### Random Variables

15 March 2023 11:43

What are Algebraic Variables?
 In Algebra a variable, like x, is an unknown value

What are Random Variables in Stats and
 Probability? A Random Variable is a set of
 possible values from a random experiment.

• Types of Random Variables?

# Session 3 - Descriptive Statistics Page 1 Probability Distributions

15 March 2023 11:53

1. What are Probability Distributions?

A probability distribution is a list of all of the possible outcomes of a random variable along with their corresponding probability values.

### Problem with Distribution?

In many scenarios, the number of outcomes can be much larger and hence a table would be tedious to write down. Worse still, the number of possible outcomes could be infinite, in which case, good luck writing a table for that.

Example - Height of people, Rolling 10 dice together

## Solution - Function?

What if we use a mathematical function to model the relationship between outcome and probability?

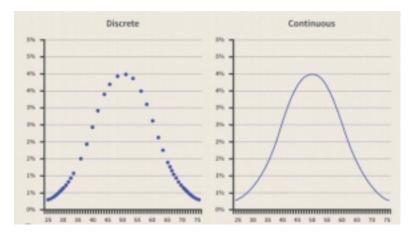
## Note - A lot of time Probability Distribution and Probability

# Distribution Functions are Session 3 - Descriptive Statistics

## Page 2

Note - A lot of time Probability
Distribution and Probability Distribution
Functions are used interchangeably.

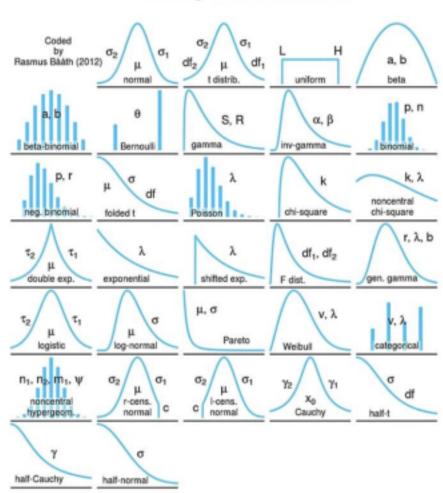
## 1. Types of Probability Distributions



**Famous Probability Distributions** 

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# **Probability Distributions**



## Why are Probability Distributions important?

- Gives an idea about the shape/distribution of the data.

And if our data follows a famous distribution then we automatically know a lot about the

data.

#### A note on Parameters

Parameters in probability distributions are numerical values that determine the shape, location, and scale of the distribution.

Different probability distributions have different sets of parameters that determine their shape and characteristics, and understanding these parameters is essential in statistical analysis and inference.

# Session 3 - Descriptive Statistics Page 4 robability Distribution Functions

15 March 2023 20:08

A probability distribution function (PDF) is a mathematical function that describes the probability of obtaining different values of a random variable in a particular probability distribution.

Session 3 - Descriptive Statistics Page 5 Probability Mass Function (PMF)

15 March 2023 15:25

PMF stands for Probability Mass Function. It is a mathematical function that

describes the probability distribution of a discrete random variable.

The PMF of a discrete random variable assigns a probability to each possible value of the random variable. The probabilities assigned by the PMF must satisfy two conditions:

a.

The probability assigned to each value must be non-negative (i.e., greater than or equal to zero).

b. The sum of the probabilities assigned to all possible values must equal 1.

## **Examples**

https://en.wikipedia.org/wiki/Bernoulli\_distribution https://en.wikipedia.org/wiki/Binomial\_distribution Session 3 - Descriptive Statistics Page 6
Cumulative Distribution Function(CDF) of PMF

15 March 2023 20:09

The cumulative distribution function (CDF) F(x) describes the probability that a random variable X with a given probability distribution will be found at a value less than or equal to x

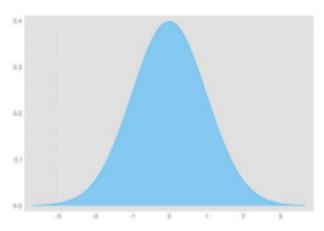
$$F(x) = P(X \le x)$$

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https://en.wikipedia.org/wiki/Bernoulli\_distribution

https://en.wikipedia.org/wiki/Binomial distribution

PDF stands for Probability Density Function. It is a mathematical function that describes the probability distribution of a **continuous** random variable.



- 1. Why Probability Density and why not Probability?
- 2. What does the area of this graph represents?
- 3. How to calculate Probability then?
- 4. Examples of PDF
  - a. <a href="https://en.wikipedia.org/wiki/Normal\_distribution">https://en.wikipedia.org/wiki/Normal\_distribution</a>
  - b. <a href="https://en.wikipedia.org/wiki/Log-normal\_distribution">https://en.wikipedia.org/wiki/Log-normal\_distribution</a>
  - c. <a href="https://en.wikipedia.org/wiki/Poisson\_distribution">https://en.wikipedia.org/wiki/Poisson\_distribution</a>
- 5. How is graph calculated?

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Density Estimation
16 March 2023 06:54

Density estimation is a statistical technique used to estimate the probability density function (PDF) of a random variable based on a set of observations or data. In simpler terms, it involves estimating the underlying distribution of a set of data points.

Density estimation can be used for a variety of purposes, such as **hypothesis testing**, **data analysis**, **and data visualization**. It is particularly useful in areas such as **machine learning**, where it is often used to estimate the probability distribution of input data or to model the likelihood of certain events or outcomes.

There are various methods for density estimation, including **parametric** and **non parametric** approaches. Parametric methods assume that the data follows a specific probability distribution (such as a normal distribution), while non parametric methods do not make any assumptions about the distribution and instead estimate it directly from the data.

Commonly used techniques for density estimation include **kernel density estimation** (KDE), histogram estimation, and Gaussian mixture models (GMMs). The choice of method depends on the specific characteristics of the data and the intended use of the density estimate.

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Parametric Density Estimation

16 March 2023 06:54

Parametric density estimation is a method of estimating the probability density function (PDF) of a random variable by assuming that the underlying distribution belongs to a specific parametric family of probability distributions, such as the normal, exponential, or Poisson distributions.

Session 3 - Descriptive Statistics Page 10 Non-Parametric Density Estimation (KDE)

16 March 2023 06:55

But sometimes the distribution is not clear or it's not one of the

famous distributions.

Non-parametric density estimation is a statistical technique used to estimate the probability density function of a random variable without making any assumptions about the underlying distribution. It is also referred to as non-parametric density estimation because it does not require the use of a predefined probability distribution function, as opposed to parametric methods such as the Gaussian distribution.

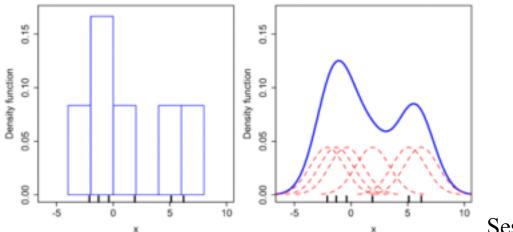
The non-parametric density estimation technique involves constructing an estimate of the probability density function using the available data. This is typically done by creating a **kernel density estimate** 

Non-parametric density estimation has several advantages over parametric density estimation. One of the main advantages is that it does not require the assumption of a specific distribution, which allows for more flexible and accurate estimation in situations where the underlying distribution is unknown or complex. However, non-parametric density estimation can be computationally intensive and may require more data to achieve accurate estimates compared to parametric methods.

Session 3 - Descriptive Statistics Page 11 Kernel Density Estimate(KDE)

16 March 2023 16:08

The KDE technique involves using a kernel function to smooth out the data and create a continuous estimate of the underlying density function.

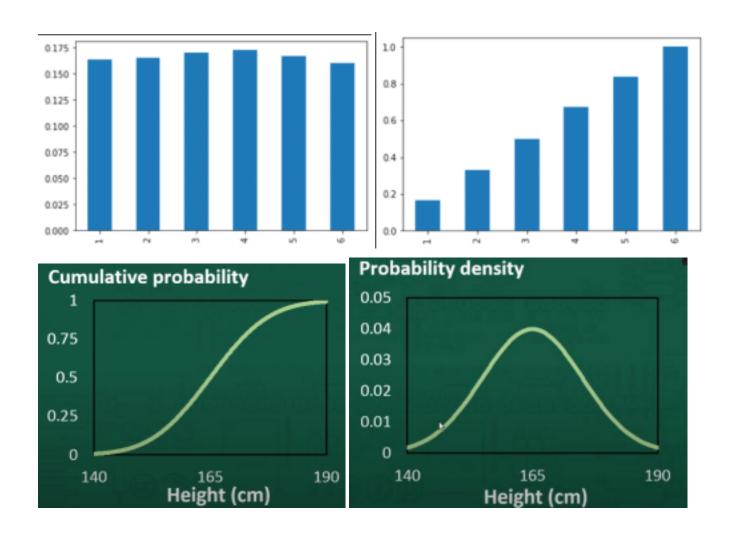


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## Cumulative Distribution Function(CDF) of PDF

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Session 3 - Descriptive Statistics Page 13 How to use PDF and CDF in Data Analysis

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