Results Exp and GPR Uncertainties

February 23, 2022

1 Results with GPR and experimental uncertainties

This workbook propagates the uncertainties from experimental repeats and GPR model variance into the final ternary compositions.

```
[251]: # import packages
       import os, sys, platform
       import numpy as np
       import pandas as pd
       import GPy
       import matplotlib.pyplot as plt
       from matplotlib import gridspec
       print('Python version', sys.version)
       print('Running on', platform.system())
       # colours (From Birmingham With Love)
       jade = np.array([0, .66, .436]) # statue green
       blue = np.array([.057, .156, .520]) # hey there mr blue
       brown = np.array([.515, .158, .033]) # did someone order CDM?
       red = np.array([.85, .20, 0]) # tikka masala
       gold = np.array([1, .67, .14]) # Staffordshire hoard
       claret = np.array([.429, .073, .238]) # claret
       grey = np.array([.585, .612, .675]) # library grey
       black = np.array([0,0,0]) # this is a black
```

Python version 3.10.2 (v3.10.2:a58ebcc701, Jan 13 2022, 14:50:16) [Clang 13.0.0 (clang-1300.0.29.30)]
Running on Darwin

1.1 Averaging uncertainties

- $\sigma_{\rm exp}$: Standard deviation from across the repeated Hittorf experiment measurements
- σ_{GPR} : Standard deviation from GPR model used to infer the composition

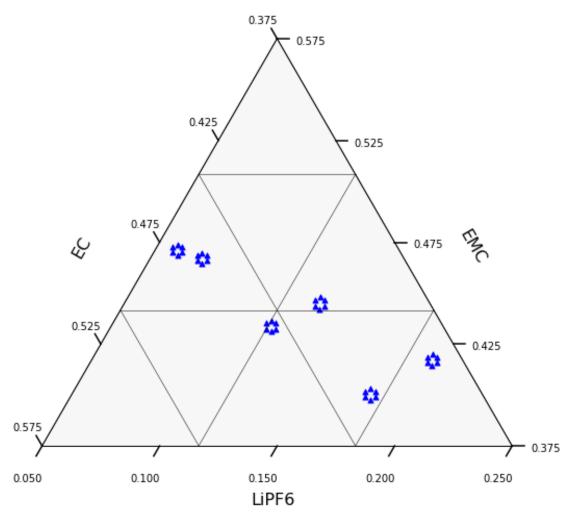
Combined uncertainty is then given by:

$$\sigma = \sqrt{\sigma_{\rm exp}^2 + \sigma_{\rm GPR}^2}$$

```
[249]: #Define a function that combines uncertainties and adds/subtracts to the
       ⇔ternary dataset
      #-----
      def combine_uncertainties(results_path):
          #Results file
          df = pd.read_csv (results_path)
          df = df[(df.side == 'anodic') | (df.side == 'cathodic')]
          #GPR standard deviations
          sd_gpr = np.mean(df.stdev)*np.array([1,1,1]) #For each species
          #Experimental standard deviations
          anodic = df[df.side == 'anodic'][['xLi','xEMC','xEC']].to_numpy()
          x_anodic = np.mean(anodic,0) #mean
          sd_exp_anodic = np.std(anodic,0)
          cathodic = df[df.side == 'cathodic'][['xLi','xEMC','xEC']].to_numpy()
          x_cathodic = np.mean(cathodic,0) #mean
          sd_exp_cathodic = np.std(cathodic,0)
          #Combining the two sources of uncertainty:
          sd_anodic = np.sqrt(sd_gpr**2 + sd_exp_anodic**2)
          sd_cathodic = np.sqrt(sd_gpr**2 + sd_exp_cathodic**2)
          #Each average ternary point needs to have uncertainty included in 6_{\sqcup}
       \rightarrow directions
          from itertools import permutations
          def unique_permutations(iterable, r=None):
             previous = tuple()
             for p in permutations(sorted(iterable), r):
                 if p > previous:
                     previous = p
                     yield p
          #2 groups for anodic and cathodic compositions where you +err and -1/2 err
       ⇔to the other 2
          perm = np.array(list(unique_permutations([1, -0.5, -0.5])))
          perm = np.append(perm,perm*-1,0)
          perm = np.tile(perm,(2,1))
          x_{array} = p_{vstack}((p_{tile}(x_{anodic}, (6,1)), p_{tile}(x_{cathodic}, (6,1)))) 
       →#Tile average ternary compositions
          sd_array = np.vstack((np.tile(sd_anodic,(6,1)), np.
```

```
return x_with_uncertainties
[240]: #Apply the uncertainties to each composition tested, and output arrays with
       →uncertainties included
      # Processing 55050
      results_path = 'results/Result_Summary_55050.csv'
      x1 = combine_uncertainties(results_path)
      # Processing 55100
      results_path = 'results/Result_Summary_55100.csv'
      x2 = combine_uncertainties(results_path)
      # Processing 55150
      results_path = 'results/Result_Summary_55150.csv'
      x3= combine_uncertainties(results_path)
      #Stack all points together
      x_data = np.vstack((x1,x2,x3))
[252]: #Plot the polarized ternary compositions
      #----
      import ternary
      fig = ternary.plt.figure(figsize=(15, 8))
      ax = fig.add_subplot(2, 1, 2)
      tax = ternary.TernaryAxesSubplot(ax=ax,scale=30)
      axes_colors = {'b': 'k', 'r': 'k', 'l': 'k'}
      tax.boundary(linewidth=1.0, axes colors=axes colors)
      tax.gridlines(color="k", multiple=10, linewidth=0.5, ls='-')
      tax.ax.axis("equal")
      tax.ax.axis("off")
      fontsize = 16
      # tax.set_title("Zoomed region", color='r')
      tax.left_axis_label("EC", fontsize=fontsize, offset=0.17, color='k')
      tax.right_axis_label("EMC", fontsize=fontsize, offset=0.17, color='k')
      tax.bottom_axis_label("LiPF6", fontsize=fontsize, offset=0.03, color='k')
```

x_with_uncertainties = x_array + (sd_array*perm)



[]:[