

## Andrew Moore, 09/26/2021

### MATH-471, Homework 3.2

#### Question 1.

Read Ch.4.10 in the textbook and do the following questions from the textbook: pp. 222-223: 4.65, 4.66, 4.70, 4.72.

#### 4.65

Let  $y$  be a random variable having a normal distribution with a mean equal to 250 and a standard deviation equal to 50. Find the following probabilities:

- $P(y > 250)$
- $P(y > 150)$
- $P(150 < y < 350)$
- Find  $k$  such that  $P(250 - k < y < 250 + k) = .60$

#### 4.66

Suppose that  $y$  is a random variable having a normal distribution with a mean equal to 250 and a standard deviation equal to 10.

- Show that the event  $y < 260$  has the same probability as  $z < 1$ .
- Convert the event  $y > 230$  to the  $z$ -score equivalent.
- Find  $P(y < 260)$  and  $P(y > 230)$ .
- Find  $P(y > 265)$ ,  $P(y < 242)$ , and  $P(242 < y < 265)$ .

#### 4.70

The College Boards, which are administered each year to many thousands of high school students, are scored so as to yield a mean of 513 and a standard deviation of 130. These scores are close to being normally distributed. What percentage of the scores can be expected to satisfy each of the following conditions?

- Greater than 600
- Greater than 700
- Less than 450
- Between 450 and 600

#### 4.72

Refer to Exercise 4.70. An honor society wishes to invite those scoring in the top 5% on the College Boards to join their society.

- What score is required to be invited to join the society?

- b. What score separates the top 75% of the population from the bottom 25%? What do we call this value?

## Question 2.

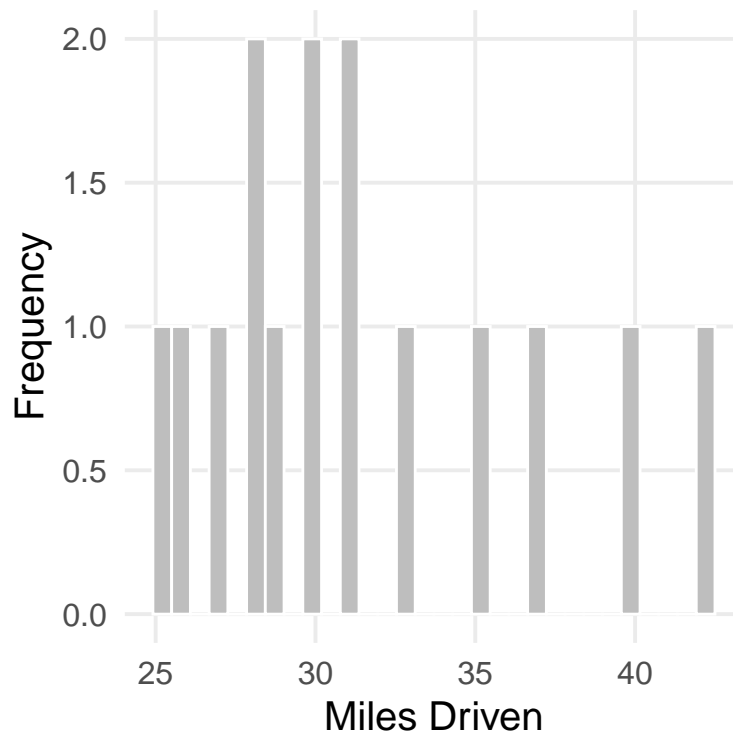
A consumer testing agency wants to evaluate the claim made by a manufacturer of discount tires. The manufacturer claims that their tires can be driven at least 35,000 miles before wearing out. To determine the average number of miles that can be obtained from the manufacturer's tires, the agency randomly selects 60 tires from the manufacturer's warehouse and places the tires on 15 cars driven by test drivers on a 2-mile oval track. The number of miles driven (in thousands of miles) until the tires are determined to be worn out is given in the following table.

| Car          | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  | 10 | 11 | 12 | 13 | 14 | 15 |
|--------------|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| Miles driven | 25 | 27 | 35 | 42 | 28 | 37 | 40 | 31 | 29 | 33 | 30 | 26 | 31 | 28 | 30 |

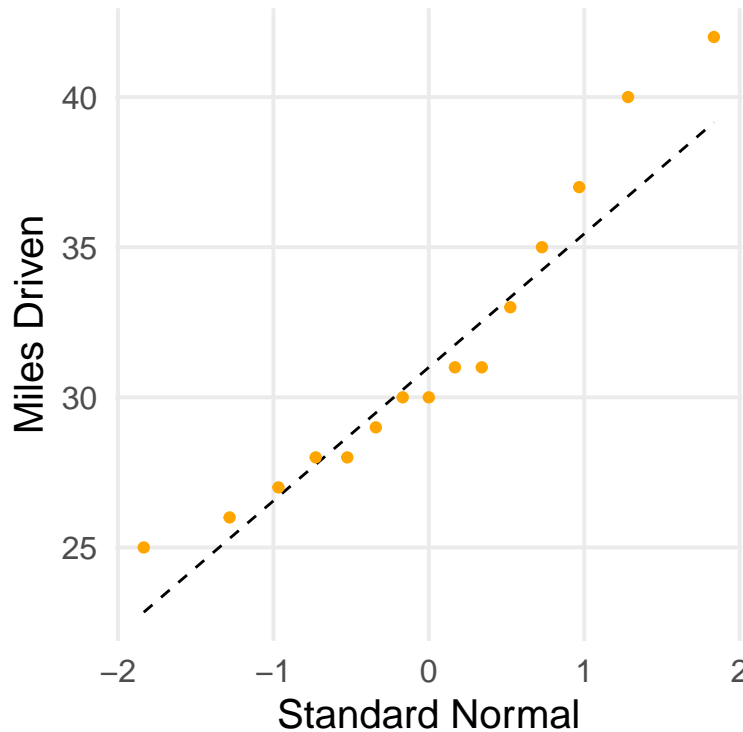
- a. Describe the descriptive statistics about the variable 'Miles driven'. Also describe the shape of its distribution.
- b. Estimate a population distribution of 'Miles driven' using Q-Q plot.
- a. Below is a table of descriptive statistics for the sample of cars, and a histogram.

Table 2: Descriptive statistics for the sample of cars.

| N (# cars) | Mean | Median | SD | 25th Pctile. | 75th Pctile. | Range    |
|------------|------|--------|----|--------------|--------------|----------|
| 15         | 31.5 | 30     | 5  | 28           | 34           | [25, 42] |



- b. Below is a QQ-plot of the sample of cars.



### Question 3.

Read Ch.4.14 in the textbook and submit the following questions from the textbook: pp. 227-229: 4.94 and 4.114.

#### 4.94

The fracture toughness in concrete specimens is a measure of how likely it is that blocks used in new home construction may fail. A construction investigator obtains a random sample of 15 concrete blocks and determines the following toughness values:

```
blocks <- c(.47, .58, .67, .70, .77, .79, .81, .82, .84, .86, .91, .95, .98, 1.01, 1.04)
```

- Use a normal quantile plot to assess whether the data appear to fit a normal distribution.
- Compute the correlation coefficient and p-value for the normal quantile plot. Comment on the degree of fit of the data to a normal distribution.

#### 4.114

As part of a study to determine factors that may explain differences in animal species relative to their size, the following body masses (in grams) of 50 different bird species were reported in the paper “Temperature and the Northern Distributions of Wintering Birds,” by Richard Repasky (1991).

```
mass <- c(
  7.7, 10.1, 21.6, 8.6, 12.0, 11.4, 16.6, 9.4, 11.5, 9.0, 8.2, 20.2, 48.5, 21.6,
  26.1, 6.2, 19.1, 21.0, 28.1, 10.6, 31.6, 6.7, 5.0, 68.8, 23.9, 19.8, 20.1, 6.0,
  99.6, 19.8, 16.5, 9.0, 448.0, 21.3, 17.4, 36.9, 34.0, 41.0, 15.9, 12.5, 10.2,
```

31.0, 21.5, 11.9, 32.5, 9.8, 93.9, 10.9, 19.6, 14.5

)

- a. Does the distribution of the body masses appear to follow a normal distribution? Provide both a graphical and a quantitative assessment.
- b. Repeat part (a), with the outlier 448.0 removed.
- c. Determine the sample mean and median with and without the value 448.0 in the data set.
- d. Determine the sample standard deviation and MAD with and without the value 448.0 in the data set.