, Damage Tolerance
- 28 Apr - SPTE, AFGROW, Finite Elements
- 3 May - Finite Elements
- 5 May - Non-Destructive Testing, Composites, Final Project Due  
May 10

1. special topics
2. review
3. damage tolerance
4. inspection cycle

## SPECIAL TOPICS

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- Other questions?

## REVIEW

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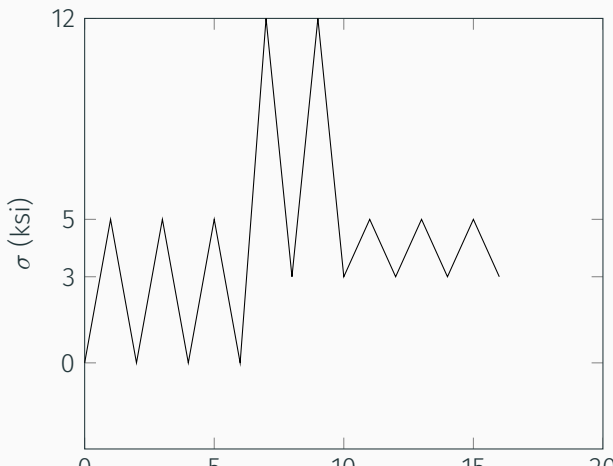
Find the fatigue life of 2024-T4 aluminum ( $\sigma'_f = 131$  ksi,  $b = -0.102$ ) under the following load scenario

Stress Term	Min	Max
$\sigma_x$	0	15
$\sigma_y$	-5	10
$\tau_{xy}$	5	15

Show how to find the cycles to failure for 7075-T6 ( $\sigma'_f = 213$  ksi,  $b = -0.143$ ,  $\epsilon'_f = 0.262$  and  $c = -0.619$ ) with  $\epsilon_a = 0.40$  and  $\sigma_m = 15$ ksi

## GROUP 3

Use the Boeing method to find an equivalent load cycle for the following load spectrum. Repeat this calculation using two different "cycle counting" methods. Use material properties for 4340 steel ( $p = 2.7$ ,  $q = 0.84$ ,  $M_T = 70.0$ ).





For a wide, center-cracked panel with  $C = 10^{-9}$ ,  $n = 4$  and  $a_0 = 1.5$  in. Assume  $\sigma_{YS} = 70$  ksi.

1. Integrate to find the crack length after 10,000 cycles of  $R = 0$ ,  $\sigma_{max} = 10$  ksi loading
2. Calculate the plane stress plastic zone after an overload of  $\sigma = 30$  ksi
3. Find the Wheeler parameter ( $\phi$ ) for the next cycle of  $\sigma_{max} = 10$  ksi loading with  $m = 1.5$

## DAMAGE TOLERANCE

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- Assume cracks are present
- When cracks grow to a sufficient size, they are inspectable
- Inspection cycles are set such that we can be sure crack will not become critical during regular operation

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- **Operating load** stress spectrum (used for crack propagation/fatigue)

- Single load path - safe life

## STRUCTURAL CATEGORIES

- Single load path - safe life
- Single load path - damage tolerant



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- Multiple load path - externally inspectable

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- Single load path - damage tolerant
- Multiple load path - externally inspectable
- Multiple load path - inspectable prior to failure

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- In these cases, safe life design is used to identify a certain number of cycles a part can sustain before it needs to be replaced
- This often requires replacing parts pre-maturely

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- When the detectable crack size is much less than the critical crack length, we can safely inspect a part so that it is only replaced when damage is detected
- Many times this damage can be repaired to avoid replacing the part entirely
- Ideal for large, expensive parts that are easy to access (inspection and repair)

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- A secondary structure is inspectable
- The secondary structure can support a certain number of cycles after failure of the primary structure
- Secondary structure can be inspected to observe damage in primary structure

- In this case the primary structure is inspectable



## MULTIPLE LOAD PATH - INSPECTABLE PRIOR TO FAILURE

- In this case the primary structure is inspectable
- Otherwise same as externally inspectable structure

## INPSECTION CYCLE

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- We have developed all the equations necessary to determine our own
  1. Determine loading cycle (or equivalent load cycle using Boeing method)
  2. Determine maximum crack length
  3. Determine initial assumed crack length (minimum detectable crack)
  4. Calculate number of cycles/flights until crack grows to maximum allowable size



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$$\sum_i (z\sigma_{max})_i^p N_i = (S)^p \quad (23.1)$$

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- Crack growth becomes unstable in Region III

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- Radiographic (X-Ray, nearly any material)

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- $\Delta N$  should be small enough to give converged solution

