Jaypee Institute of Information Technology, Noida T2 Examination, Even Semester-2024 **B.Tech.-IV Semester**

Course Title: Probability and Random Processes

Course Code: 15B11MA301

Max. Time: 1 Hr. Max. Marks: 20

CO1	Rocall
CO ₂	Recall the concepts of probability theory and probability distributions Explain random and the probability distributions and reliability medians.
CO ₃	Explain random variables, probability distributions and reliability models Solve the problems are graing random variables, their distributions reliability
	Examine random process models and solve the related problems

Note: Attempt all the questions (Non programmable calculator will be allowed).

Q1. The number of industrial errors per working week in a particular factory is known to follow a Poisson distribution with mean 0.5.

Construct the probability that

(a) In a particular week, there will be

(i) less than 2 errors, (ii) more than 2 errors, and (iii) at most 2 errors,

(b) In three week period, there will be no errors.

[CO2 (Understanding), 4 marks]

Q2. The daily consumption of rice in a hostel in excess of 2000 Kg is following the Erlang distribution with parameters K = 2 and $\lambda = 1/1000$. The hostel has a daily stock of 3000 Kg rice. Make use of stated distribution, what is the probability that the stock is insufficient on a particular day?

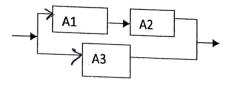
[CO3(Applying), 4 marks]

Q3. If marks obtained by the students in a course of probability theory are given to be distributed normally with mean marks 58 and standard deviation 8. A student gets a 'D' grade when marks obtained are between 34 and 42, and 'A' grade is awarded if marks are at least 72. If the class strength is 200, identify how many students obtained 'D' or 'A' grade? Also, find the probability that 3 out of 4 randomly selected students are A-graders. [CO3(Applying), 5 marks]

Q4. Each of the 6 tubes of a radio set has a life length (in years) which may be considered as a random variable that follows a Weibull distribution with scale and shape parameters 25 and 2 respectively. If these tubes function independently of one another, make use of stated distribution to find the probability that no tube will have to be replaced during the first 2 months of service.

[CO2(Applying), 4 marks]

Q5. Consider the system of 3- components A1, A2, and A3 as given in the following figure. The components A1 and A2 are supposed to be equally reliable and follows constant failure rate distribution with parameter 0.2. If the reliability of the system as calculated after a span of 10 weeks is 0.75, then identify the reliability of component A3. [CO3(Applying), 3 marks]



Note: Normal table is given at the back side of paper





Standard Normal (Z) Table Area between () and z



	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0		0.0040	0.0080	0.0120	0.0160	0.0199	0.0239	0.0279	0.0319	0.0359
0.1	0.0398	0.0438	0.0478	0.0517		0.0596	0.0636	0.0675	0.0714	
0.2	0.0793	0.0832	0.0871	0.0910		0.0987	0.1026	0.1064	0.1103	
0.3	0.1179	0.1217	0.1255	0.1293	0.1331	0.1368	0.1406	0.1443	0.1480	
0.4	0.1554	0.1591	0.1628	0.1664	0.1700	0.1736	0.1772	0.1808	0.1844	0.1879
0.5	0.1915	0.1950	0.1985	0.2019	0.2054	0.2088	0.2123	0.2157	0.2190	0.2224
0.6	0.2257	0.2291	0.2324	0.2357	0.2389	0.2422	0.2454	0.2486	0.2517	0.2549
0.7	0.2580	0.2611	0.2642	0.2673	0.2704	0.2734	0.2764	0.2794	0.2823	0.2852
0.8	0.2881	0.2910	0.2939	0.2967	0.2995	0.3023	0.3051	0.3078	0.3106	0.3133
0.9	0.3159	0.3186	0.3212	0.3238	0.3264	0.3289	0.3315	0.3340	0.3365	0.3389
1.0	0.3413	0.3438	0.3461	0.3485	0.3508	0.3531	0.3554	0.3577	0.3599	0.3621
1.1	0.3643	0.3665	0.3686	0.3708	0.3729	0.3749	0.3770	0.3790	0.3810	0.3830
1.2	0.3849	0.3869	0.3888	0.3907	0.3925	0.3944	0.3962	0.3980	0.3997	0.4015
1.3	0.4032	0.4049	0.4066	0.4082	0.4099	0.4115	0.4131	0.4147	0.4162	0.4177
1.4	0.4192	0.4207	0.4222	0.4236	0.4251	0.4265	0.4279	0.4292	0.4306	0.4319
1.5	0.4332	0.4345	0.4357	0.4370	0.4382	0.4394	0.4406	0.4418	0.4429	0.4441
1.6	0.4452	0.4463	0.4474	0.4484	0.4495	0.4505	0.4515	0.4525	0.4535	0.4545
1.7	0.4554	0.4564	0.4573	0.4582	0.4591	0.4599	0.4608	0.4616	0.4625	0.4633
1.8	0.4641	0.4649	0.4656	0.4664	0.4671	0.4678	0.4686	0.4693	0.4699	0.4706
1.9	0.4713	0.4719	0.4726	0.4732	0.4738	0.4744	0.4750	0.4756	0.4761	0.4767
2.0	0.4772	0.4778	0.4783	0.4788	0.4793	0.4798	0.4803	0.4808	0.4812	0.4817
2.1	0.4821	0.4826	0.4830	0.4834	0.4838	0.4842	0.4846	0.4850	0.4854	0.4857
2.2	0.4861	0.4864	0.4868	0.4871	0.4875	0.4878	0.4881	0.4884	0.4887	0.4890
2.3	0.4893	0.4896	0.4898	0.4901	0.4904	0.4906	0.4909	0.4911	0.4913	0.4916
2.4	0.4918	0.4920	0.4922	0.4925	0.4927	0.4929	0.4931	0.4932	0.4934	0.4936
2.5	0.4938	0.4940	0.4941	0.4943	0.4945	0.4946	0.4948	0.4949	0.4951	0.4952
2.6	0.4953	0.4955	0.4956	0.4957	0.4959	0.4960	0.4961	0.4962	0.4963	0.4964
2.7	0.4965	0.4966	0.4967	0.4968	0.4969	0.4970	0.4971	0.4972	0.4973	0.4974
2.8	0.4974	0.4975	0.4976	0.4977	0.4977	0.4978	0.4979	0.4979	0.4980	0.4981
2.9	0.4981	0.4982	0.4982	0.4983	0.4984	0.4984	0.4985	0.4985	0.4986	0.4986
3.0	0.4987	0.4987	0.4987	0.4988	0.4988	0.4989	0.4989	0.4989	0.4990	0.4990
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