4/28/22, 10:50 PM

```
In [1]: # Initialize Otter
import otter
grader = otter.Notebook("lab4-smoothing.ipynb")
In [2]: import numpy as np
import pandas as pd
import altair as alt

pd.options.mode.chained_assignment = None # default='warn'
```

# Lab 4: Smooth visuals

So far, you've encountered a number of visualization techniques for displaying tidy data. In those visualizations, all graphic elements represent the values of a dataset -- they are visual displays of actual data.

In general, smoothing means evening out. Visualizations of actual data are often irregular -- points are distributed widely in scatterplots, line plots are jagged, bars are discontinuous. When we look at such visuals, we tend to attempt to look past these irregularities in order to discern patterns -- for example, the overall shape of a histogram or the general trend in a scatterplot. Showing what a graphic might look like with irregularities evened out often aids the eye in detecting pattern. This is what **smoothing** is: **evening out irregularities in graphical displays of actual data**.

For our purposes, usually smoothing will consist in drawing a line or a curve on top of an existing statistical graphic. From a technical point of view, this amounts to adding derived geometric objects to a graphic that have fewer irregularities than the displays of actual data.

#### **Objectives**

In this lab, you'll learn some basic smoothing techniques -- kernel density estimation, LOESS, and linear smoothing via regression -- and how to implement them in Altair. Your focus will be on understanding the techniques graphically, not mathematically.

In Altair, smoothed geometric objects are constructed and plotted through what Altair describes as *transforms* -- operations that modify a dataset. Try not to get too attached to this terminology -- 'transform' and 'transformation' are used to mean a variety of things in other contexts. You'll begin with a brief introduction to Altair transforms before turning to smoothing techniques.

The **sections** of the lab are divided as follows:

- 1. Introduction to Altair transforms
- 2. Histogram smoothing: kernel density estimamtion
- 3. Scatterplot smoothing: LOESS and linear smoothing
- 4. A neat graphic

And our main **goals** are:

- Get familiar with Altair transforms for dataframe operations: filter, bin, aggregate, calculate.
- 'Handmande' histograms: step-by-step construction
- Implement kernel density estimation via .transform\_density(...)

77.8

- Implement LOESS via .transform\_loess(...)
- Implement linear smoothing via transform\_regression(...)

You'll use the same data as last week to stick to a familiar example:

```
In [3]: # import tidied lab 3 data
         data = pd.read_csv('data/lab3-data.csv')
         data.head()
Out[3]:
            Country Name Year Life Expectancy Male Life Expectancy Female Life Expectancy GDP per capita region
                                                                                                                    sub-region Population
               Afghanistan 2019
                                                                                            507.103432
                                                                                                                  Southern Asia 38041754.0
                                                                                                                 Southern Asia 34413603.0
               Afghanistan 2015
                                          61.7
                                                              61.0
                                                                                    62.3
                                                                                            578.466353
               Afghanistan 2010
                                          59.9
                                                              59.6
                                                                                    60.3
                                                                                            543.303042
                                                                                                                 Southern Asia 29185507.0
                  Albania 2019
                                          78.0
                                                              76.3
                                                                                    79.9
                                                                                           5353.244856 Europe Southern Europe
```

# O. Background: transforms in Altair

Albania 2015

In Altair, operations that modify a dataset are referred to as *transforms*. Mostly, these are operations that could be performed manually with ease -- the utility of transforms is that they wrap common operations within plotting commands, although they also make plotting codes more verbose.

3952.801215 Europe Southern Europe

Transforms encompass a broad range of types of operations, from relatively simple ones like filtering to more complex ones like smoothing. Here you'll see a few intuitive transforms in Altair that integrate simple dataframe manipulations into the plotting process.

You'll focus on the construction of histograms as a sort of case study. This will be a useful primer for histogram smoothing in the next section.

76.1

# Filter transform

34

46

50 54 58

Life Expectancy at Birth

62

Last week you saw a way to make histograms. As a quick refresher, to make a histogram of life expectancies across the globe in 2010, one can filter the data and then plot using the following commands:

```
In [4]: # filter
         data2010 = data[data.Year == 2010]
         # plot
         alt.Chart(data2010).mark_bar().encode(
             x = alt.X('Life Expectancy',
                       bin = alt.Bin(step = 2),
                       title = 'Life Expectancy at Birth'),
             y = 'count()'
          24
Out[4]:
          22
           20
           18
           16
         ਰ 14
         of Re
```

However, the filtering step can be handled within the plotting commands using .transform\_filter().

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50 54 58 62 66 70 74 78 82

Life Expectancy at Birth

This uses a helper command to specify the filtering condition -- in the above example, the filtering condition is that Year is equal to 2010. A filtering condition is referred to in Altair as a 'field predicate'. In the above example:

- filtering field: Year
- field predicate: equals 2010

There are different helpers for different types of field predicates -- you can find a complete list in the documentation.

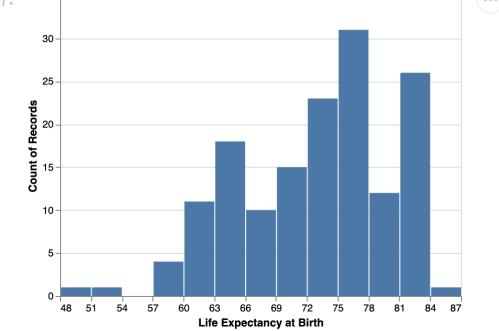
Here is how to use <a href="transform\_filter">transform\_filter</a>() to make the same histogram shown above, but skipping the step of storing a subset of the data under a separate name:

```
In [5]: # filter and plot
         alt.Chart(data).transform_filter(
             alt.FieldEqualPredicate(field = 'Year',
                                      equal = 2010)
         ) • mark_bar() • encode(
             x = alt.X('Life Expectancy',
                       bin = alt.Bin(step = 2),
                       title = 'Life Expectancy at Birth'),
             y = 'count()'
           24
Out[5]:
           22
           20
           18
           16
        16-
14-
12-
```

#### Question 0a. Filter transform

30 34 38 42 46

Construct a histogram of life expectancies across the globe in 2019 using a filter transform as shown above to filter the appropriate rows of the dataset. Use a bin size of three (not two) years.



# Bin transform

The codes above provide a sleek way to construct the histogram that handles binning via arguments to alt.X(...). However, binning actually involves an operation: creating a new variable that is a discretization of an existing variable into contiguous intervals of a specified width.

To illustrate, have a look at how the histogram could be constructed 'manually' by the following operations.

- 1. Bin life expectancies
- 2. Count values in each bin
- 3. Make a bar plot of counts against bin centers.

Here's step 1:

Out

In [7]: # bin life expectancies into 20 contiguous intervals
 data2010['Bin'] = pd.cut(data2010["Life Expectancy"], bins = 20) #cut is used to sort values into bins
 data2010.head()

t[7]:		<b>Country Name</b>	Year	Life Expectancy	Male Life Expectancy	Female Life Expectancy	GDP per capita	region	sub-region	Population	Bin
	2	Afghanistan	2010	59.9	59.6	60.3	543.303042	Asia	Southern Asia	29185507.0	(59.57, 62.14]
	5	Albania	2010	76.2	74.2	78.3	4094.350334	Europe	Southern Europe	2913021.0	(74.99, 77.56]
	9	Algeria	2010	75.9	75.0	76.8	4479.341720	Africa	Northern Africa	35977455.0	(74.99, 77.56]
	13	Angola	2010	58.1	55.8	60.5	3587.883798	Africa	Sub-Saharan Africa	23356246.0	(57.0, 59.57]
	<b>17</b> Ar	ntigua and Barbuda	2010	75.9	73.6	78.2	13049.257050	Americas	Latin America and the Caribbean	88028.0	(74.99, 77.56]

Here's step 2:

```
In [8]: # count values in each bin and store midpoints
    histdata = data2010.loc[:, ['Life Expectancy', 'Bin']].groupby('Bin').count()
    histdata['Bin midpoint'] = histdata.index.values.categories.mid.values
    histdata
```

Life Expectancy Bin midpoint Out[8]: Bin (31.249, 33.87] 32.5595 (33.87, 36.44] 35.1550 (36.44, 39.01] 0 37.7250 (39.01, 41.58] 40.2950 (41.58, 44.15] 42.8650 0 45.4350 (44.15, 46.72] (46.72, 49.29] 3 48.0050 (49.29, 51.86] 50.5750 (51.86, 54.43] 53.1450 55.7150 (54.43, 57.0] (57.0, 59.57] 11 58.2850 (59.57, 62.14] 60.8550 (62.14, 64.71] 8 63.4250 (64.71, 67.28] 65.9950 (67.28, 69.85] 12 68.5650 (69.85, 72.42] 16 71.1350 73.7050 (72.42, 74.99] 24 (74.99, 77.56] 24 76.2750 (77.56, 80.13] 10 78.8450

And finally, step 3:

(80.13, 82.7]

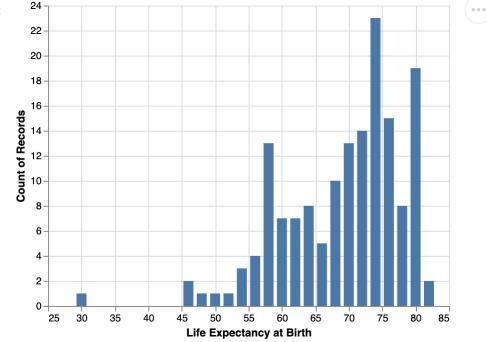
```
In [9]: # plot histogram
         alt.Chart(histdata).mark_bar(width = 10).encode(
             x = 'Bin midpoint',
             y = alt.Y('Life Expectancy', title = 'Count')
Out[9]:
           22
           20
           18
           16
           14
         Count 12
           10
           2
                35
                      40
                           45
                                50
                                          60
                                     55
                                    Bin midpoint
```

20

81.4150

Well, these operations can be articulated as a transform in Altair using  $\verb|.bin_transform()|$ :

```
In [10]: # filter, bin, and plot
         alt.Chart(
             data
         ).transform_filter(
             alt.FieldEqualPredicate(field = 'Year',
                                     equal = 2010)
         ).transform_bin(
             'Life Expectancy at Birth', # name to give binned variable
             field = 'Life Expectancy', # variable to bin
             bin = alt.Bin(step = 2) # binning parameters
         ).mark_bar(size = 10).encode(
             x = 'Life Expectancy at Birth:Q',
             y = 'count()'
Out[10]:
           22
           20
```

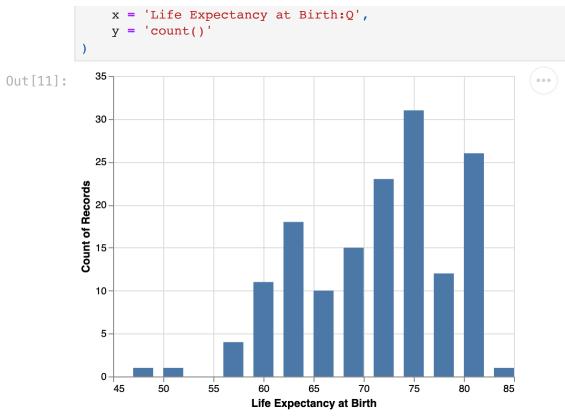


The plotting codes are a little more verbose, but they're much more efficient than performing the manipulations separately in pandas!

# Question Ob. Bin transform

Follow the example above and make a histogram of life expectancies across the globe in 2019 using an explicit bin transform to create bins spanning three years.

(Hint: copy your solution to Question 0a and modify to use .transform\_bin(...) instead of alt.X(...) .)



#### Aggregate transform

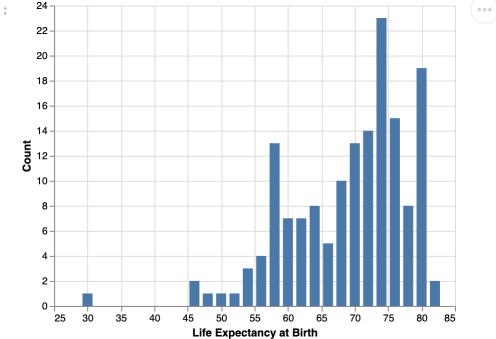
Now, the counting of observations in each bin is also an under-the-hood operation in constructing the histogram. You already saw how this was done 'manually' in the example above before introducing the bin transform.

Grouped counting is a form of aggregation: it produces output that has fewer values than the input by combining multiple values (in this case rows) into one value (in this case a count of the number of rows).

This operation can also be made explicit using <a href="transform\_aggregate">transform\_aggregate()</a>. This makes use of Altair's aggregation shorthands for common aggregation functions; see the documentation on Altair encodings for a full list of shorthands.

Here is how .transform\_aggregate() would be used to perform the counting:

```
In [12]: # filter, bin, count, and plot
         alt.Chart(
         ).transform_filter(
             alt.FieldEqualPredicate(field = 'Year',
                                      equal = 2010)
          ).transform_bin(
              'Life Expectancy at Birth',
             field = 'Life Expectancy',
             bin = alt.Bin(step = 2)
         ).transform_aggregate(
             Count = 'count()', # altair shorthand operation -- see docs for full list
             groupby = ['Life Expectancy at Birth'] # grouping variable(s)
          ).mark_bar(size = 10).encode(
             x = 'Life Expectancy at Birth:Q',
             y = 'Count:Q'
           24
Out[12]:
           22
```



# Calculate transform

One peculiarity of Altair's histograms is that they are displayed on the count scale rather than the density scale, and there is no simple option to change this.

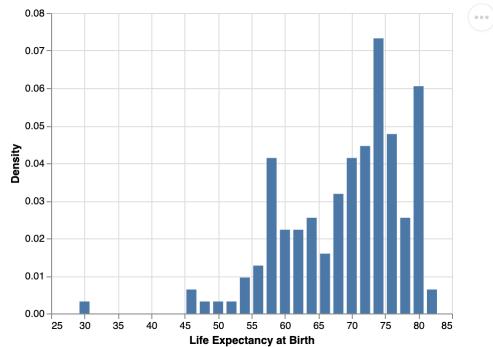
The **count scale** means that the y-axis shows **counts of observations in each bin**.

By contrast, on the **density scale**, the y-axis would show **proportions of total bar area** (so that the area of plotted bars sums to 1).

It might seem like a silly distinction -- after all, the two scales differ simply by a proportionality constant (the sample size times the bin width) -- but as you will see shortly, the density scale is more useful for statistical thinking about the distribution of values.

The scale conversion can be done using .transform\_calculate(), which computes derived variables using arithmetic operations. In this case, one only needs to divide the count by the total number of observations.

```
In [13]: # filter, bin, count, convert scale, and plot
         alt.Chart(
             data
         ).transform_filter(
             alt.FieldEqualPredicate(field = 'Year',
                                     equal = 2010)
         ).transform_bin(
             'Life Expectancy at Birth',
             field = 'Life Expectancy',
             bin = alt.Bin(step = 2)
         ).transform_aggregate(
             Count = 'count()',
             groupby = ['Life Expectancy at Birth']
         ).transform calculate(
             Density = 'datum.Count/(2*157)' # divide counts by sample size x binwidth
         ).mark_bar(size = 10).encode(
             x = 'Life Expectancy at Birth:Q',
             y = 'Density:Q'
```



## Question Oc. Density scale histogram

Follow the example above and convert your histogram from Question 0b (with the year 2019, the step size of 3, and the usage of <a href="transform\_bin(...">transform\_bin(...</a>) to the density scale. First calculate the count explicitly using <a href="transform\_aggregate(...">transform\_aggregate(...)</a> and then convert to a proportion using <a href="transform\_calculate(...">transform\_calculate(...)</a>.

(Note: you will need to find the sample size separately and hard-code this into the calculate step.)

#### Question Oci. Density scale histogram

First, calculate the sample size and store the result in sample\_size. Store the step size as bin\_width.

```
In [14]: # find sample size
    sample_size = np.sum(data.Year==2019)
    bin_width = 3
In [15]: grader.check("q0_ci")
```

# Out[15]: **q0\_ci** passed!

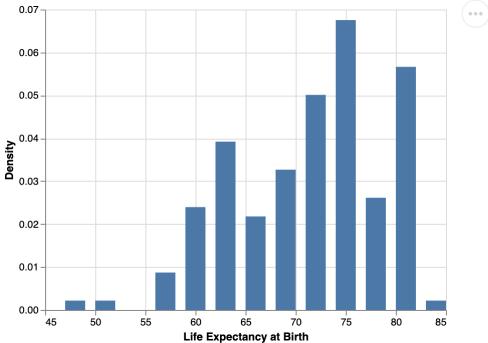
Out[16]:

Out[13]:

### Question Ocii. Density scale histogram

Convert your histogram from Question 0b (with the year 2019, the step size of 3, and the usage of .transform\_bin(...) ) to the density scale. First calculate the count explicitly using .transform\_aggregate(...) and then convert to a proportion using .transform\_calculate(...). Multiply sample\_size with bin\_width calculated in Question 0ci and hardcode it into your implementation.

```
In [16]: # construct histogram
          # filter, bin, count, convert scale, and plot
         alt.Chart(
             data
         ).transform_filter(
             alt.FieldEqualPredicate(field = 'Year',
                                     equal = 2019)
         ).transform_bin(
              'Life Expectancy at Birth',
             field = 'Life Expectancy',
             bin = alt.Bin(step = 3)
         ).transform_aggregate(
             Count = 'count()',
             groupby = ['Life Expectancy at Birth']
         ).transform_calculate(
             Density = 'datum.Count/(3*153)' # divide counts by sample size x binwidth
         ).mark_bar(size = 20).encode(
             x = 'Life Expectancy at Birth:Q',
             y = 'Density:Q'
```



# 1. Density estimation

Now that you have a sense of how transforms work, we can explore transforms that perform more sophisticated operations. We're going to focus on a technique known as kernel density estimation.

Histograms show the distribution of values in the sample. Let's call the density-scale histogram the empirical density. A kernel density estimate is simply a smoothing of the empirical density. (It's called an 'estimate' because it's often construed as an approximation of the distribution of population values that the sample came from.)

Often the point of visualizing the distribution of a variable is to discern the shape, spread, center, and tails of the distribution to answer certain questions:

- what's a typical value?
- are there multiple typical values (multi-modal)?
- are there outliers?
- is the distribution skewed?

Density estimates are often easier to work with in exploratory analysis because it is visually easier to distinguish the shape of a smooth curve than the shape of a bunch of bars (unless you're really far away!).

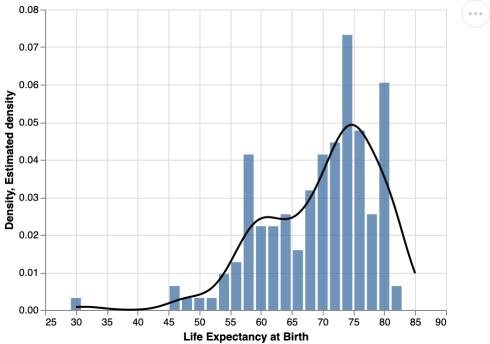
'Kernel density estimate' sounds fancy, but it's surprisingly easy to plot using .transform\_density(). The cell below generates a density estimate of life expectancies across the globe in 2010. Notice the commented lines explaining the syntax.

```
bandwidth = 3, # how smooth?
               extent = [30, 85], # domain on which the smooth is defined
               steps = 1000 # for plotting: number of points to generate for plotting line
          ).mark_line(color = 'black').encode(
              x = 'Life Expectancy at Birth:Q',
              y = 'Estimated Density:Q'
            0.050
Out[17]:
            0.045
            0.040
            0.035
          Density
             0.030
          0.025
             0.020
            0.015
            0.010
            0.005
            0.000 -
                          40
                                                    65
                                     Life Expectancy at Birth
```

as\_ = ['Life Expectancy at Birth', 'Estimated Density'], # names of outputs

This estimate can be layered onto the empirical density to get a better sense of the relationship between the two. The cell below accomplishes this. Notice that the plot elements are constructed as separate layers.

```
In [18]: # base plot
         base = alt.Chart(data).transform_filter(
             alt.FieldEqualPredicate(field = 'Year',
                                     equal = 2010)
          # empirical density
         hist = base.transform_bin(
             as_ = 'Life Expectancy at Birth',
             field = 'Life Expectancy',
             bin = alt.Bin(step = 2)
         ).transform_aggregate(
             Count = 'count()',
             groupby = ['Life Expectancy at Birth']
         ).transform_calculate(
             Density = 'datum.Count/(2*157)'
          ).mark_bar(size = 10, opacity = 0.8).encode(
             x = 'Life Expectancy at Birth:Q',
             y = 'Density:Q'
          # kernel density estimate
          smooth = base.transform_density(
             density = 'Life Expectancy',
             as_ = ['Life Expectancy at Birth', 'Estimated density'],
             bandwidth = 3,
             extent = [30, 85],
             steps = 1000
          ).mark line(color = 'black').encode(
             x = 'Life Expectancy at Birth:Q',
             y = 'Estimated density:Q'
          # layer
         hist + smooth
Out[18]:
```



What if you want a different amount of smoothing? That's what the extent parameter is for. The smoothing is *local*, in the following sense: at any given point, the kernel density estimate averages bar heights in a neighborhood of nearby bars proportional to how far the bars are from the point in question.

The extent parameter specifies the size of the smoothing neighborhood in standard deviations. For instance, above extent = 3, which means that the empirical density is smoothed 3SD in either direction to produce the kernel density estimate. This is also known as the *bandwidth*.

- If the bandwidth is increased, averaging is more global, so the density estimate will get smoother.
- If the bandwidth is decreased, averaging is more local, so the density estimate will get wiggly.

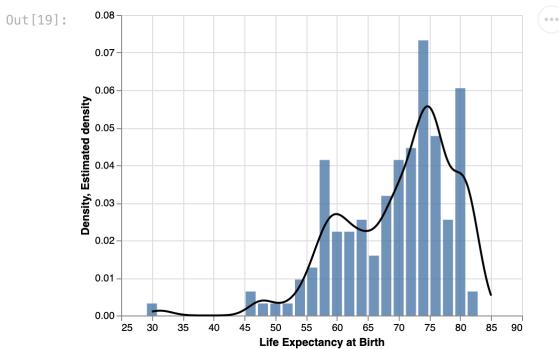
There are some methods out there for automating bandwidth choice, but often it is done by hand. Arguably this is preferable, as it allows the analyst to see a few possibilities and decide what best captures the shape of the distribution.

# Question 1a. Selecting a bandwidth

Modify the ploting codes by decreasing the bandwidth parameter. Try several values, and then choose one that you feel captures the shape of the distribution well without getting too wiggly.

```
In [19]: # change bandwidth
hist + base.transform_density(
    density = 'Life Expectancy',
    as_ = ['Life Expectancy at Birth', 'Estimated density'],
    bandwidth = 2, # play here
    extent = [30, 85],
    steps = 1000
).mark_line(color = 'black').encode(
    x = 'Life Expectancy at Birth:0',
    y = 'Estimated density:0'
)

#re run this at home it is taking forever to print
```



## Comparing distributions

0.02

0.01

0.00

30

35

40

45

50

55

60

Life Expectancy at Birth

65

75

80

70

The visual advantage of a kernel density estimate for discerning shape is even more apparent when comparing distributions.

As you will see as the course progresses, a major task in exploratory analysis is understanding how the distribution of a variable of interest changes depending on other variables -- for example, you have already seen in the last lab that life expectancy seems to change over time. We can explore this phenomenon from a different angle by comparing distributions in different years.

lab4-smoothing

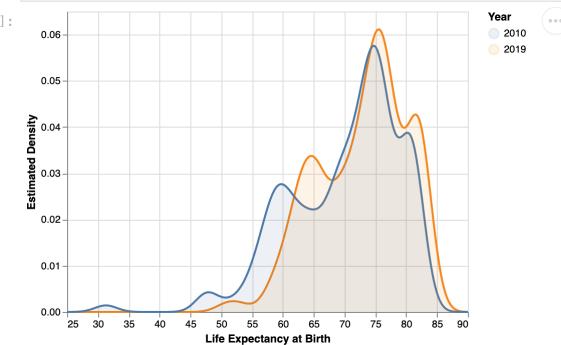
Multiple density estimates can be displayed on the same plot by passing a grouping variable (or set of variables) to <a href="transform\_density">transform\_density</a>(...) . For example, the cell below computes density estimates of life expectancies for each of two years.

```
In [20]: alt.Chart(data).transform_filter(
              alt.FieldOneOfPredicate(field = 'Year',
                                        oneOf = [2010, 2019])
          ).transform_density(
              density = 'Life Expectancy',
              groupby = ['Year'],
              as_ = ['Life Expectancy at Birth', 'Estimated Density'],
              bandwidth = 1.8,
              extent = [25, 90],
              steps = 1000
          ).mark_line().encode(
              x = 'Life Expectancy at Birth:Q',
              y = 'Estimated Density:Q',
              color = 'Year:N'
                                                                          Year
Out[20]:
                                                                          — 2010
            0.06
                                                                          <del>-</del> 2019
            0.05
          Density
          Estimated I
```

Often the area beneath each density estimate is filled in. This can be done by simply appending a \_mark\_area() call at the end of the plot.

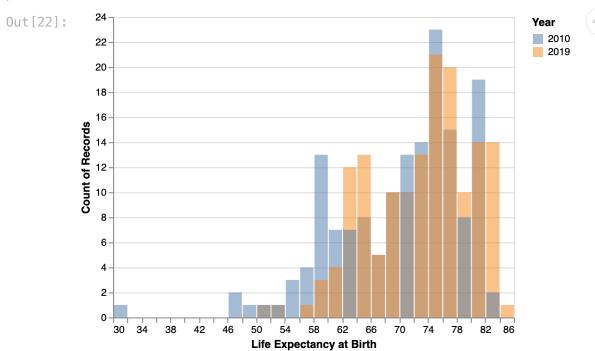
85 90

```
In [21]: p = alt.Chart(data).transform_filter(
             alt.FieldOneOfPredicate(field = 'Year',
                                     oneOf = [2010, 2019])
         ).transform_density(
             density = 'Life Expectancy',
             groupby = ['Year'],
             as_ = ['Life Expectancy at Birth', 'Estimated Density'],
             bandwidth = 1.8,
             extent = [25, 90],
             steps = 1000
         ).mark_line().encode(
             x = 'Life Expectancy at Birth:Q',
             y = 'Estimated Density:Q',
             color = 'Year:N'
         p + p.mark_area(opacity = 0.1)
Out[21]:
```



Notice that this makes it much easier to compare the distributions between years -- you can see a pronounced rightward shift of the smooth for 2019 compared with 2010.

We could make the same comparison based on the histograms, but the shift is a lot harder to make out.



#### Question 1b. Multiple density estimates

Follow the appropriate example above to construct a plot showing separate density estimates of life expectancy for each region in the 2010. You can choose whether you prefer to fill in the area beneath the smooth curves, or not. Be sure to play with the bandwidth parameter and choose a value that seems sensible to you.

```
In [23]: alt.Chart(data).transform_filter(
              alt.FieldOneOfPredicate(field = 'Year',
                                       oneOf = [2010])
          ).transform_density(
              density = 'Life Expectancy',
              groupby = ['region'],
              as_ = ['Life Expectancy at Birth', 'Estimated Density'],
              bandwidth = 1.8,
              extent = [25, 90],
              steps = 1000
          ).mark_line().encode(
              x = 'Life Expectancy at Birth:Q',
              y = 'Estimated Density:Q',
              color = 'region'
           0.12-
Out[23]:
                                                                        region
                                                                        Africa
                                                                        Americas
                                                                        — Asia
            0.10
                                                                        Europe
                                                                        Oceania
          Density
80.0
```

# Question 1c. Interpretation

40

50

55

Life Expectancy at Birth

60

65

35

0.02

0.00 -

25 30

Do the distributions of life expectancies seem to differ by region? If so, what is one difference that you notice? Answer in 1-2 sentences.

Yes, the distribution of life expectancies differs by region. All of the regions life expectancy is left skewed and I noticed that Europe has the greatest life expectancy and Africa has the least life expectancy.

# Question 1d. Outlier

Notice that little peak way off to the left in the distribution of life expectancies in the Americas. That's an outlier.

# (i) Which country is it?

Check by filtering data appropriately and using sort\_values(...) to find the lowest life expectancy in the Americas. Save the row of data that shows the outlying observation in lowest\_Americas.

(Hint: You might want to check the documentation.)

```
In [24]: # show row of outlier
lowest_Americas = data.loc[(data['region'] == 'Americas') & (data['Year'] == 2010)]
lowest_Americas = lowest_Americas.sort_values(by=['Life Expectancy'])
lowest_Americas.head(1)
# Haiti has the lowest life expectancy in the Americas
Out[24]: Country Name Year Life Expectancy Male Life Expectancy Female Life Expectancy GDP per capita region sub-region Population
```

Out[24]:		Country Name	Year	Life Expectancy	Male Life Expectancy	Female Life Expectancy	GDP per capita	region	sub-region	Population
	246	Haiti	2010	31.3	28.0	35.4	1172.098543	Americas	Latin America and the Caribbean	9949322.0
In [25]:	grad	ler.check("q1_	_d_i")							

Out[25]:

# q1\_d\_i passed!

# (ii) What was the life expectancy for that country in other years?

Now filter the data to examine the life expectancy in the country you identified as the outlier in all years. Save the corresponding four rows of data: one row for each year into outlier\_country.

(Hint: filter by country.)

```
In [26]: # show rows for all years for country of interest
    outlier_country = data.loc[(data['Country Name']=='Haiti')]
    outlier_country = outlier_country.sort_values(by=['Year'])
    outlier_country
```

Out[26]:		Country Name	Year	Life Expectancy	Male Life Expectancy	Female Life Expectancy	GDP per capita	region	sub-region	Population
	247	Haiti	2000	57.0	57.0	57.2	811.533974	Americas	Latin America and the Caribbean	8463806.0
	246	Haiti	2010	31.3	28.0	35.4	1172.098543	Americas	Latin America and the Caribbean	9949322.0
	245	Haiti	2015	62.6	62.1	63.1	1389.119520	Americas	Latin America and the Caribbean	10695542.0
	244	Haiti	2019	64.1	63.3	64.8	1272.490925	Americas	Latin America and the Caribbean	11263077.0

# (iii) What Happened in 2010?

Can you explain why the life expectancy was so low in that country for that particular year?

(Hint: if you don't remember, Google the country name and year in question.)

4/28/22, 10:50 PM

The reason that the life expectancy is so low in Haiti is beacause there was an earthquake in 2010 and it disintegrated hospitals and treatment facilities.

# 2. Scatterplot smooths

In this brief section you'll see two techniques for smoothing scatterplots: LOESS, which produces a curve; and regression, which produces a linear smooth.

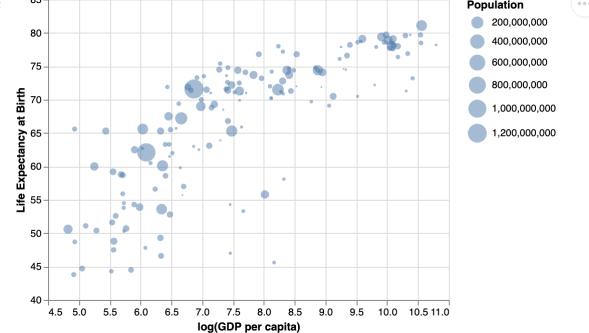
The next parts will modify the dataframe data by adding a column. We'll create a copy data\_mod1 of the original dataframe data to modify as to not lose track of our previous work:

```
In [27]: data_mod1 = data.copy()
```

#### **LOESS**

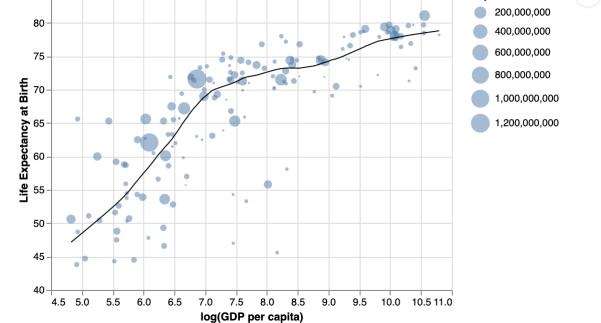
**Lo**cally weighted scatterplot smoothing (LOESS) is a flexible smoothing technique for visualizing trends in scatterplots. The technical details are a little beyond us at the moment, but it's easy enought to implement.

To illustrate, consider the scatterplots you made in lab 3 showing the relationship between life expectancy and GDP per capita. The plot for 2010 looked like this:



To add a LOESS curve, simply append .transform\_loess() to the base plot:

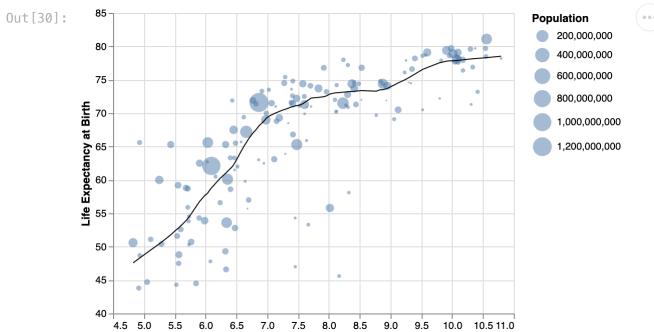
```
In [29]: # compute smooth
          smooth = scatter.transform_loess(
             on = 'log(GDP per capita)', # x variable
             loess = 'Life Expectancy', # y variable
             bandwidth = 0.25 # how smooth?
          ).mark line(color = 'black')
          # add as a layer to the scatterplot
         scatter + smooth
Out[29]:
                                                                     Population
                                                                      200,000,000
            80
                                                                      400,000,000
                                                                      600,000,000
            75
                                                                      800,000,000
```



Just as with kernel density estimates, LOESS curves have a bandwidth parameter that controls how smooth or wiggly the curve is. In Altair, the LOESS bandwidth is a unitless parameter between 0 and 1.

# Question 2a. LOESS bandwidth selection

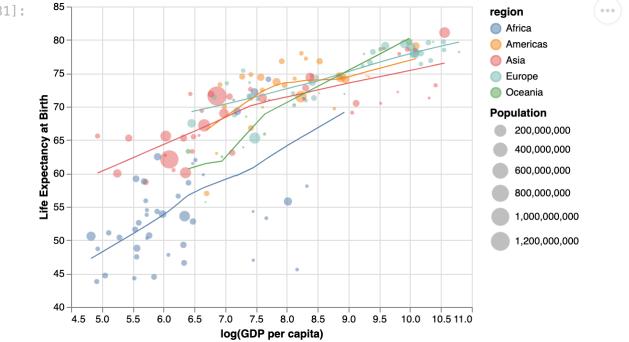
Tinker with the bandwidth parameter to see its effect in the cell below. Then choose a value that produces a smoothing you find appropriate for indicating the general trend shown in the scatter.



log(GDP per capita)

LOESS curves can also be computed groupwise. For instance, to display separate curves for each region, one need only pass a groupby = ... argument to .transform\_loess():

```
In [31]: # scatterplot
         scatter = alt.Chart(data_mod1).transform_filter(
             alt.FieldEqualPredicate(field = 'Year', equal = 2000)
          ).mark_circle(opacity = 0.5).encode(
             x = alt.X('log(GDP per capita)', scale = alt.Scale(zero = False)),
             y = alt.Y('Life Expectancy', title = 'Life Expectancy at Birth', scale = alt.Scale(zero = False)),
             size = alt.Size('Population', scale = alt.Scale(type = 'sqrt')),
             color = 'region'
          # compute smooth
          smooth = scatter.transform_loess(
             groupby = ['region'], # add groupby
             on = 'log(GDP per capita)',
             loess = 'Life Expectancy',
             bandwidth = 0.8
          ).mark_line(color = 'black')
          # add as a layer to the scatterplot
          scatter + smooth
Out[31]:
                                                                    region
```



The curves are a little jagged because there aren't very many countries in each region.

```
In [32]: data_mod1[data_mod1.Year == 2000].groupby('region').count().iloc[:, [0]]
```

 Out [32]:
 Country Name

 region
 45

 Africa
 45

 Americas
 27

 Asia
 38

 Europe
 35

Oceania

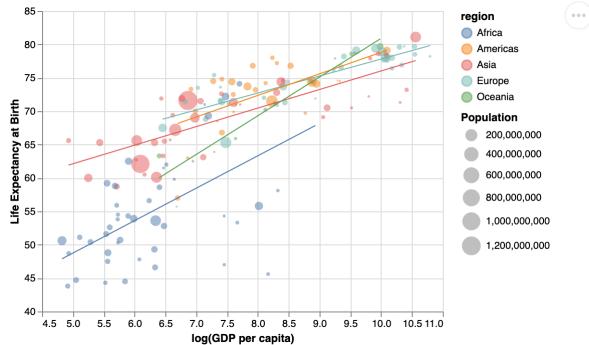
# Regression

9

You will be learning more about linear regression later in the course, but we can introduce regression lines now as a visualization technique. As with LOESS, you don't need to concern yourself with the mathematical details (yet!). From this perspective, regression is a form of *linear* smoothing -- a regression smooth is a straight line. By contrast, LOESS smooths have *curvature* -- they are not straight lines.

In the example above, the LOESS curves don't have much curvature. So it may be a cleaner choice visually to show linear smooths. This can be done using \_transform\_regression(...) with a similar argument structure.

```
In [33]: # scatterplot
         scatter = alt.Chart(data_mod1).transform_filter(
             alt.FieldEqualPredicate(field = 'Year', equal = 2000)
         ).mark_circle(opacity = 0.5).encode(
            x = alt.X('log(GDP per capita)', scale = alt.Scale(zero = False)),
             y = alt.Y('Life Expectancy', title = 'Life Expectancy at Birth', scale = alt.Scale(zero = False)),
             size = alt.Size('Population', scale = alt.Scale(type = 'sqrt')),
             color = 'region'
         # compute smooth
         smooth = scatter.transform_regression(
             groupby = ['region'],
             on = 'log(GDP per capita)',
             regression = 'Life Expectancy'
         ).mark_line(color = 'black')
         # add as a layer to the scatterplot
         scatter + smooth
```



#### Question 2b. Simple regression line

Out[33]:

Based on the example immediately above, construct a scatterplot of life expectancy against log GDP per capita in 2010 with points sized according to population (and no distinction between regions). Layer a single linear smooth on the scatterplot using .transform\_regression(...).

(Hint: remove the color aesthetic and grouping from the previous plot.)

```
In [34]: # scatterplot
          scatter = alt.Chart(data_mod1).transform_filter(
              alt.FieldEqualPredicate(field = 'Year', equal = 2010)
          ).mark_circle(opacity = 0.5).encode(
              x = alt.X('log(GDP per capita)', scale = alt.Scale(zero = False)),
              y = alt.Y('Life Expectancy', title = 'Life Expectancy at Birth', scale = alt.Scale(zero = False)),
              size = alt.Size('Population', scale = alt.Scale(type = 'sqrt')),
              # color = 'region'
          # construct smooth
          smooth = scatter.transform_regression(
              # groupby = ['region'],
              on = 'log(GDP per capita)',
              regression = 'Life Expectancy'
          ).mark_line(color = 'black')
          # layer
          scatter + smooth
Out[34]:
                                                                        200,000,000
            80
                                                                        400,000,000
            75
                                                                        600,000,000
            70
                                                                        800,000,000
          Birt 65
                                                                        1,000,000,000
                                                                        1,200,000,000
          වු 60
          Expectan 50
            50
            45
            40
            35
            30
                                   log(GDP per capita)
```

# 3. Neat trick

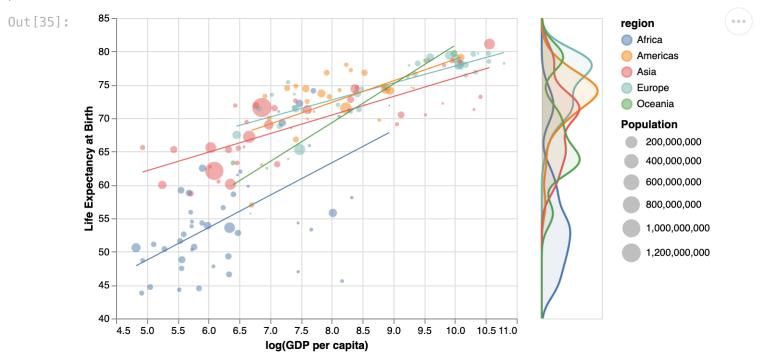
Let's combine the scatterplot with a smooth from part 2 with the density estimates in part 1. This is an example of combining multiple plots into one visual.

Why combine? Well, sometimes it's useful to visualize the distribution of the variable of interest together with its relationship to another variable. Imagine, for example, that you're interested in seeing both:

- the relationship between life expectancy and GDP per capita by region; and
- the distributions of life expeectancies by region.

We can flip the density estimates on their side and append them as a facet to the right-hand side of the scatterplot as follows:

```
In [35]: # scatterplot with linear smooth
         scatter = alt.Chart(data mod1).transform filter(
             alt.FieldEqualPredicate(field = 'Year', equal = 2000)
         ).mark_circle(opacity = 0.5).encode(
             x = alt.X('log(GDP per capita)', scale = alt.Scale(zero = False)),
             y = alt.Y('Life Expectancy', title = 'Life Expectancy at Birth', scale = alt.Scale(zero = False)),
             size = alt.Size('Population', scale = alt.Scale(type = 'sqrt')),
             color = 'region'
         smooth = scatter.transform_regression(
             groupby = ['region'],
             on = 'log(GDP per capita)',
             regression = 'Life Expectancy'
         ).mark_line(color = 'black')
         # density estimates
         p = alt.Chart(data mod1).transform filter(
             alt.FieldEqualPredicate(field = 'Year',
                                     equal = 2000)
         ).transform_density(
             density = 'Life Expectancy',
             groupby = ['region'], # change here
             as_ = ['Life Expectancy at Birth', 'Estimated density'],
             bandwidth = 2,
             extent = [40, 85],
             steps = 1000
         ).mark_line(order = False).encode(
             y = alt.Y('Life Expectancy at Birth:Q',
                       scale = alt.Scale(domain = (40, 85)),
                       title = '',
                       axis = None),
             x = alt.X('Estimated density:Q',
                       title = '',
                       axis = None),
             color = alt.Color('region:N')
         ).properties(width = 60)
         # facet structure
         (scatter + smooth) | (p + p.mark_area(order = False, opacity = 0.1))
```



# **Submission Checklist**

- 1. Save file to confirm all changes are on disk
- 2. Run Kernel > Restart & Run All to execute all code from top to bottom
- 3. Save file again to write any new output to disk
- 4. Select File > Download as > HTML.
- 5. Open in Google Chrome and print to PDF on A3 paper in portrait orientation.
- 6. Submit to Gradescope

To double-check your work, the cell below will rerun all of the autograder tests.

In [36]: grader.check\_all()

Out[36]: q0\_ci results: All test cases passed!

q1\_d\_i results: All test cases passed!

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