

Student ID:      -     

PHYS121 2005F

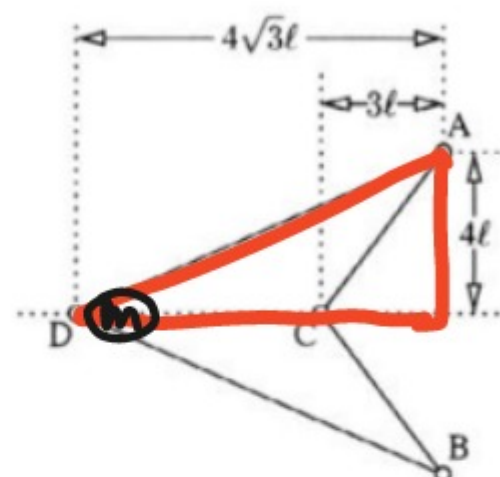
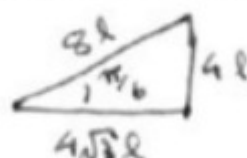
Test #2

17:00-19:00 Saturday 2005-11-12

Surname: O'Donovan

Given Name: \_\_\_\_\_

4. A light rubber band has an unstretched length  $10\ell$  and obeys Hooke's Law with a spring constant  $k$ . Its ends are connected, as shown, to a horizontal, frictionless desktop with pins at A and B a distance  $8\ell$  apart, forming a catapult. A small stone of mass  $m$  is placed at the middle of the rubber band and it is pulled back from the unstretched position C to the position D (both of which are on the desktop) where it is released.



- (2) (a) Use dimensional analysis to find an expression, to within a dimensionless multiplicative constant, for the speed,  $v_1$ , of the stone after it leaves the catapult. Your result should depend upon the given quantities,  $m$ ,  $k$  &  $\ell$ .
- $[v] = L T^{-1} \sim k^{1/2} \ell^{1/2} m^{-1/2}$
- (3) (b) Calculate the speed,  $v_1$ , of the stone after it leaves the catapult.
- (2) (c) The stone strikes a piece of putty of mass  $M$  balanced at the edge of the desk and becomes embedded in it. Calculate the speed of the compound object,  $v_2$ , after the collision.
- (2) (d) What is the speed,  $v_3$ , of the compound object when it lands on the ground if the height of the desk is  $h$ ?
- (1) (e) What is the  $M \rightarrow \infty$  limit of your answer to part (d)?