Mechanics of Materials

Lecture 4 - Mechanical Properties

Dr. Nicholas Smith

Wichita State University, Department of Aerospace Engineering

25 August, 2021

schedule

- 25 Aug - Mechanical Properties
- 27 Aug - Homework 1 Due
- 30 Aug - Axial Load
- 1 Sep - Exam Review
- 3 Sep - Homework 2 Due, Homework 1 Self-Grade Due
- 8 Sep - Exam 1
- 10 Sep - Project 1 Due

outline

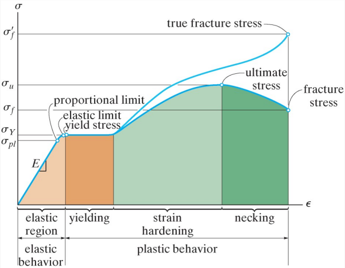
- stress-strain
- strain energy
- poisson's ratio
- shear stress-strain

stress-strain

stress-strain

- Most engineering materials can be characterized by their stress-strain diagram
- Comes from a tensile or compressive test, where a load is applied (gives stress) and the strain is measured (via an extensometer or strain gauge)
- *Engineering stress* is plotted on the y-axis vs. *engineering strain* on the x-axis

stress-strain



Conventional and true stress–strain diagram for ductile material (steel) (not to scale)

elastic behavior

- Most of the time, the linear region is the one we are most interested in
- In this region, the material is elastic, meaning when the load is removed the material will return to its original state

elastic behavior

- Because the stress-strain curve is a straight line, we can relate stress and strain with a single constant
- This constant is known as the *modulus of elasticity* or *Young's modulus*

$$\sigma = E\epsilon$$

plastic behavior

- Yielding occurs when stress increases beyond the *yield stress* or *elastic limit*, this is when plastic deformation occurs, meaning the material will not go back to its original shape
- Strain hardening is common in many metals, and means as more stress is applied the material becomes more stiff

plastic behavior

- Necking occurs when the material begins to have a noticeable "neck" due to being stretched very thin and lower forces are required to deform the material

true stress-strain

- True stress and strain use the actual material cross-section (instead of the original cross-section) to calculate stress and strain
- In the elastic region the difference is negligible, so in many cases we just stick with engineering strain, even if we know it is *wrong*

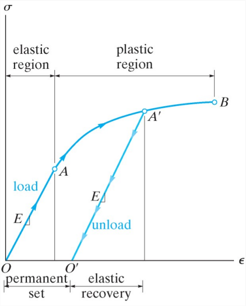
ductile materials

- Ductile materials can undergo large strains before failure
- One way to report how ductile a material is is known as percent elongation
- Steel, brass, molybdenum, and zinc exhibit similar ductile stress-strain characteristics
- Aluminum is often considered ductile, but its stress-strain behavior is a bit different

brittle materials

- Materials that exhibit little or no yielding before failure are called *brittle*
- Cast iron, concrete, and glass are common brittle materials
- Brittle materials fail easily in tension, but are very strong in compression

strain hardening



strain energy

strain energy

- Work in physics is defined as force times distance
- As a force is applied to a material, the energy from the work done by the load is stored in the material and called strain energy
- In engineering, we often use the strain energy density, or the amount of strain energy per unit volume of material

$$u = \frac{1}{2}\sigma\epsilon$$

toughness

- Graphically, the area under the stress strain curve represents the strain energy density
- We call the entire region (usually for a ductile material) the *toughness*
- Some hardened steels have a high failure strength, but are not very ductile, this gives them a lower toughness

example 3.3

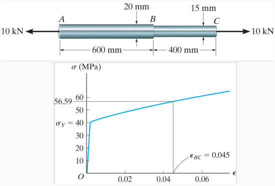


Figure 1: A bar is under a 10 kilonewton tensile load. One section of the bar is 600 mm long with a 20 mm diameter, while the other section is 400 mm long with a 15 mm diameter. The stress-strain diagram below shows that for a stress of 56.59 MPa

The aluminum rod shown has a circular cross-section. Determine the elongation of the rod when load is applied using the given stress-strain diagram.

poisson's ratio

poisson's ratio

- When a material is stretched in one direction, it tends to contract in the transverse direction
- The ratio of transverse to axial strain is called *Poisson's ratio*

$$\nu = -\frac{\epsilon_{transverse}}{\epsilon_{axial}}$$

shear stress-strain

shear stress-strain

- It can be experimentally difficult to obtain a state of pure shear, but a common method for many materials is to place a thin tube in torsion
- For most engineering materials, the shear stress-strain behavior is linear in the elastic region, but has a different constant relating stress to strain, known as the *Shear Modulus*

$$\tau = G\gamma$$

elastic constants

- For most materials, E, G and ν are related by the following expression

$$G = \frac{E}{2(1+\nu)}$$

example 3.5

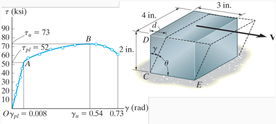


Figure 2: A block 4 inches deep, 3 inches wide, and 2 inches tall is loaded in shear (in the 3 inch direction). The stress-strain diagram shows that at the elastic limit of 52 ksi there is a strain of 0.008.

Determine G for the specimen shown. Also find the maximum distance d, that the top could be displaced horizontally while remaining elastic. What force V is required to cause this displacement?