

# Ground Station Tracker Kinematics

$$S(\theta) = \begin{bmatrix} \cos\theta & 0 & -\sin\theta \\ 0 & 1 & 0 \\ \sin\theta & 0 & \cos\theta \end{bmatrix}$$

$$\begin{aligned} \theta_F &= \theta_R - \theta_D \\ \phi_F &= \phi_R - \phi_0 \end{aligned}$$

Feed Rocket Dish

$$S(\phi) = \begin{bmatrix} \cos\phi & \sin\phi & 0 \\ -\sin\phi & \cos\phi & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$R = \begin{bmatrix} \cos\theta \cos\phi & -\sin\phi & \sin\theta \cos\phi \\ \cos\theta \sin\phi & \cos\phi & \sin\theta \sin\phi \\ -\sin\theta & 0 & \cos\theta \end{bmatrix} = S(\theta)S(\phi)$$

$\phi, \theta \rightarrow$  given (to point @ rocket)

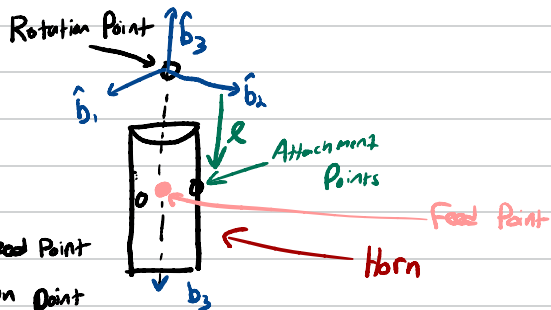
$$\{b'\} = R \{b\} \quad \text{where } b = \text{initial axes}$$

$b' = \text{after some rotation}$

$$\begin{aligned} \hat{b}_1 &= \hat{X} \\ \hat{b}_2 &= \hat{Y} \\ \hat{b}_3 &= \hat{Z} \end{aligned} \quad \left. \vphantom{\begin{aligned} \hat{b}_1 &= \hat{X} \\ \hat{b}_2 &= \hat{Y} \\ \hat{b}_3 &= \hat{Z} \end{aligned}} \right\} \text{Initially}$$

$$\beta = 120^\circ \rightarrow \text{angle between attachment points}$$

$r$  = radius of horn  
 $R$  = radius of pulley positions  
 $l$  = dist. from rotation point to Feed Point  
 $h$  = height difference from rotation point to pulley point



Tension Point  
(Attachment point)

$$\vec{T}_{A_0, b} = r \hat{b}_1 - l \hat{b}_3$$

$$\vec{T}_{B_0, b} = r \cos \beta \hat{b}_1 + r \sin \beta \hat{b}_2 - l \hat{b}_3$$

$$\vec{T}_{C_0, b} = r \cos 2\beta \hat{b}_1 + r \sin 2\beta \hat{b}_2 - l \hat{b}_3$$

Pulley Point

$$\vec{P}_A = R \underline{X} + h \underline{Z}$$

$$\vec{P}_B = R \cos \beta \underline{X} + R \sin \beta \underline{Y} + h \underline{Z}$$

$$\vec{P}_C = R \cos 2\beta \underline{X} + R \sin 2\beta \underline{Y} + h \underline{Z}$$

$$\vec{F}_{,b} = l \hat{b}_3 \quad \leftarrow \text{Feed Point}$$

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$$\vec{F}_{,I} = [R] \{F_{,b}\}$$

$$\vec{T}_{A,I} = [R] \{T_{A,b}\}$$

$$\vec{T}_{B,I} = [R] \{T_{B,b}\}$$

$$\vec{T}_{C,I} = [R] \{T_{C,b}\}$$

Rotation of motor 1, in rad

$$L_A = \|\vec{T}_{A,I} - \vec{P}_A\| \quad \rightarrow \quad M_1 = (L_{A_0} - L_A) \frac{1}{\pi D}$$

$$L_B = \|\vec{T}_{B,I} - \vec{P}_B\| \quad M_2 = (L_{B_0} - L_B) \frac{1}{\pi D}$$

$$L_C = \|\vec{T}_{C,I} - \vec{P}_C\| \quad M_3 = (L_{C_0} - L_C) \frac{1}{\pi D}$$