

Exercise 06 - Select Algorithm

The **Select()** algorithm finds the i th smallest element in a collection in linear time. It consists of five steps:

1. Divide the collection into consecutive groups of five (last group may contain fewer than 5 elements).
2. Find the median of each group (sorting may be required).
3. Recursively apply **Select()** to the list of medians to find the pivot, the median of medians.
4. Partition over the pivot and find k , the count of elements less than the pivot.
5. Compare the i (desired position) and k . If $i = k$, return the pivot; otherwise, if $i > k$, perform **Select()** on the lesser partition; otherwise, perform **Select()** on the upper partition with $i = i - k$.

However, if the collection contains only a single element, the **Select()** algorithm simply returns that element.

Create a header file named '**exercises06.h**' that defines the **Select()** algorithm with the following parts and uses a vector as the array.

1. Define an integer function **Mid()** that accepts an array and two integer indices low and $high$ (with $low \leq high$) and returns the index of the median of the subarray $A[low \dots high]$. If the subarray length exceeds 5, it returns -1.
2. Define a vector function **Medians()** that takes an array parameter and returns an array of the medians of consecutive groups of five elements of the array.
3. Define the integer function **Partition()** that takes an array, two integer indices low and $high$ (with $low \leq high$), and a pivot value, and partitions the array around the pivot, returning the count of the lower partition.
4. Define the **Select()** function using the previous functions and its description.