

## Exercise 06 - Select Algorithm

The `Select()` algorithm finds the  $i$ th smallest element in a collection in linear time. It consists of five steps:

1. Divide the collection into consecutive groups of five (last group may contain fewer than 5 elements).
2. Find the median of each group (sorting may be required).
3. Recursively apply `Select()` to the list of medians to find the pivot, the median of medians.
4. Partition over the pivot and find  $k$ , the count of elements less than the pivot.
5. Compare the  $i$  (desired position) and  $k$ . If  $i = k$ , return the pivot; otherwise, if  $i < k$ , perform `Select()` on the lesser partition; otherwise, perform `Select()` on the upper partition with  $i = i - k$ .

However, if the collection contains only a single element, the `Select()` algorithm simply returns that element.

Create a header file named ‘`exercises06.h`’ that defines the `Select()` algorithm with the following parts and uses a vector as the array.

1. Define an integer function `Mid()` that accepts an array and two integer indices  $low$  and  $high$  (with  $low \leq high$ ) and returns the index of the median of the subarray  $A[low\dots high]$ . If the subarray length exceeds 5, it returns -1.
2. Define a vector function `Medians()` that takes an array parameter and returns an array of the medians of consecutive groups of five elements of the array.
3. Define the integer function `Partition()` that takes an array, two integer indices  $low$  and  $high$  (with  $low \leq high$ ), and a pivot value, and partitions the array around the pivot, returning the count of the lower partition.
4. Define the `Select()` function using the previous functions and its description.