

ClassWork 7:

1. $T(n) = 8 * T(n / 2) + n$

$\log_2(8) = 3$ & $d = 1$, decomposition dominant $\implies \Theta(n^3)$

2. $T(n) = 6 * T(n / 3) + n^2$

$\log_3(6) < 2$ & $d = 2$ recombination dominant $\implies \Theta(n^2)$

3. $T(n) = 3 * T(n / 4) + n^3$

$\log_4(3) < 2$ & $d = 3$ recombination dominant $\implies \Theta(n^3)$

4. $T(n) = 0.5 * T(n / 2) + n$

$a < 1$ we cannot apply master theorem

5. $T(n) = 4 * T(n / 4) + \sqrt{n}$

$\log_4(4) = 1$ & $d = 1/2$ decomposition dominant $\implies \Theta(n)$

6. $T(n) = T(n) + n/2$

$b = 1$ we cannot apply master theorem

7. $T(n) = 5 * T(n / 5) + n/5$

$\log_5(5) = 1$ & $d = 1$ neutral $\implies \Theta(n \log n)$

8. $T(n) = 3 * T(n / 4) + n^{0.9}$

$\log_4(3) < 0.9$ & $d = 0.9$ recombination dominant $\implies \Theta(n^{0.9})$

9. $T(n) = 64 * T(n / 4) + n^3$

$\log_4(64) = 3$ & $d = 3 \implies \Theta(n^3 \log n)$

10. $T(n) = 64 * T(n / 8) + n^n$

$d = n$ asymptotically will always be larger (recomposition) $\implies O(n^n)$