

# Flipped Assignment 13

Group 5

2022/3/31

## Input Data

```
setwd('G:/OneDrive - Texas Tech University/IE 5344 Statistical Data Analysis/Flipped Assignment 13')
data <- read.csv('data-heartbeat-3.csv', header = TRUE)
dat <- data %>%
  na_if("") %>%
  na.omit
dat <- dat[,-c(5,6,7,8,9,10)]
colnames(dat) <- c('y', 'x1', 'x2', 'x3', 'x4')
head(dat)
```

```
##      y x1 x2 x3  x4
## 51 72 AS  2  M Some
## 52 68 AS  4  M Yes
## 53 88 AS  3  M Some
## 54 80 AS  3  M Yes
## 55 96 AS  3  M Yes
## 56 68 AF  3  M No
```

## Part a.

Continent is categorical.

```
dat$x1 <- as.factor(dat$x1)
fit1 <- lm(y ~ x1, dat)
summary(fit1)
```

```
##
## Call:
## lm(formula = y ~ x1, data = dat)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -9.667 -5.667 -1.667  2.333 18.333
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    71.000      3.842  18.479 3.13e-11 ***
## x1AS           6.667      4.436   1.503  0.155
## x1SA           1.000      8.591   0.116  0.909
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
```

```
## Residual standard error: 7.684 on 14 degrees of freedom
## Multiple R-squared:  0.1522, Adjusted R-squared:  0.03107
## F-statistic: 1.257 on 2 and 14 DF,  p-value: 0.3148
```

We don't think continent is significant because p-values of both its coded variables are greater than 0.05. Moreover, the p-value of whole model is also greater than 0.05. For parameters' interpretation, when an observation is from Africa, his/her heartbeat is expected to be 71 bpm. If an observation is from Asia, his/her heartbeat is expected to be 77.667 bpm. If an observation is from South America, his/her heartbeat is expected to be 72 bpm.

## Part b.

Exercise frequency is ordinal. Assume that the marginal response is fixed.

```
str(dat)

## 'data.frame':  17 obs. of  5 variables:
## $ y : int  72 68 88 80 96 68 80 80 72 76 ...
## $ x1: Factor w/ 3 levels "AF","AS","SA": 2 2 2 2 2 1 1 2 2 2 ...
## $ x2: int   2 4 3 3 3 3 2 4 2 1 ...
## $ x3: chr   "M" "M" "M" "M" ...
## $ x4: chr  "Some" "Yes" "Some" "Yes" ...

fit2 <- lm(y ~ x2, dat)
summary(fit2)

##
## Call:
## lm(formula = y ~ x2, data = dat)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -9.500 -5.000 -2.667  3.000 20.167
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   72.333      6.012  12.032 4.17e-09 ***
## x2             1.167      1.936   0.603  0.556
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 7.967 on 15 degrees of freedom
## Multiple R-squared:  0.02365, Adjusted R-squared: -0.04144
## F-statistic: 0.3633 on 1 and 15 DF,  p-value: 0.5557
```

We don't think exercise frequency is significant because its p-value greater than 0.05. Moreover, the p-value of whole model is also greater than 0.05. For parameters' interpretation, when the level of exercise frequency increases by 1, the expected increase in heartbeat is 1.167 bpm.

## Part c.

Exercise frequency is ordinal. Assuming that the marginal response varies, it is treated categorical.

```
dat$x2 <- as.factor(dat$x2)
str(dat)

## 'data.frame':  17 obs. of  5 variables:
## $ y : int  72 68 88 80 96 68 80 80 72 76 ...
```

```
## $ x1: Factor w/ 3 levels "AF","AS","SA": 2 2 2 2 2 1 1 2 2 2 ...
## $ x2: Factor w/ 4 levels "1","2","3","4": 2 4 3 3 3 3 2 4 2 1 ...
## $ x3: chr "M" "M" "M" "M" ...
## $ x4: chr "Some" "Yes" "Some" "Yes" ...
```

```
fit3 <- lm(y ~ x2, dat)
summary(fit3)
```

```
##
## Call:
## lm(formula = y ~ x2, data = dat)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -11.333  -6.000  -2.667   5.333  16.667
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    70.000     5.620  12.454 1.34e-08 ***
## x22             4.667     7.256   0.643   0.531
## x23             9.333     6.490   1.438   0.174
## x24             4.667     6.490   0.719   0.485
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 7.949 on 13 degrees of freedom
## Multiple R-squared:  0.1577, Adjusted R-squared:  -0.03673
## F-statistic: 0.8111 on 3 and 13 DF,  p-value: 0.5102
```

We don't think exercise frequency is significant because p-values of all its coded variables are greater than 0.05. Moreover, the p-value of whole model is also greater than 0.05. For parameters' interpretation, when an observation's exercise frequency is 1, his/her heartbeat is expected to be 70 bpm. If an observation's exercise frequency is 2, his/her heartbeat is expected to be 74.667 bpm. If an observation's exercise frequency is 3, his/her heartbeat is expected to be 79.333 bpm. If an observation's exercise frequency is 4, his/her heartbeat is expected to be 74.667 bpm.

## Part d.

### (1)

We consider the marginal effects of  $x_2$  and  $x_4$  to vary because we have no background knowledge for their effects. Assuming the marginal effects of them gives flexibility to do regression. The full model is

```
dat$x4 <- as.factor(dat$x4)
dat$x3 <- as.factor(dat$x3)
str(dat)
```

```
## 'data.frame':  17 obs. of  5 variables:
## $ y : int  72 68 88 80 96 68 80 80 72 76 ...
## $ x1: Factor w/ 3 levels "AF","AS","SA": 2 2 2 2 2 1 1 2 2 2 ...
## $ x2: Factor w/ 4 levels "1","2","3","4": 2 4 3 3 3 3 2 4 2 1 ...
## $ x3: Factor w/ 2 levels "F","M": 2 2 2 2 2 2 2 1 1 2 ...
## $ x4: Factor w/ 3 levels "No","Some","Yes": 2 3 2 3 3 1 2 2 1 2 ...
```

```
fit4 <- lm(y ~., dat)
summary(fit4)
```

```
##
## Call:
## lm(formula = y ~ ., data = dat)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -9.820 -3.564 -1.085  1.277 13.597
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   67.470     10.912   6.183 0.000264 ***
## x1AS           3.573       5.634   0.634 0.543660
## x1SA          -1.349     10.688  -0.126 0.902674
## x22            2.234       8.424   0.265 0.797590
## x23            6.905       7.575   0.912 0.388620
## x24            1.424       8.466   0.168 0.870576
## x3M           -2.384       7.973  -0.299 0.772533
## x4Some         6.256       5.581   1.121 0.294878
## x4Yes          6.839       6.536   1.046 0.325933
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 8.717 on 8 degrees of freedom
## Multiple R-squared:  0.3765, Adjusted R-squared:  -0.2469
## F-statistic: 0.6039 on 8 and 8 DF,  p-value: 0.7542
```

Here we remove the variable that has the largest p-value, which is continent. The model becomes

```
dat <- dat[, -2]
fit5 <- lm(y ~ ., dat)
summary(fit5)
```

```
##
## Call:
## lm(formula = y ~ ., data = dat)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -9.784 -3.154 -1.693  2.370 14.307
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   70.528     9.212   7.656 1.73e-05 ***
## x22            2.071       7.795   0.266  0.796
## x23            8.154       6.816   1.196  0.259
## x24            1.614       7.729   0.209  0.839
## x3M           -4.157       7.016  -0.593  0.567
## x4Some         7.260       4.961   1.463  0.174
## x4Yes          7.169       5.866   1.222  0.250
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 8.069 on 10 degrees of freedom
## Multiple R-squared:  0.3322, Adjusted R-squared:  -0.06846
## F-statistic: 0.8291 on 6 and 10 DF,  p-value: 0.5732
```

Removing exercise frequency, the model becomes

```
dat <- dat[,-2]
fit6 <- lm(y ~., dat)
summary(fit6)
```

```
##
## Call:
## lm(formula = y ~ ., data = dat)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -9.333 -5.333 -1.333  2.286 18.667
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   72.571      6.115  11.868 2.39e-08 ***
## x3M           -1.714      6.219  -0.276   0.787
## x4Some         6.857      4.818   1.423   0.178
## x4Yes          6.476      4.971   1.303   0.215
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 7.949 on 13 degrees of freedom
## Multiple R-squared:  0.1577, Adjusted R-squared:  -0.03673
## F-statistic: 0.8111 on 3 and 13 DF,  p-value: 0.5102
```

Removing gender, the model becomes

```
dat <- dat[,-2]
fit7 <- lm(y ~., dat)
summary(fit7)
```

```
##
## Call:
## lm(formula = y ~ ., data = dat)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -9.333 -5.333 -1.333  2.000 18.667
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   71.200      3.435  20.725 6.63e-12 ***
## x4Some         6.800      4.652   1.462   0.166
## x4Yes          6.133      4.652   1.319   0.208
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 7.682 on 14 degrees of freedom
## Multiple R-squared:  0.1527, Adjusted R-squared:  0.0317
## F-statistic: 1.262 on 2 and 14 DF,  p-value: 0.3134
```