Convolutional Neural Networks

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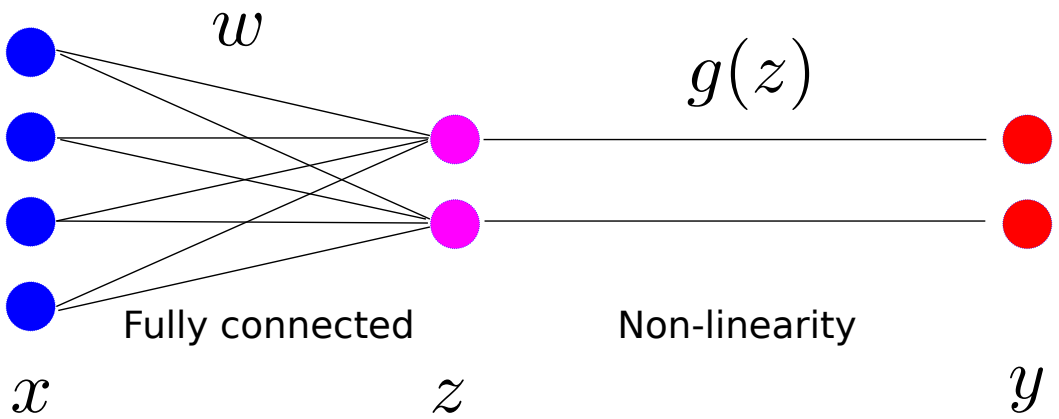
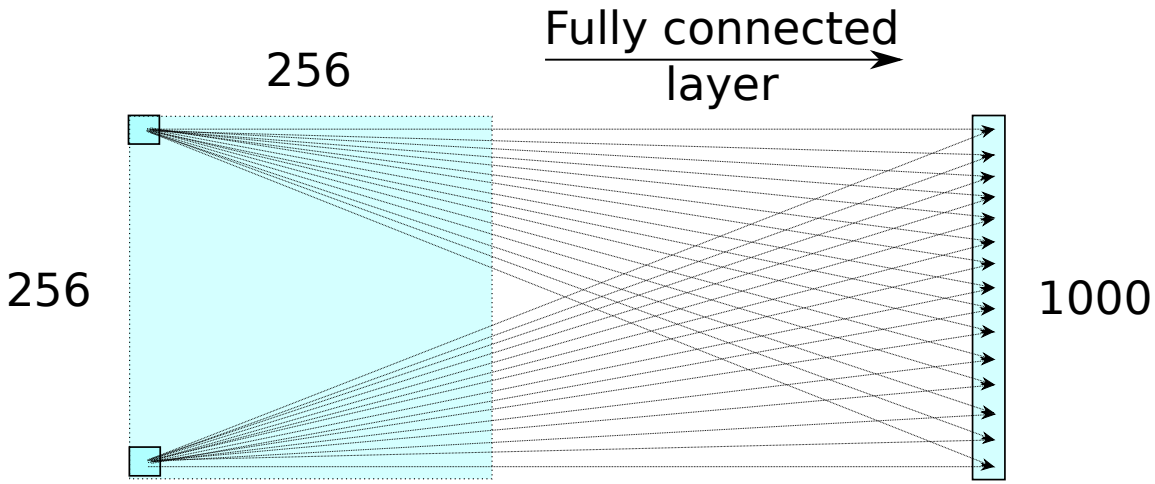
Introduction

- Neural networks provide a highly flexible way to model complex dependencies and patterns in data
- In the previous lessons, we saw the following elements :
  - MLPs : fully connected layers, biases
  - Activation functions : sigmoid, soft max, ReLU
  - Optimisation : gradient descent, stochastic gradient descent
  - Regularisation : weight decay, dropout, batch normalisation
  - RNNs : for sequential data



Introduction

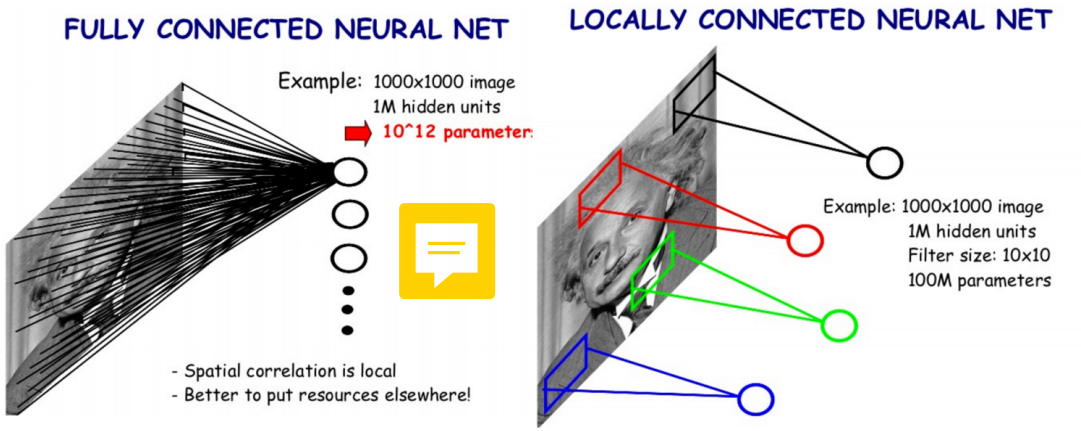
- In MLPs each layer of the network contained **fully connected** layers
- Unfortunately, there are great drawbacks with such an approach



- Each hidden unit is connected to each input unit;
- There is high redundancy in these weights :
  - In the above example, 65 million weights are required

Introduction

- For many types of data with **grid-like topological structures** (eg. images), it is not necessary to have so many weights
- For these data, the **convolution** operation is often extremely useful
- Reduces the number of parameters to train
  - Training is faster
  - Convergence is easier : smaller parameter space



- A neural network with convolution operations is known as a **Convolutional Neural Network** (CNN)

Introduction - some history

- "Neocognitron" of Fukushima* : first to incorporate notion of receptive field into a neural network, based on work on animal perception of Hubert and Weisel†
- Yann LeCun first to propose **back-propagation** for training convolutional neural networks‡
  - Automatic learning of parameters instead of hand-crafted weights
  - However, training was very long : required 3 days (in 1990)

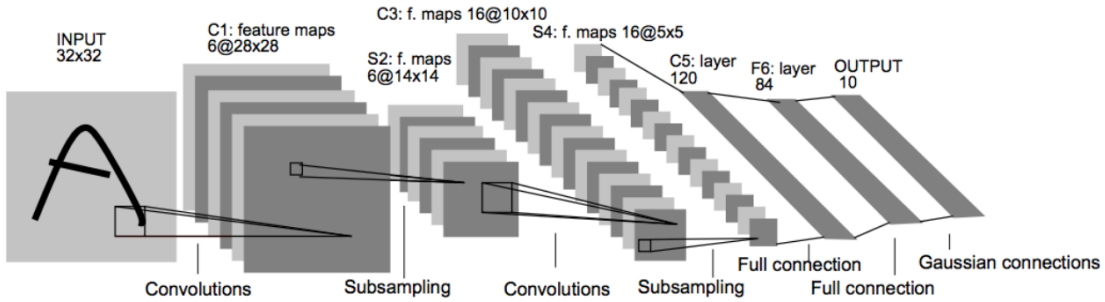


Fig. 2. Architecture of LeNet-5, a Convolutional Neural Network, here for digits recognition. Each plane is a feature map, i.e. a set of units whose weights are constrained to be identical.

* ***Neocognitron: A Self-organizing Neural Network Model for a Mechanism of Pattern Recognition Unaffected by Shift in Position***, *Fukushima, K., Biological Cybernetics, 1980*

† ***Receptive fields and functional architecture of monkey striate cortex***, *Hubel, D. H. and Wiesel, T. N, 1968*

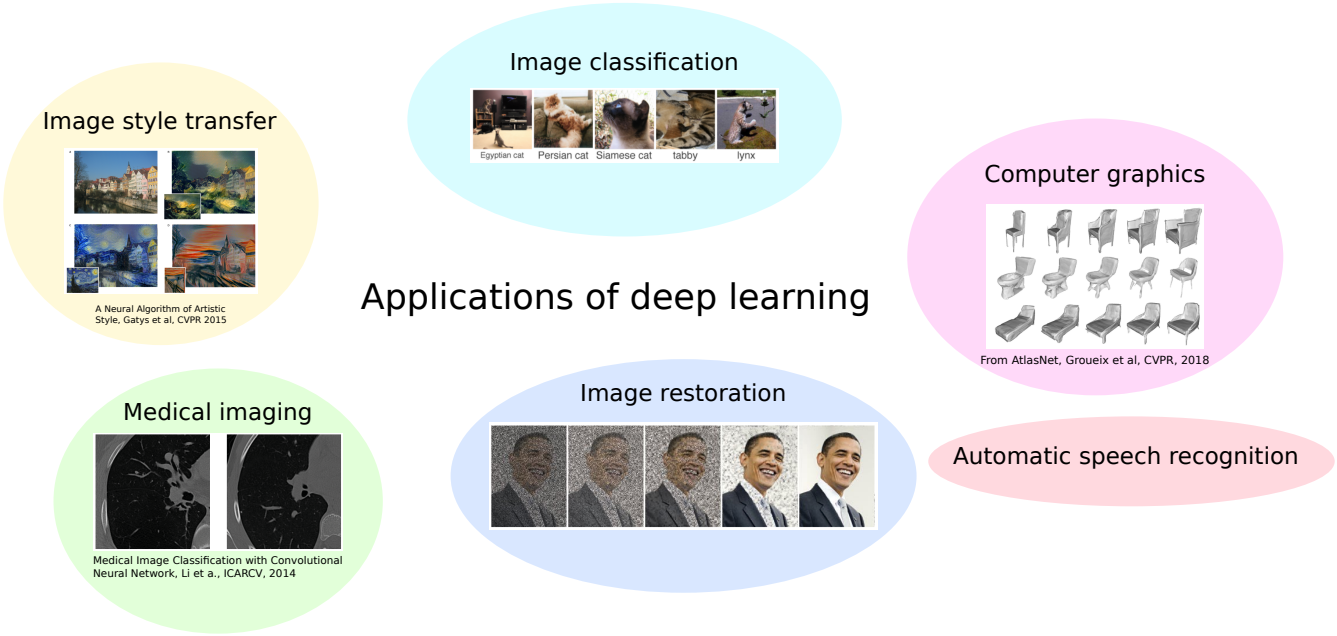
‡ ***Backpropagation Applied to Handwritten Zip Code Recognition***, *LeCun, Y. et al., AT&T Bell Laboratories*

Introduction - some history

- In the years 1998-2012, research continued on shallow and deep neural networks, but other machine learning approaches were preferred (GMMs, SVMs etc.)
- In 2012, Alex Krizhevsky et al. used **Graphics Processing Units** (GPUs) to carry out backpropagation on a very deep convolutional neural network
  - Greatly outperformed classic approaches in the ImageNet Large Scale Visual Recognition Challenge (ILSVRC)
- GPUs turned out to be very efficient for training neural nets (lots of parallel computations)
- Signalled the beginning of deep learning revolution

Introduction - some history

- In the past six years, CNNs have completely revolutionised many domains
- CNNs produce competetive/best results for most problems in image processing and computer vision



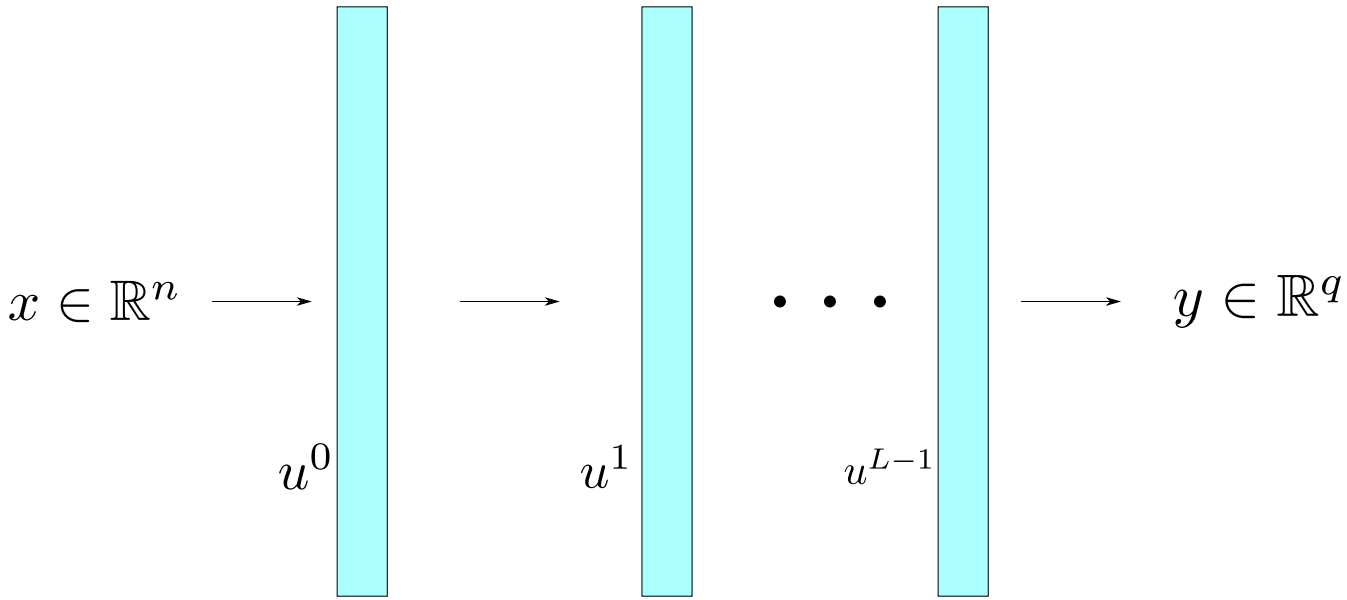
- Being applied to an ever-increasing number of problems

Summary

Introduction - some notation

Notations

- $x \in \mathbb{R}^n$: input vector
- $y \in \mathbb{R}^q$: output vector
- u_ℓ : feature vector at layer ℓ
- θ_ℓ : network parameters at layer ℓ



Neural network with L layers

Introduction

- A "**Convolutional Neural Network**" (CNN) is simply a concatenation of :
  1. Convolutions (filters)
  2. Additive biases
  3. Down-sampling ("Max-Pooling" etc.)
  4. Non-linearities

- In this lesson, we will be mainly concentrating on **convolutional** and **down-sampling** layers

Summary

Convolutional Layers

Convolution operator

Let f and g be two integrable functions. The **convolution operator** $*$ takes as its input two such functions, and outputs another function $h = f * g$, which is defined at any point $t \in \mathbb{R}$ as :

$$h(t) = (f * g)(t) = \int_{-\infty}^{+\infty} f(\tau) g(t - \tau) d\tau.$$

- Intuitively, the function h is defined as the inner product between f and a *shifted* version of g

Convolutional Layers

- In many practical applications, in particular for CNNs, we use the **discrete convolution** operator, which acts on discretised functions;

Discrete convolution operator

Let f_n and g_n be two summable series, with $n \in \mathcal{N}$. The discrete convolution operator is defined as :

$$(f * g)(n) = \sum_{i=-\infty}^{+\infty} f(i)g(n-i)$$

- Intuitively, the function h is defined as the inner product between f and a *shifted* version of w
- In practice, the filter is of small spatial support, around 3×3, or 5×5
- Therefore, only a **small number** of parameters need to be trained (9 or 25 for these filters)

Properties of convolution

1. Associativity : $(f * g) * h = f * (g * h)$
2. Commutativity : $f * g = g * f$
3. Bilinearity : $(\alpha f) * (\beta g) = \alpha\beta(f * g)$, for $(\alpha, \beta) \in \mathbb{R} \times \mathbb{R}$
4. Equivariance to translation : $(f * (g + \tau))(t) = (f * g)(t + \tau)$

Convolutional Layers

Associativity, commutativity

- Associativity+commutativity implies that we can carry out convolution in any order
- There is no point in having two or more consecutive convolutions
  - This is true in fact for any linear map

Equivariance to translation

- Equivariance implies that the convolution of any shifted input $(f + \tau) * g$ contains the **same information** as $f * g$ [†]
- This is useful, since we want to detect objects **anywhere in the image**

[†] if we forget about border conditions for a moment

Convolutional Layers - 2D Convolution

- Most often, we are going to be working with **images**
- Therefore, we require a 2D convolution operator : this is defined in a very similar manner to 1D convolution :

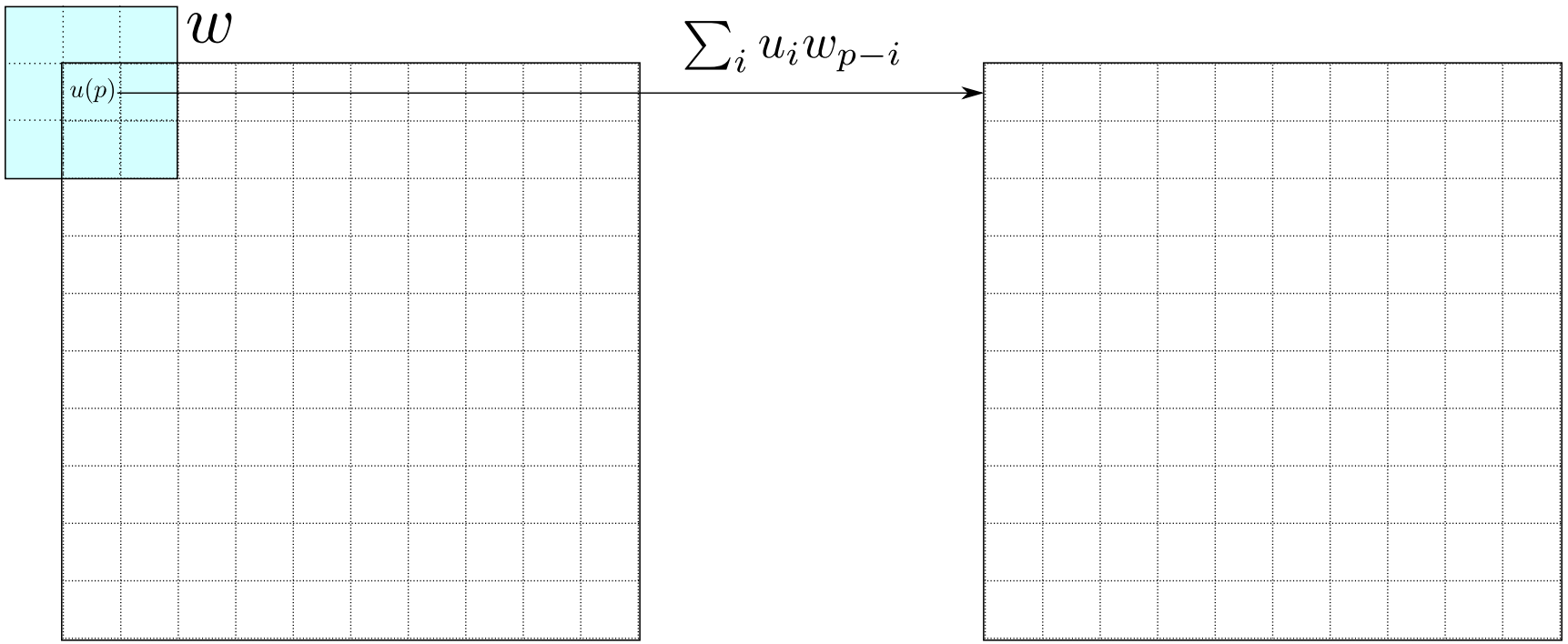
2D convolution operator

$$(f * g)(s,t) = \sum_{i=-\infty}^{+\infty} \sum_{j=-\infty}^{+\infty} f(i,j)g(s-i,t-j)$$

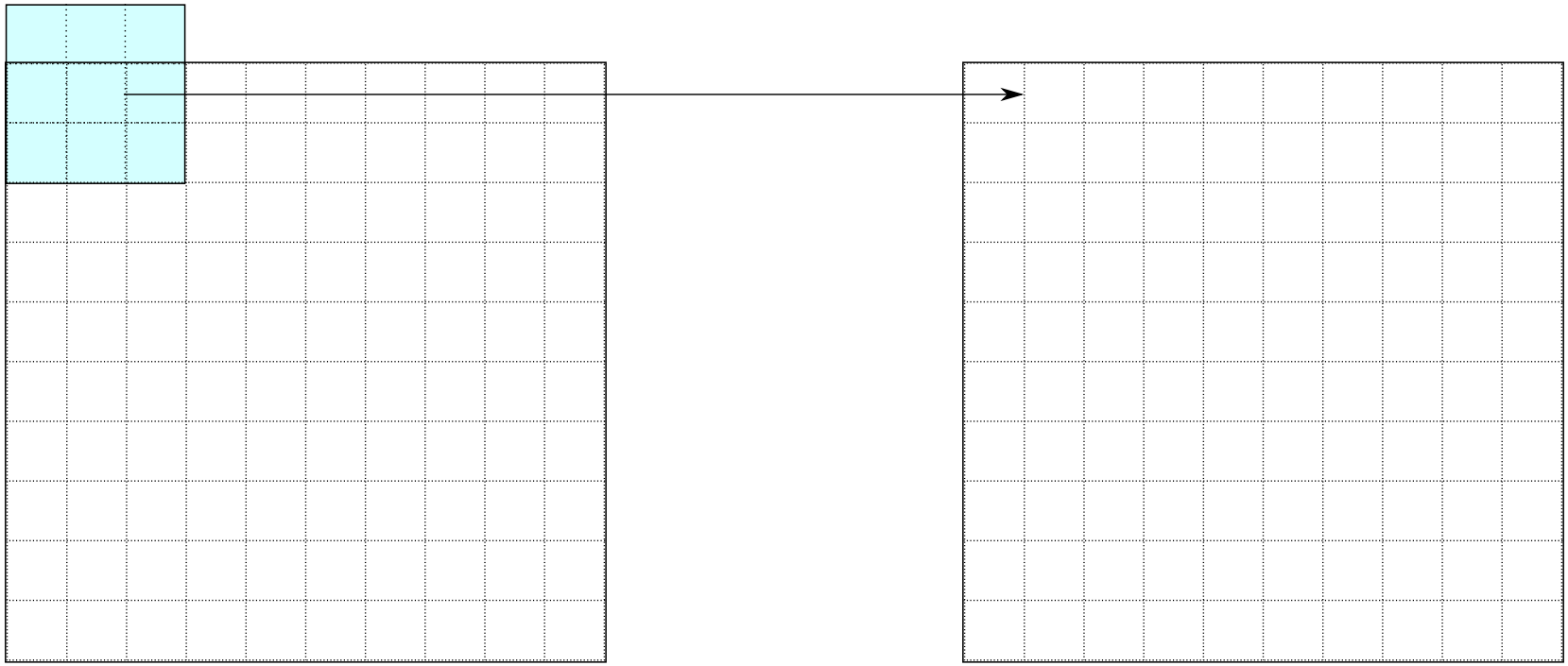
Important remarks for the rest of the lesson!

- We are going to denote the **filters with** w
- For lighter notation, we write $w(i) =: w_i$ (and the same for x_i etc.)

Convolutional Layers : Visual Illustration

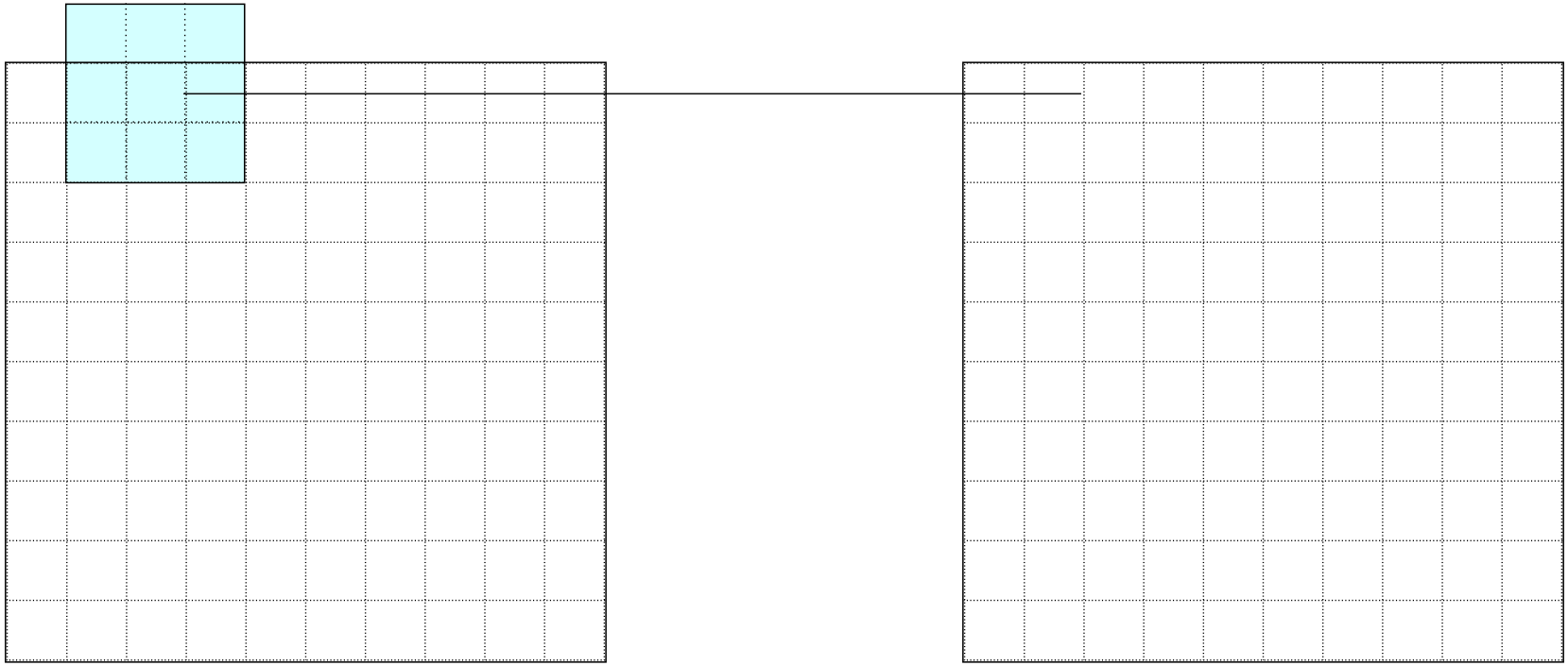


Convolutional Layers : Visual Illustration



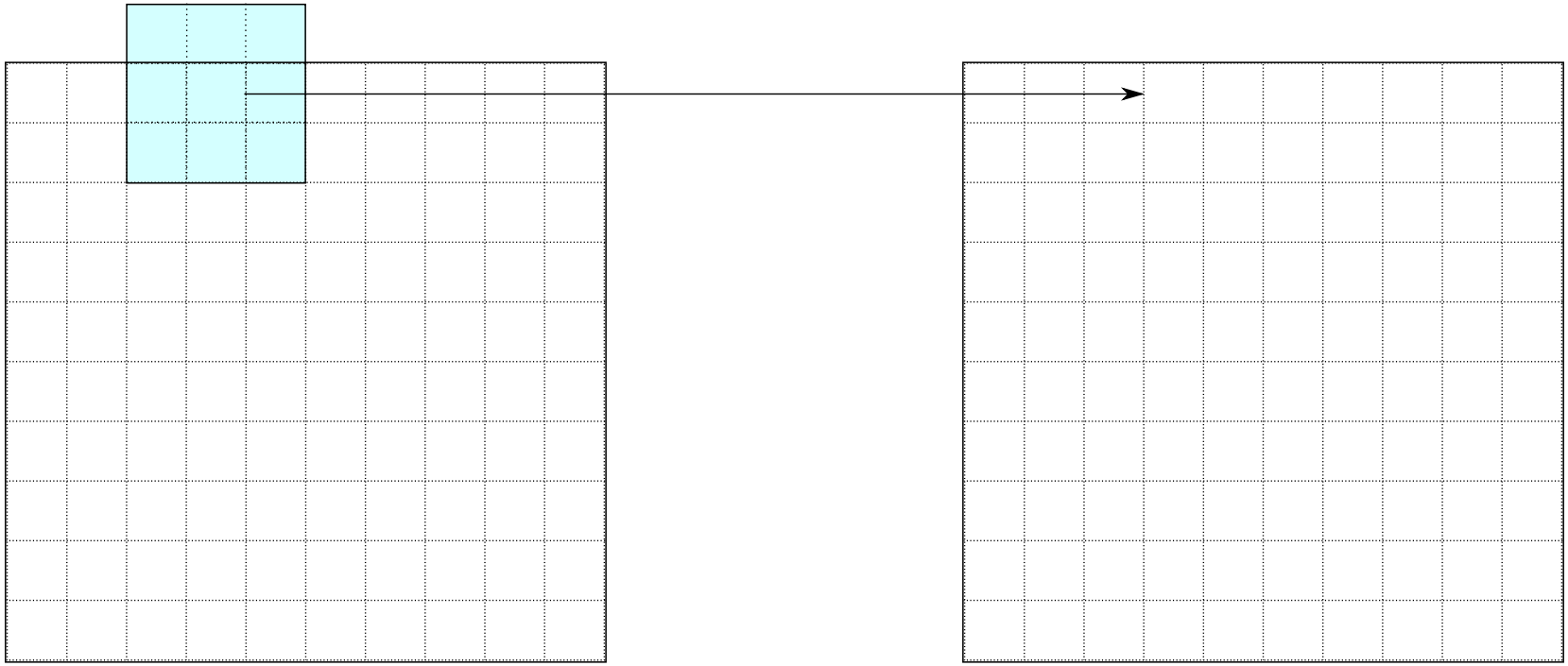
u $u * w$

Convolutional Layers : Visual Illustration



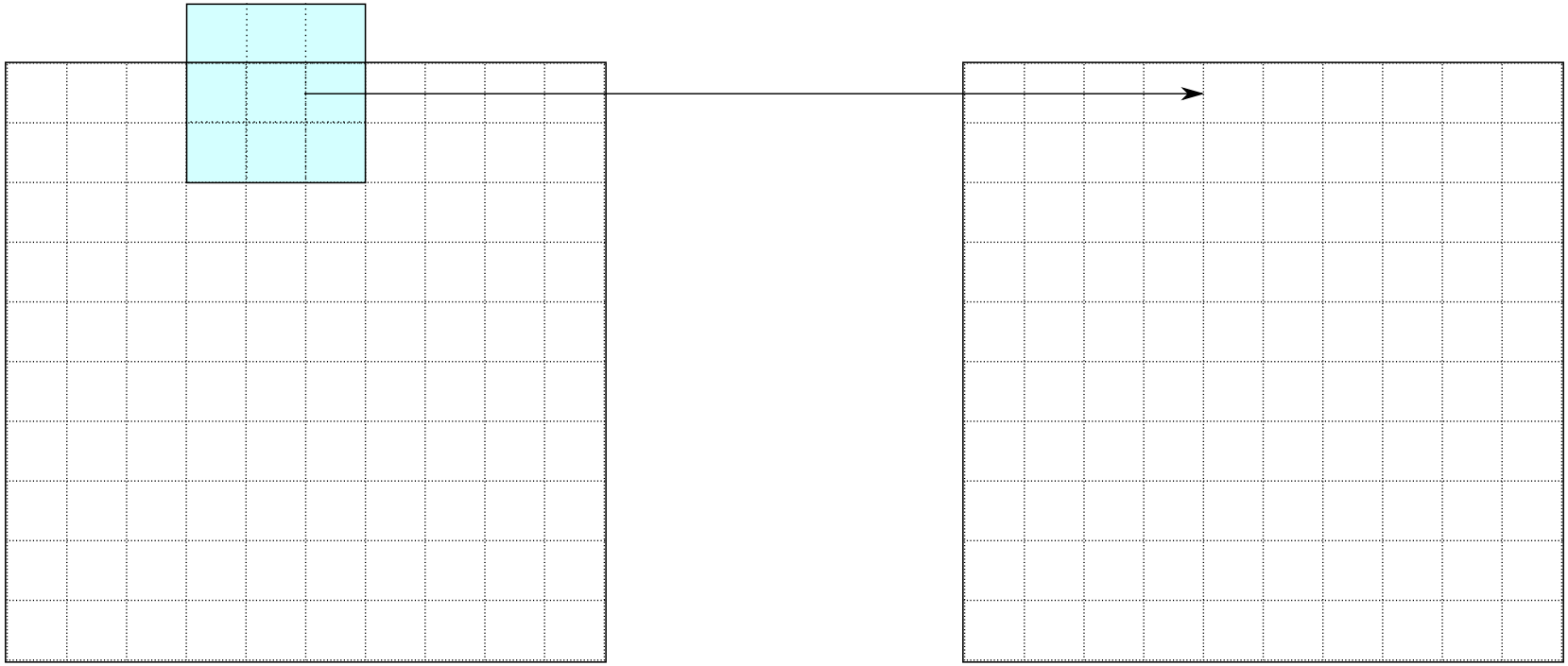
u $u * w$

Convolutional Layers : Visual Illustration



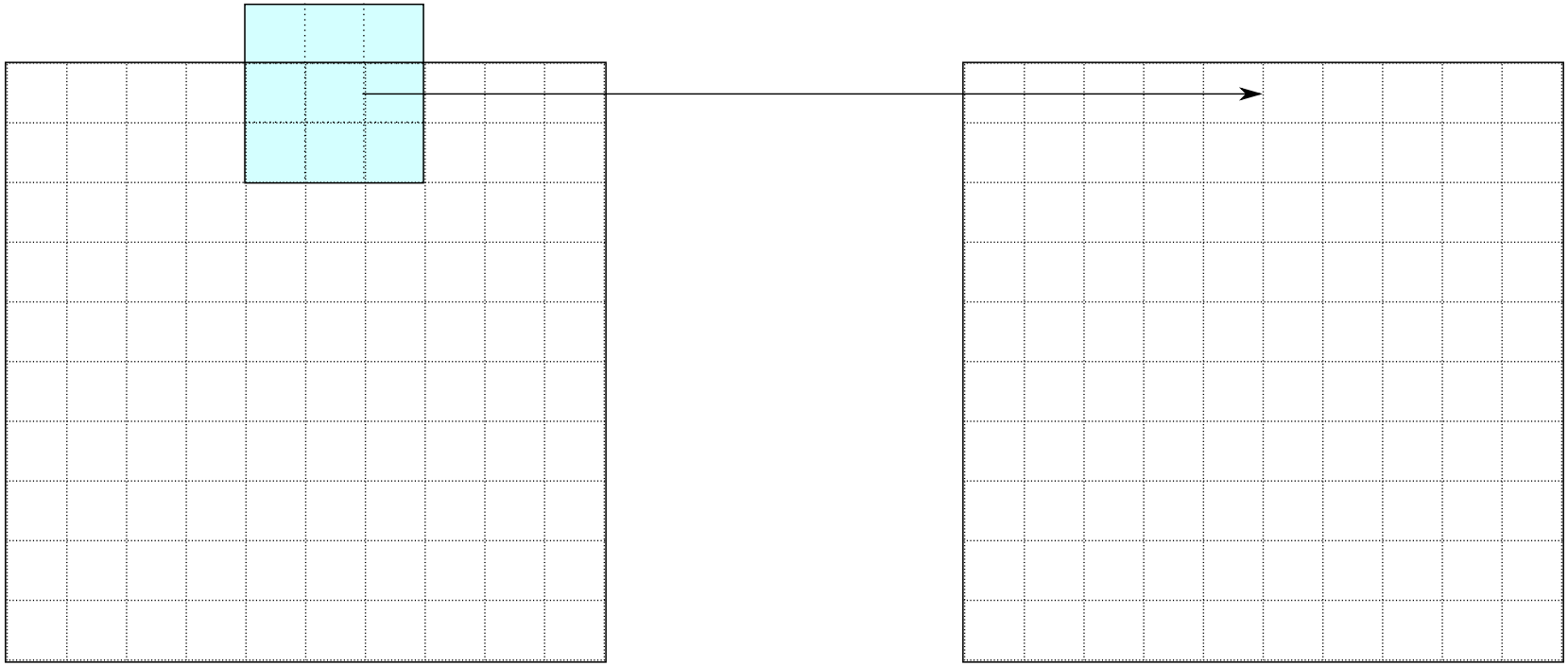
u $u * w$

Convolutional Layers : Visual Illustration



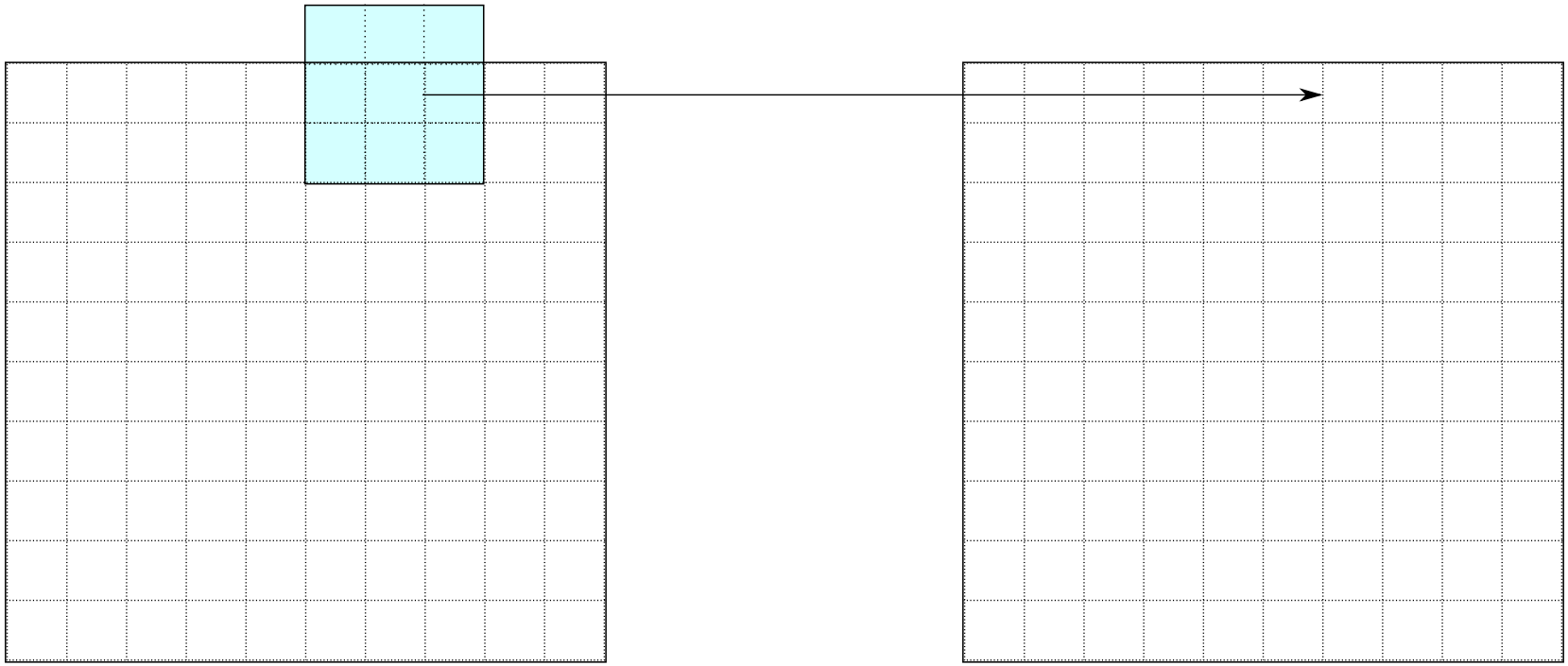
u $u * w$

Convolutional Layers : Visual Illustration



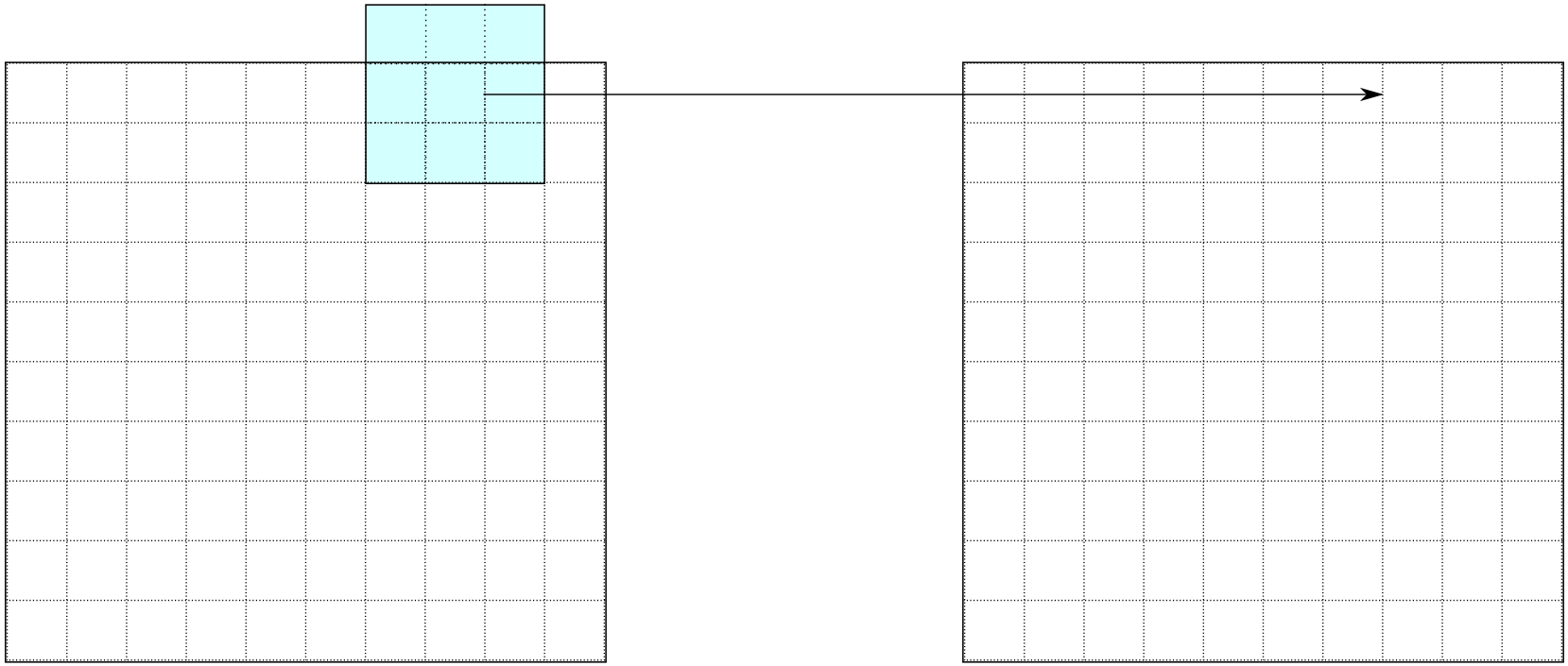
u $u * w$

Convolutional Layers : Visual Illustration



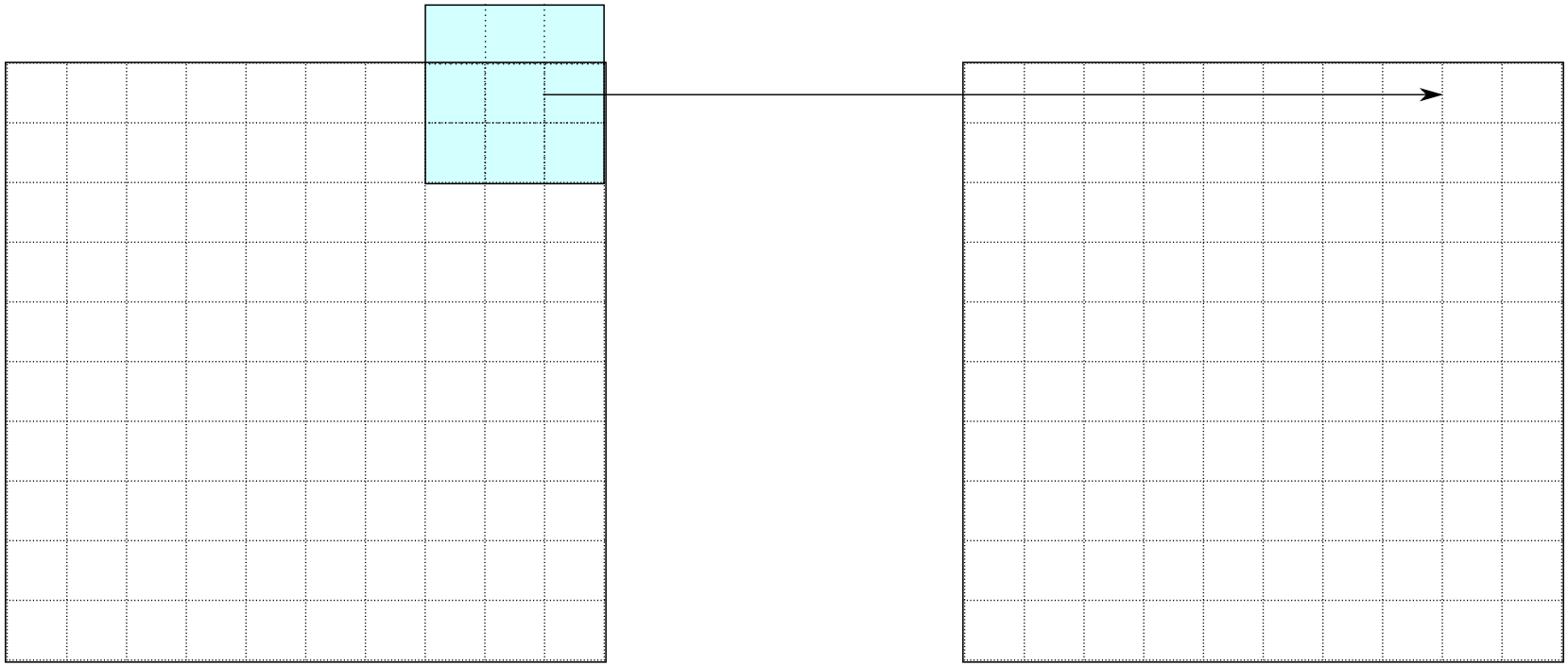
u $u * w$

Convolutional Layers : Visual Illustration



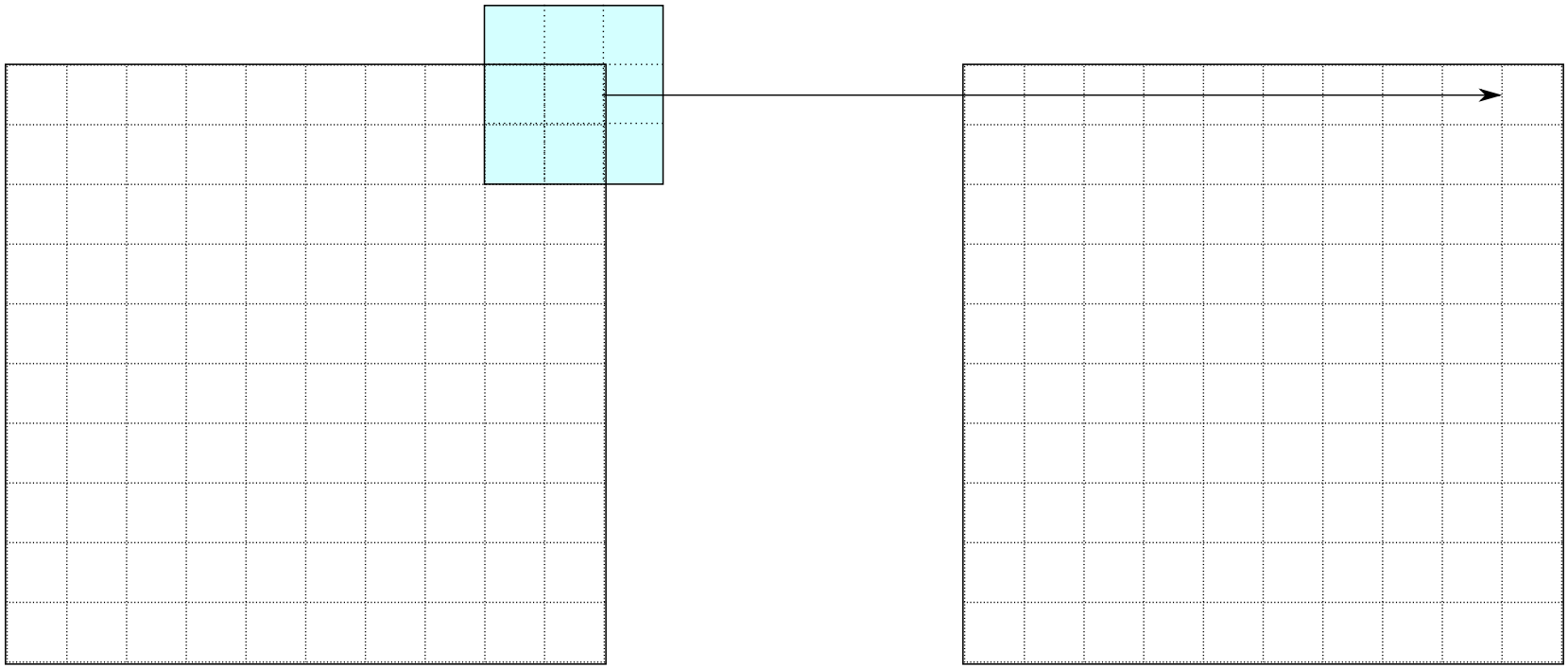
u $u * w$

Convolutional Layers : Visual Illustration



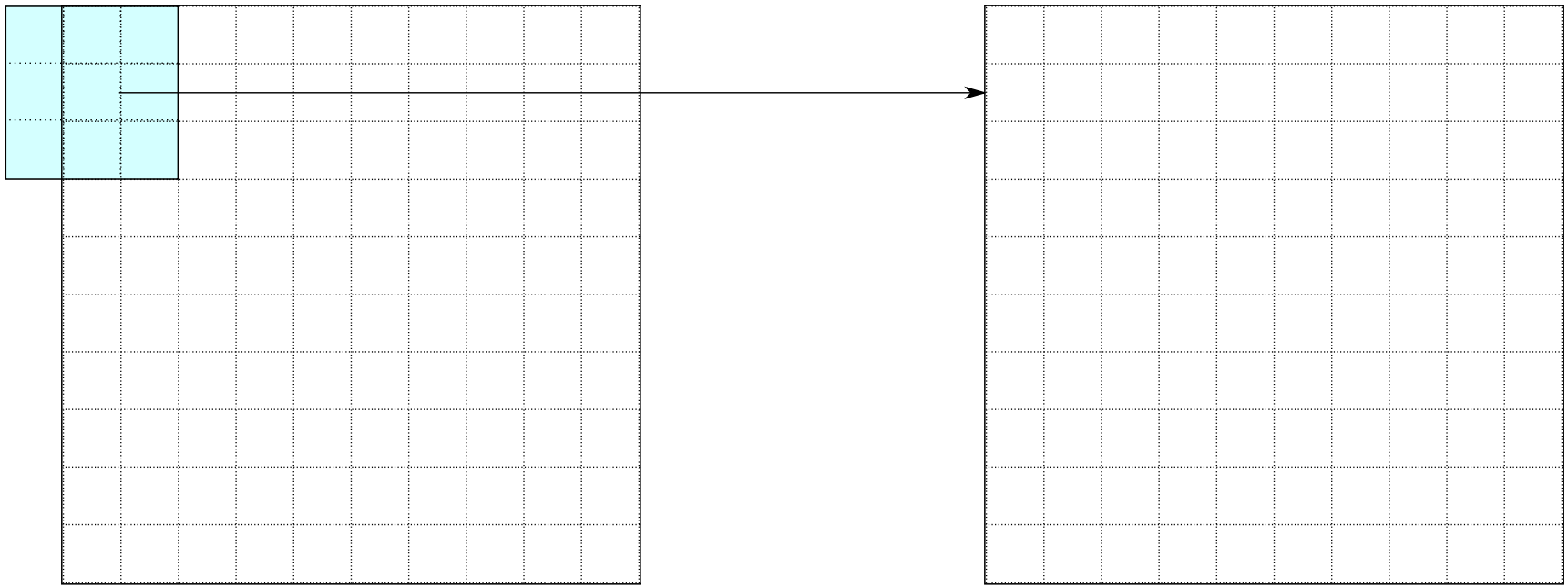
u $u * w$

Convolutional Layers : Visual Illustration



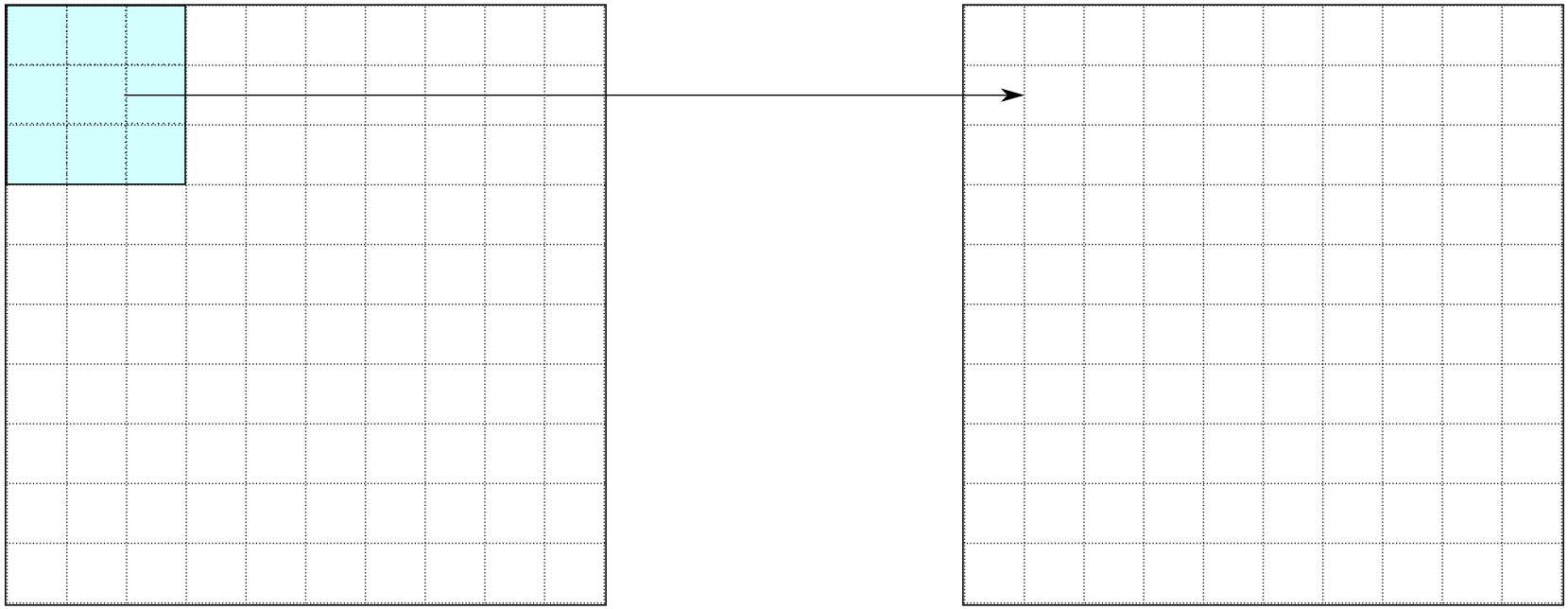
u $u * w$

Convolutional Layers : Visual Illustration



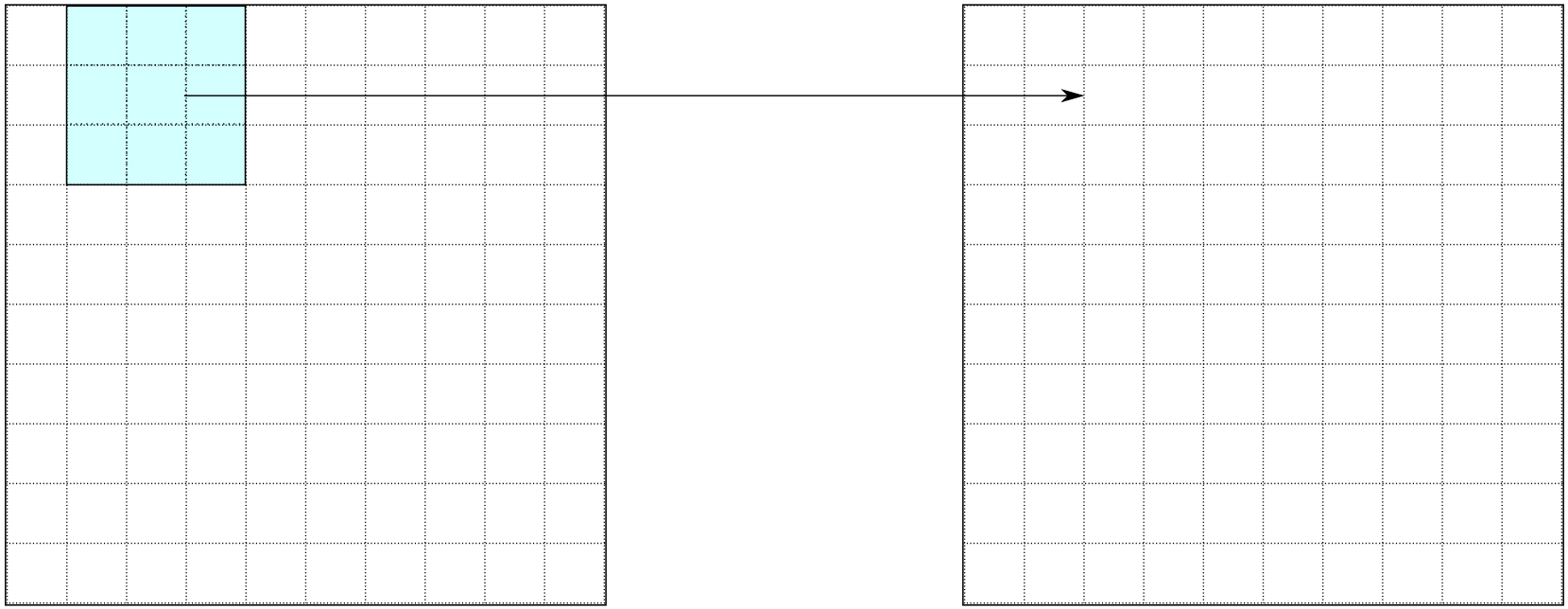
u $u * w$

Convolutional Layers : Visual Illustration



u $u * w$

Convolutional Layers : Visual Illustration



u $u * w$

Convolutional Layers

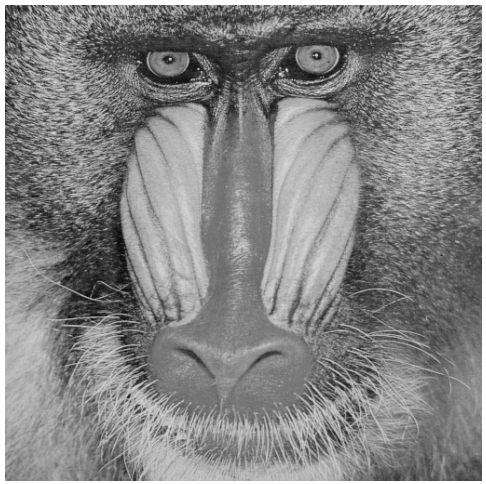
- The filter weights w_i determine what type of "feature" can be detected by convolutional layers;
- Example, sobel filters :

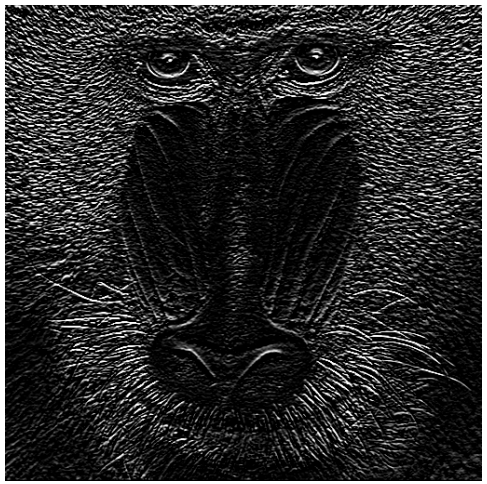
Horizontal edge

$$\begin{bmatrix} 1 & 2 & 1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{bmatrix}$$

Vertical edge

$$\begin{bmatrix} 1 & 0 & -1 \\ 2 & 0 & -2 \\ 1 & 0 & -1 \end{bmatrix}$$





Convolutional Layers

- We can also write convolution as a matrix/vector product, as in the case of fully connected layers

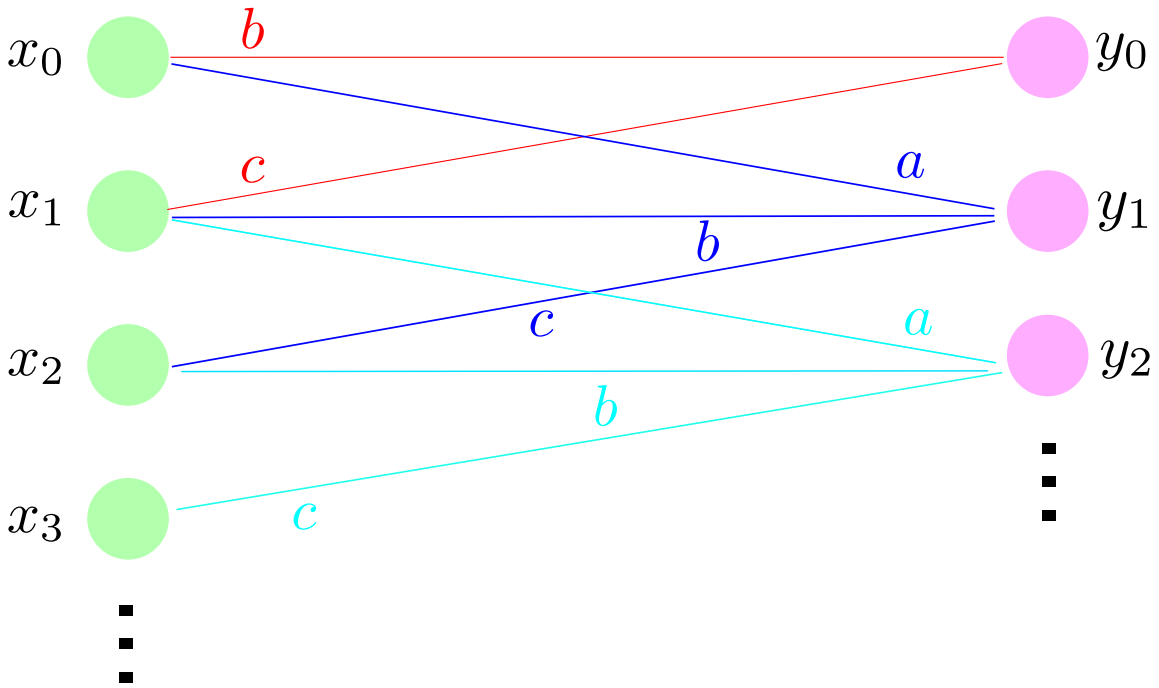
Example : discrete Laplacian operator

$$w = \begin{pmatrix} 0 & -1 & 0 \\ -1 & 4 & -1 \\ 0 & -1 & 0 \end{pmatrix} \rightarrow A_w = \begin{array}{c} \\ \\ \\ \\ \downarrow \\ \kappa \end{array} \overbrace{\hphantom{\begin{pmatrix} 4 & -1 & \overset{0}{\cdots} & -1 & \overset{0}{\cdots} & & \\ -1 & 4 & -1 & \overset{0}{\cdots} & -1 & \overset{0}{\cdots} & \\ 0 & -1 & 4 & -1 & \overset{0}{\cdots} & -1 & \overset{0}{\cdots} \\ \ddots & \ddots & \ddots & \ddots & \ddots & \ddots & \\ & & \overset{0}{\cdots} & -1 & \overset{0}{\cdots} & -1 & 4 \end{pmatrix}}}^{n} \begin{pmatrix} 4 & -1 & \overset{0}{\cdots} & -1 & \overset{0}{\cdots} & & \\ -1 & 4 & -1 & \overset{0}{\cdots} & -1 & \overset{0}{\cdots} & \\ 0 & -1 & 4 & -1 & \overset{0}{\cdots} & -1 & \overset{0}{\cdots} \\ \ddots & \ddots & \ddots & \ddots & \ddots & \ddots & \\ & & \overset{0}{\cdots} & -1 & \overset{0}{\cdots} & -1 & 4 \end{pmatrix}$$

- This further illustrates the drastic reduction in weight parameters (9 instead of Kn)

Convolutional Layers

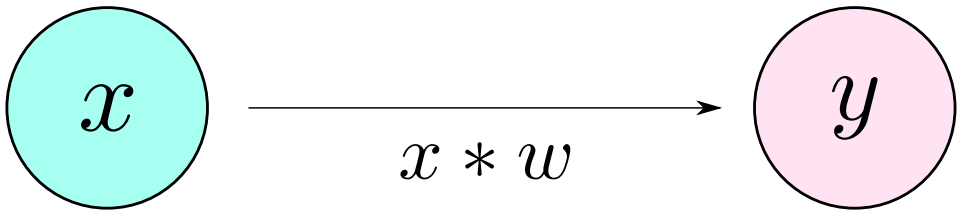
- At this point, it is good to have a more "neural network"-based illustration of CNNs



- We can see two of the main justifications for CNNs
  1. Sparse connectivity
  2. Weight sharing

Convolutional Layers

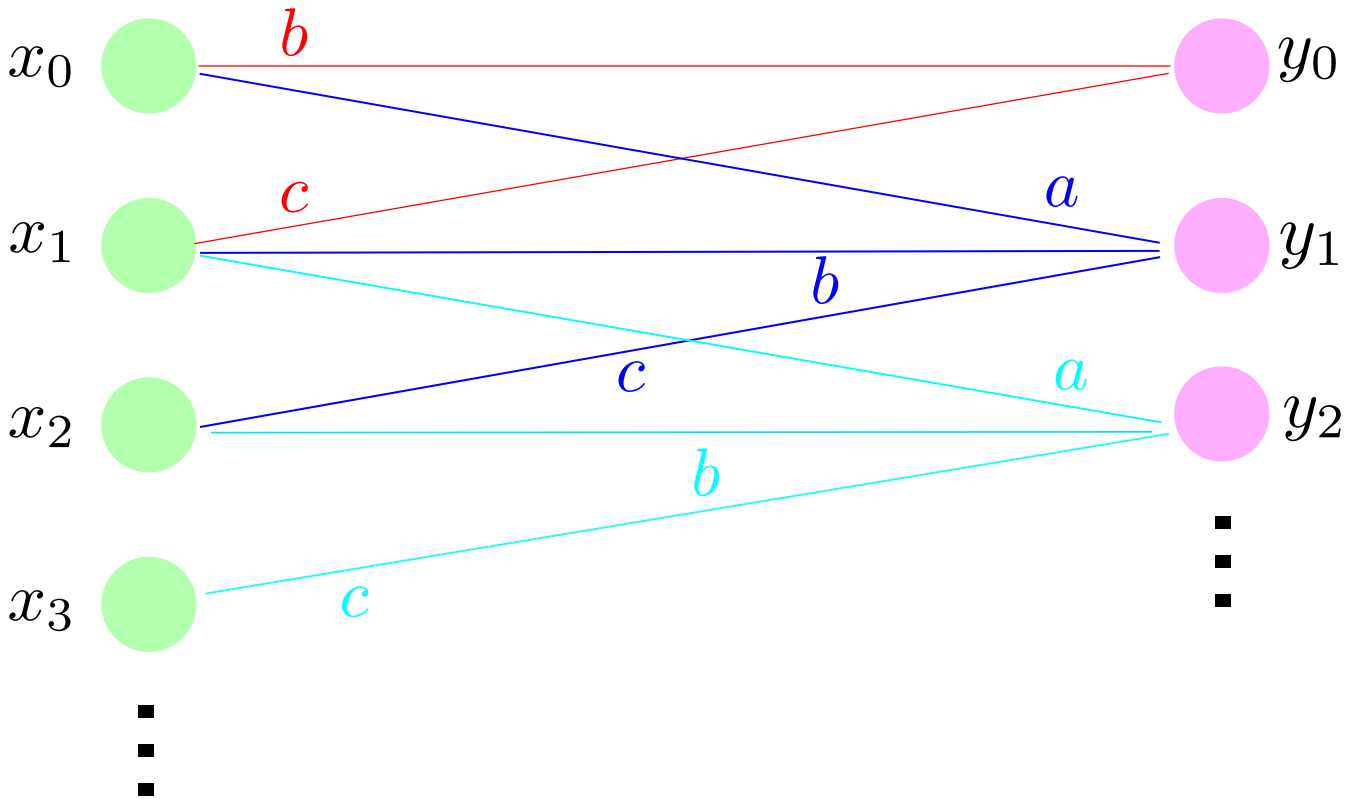
- Now that we understand convolution, how do we **optimize** a neural network with convolutional layers ? **Back-propagation**
- Consider a layer with just a convolution with w



- We have the derivatives $\frac{\partial \mathcal{L}}{\partial y_i}$ available
- We want to calculate the following quantities :
  - $\frac{\partial \mathcal{L}}{\partial x_k}$ (for further back-propagation) and
  - $\frac{\partial \mathcal{L}}{\partial w_k}$
- We shall use the abbreviation $\frac{\partial \mathcal{L}}{\partial y_i} =: dy_i$

Convolutional Layers

- Before considering the general case, let's take an example from the illustration from above



- Say we want to calculate $dx_1 := \frac{\partial \mathcal{L}}{\partial x_1}$

Convolutional Layers

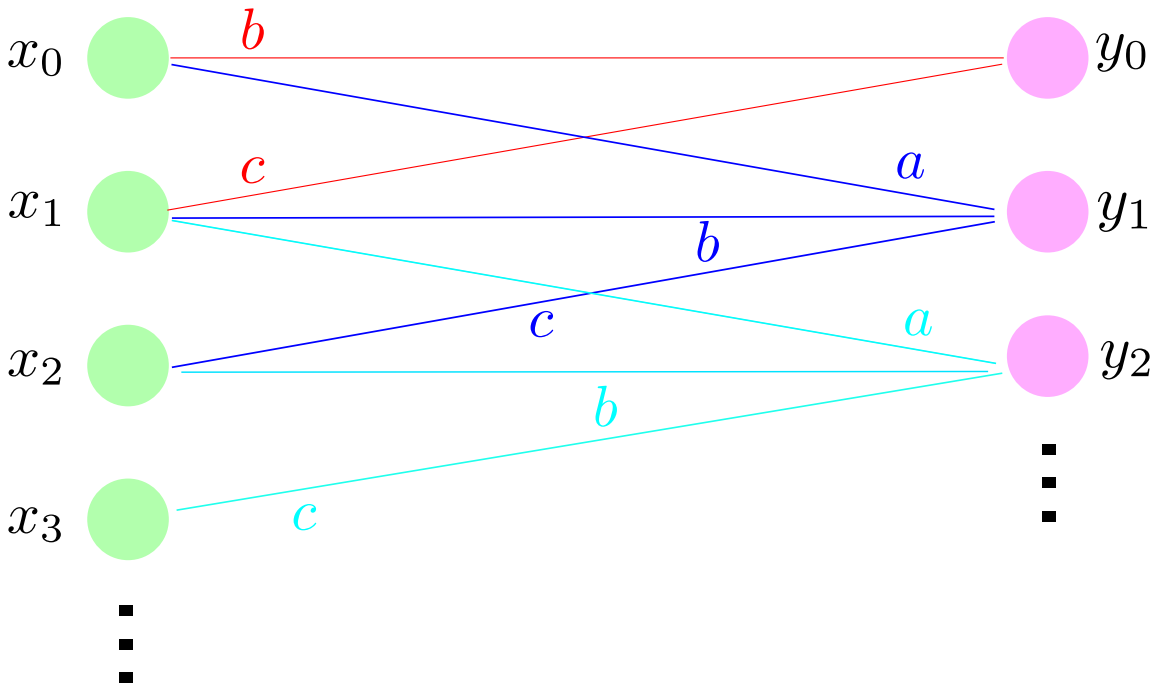
- Each element y_i depends on the input x_i and the weight w_k
- Therefore, we can consider that the loss is a function of several variables :

$$\mathcal{L} = f\left(x_1, \ldots, x_n, w_1, \ldots, w_K, y_1(x_\cdot, w_\cdot), \ldots, y_m(x_\cdot, w_\cdot)\right)$$

- We use the multi-variate chain rule

$$dx_1 = \sum_i \frac{\partial \mathcal{L}}{\partial y_i} \frac{\partial y_i}{\partial x_1}$$

Convolutional Layers



$$dx_1 = dy_0 \frac{\partial y_0}{\partial x_1} + dy_1 \frac{\partial y_1}{\partial x_1} + dy_1 \frac{\partial y_2}{\partial x_1} = dy_0 c + dy_1 b + dy_2 a$$

- As we can see, the order of the weights is flipped

Convolutional Layers

- Now, let us calculate $\frac{\partial \mathcal{L}}{\partial x_k}$ for any k

$$\frac{\partial \mathcal{L}}{\partial x_k} = \sum_i dy_i \frac{\partial y_i}{\partial x_k} \qquad \text{multi-variate chain rule}$$

$$= \sum_i dy_i \frac{\partial (x * w)_i}{\partial x_k}$$

$$= \sum_i dy_i \frac{\partial \left(\sum_j x_j w_{i-j} \right)}{\partial x_k}$$

$$= \sum_i dy_i w_{i-k} = \sum_i dy_i w_{-(k-i)}$$

- More compactly : $dx_k = (dy * \text{flip}(w))_k$

Convolutional Layers

- Recall that the convolution operator can be written $y = Ax$, with A the convolution matrix
- The flipping of the weights corresponds to a transpose of A

$$dx = A^\intercal dy \tag{1}$$

- This gives an easy method of backpropagation in convolutional layers
  - Although you will not actually have to implement this

Convolutional Layers

- Now for the second part : $\frac{\partial \mathcal{L}}{\partial w_k}$

$$\frac{\partial \mathcal{L}}{\partial w_k} = \sum_i dy_i \frac{\partial y_i}{\partial w_k} \qquad \text{multi-variate chain rule}$$

$$= \sum_i dy_i \frac{\partial (x * w)_i}{\partial w_k}$$

$$= \sum_i dy_i \frac{\partial \left(\sum_j x_j w_{i-j} \right)}{\partial w_k}$$

$$= \sum_i dy_i x_{i-k} = \sum_i dy_i x_{-(k-i)} \qquad k = i - j$$

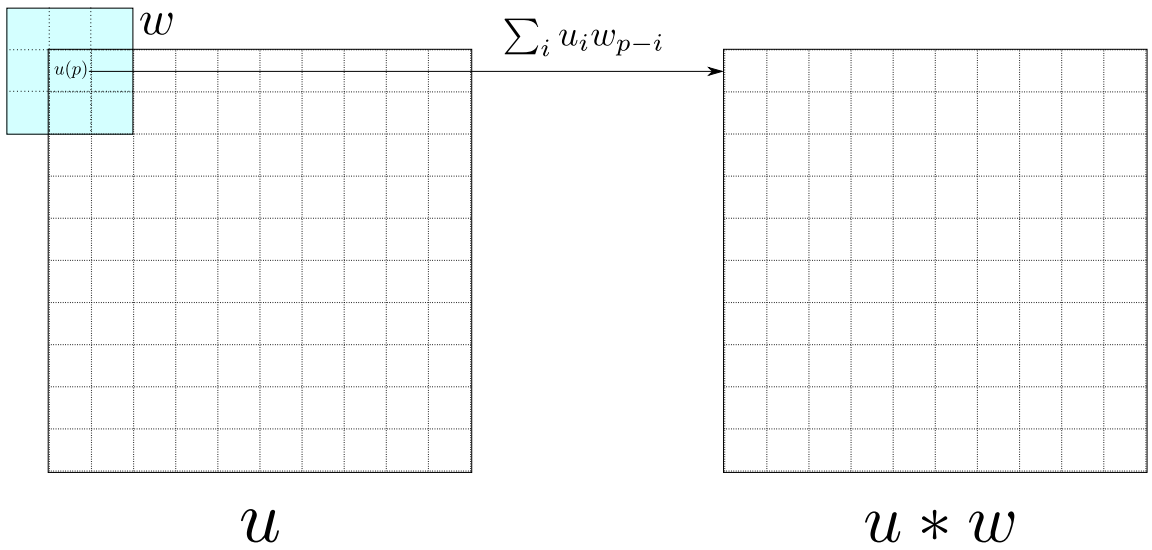
- More compactly : $dw_k = (dy * \text{flip}(x))_k$

Convolutional Layers

- Note : optimisation of loss w.r.t one parameter w_k **involves entire image**
- **Weights are "shared" across the entire image**
- This notion of **weight sharing** is one of the main justifications of using CNNs
- In practice, we do not calculate dw_k and dx_k ourselves, we use the **automatic differentiation** tools of Tensorflow, Pytorch etc.

Convolutional Layers - border conditions

- The convolution operator poses a problem at the borders
- Theoretically, we consider functions defined over an infinite domain, but which have compact support
- In reality, we only have finite vectors/matrices to work on

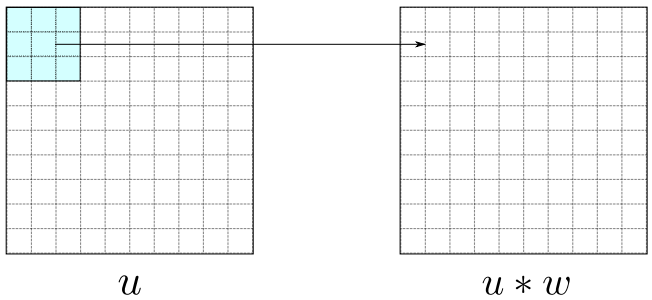


Convolutional Layers - border conditions

Two common approaches to border conditions

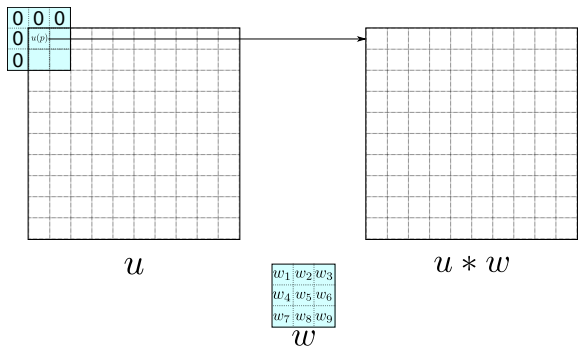
"VALID" approach

- Only take shift/dot products that do not extend beyond $\mathrm{Supp}(u)$
- Output size : $m - |w| + 1$



"SAME" approach

- Keep output size m
- Need to choose values outside of $\mathrm{Supp}(u)$: zero-padding



2D+feature convolution

- Several filters are used per layer, let us say K filters : $\{w_1, \ldots, w_K\}$
- The resulting vectors/images are then stacked together to produce the next layer's input $u^{\ell+1} \in \mathbb{R}^{m \times n \times K}$

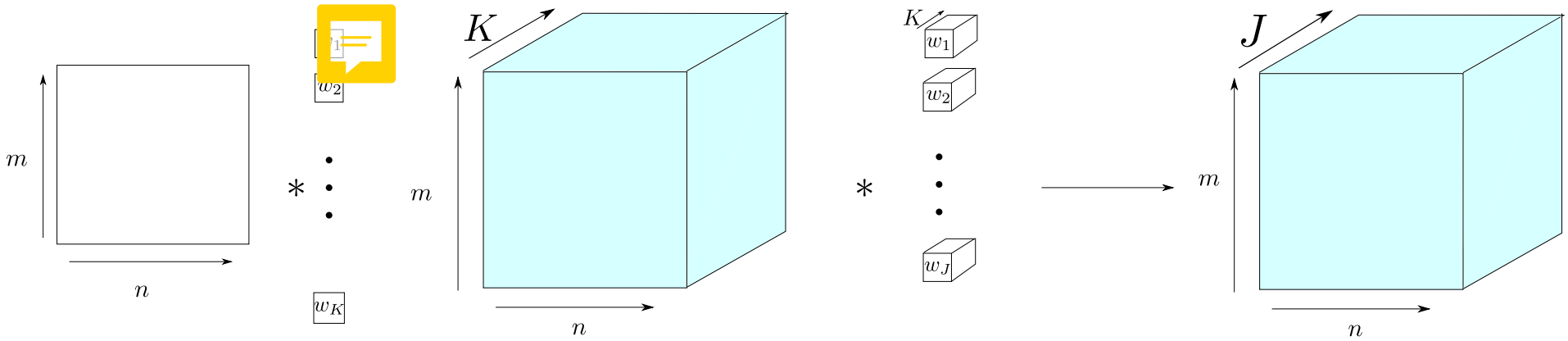
$$u^{\ell+1} = [u * w_1, \ldots, u * w_K]$$

- Therefore, the next layer's weights must have a depth of K. The 2D convolution with an image of depth K is defined as

$$(u * w)_{x,y} = \sum_{i,j,k} u(i, j, \mathbf{k})\, w(x - i, y - j, \mathbf{k})$$

Convolutional layers

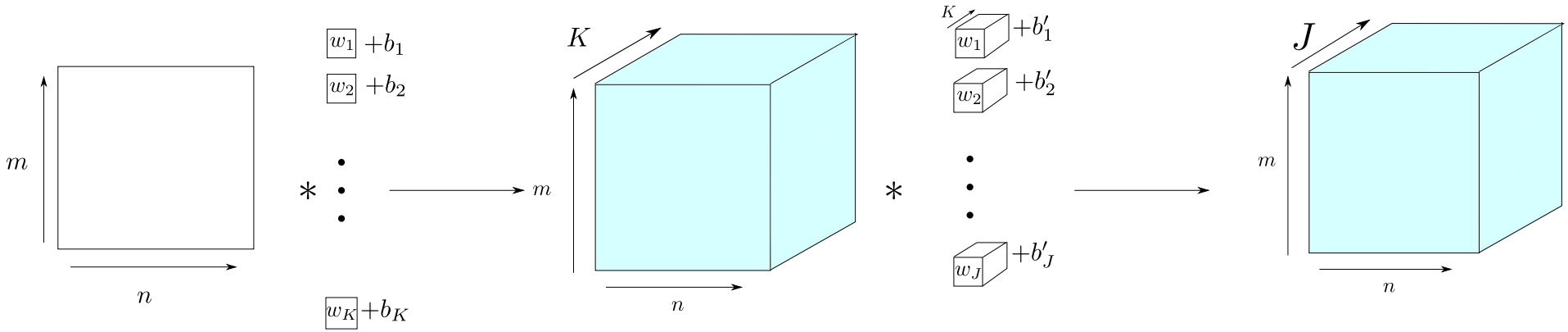
- Illustration of several consecutive convolutional layers with different numbers of filter



- Each layer contains "image" with a depth, where each channel corresponds to a different filter response
- Each layer is a concatenation of several features : rich information

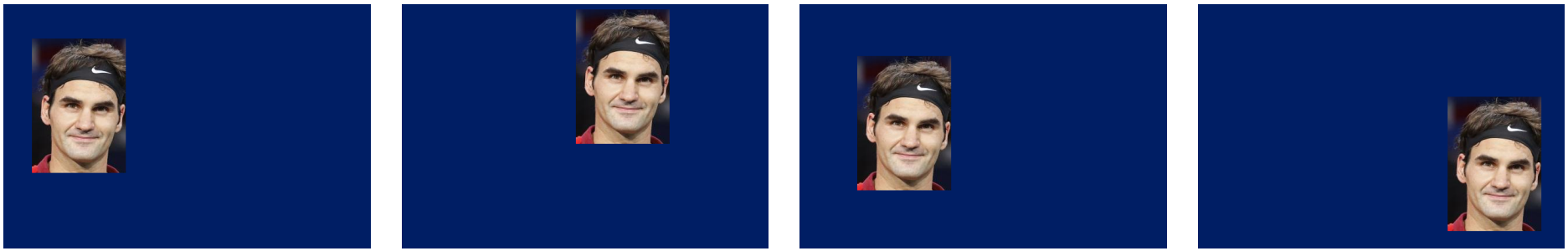
Convolutional layers - a note on Biases

- A note on biases in neural networks : **each output layer is associated with one bias**
- There is **not** one bias per pixel
- This is coherent with the idea of **weight sharing** (bias sharing)



Convolutional Layers

- In many cases, we are primarily interested in **detection**;
- We would like to detect objects **wherever they are in the image**



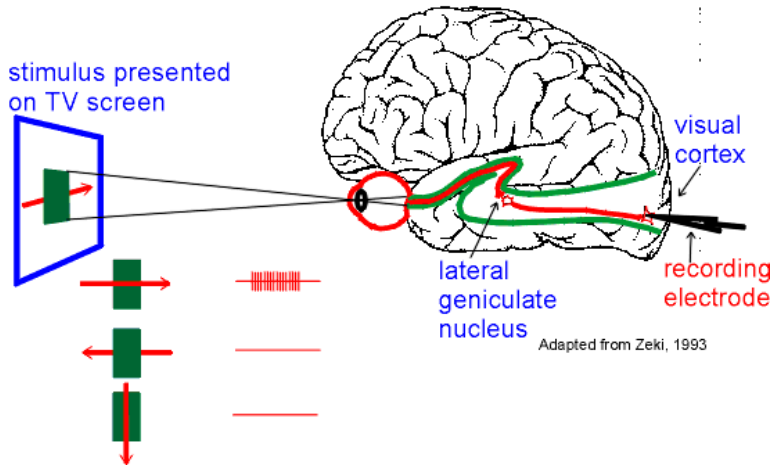
- Formally, we would like to have some **shift invariance property**;
- This is done in CNNs by using **subsampling**, or some variant :
  - Strided convolutions
  - Max pooling
- We explain these now

Summary

Down-sampling and the receptive field

The Receptive Field

- Neural networks were initially inspired by the brain's functioning
- Hubel and Weisel[†] showed that the visual cortex of cats and monkeys contained cells which individually responded to different small regions of the visual field
- The region which an individual cell responds to is known as the "receptive field" of that cell



[†] ***Receptive fields and functional architecture of monkey striate cortex***, *Hubel, D. H.; Wiesel, T. N, 1968 Illustration from :* `http://www.yorku.ca/eye/cortfld.htm`

The Receptive Field

- This idea was imitated in convolutional neural networks by adding **down-sampling** operations

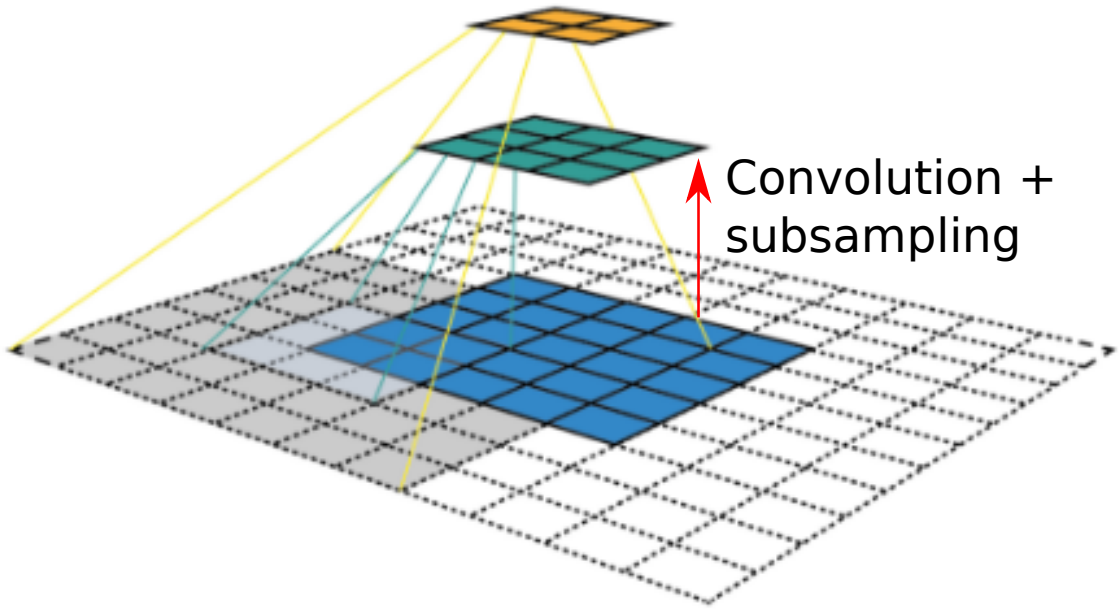


Illustration from : Applied Deep Learning, Andrei Bursuc, https://www.di.ens.fr/~lelarge/dldiy/slides/lecture_7/

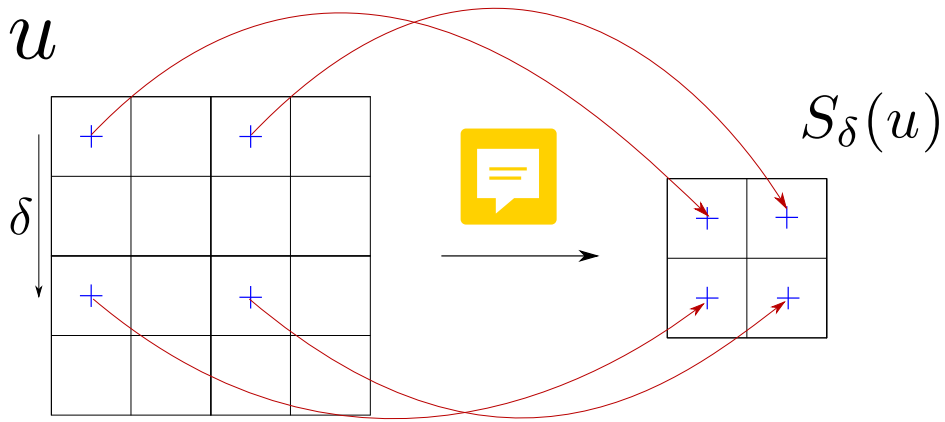
Strided convolution

- **Strided convolution** is simply convolution, followed by **subsampling**

Subsampling operator (for 1D case)

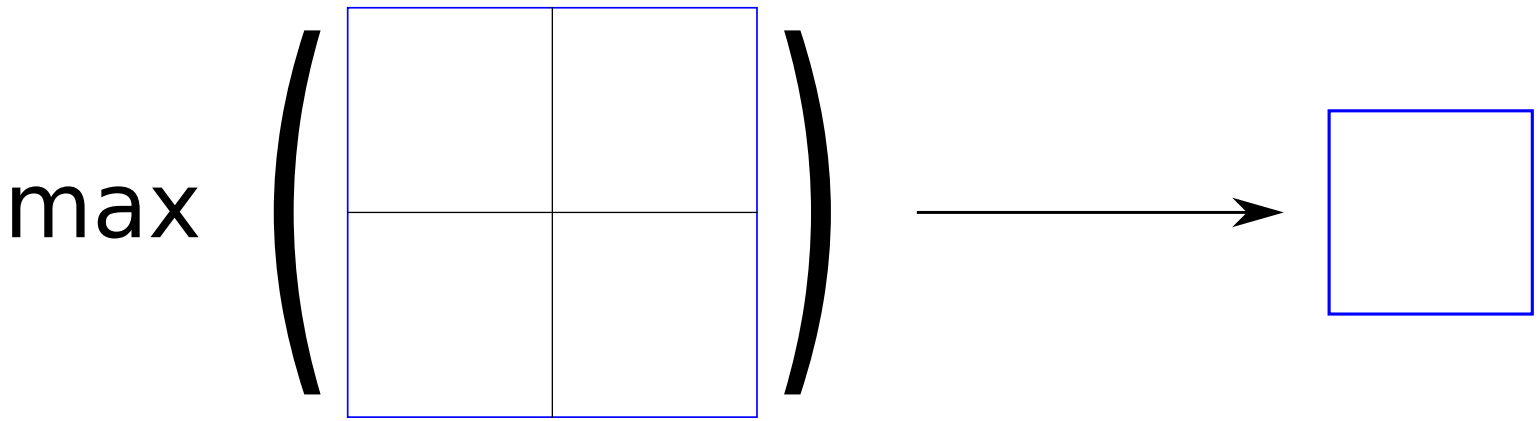
Let $x \in \mathbb{R}^n$. We define the subsampling step as $\delta > 1$, and the subsampling operator $S\delta : \mathbb{R}^n \to \mathbb{R}^{\frac{n}{\delta}}$, applied to x, as

$$S_\delta(x)\ (t) = x(\delta t), \ \text{ for } t = 0 \dots \frac{n}{\delta}$$



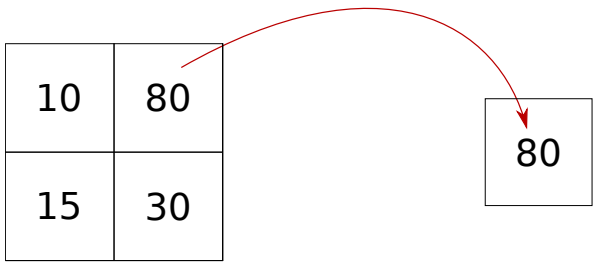
Max pooling

- **Max pooling** subsampling consists in taking the **maximum** value over a certain region
- This maximum value is the new subsampled value
- We will indicate the max pooling operator with S_m

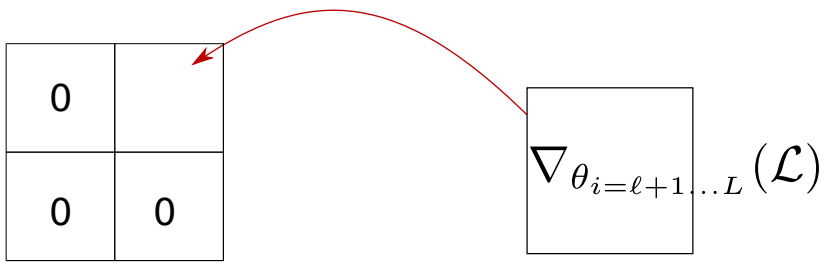


Max pooling

- Back propagation of max pooling only passes the gradient through the **maximum**



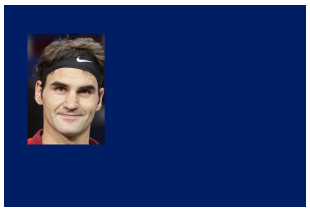
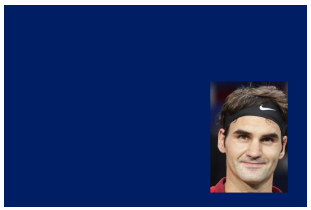
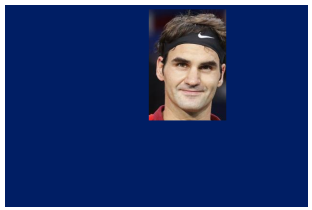
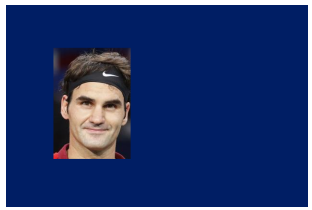
Max pooling



Back propagation

Down-sampling

- Conclusion : cascade of convolution, non-linearities and subsampling produces **shift-invariant** classification/detection
- We can detect Roger wherever he is in the image !

$$u * w$$

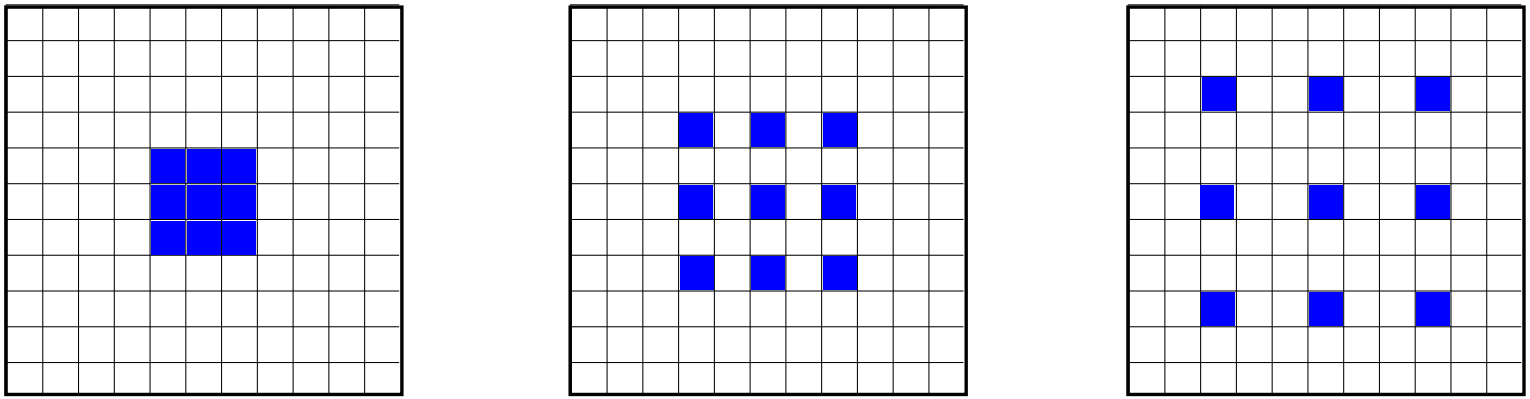
Convolution + non-linearity +max pooling

✓ ✓ ✓ ✓

Summary

Dilated Convolution

- There is a variant of convolution called *dilated convolution*[*]
- Increase spatial extent of convolution without adding parameters
  - Add a space D between each point in the convolution

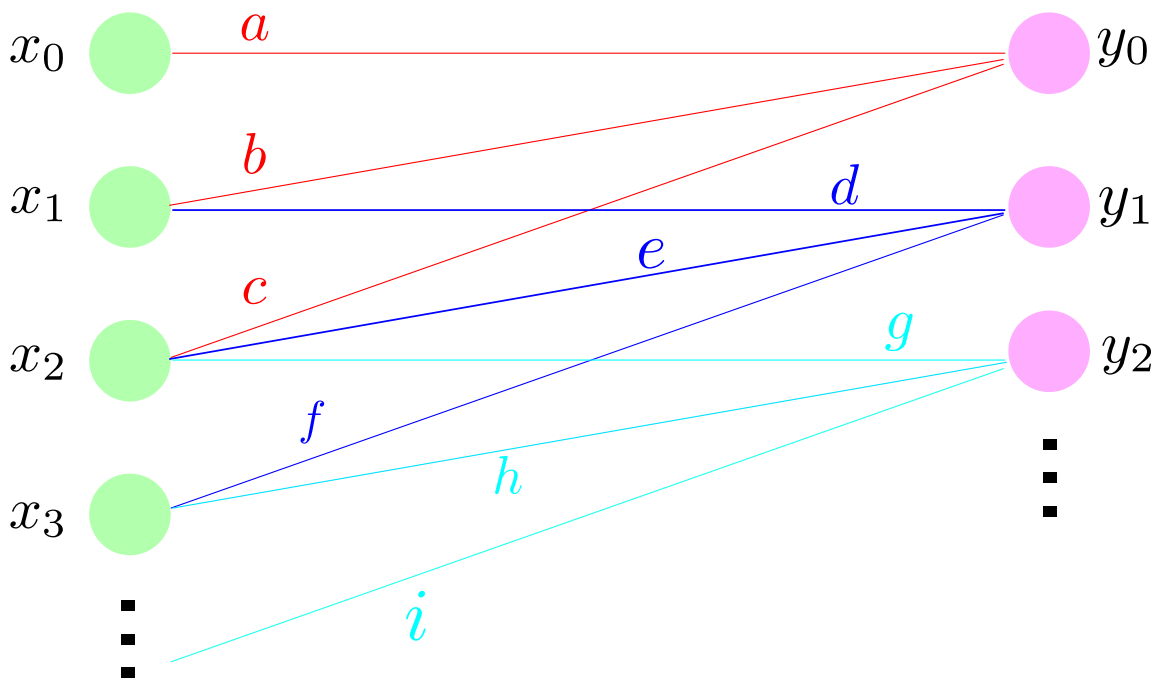


$$(u * v)(x, y) = \sum_{i,j,k} u(i, j, k)v(x - Di, y - Dj, k) \tag{2}$$

[*] ***Multi-Scale Context Aggregation by Dilated Convolution***, *Yu, F, Kolten, V, ICLR 2016*

Locally connected layers / unshared convolution

- We might wish for a mix of a dense layer and a convolutional layer
- One possibility : **locally-connected layers** (sometimes called "unshaped convolution")
  - Local connectivity but no weight sharing



- Number of weights increases linearly with the number of pixels, rather than quadratically (for MLPs)

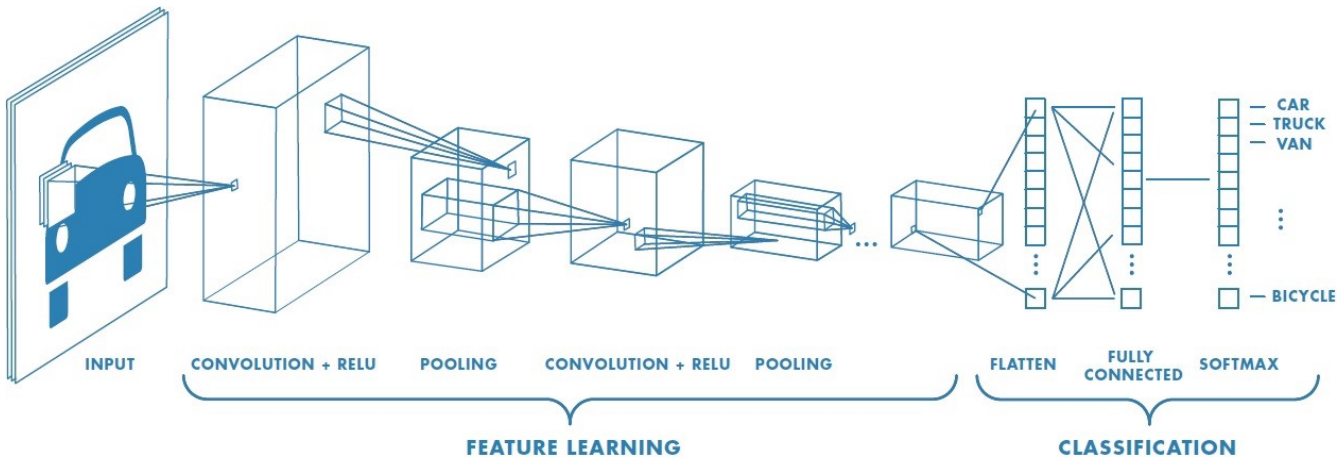
Summary

How to build your CNN ?

- We have looked at the following operations : convolutions, additive biases, non-linearities
- All of these elements make up convolutional neural networks
- However, how do we put these together tp create our own CNN ?
  - **Architecture ?**
  - Programming tools ?
  - Datasets ?

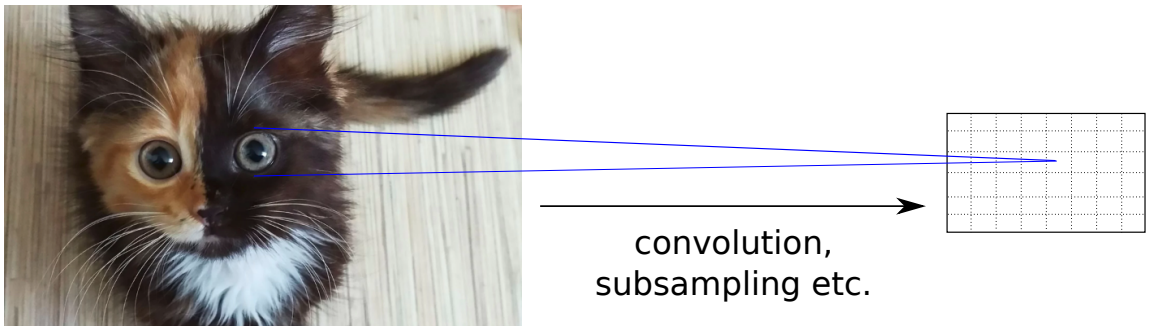
Architecture : vanilla CNN

- Simple classification CNN architecture often consists of a **feature learning section**
  - Convolution $\rightarrow$ biases $\rightarrow$ non-linearities $\rightarrow$ subsampling
  - This continues until a fixed subsampling is achieved
- After this, a **classification section** is used
  - Fully connected layer $\rightarrow$ non-linearity



Architecture

- Central question : how to choose number of layers ?
- Complicated, very little theoretical understanding, currently a hot topic of research
- However : there are a few rules of thumb to follow
  - Receptive field of the **deepest layer should encompass what we consider to be a fundamental brick** of the objects we are analysing



- Set number of layers and subsampling factors according to the problem

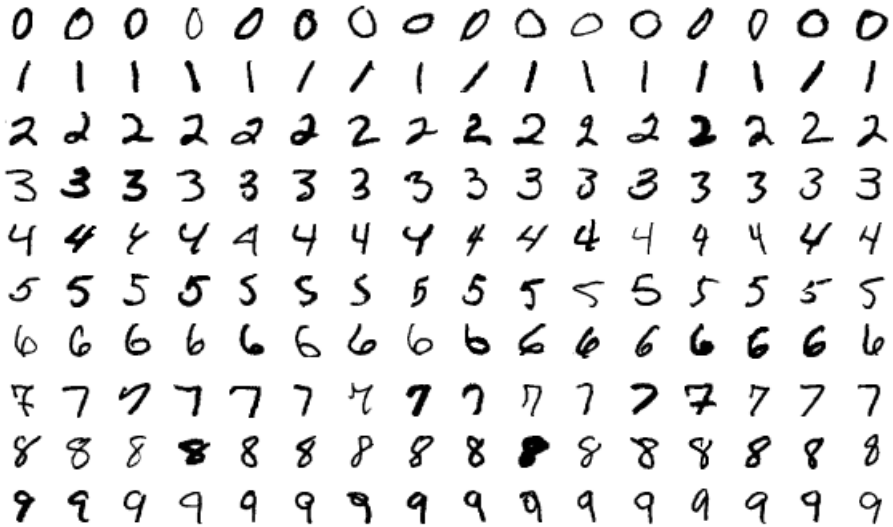
CNN programming frameworks

- Caffe
  - Open source, developed by University of California, Berkley
  - Network created in separate specific files
  - Somewhat laborious to use, less used than other frameworks
- Theano
  - Open source, created by the Université de Montréal
  - Unfortunately, to be discontinued due to strong competition
- Tensorflow
  - Open source, developed by Google
  - Implements a wide range of deep learning functionalities, widely used
- Pytorch
  - Open source, developed by Facebook
  - Implements a wide range of deep learning functionalities, widely used

Summary

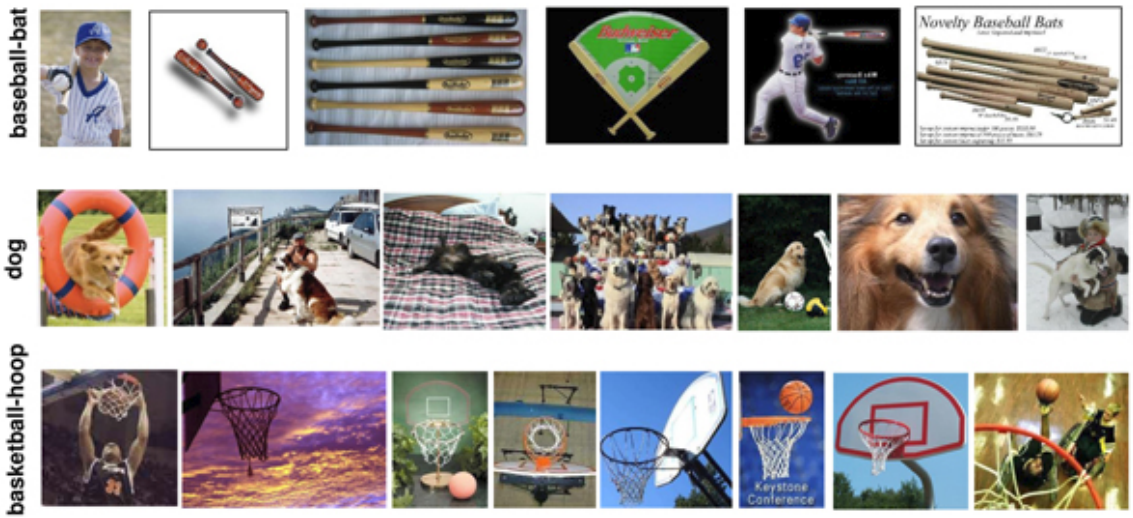
MNIST dataset

- MNIST is a dataset of 60,000 28×28 pixel grey-level images containing hand-written digits
- The digits are centred in the images and scaled to have roughly the same size
- Although quite a "simple" dataset, still used to display performance of modern CNNs



Caltech 101

- Produced in 2003, first major object recognition dataset
- 9,146 images, 101 object categories, each category contains between 40 and 800 images
- Annotations exist for each image : bounding box for the object and a human-drawn outline



ImageNet dataset

- Dataset created in 2009 by researchers from Princeton unverisity
- Very large dataset : 14,197,122 images, hand-annotated
- Used for the ImageNet Large Scale Visual Recognition Challenge, an annual benchmark competition for object recognition algorithms

LeNet (1989/1998)

- Created by Yann LeCun in 1989, goal : to recognise handwritten digits
- Able to classify digits with 98.9% accuracy, used by U.S. government to automatically read digits

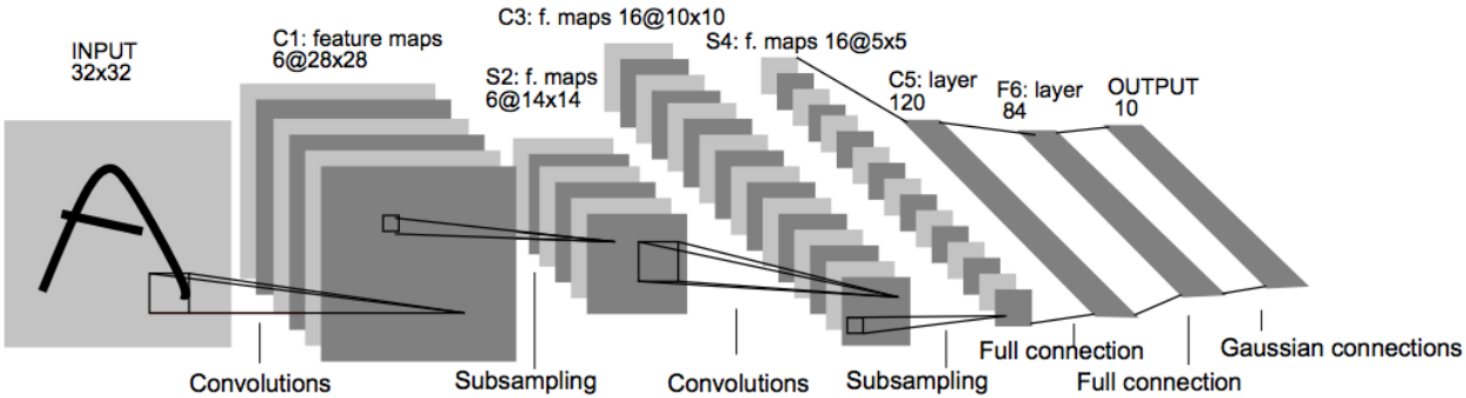
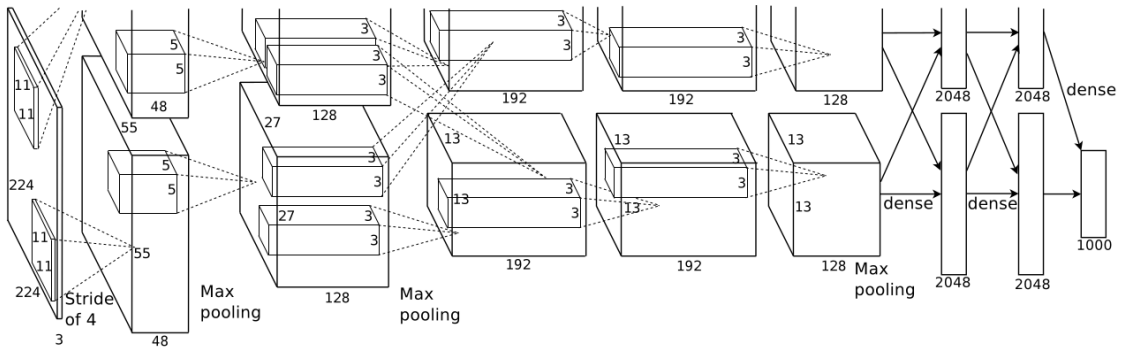


Fig. 2. Architecture of LeNet-5, a Convolutional Neural Network, here for digits recognition. Each plane is a feature map, i.e. a set of units whose weights are constrained to be identical.

Illustration from : ***Gradient-based Learning Applied to Document Recognition****, LeCun, Y. Bottou, L., Bengio, Y. and Haffner, Proceedings of the IEEE, 1989*

AlexNet (2012)

- AlexNet : created by Alex Krizhevsky in 2012
- Improved accuracy of ImageNet Large Scale Visual Recognition Challenge competition by **10 percentage points** (16.4%)
- First **truly deep neural network**
- Signaled beginning of dominance of deep learning in image processing and computer vision

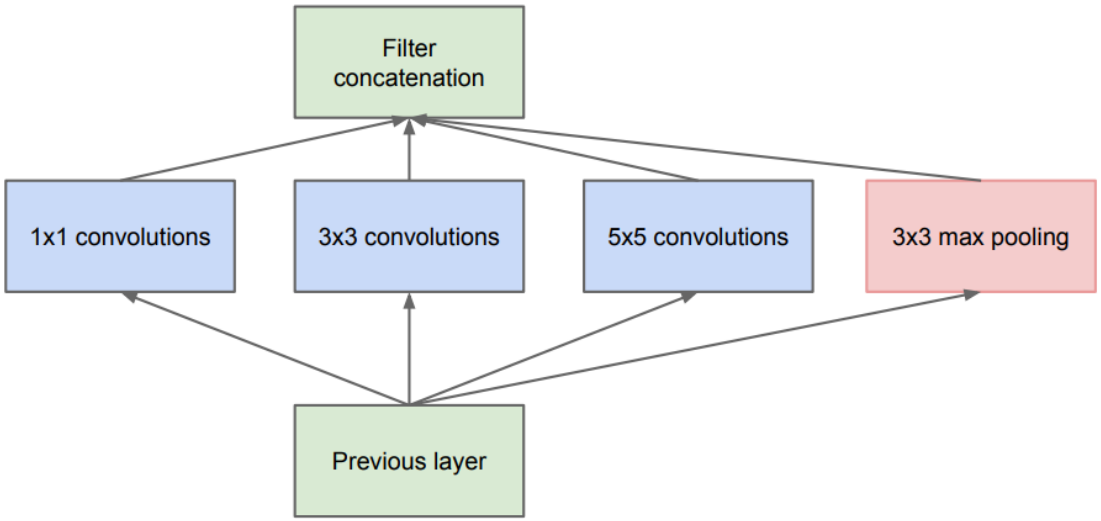


(Krizhevsky et al., 2012)

Illustration from : ***Imagenet classification with deep convolutional neural networks****, Krizhevsky, A., Sutskever, I. and Hinton, G. E, NIPS, 2012*

GoogLeNet (2015)

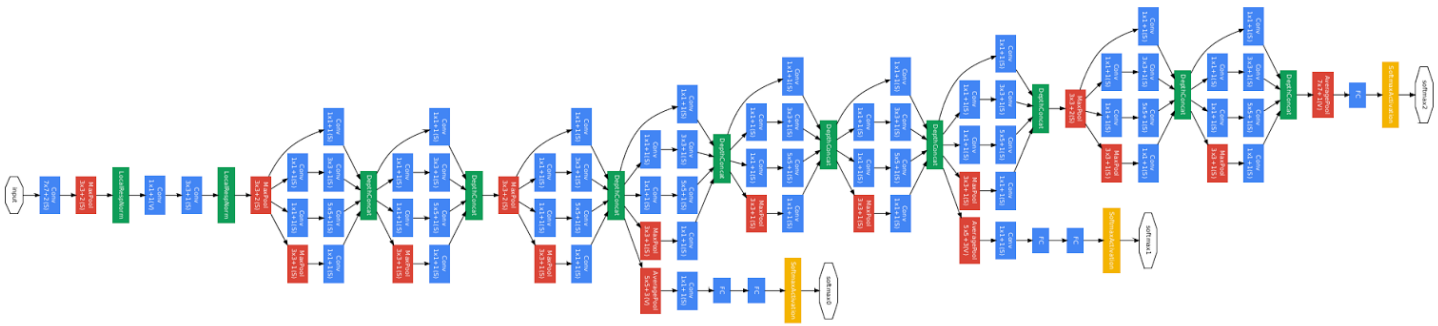
- In 2014/2015, Google introduced the "Inception" architecture/module
- Major attempt at reducing total number of parameters
- No fully connected layers, only convolutional
  - 2 million instead of 60 million for AlexNet
- Novel idea : have variable receptive field sizes in one layer



Going deeper with convolutions, *Szegedy et al, CVPR, 2015*

GoogLeNet (2015)

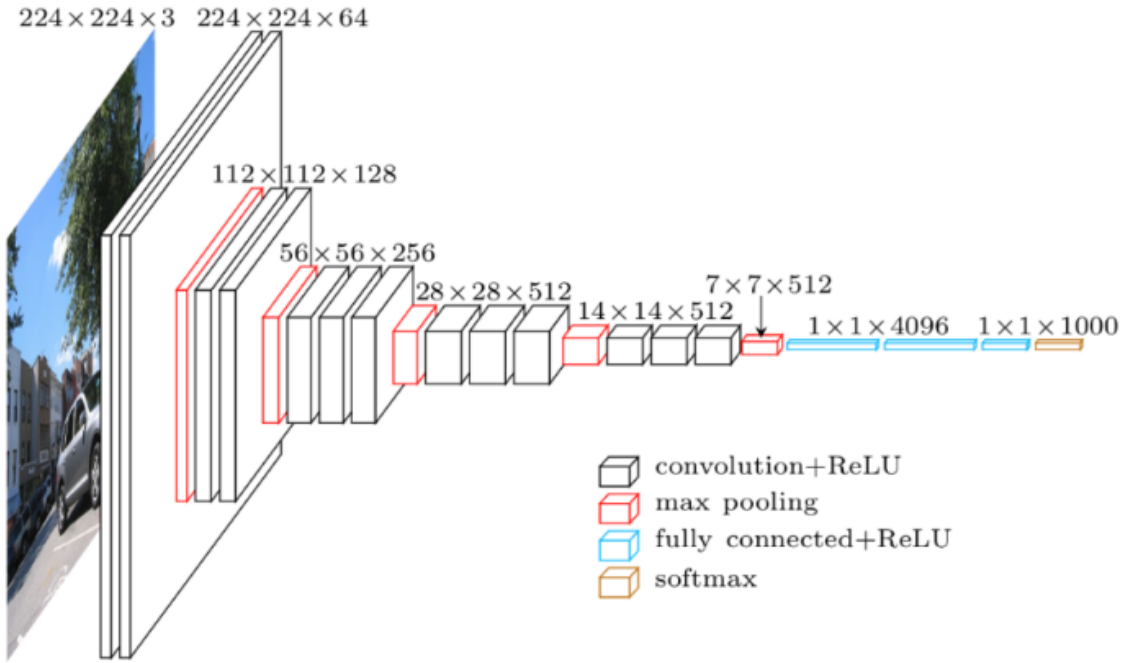
- Created by Google in 2014, GoogLeNet is a specific implementation of the "inception" architecture
- 6.6% test error rate on ImageNet (human error rate 5%)



Going deeper with convolutions, *Szegedy et al, CVPR, 2015*

VGG16 (2015)

- VGG16 is a 16-layer network, with small receptive fields (3×3 filters, with less subsampling)
- Around 7.5% test error on ILSVRC



Very Deep Convolutional Networks for Large-Scale Image Recognition, *Simonyan, K. and Zisserman, A., ICLR, 2015*
Illustration from Mathieu Cord,
https://blog.heuritech.com/2016/02/29/a-brief-report-of-the-heuritech-deep-learning-meetup-5/

Summary of advances in CNNs

Network	LeNet (1998)	AlexNet (2012)	GoogLeNet (2014)	VGG16 (2015)
Image size	28×28	$256 \times 256 \times 3$	$256 \times 256 \times 3$	$224 \times 224 \times 3$
Layers	3	8	22	16
Parameters	60,000	60 million	2 million	138 million

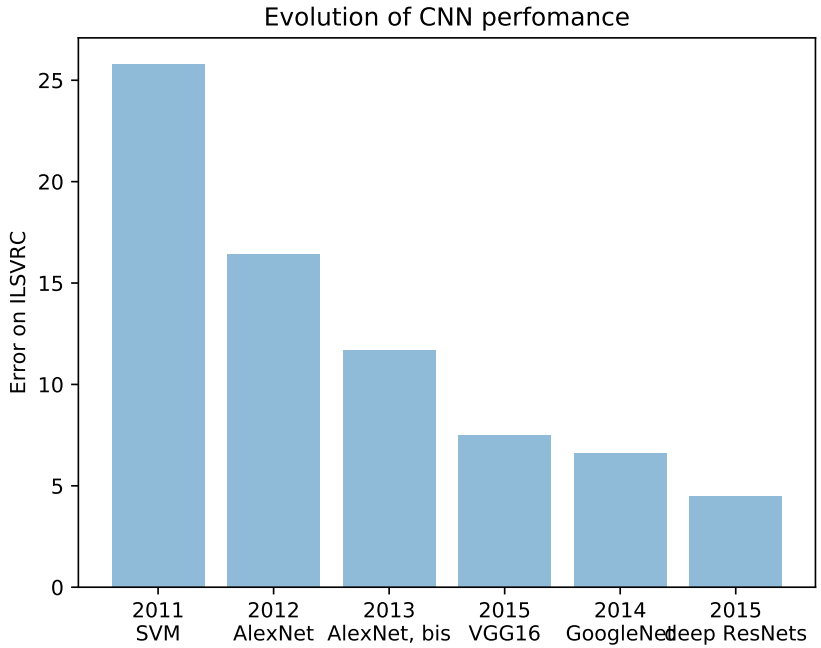


Image classification

- As we mentioned before, CNNs make sense for data with **grid-like** structures
- In particular, images are most often the target of CNNs
- Arguably the most common application of CNNs is to **image classification**
- Why is image classification important ? Closely linked to :
  - Object detection
  - Tracking
  - Image search (in large databases for example)
- In recent years, the best performing classification algorithms have been using neural networks

Image classification

- Why is image classification difficult ?
  - Images can vary in size, shape, position
  - We need to deal with variable lighting conditions, occlusions etc.

Image classification

- We have input datapoints x, which we wish to classify into several, predefined classes $\{c_i, i = 1 \dots K\}$, where K is the number of classes
- As we have seen, convolution, non-linearities, subsampling allow for robust classification that is invariant to many perturbations

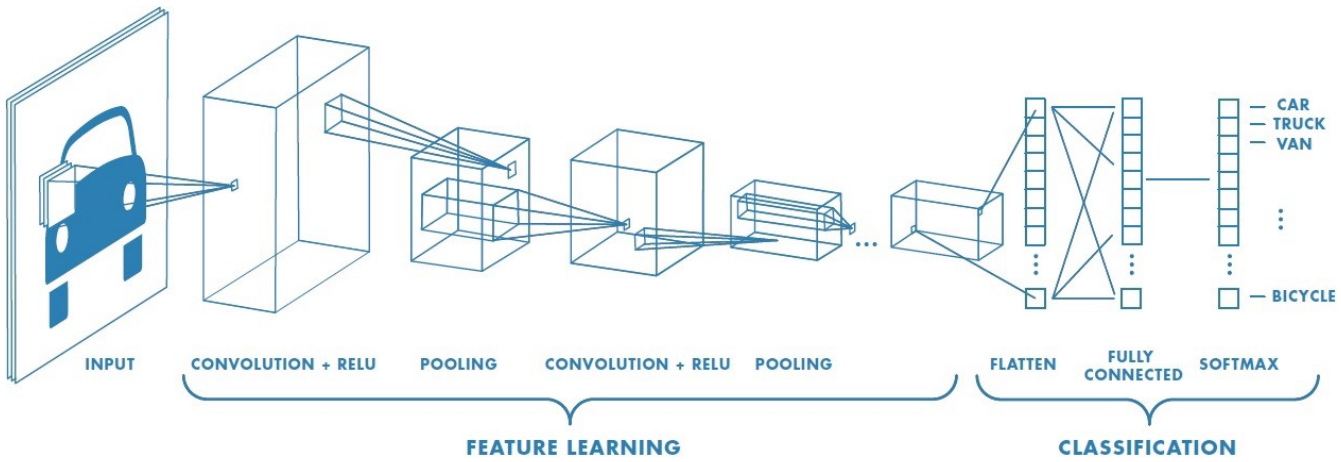
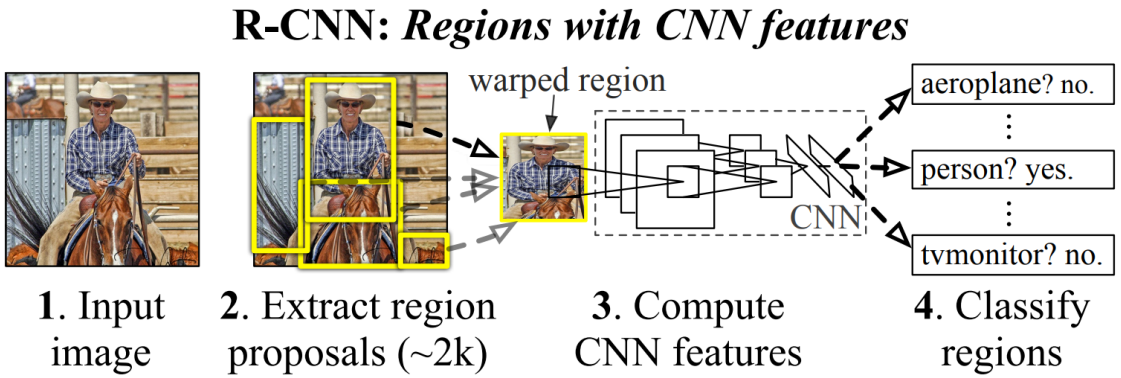


Image classification

- We can also **detect the position** of objects in images
- RNN† proposes a simple approach :
  1. Propose a list of bounding boxes in the image
  2. Pass the resized sub-images through a powerful classification network
  3. Classify each sub-image with your favourite classifier



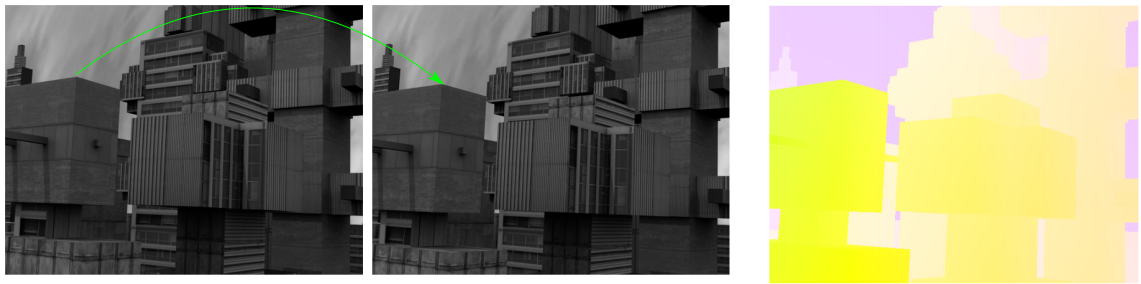
- Many variants on this work (Fast R-NN, Faster R-CNN) etc.

† ***Rich feature hierarchies for accurate object detection and semantic segmentation***, *Girschik, R. et al. CVPR 2014*

Motion estimation

- **Motion estimation** is a central task for many image processing and computer vision problems : tracking, video editing
- **Optical flow** involves estimating a vector field $(u, v) : \mathbb{R}^2 \rightarrow \mathbb{R}^2$ where each vector points to the displacement of pixel (x, y) from an image I_1 to I_2

$$I_1(x, y) = I_2(x + u(x, y), y + v(x, y))$$

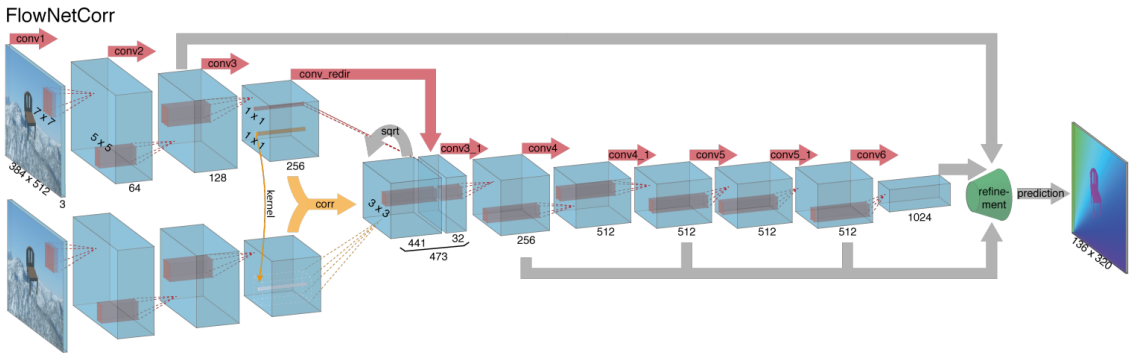


(a) Frame 1 (b) Frame 2 Optical flow

Illustration from : ***BriefMatch: Dense binary feature matching for real-time optical flow estimation****, Eilertsen, G, Forssén, P-E, Unger, J., Scandinavian Conference on Image Analysis, 2017*

Motion estimation with CNNs

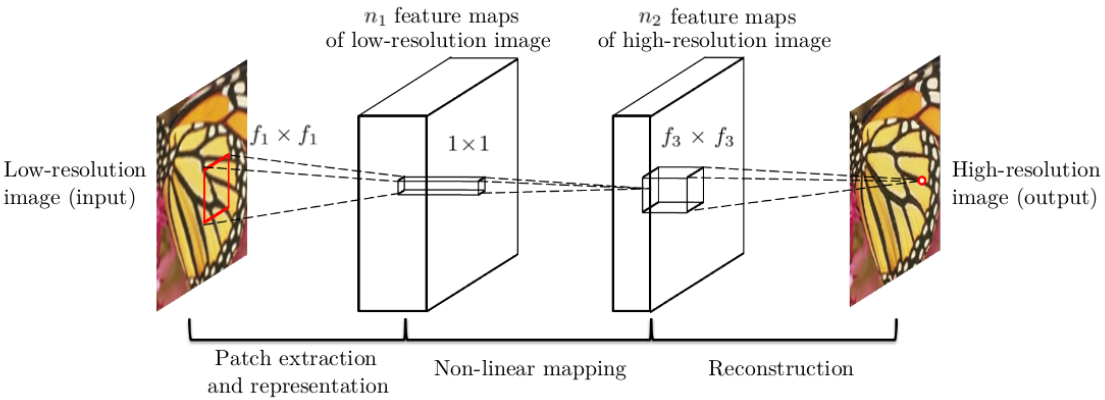
- A major challenge of optical flow estimation is to handle both fine and large-scale motions
  - This is difficult to do with classical, variational approaches
- CNNs have this multi-scale architecture already built in
- Example : FlowNet* uses this, first extracting meaningful features from the images (in parallel) and then combining them to create the optical flow

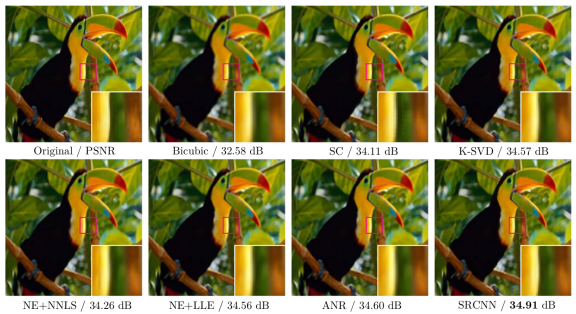


* ***FlowNet: Learning Optical Flow with Convolutional Networks***, *Fischer et al, ICCV 2015*

Super-resolution

- Image super-resolution : go from a low-resolution image to a higher-resolution one
- Relatively straightforward approach with a CNN*





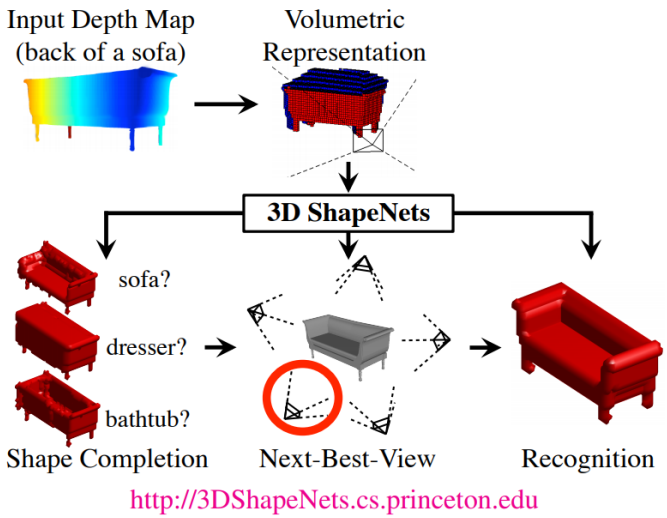
- Drawback, highly dependent on degradation used in lower-resolution images in database

* ***Learning a deep convolutional network for image super-resolution***, *Chao et al, ECCV 2014*

Point clouds

- CNNs require regular grids. Point cloud data are not in this format
- Nevertheless, ways have been found to deal with this

- ShapeNet* splits a volume up into sub-regions that are processed by CNNs
- Each region is a Bernoulli random variable representing the probability of this voxel belonging to a shape
- This general approach (using voxels) is followed in many other approaches



* ***3d shapenets: A deep representation for volumetric shapes***, *W. Zhirong et al. CVPR, 2015*

Summary

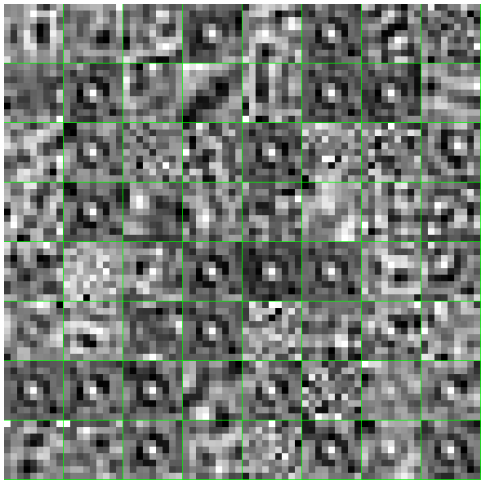
Adversarial examples

- As is often the case in deep learning, it is very difficult to understand what is going on in CNNs
- Much research is being dedicated to understanding these networks
  - Explainable AI (XAI) Darpa project*
- We discuss two topics related to interpretability
  - Visualising CNNs
  - Adversarial examples

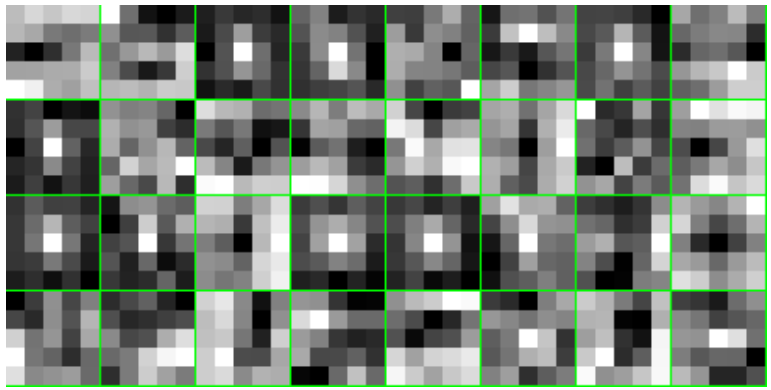
* *https://www.darpa.mil/program/explainable-artificial-intelligence*

Visualising CNNs

- We would like to **understand what CNNs are learning**
  - Unfortunately filters are difficult to interpret (especially deeper layers)



Layer 1 filters



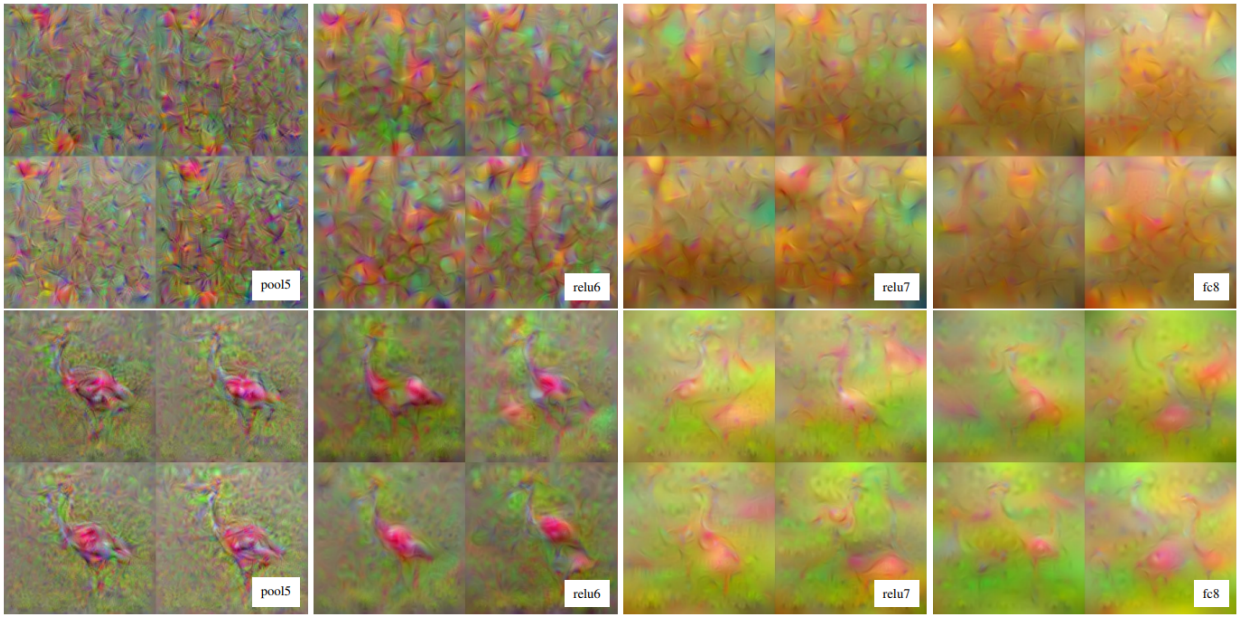
Layer 3 filters

- Therefore, much research has been dedicated to **visualising** CNNs

Visualising CNNs

- Idea : "invert" CNN : find x that gives a certain output
- Standard inverse problem with regularisation

$$\hat{x} = \arg\min_x \|f(x) - f_0\|_2^2 + \lambda \|x\|_2^2 + \mu \|\nabla x\|_2^2 \tag{3}$$



† *Mahendran and Vedaldi* ***Understanding Deep Image Representations by Inverting Them***, *Conference on Computer Vision and Pattern Recognition, 2014*

Visualising features

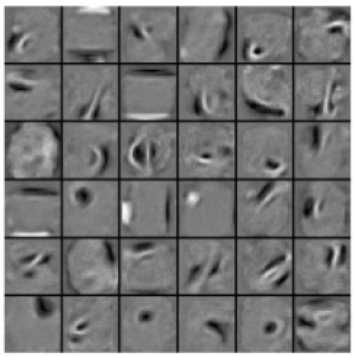
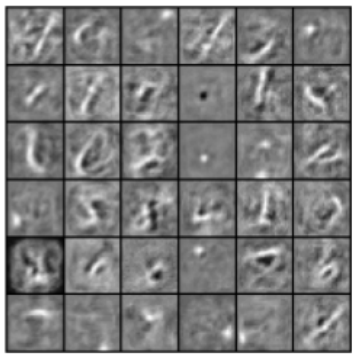
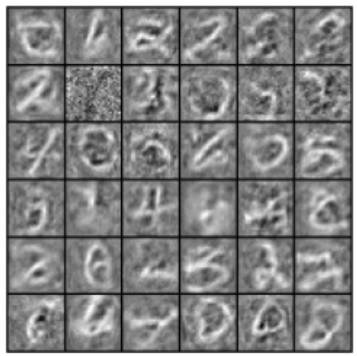
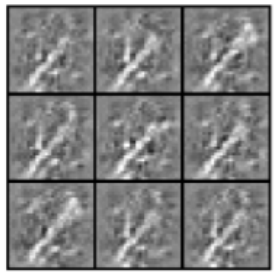
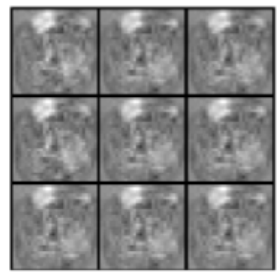
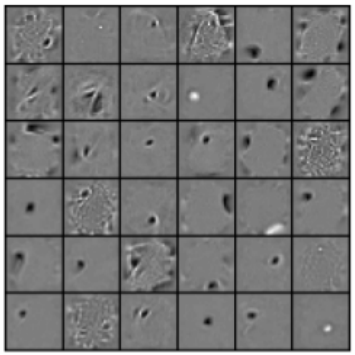
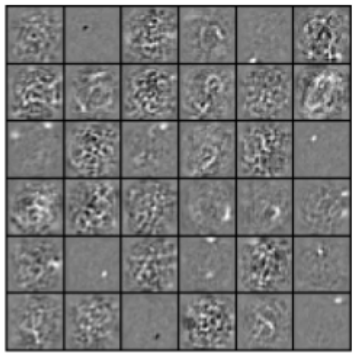
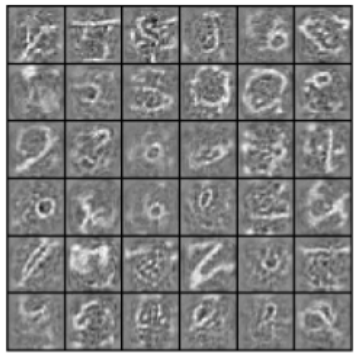
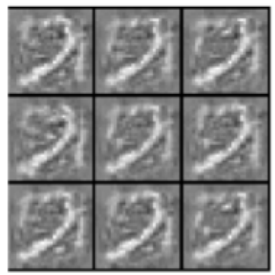
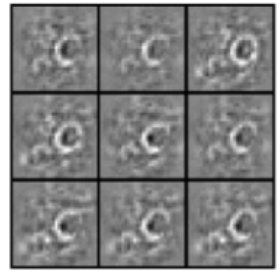
- Another approach to understanding CNNs : **maximise response** to a given filter
- Choose layer ℓ, filter k and element ("pixel") (i, j)
- Random initialisation x_0, constrain norm of solution x

$$\hat{x} = \arg\max_x u^{\ell}_{i,j,k}$$
$$\text{with } \| x \| = \rho$$

- Optimisation : **gradient ascent**

† *Erhan, Bengio, Courville, Vincent,* ***Visualizing Higher-Layer Features of a Deep Network****, University of Montreal, 2009*

Visualising CNNs

Layer 1 Layer 2 Layer 3 Layer 4

Maximisation of different activations applied to MNIST dataset

† *Erhan, Bengio, Courville, Vincent,* ***Visualizing Higher-Layer Features of a Deep Network****, University of Montreal, 2009*

Visualising CNNs

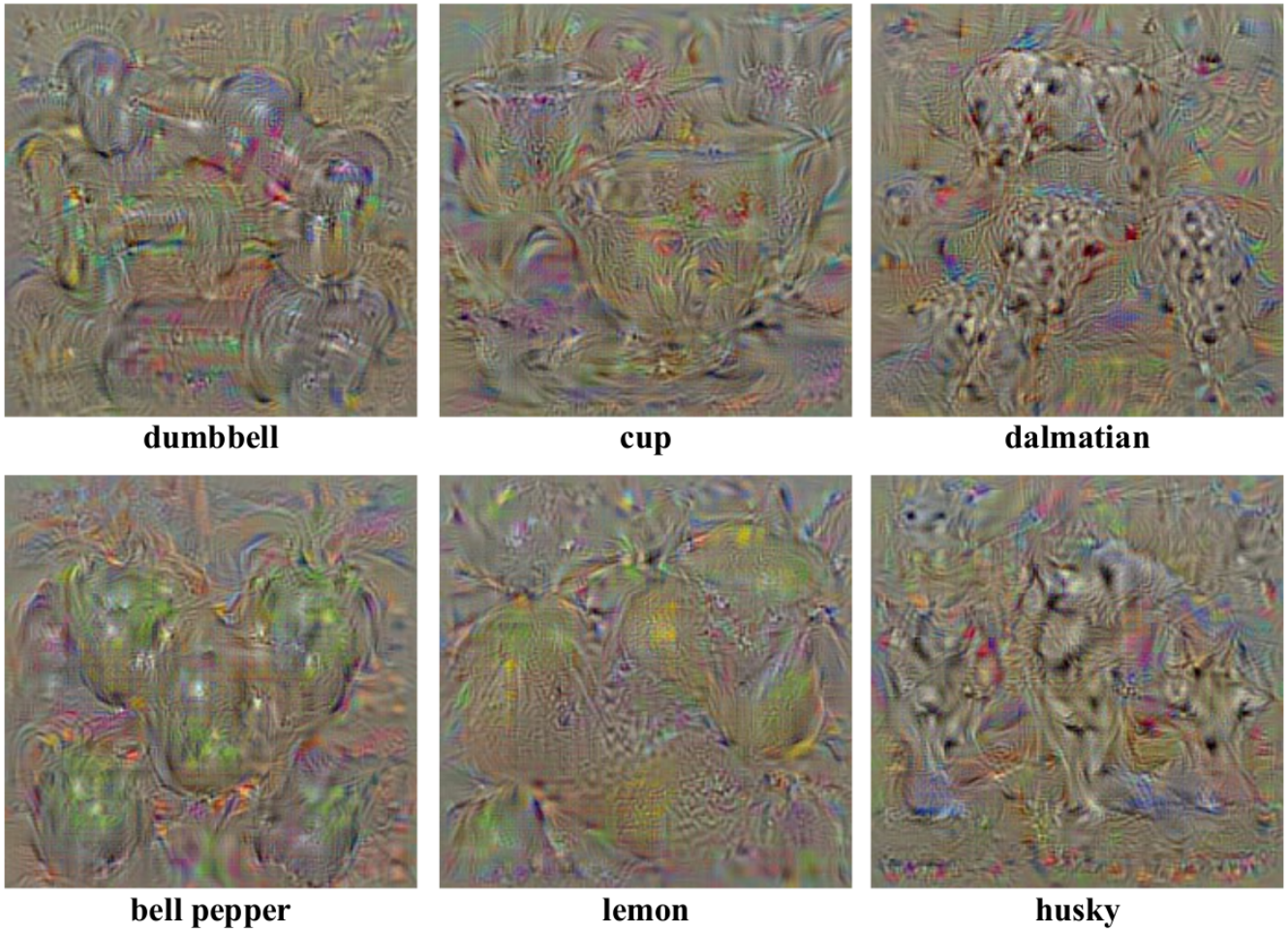
- Another approach of Simonyan et al.[†] proposes to see what images correspond to what classes
- Choose a class c, maximise the response of this class

$$\hat{x} = \arg\max_x f(x)_c - \lambda \|x\|_2^2$$

- Find an L_2-regularised image which maximises the score for a given class c
- Initialise with random input image x_0

[†] *Simonyan, Vedaldi, Zisserman* ***Deep Inside Convolutional Networks: Visualising Image Classification Models and Saliency Maps****, arXiv preprint arXiv:1312.6034, 2013*

Visualising CNNs

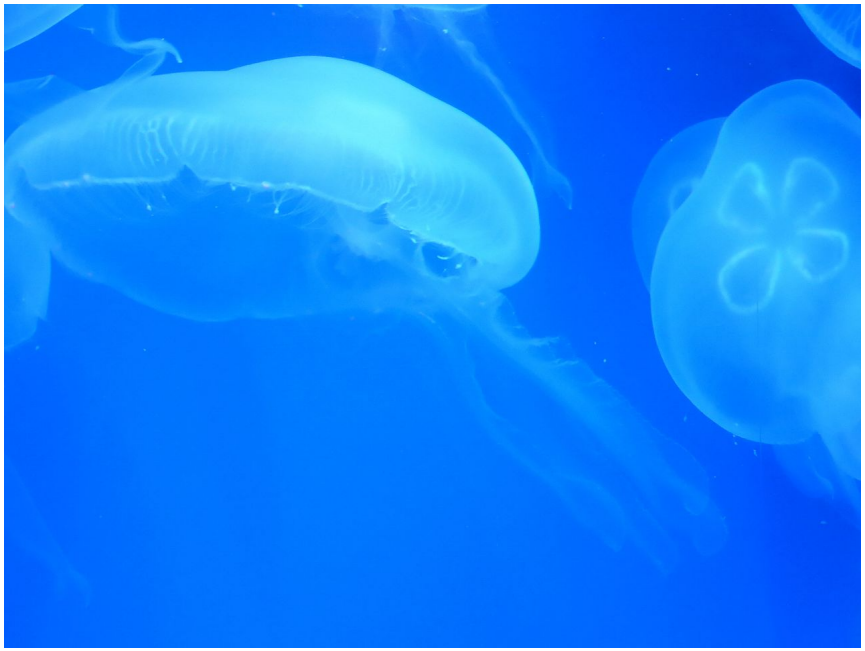


Class *model* visualisation

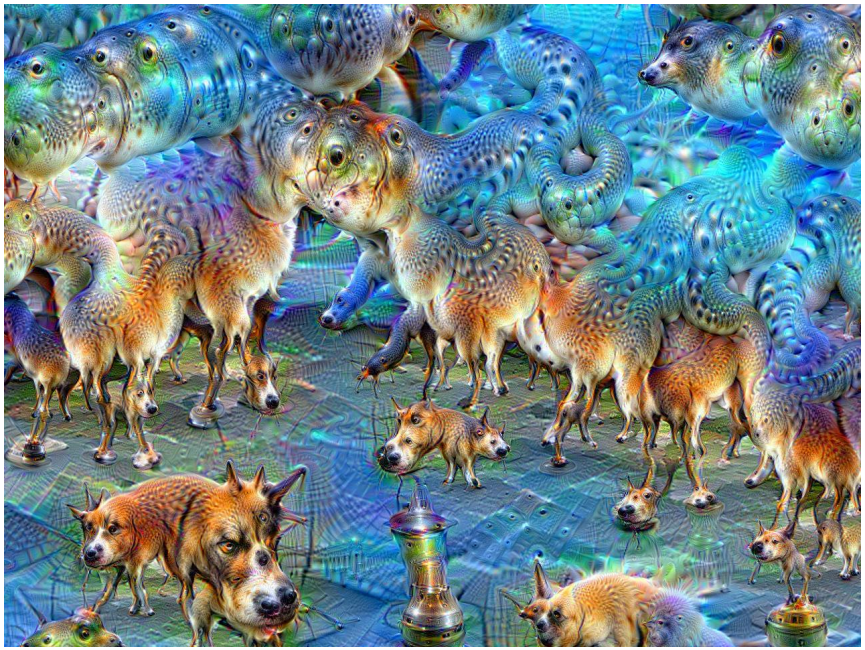
† *Simonyan, Vedaldi, Zisserman* ***Deep Inside Convolutional Networks: Visualising Image Classification Models and Saliency Maps****, arXiv preprint arXiv:1312.6034, 2013*

Visualising CNNs

- Similar idea with Inception architecture of Google : “Deep Dream”
- Maximise a class from input image



Input image

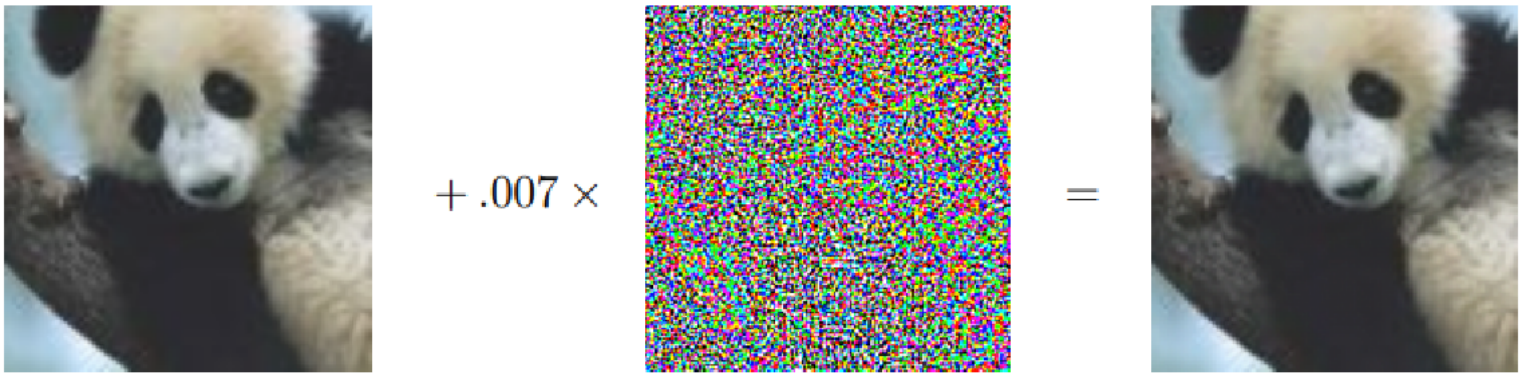


Maximising “dogs” category

Deepdream - a code example for visualizing neural networks, *Mordvintsev, A., Olah, C. and Tyka, M., Google Research, 2015*

Adversarial examples

- We often get the impression that CNNs are the end all and be all of AI
- Consistently produce state-of-the-art results on images
- However, CNNs **are not infallible** : adversarial examples[†] !



- How was this image created ???

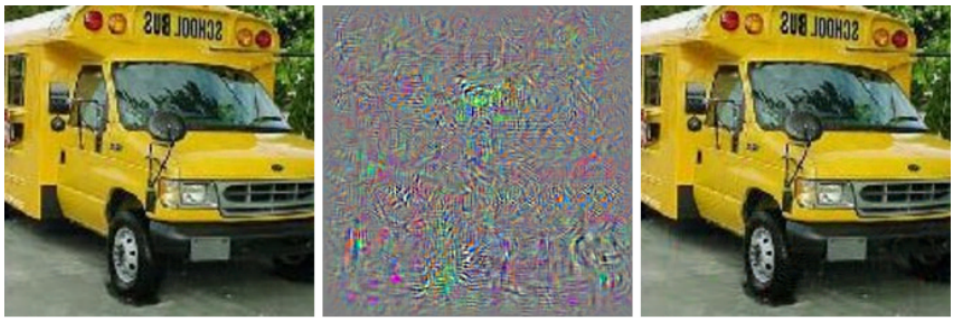
[†] ***Intriguing properties of neural networks***, *Szegedy, C. et al, arXiv preprint arXiv:1312.6199, 2013*

Adversarial examples

- Szegedy et al. propose[†] add a small perturbation r that fools the classifier network f into choosing the wrong class c for $\hat{x} = x + r$

$$\arg\min_r |r|_2^2, \ \text{s.t}\ f(x+r) = c, \ x + r \in [0,1]^n$$

- $\hat{x}$ is the closest example to x s.t $\hat{x}$ is classified as in class c
- Minimisation with box-constrained L-BFGS algorithm

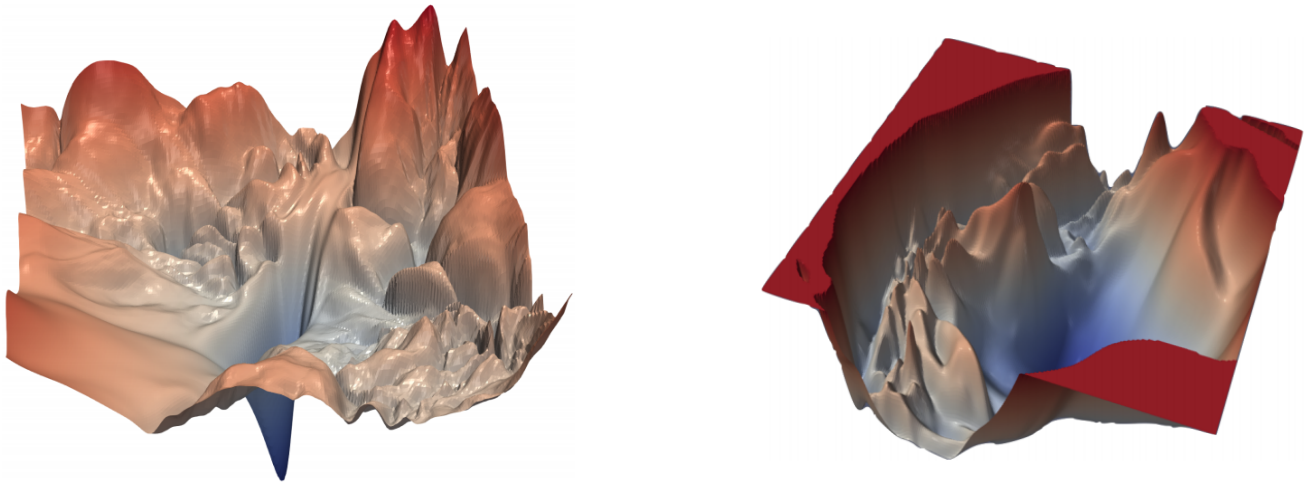


x r $\hat{x}$

[†] ***Intriguing properties of neural networks***, *Szegedy, C. et al, arXiv preprint arXiv:1312.6199, 2013*

Adversarial examples

- Common explanation : the space of images is very high-dimensional, and contains many areas that are unexplored during training time



Example of loss surfaces in commonly used networks (Res-Nets)

Illustration from ***Visualizing the Loss Landscape of Neural Nets****, Li, H et al, NIPS, 2018*

Adversarial examples

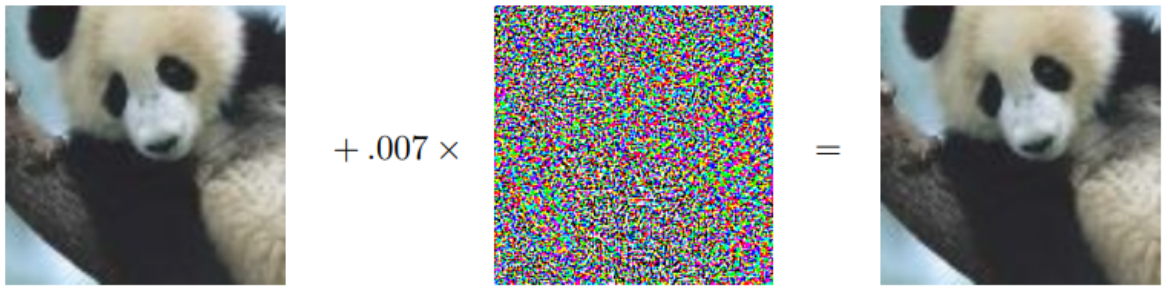
- Many approaches to adversarial examples exist. Goodfellow et al.[†] propose a principled way of creating these
- Consider the output of a fully connected layer $\langle w, \hat{x} \rangle = \langle w, x \rangle + \langle w, r \rangle$
- Let us set $r = \text{sign}(w)$. What happens to $\langle w, \hat{x} \rangle$?
  - Increase by nm as dimension n increases (m is average value of w)
  - However, $|r|_\infty$ does not increase with n
- Conclusion : we can add a small vector r that increases the output response $\langle w, \hat{x} \rangle$

[†] ***Explaining and Harnessing Adversarial Examples***, *Goodfellow, I.J, Shlens, J. and Szegedy, C., ICLR 2015*

Adversarial examples

- Goodfellow et al. consider a local linearisation of the network's loss around θ
  - $\mathcal{L}(x_0) \approx f(x_0) + w\nabla_x \mathcal{L}(\theta, x_0, y_0)$
- Thus, the perturbation image $\hat{x}$ is set to

$$\hat{x} = x + \epsilon \text{sign}(\nabla_x \mathcal{L}(\theta, x, y))$$



$\boldsymbol{x}$
"panda"
57.7% confidence

$\text{sign}(\nabla_{\boldsymbol{x}} J(\boldsymbol{\theta}, \boldsymbol{x}, y))$
"nematode"
8.2% confidence

$\boldsymbol{x} +$
$\epsilon \text{sign}(\nabla_{\boldsymbol{x}} J(\boldsymbol{\theta}, \boldsymbol{x}, y))$
"gibbon"
99.3 % confidence

† ***Explaining and Harnessing Adversarial Examples***, *Goodfellow, I.J, Shlens, J. and Szegedy, C., ICLR 2015*

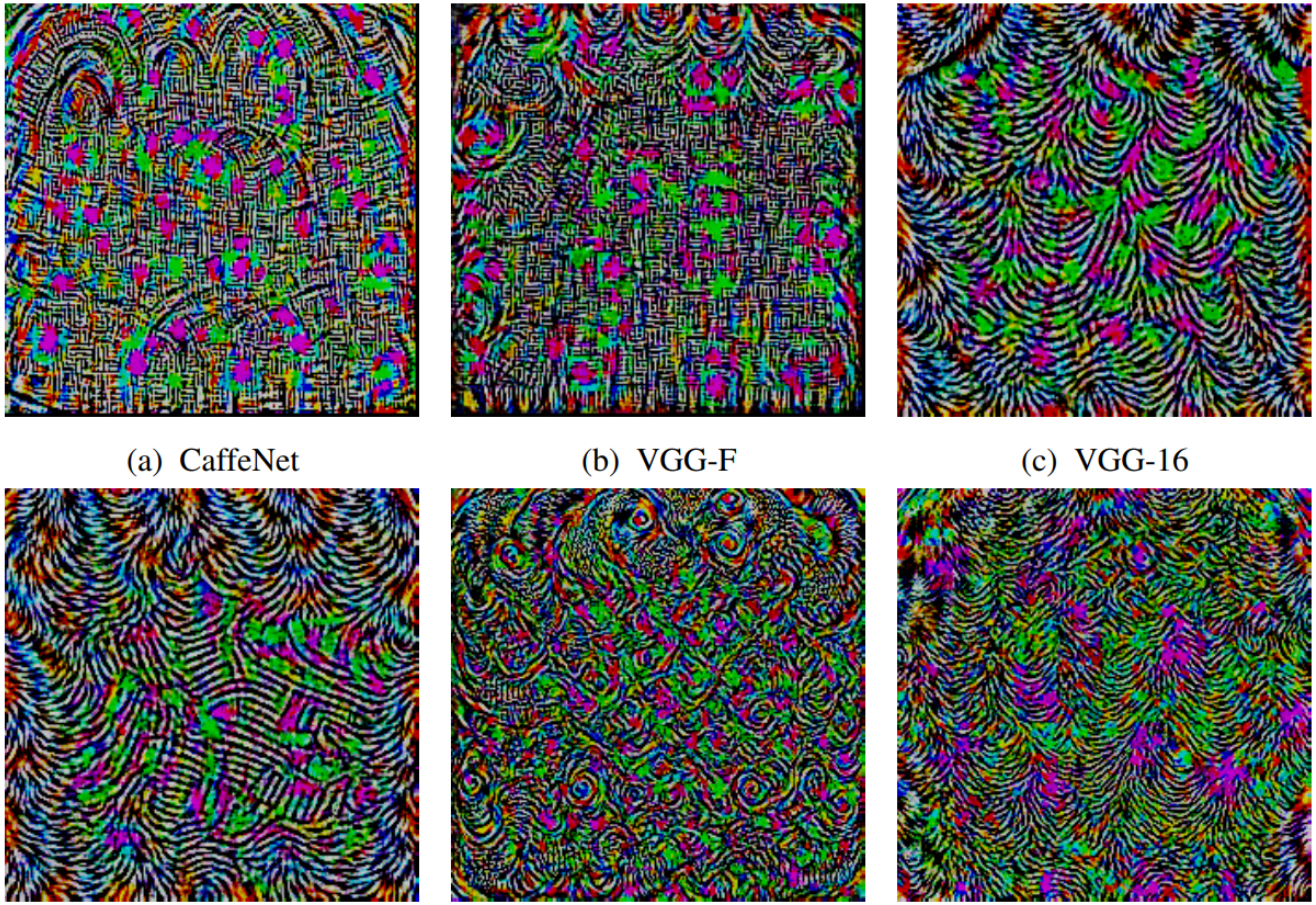
Adversarial examples

- Even worse, it is possible to create **universal adversarial** examples†
- Perturbations that fool a network for any image class

- Simple algorithm : initialise perturbation r, go through database adding specific perturbations to r, project onto set $\{ r, ||r|| < \varepsilon \}$
- What do these perturbations look like ?

† ***Universal adversarial perturbations***, *Moosavi-Dezfooli, S-M, et al arXiv preprint (2017)*

Adversarial examples



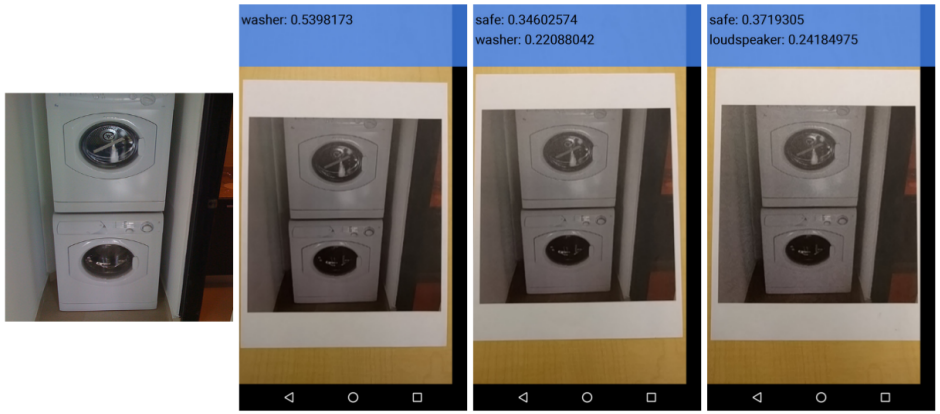
(a) CaffeNet (b) VGG-F (c) VGG-16

(d) VGG-19 (e) GoogLeNet (f) ResNet-152

† ***Universal adversarial perturbations***, *Moosavi-Dezfooli, S-M, et al arXiv preprint (2017)*

Adversarial examples

- Conclusion : CNNs are not necessarily robust
- Adversarial examples are a significant problem :
  - Even **printed photos** of adversarial examples work[†]



(a) Image from dataset (b) Clean image (c) Adv. image, $\epsilon = 4$ (d) Adv. image, $\epsilon = 8$

- Explaining and resisting adversarial examples is currently a hot research topic

[†] ***Adversarial Examples in the Physical World***, *Kurakin, A., Goodfellow, I. J, Bengio, S. et al. ICLR workshop, 2017*

Conclusion

- CNNs represent the state-of-the art in many different domains/problems
- If you have an unsolved problem, there is a good chance CNNs will produce a good/excellent result
- **However : theoretical understanding is still relatively limited**
  - This leads to problems such as adversarial examples
  - It is not clear whether CNNs are truly robust/generalisable
  - This is a hot research topic, important if CNNs are to be used in industrial applications
- 14/11/2019 : last lab work, on CNNs